

Adjusting the inhomogeneity in daily temperature series using wavelet analysis

Li Zhen and Yan Zhongwei*

*Key Laboratory of Regional Climate-Environment in Temperate East
Asia, Institute of Atmospheric Physics , Chinese Academy of Sciences*

Cao Lijuan

National Meteorological Information Center, Beijing, China

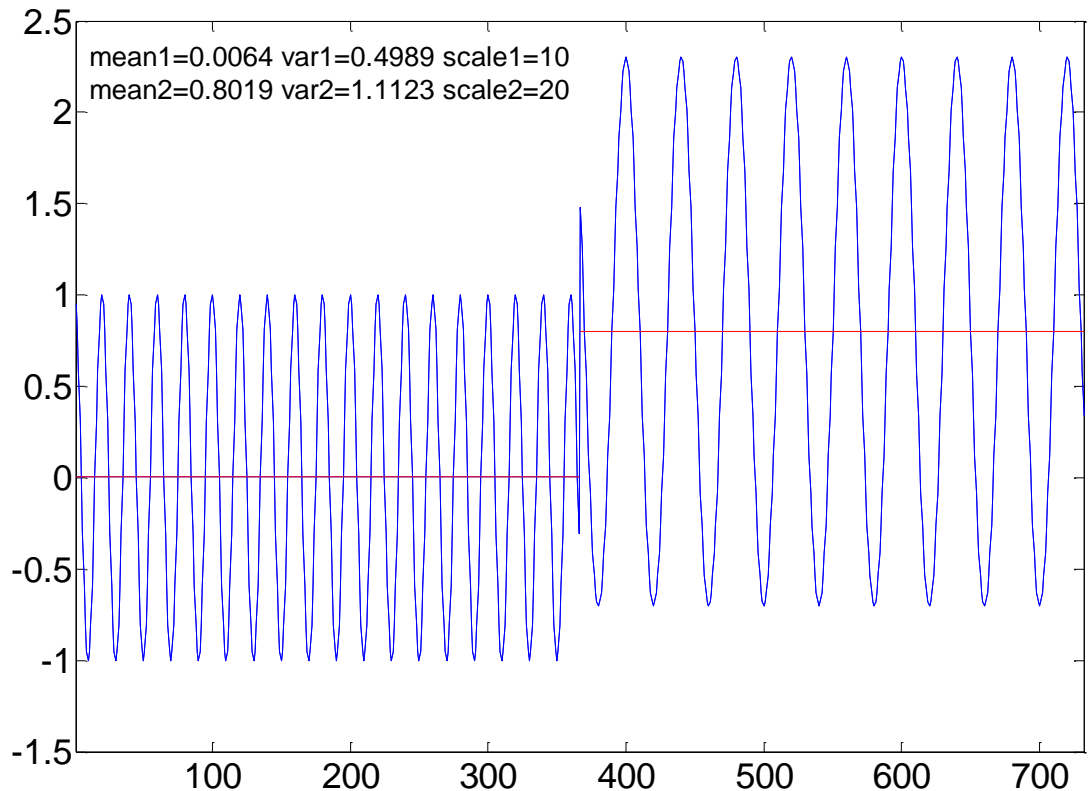
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Outline

- Introduction
- Data and method
- Results
- Conclusion

Introduction

- A homogeneous climate series is essential for quantifying climate change;
- Inhomogeneity is almost unavoidable due to various non-natural changes such as those in the observing location, environs, protocols...



Inhomogeneity not only affects **mean level**, but also **variability at different timescales.**

A summary of current methods

MASH, TPR, SNHT



mean level

Higher-order moments (HOM)
SPLIDHOM, Percentiles



High-order + Autocorrelation
(HOMAD, Rhtest v3.0)

climate extremes
in daily series

Why wavelet analysis ?

- Climate extremes / strong weather phenomena are mainly related to daily and weekly variability in observational series
– Yan et al 2001
- There are inhomogeneities existing mainly for certain time-scale variability – Yan and Jones 2008

It is beneficial to develop a wavelet-analysis-based method to adjust inhomogeneities hidden in some particular time-scale fluctuations.

This talk is to demonstrate

- Problems in current methods of homogenization of climate data;
- How the wavelet-based method works;
- Influence on estimates of climate change especially dealing with climate extremes.

via case studies

Data for case studies

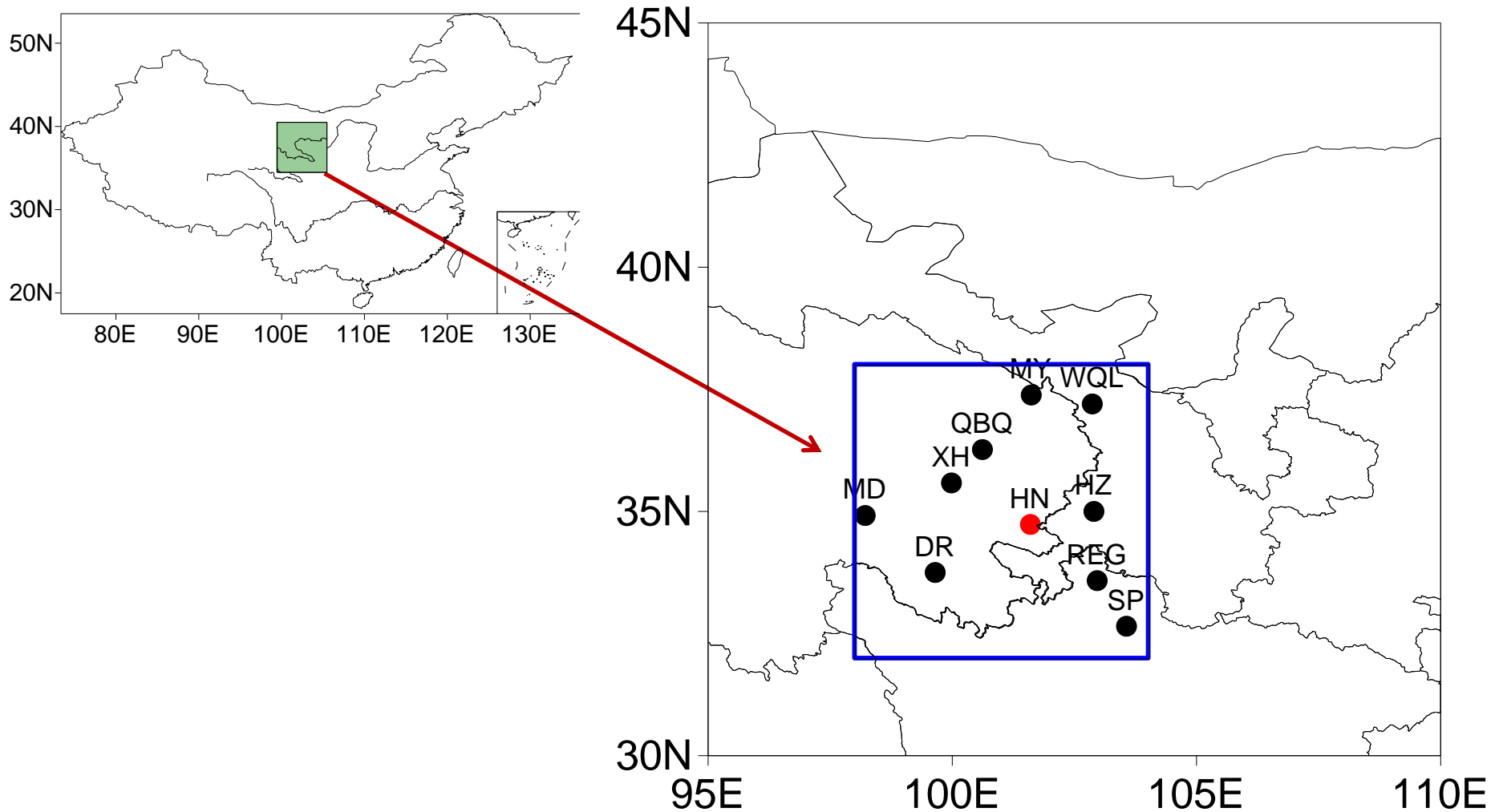
Daily mean temperature series at

➤ Central England (CE)

- 1772-2003, homogenized by Parker et al (1992)

➤ Henan(HN, western-central China)

- original,1960-2008
- MASH-homogenized 1960-2008 (Li&Yan 2009, using 9 ref. stations)
- HOM-homogenized 1960-2008 (this work, using 9 ref. stations)
- Rhtest-homogenized 1960-2008 (this work, using 9 ref. stations)
- TPR-homogenized 1960-2004 (Li et al 2006, different ref. stations)



Geographical distribution of **HN (red dot)** and reference stations used by MASH, RHtest, and HOM method (black dots)

Method

➤ Morlet wavelet analysis - Yan et al 2001

Morlet wavelet function:

$$w(t) = s^{-\frac{1}{2}}g(t') \exp(i\pi t')$$
$$g(t) = \exp(-t^2/2)$$

Timescales 2S:

$$S = 2^{p+q/Q}$$

$$p = 0, 1, \dots, P \quad P = 15$$

$$q = 0, 1, \dots, Q-1 \quad Q = 2$$

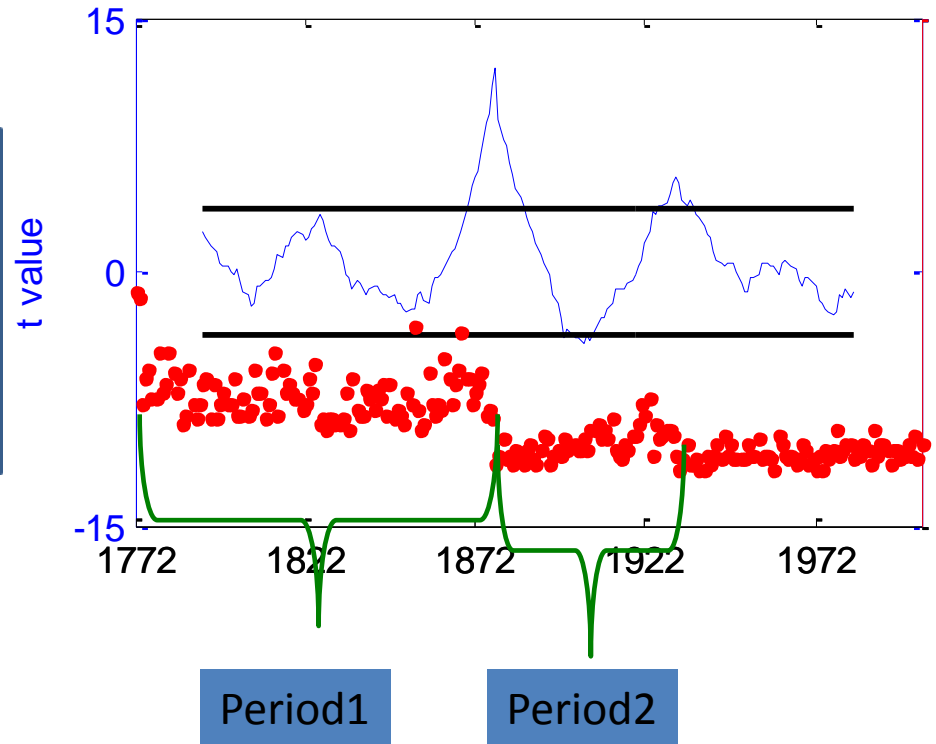
2S = 2, 2.8, 4, ..., 64, ... days

↓ ↓ ↓ ↓
band 1, band 2, band 3, ..., band 11, ...

- Daily Variability (DV): less than 3 days (bands 1-2) - **local scale**
- Weekly Variability (WV): 4 days up to 2 months (bands 3-11) - **large scale**

Adjustment of wavelet power:

$$\alpha = \frac{\Delta P_{\text{period2}}}{\Delta P_{\text{period1}}} = \frac{\frac{1}{n_1} \sum_{i=1}^{n_1} \Delta P_2}{\frac{1}{n_2} \sum_{i=1}^{n_2} \Delta P_1}$$



Adjust wavelet power of period 1 to period 2 for each band and season (if there is a jump beyond 0.001 significance threshold), relevant to a reference series

Other methods used in this study

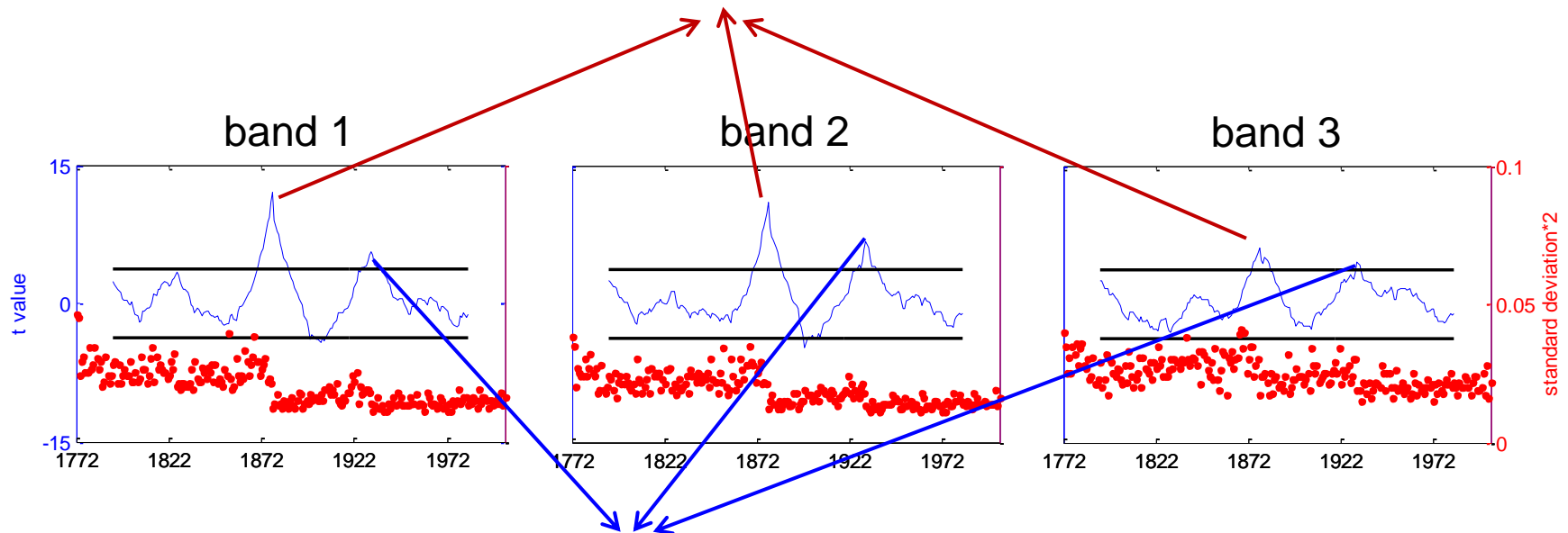
- Multiple Analysis of Series for Homogenization(MASH)
- Higher-Order Moment (HOM)
- Relative Homogenization test (RHtest)
- Two Phase Regression F-test (TPR)
- Moving t-test ($\alpha=0.001$) for detecting jumps in wavelet power

Results

Case 1: Central England Temperature (CET)

wavelet analysis of CET – for original series

From one station to three-station average on **1 January 1878** and Parker et al. (1992) adjusted the whole variance of earlier period 1772-1877.

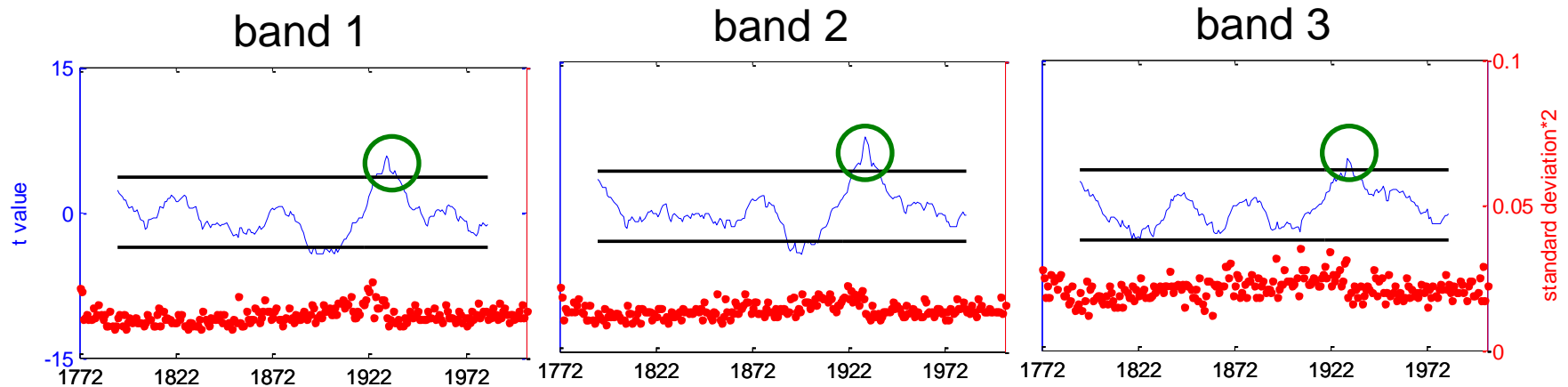


From three-station average to another three-station average on **1 January 1931** (Parker et al. 1992)

Annual wavelet power (red dots) of bands 1-3 in original CET 1772-2003, corresponding moving t-test (blue lines) and the 0.001 significance thresholds (black lines).

wavelet analysis of CET

– after the 1878 inhomogeneity has been adjusted

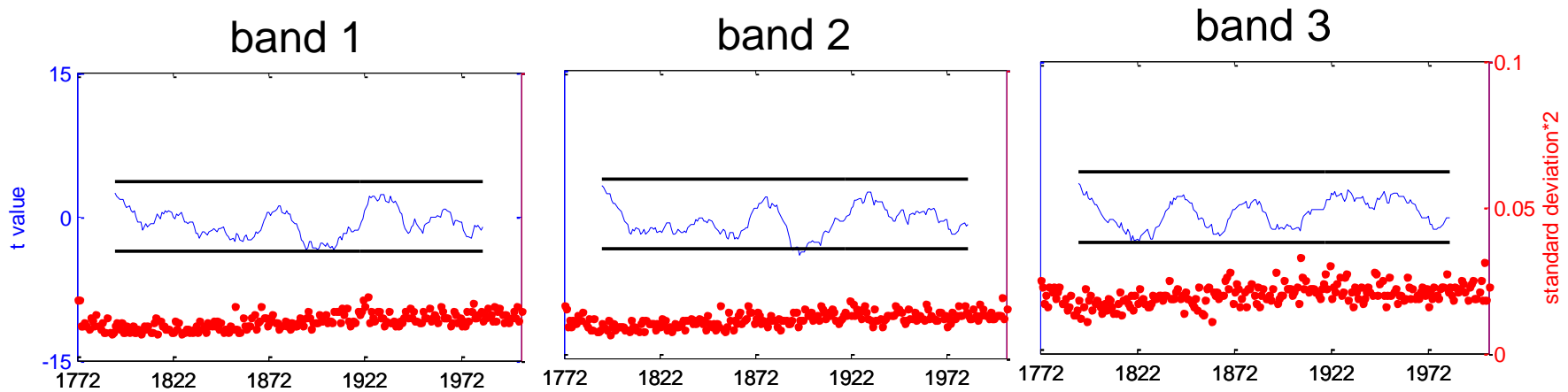


Annual wavelet power (red dots) of bands 1-3 in series after adjusting the 1878 inhomogeneity, corresponding moving t-test (blue lines) and the 0.001 significance thresholds (black lines).

Comparing Parker et al: we adjusted 'variance' for different timescales

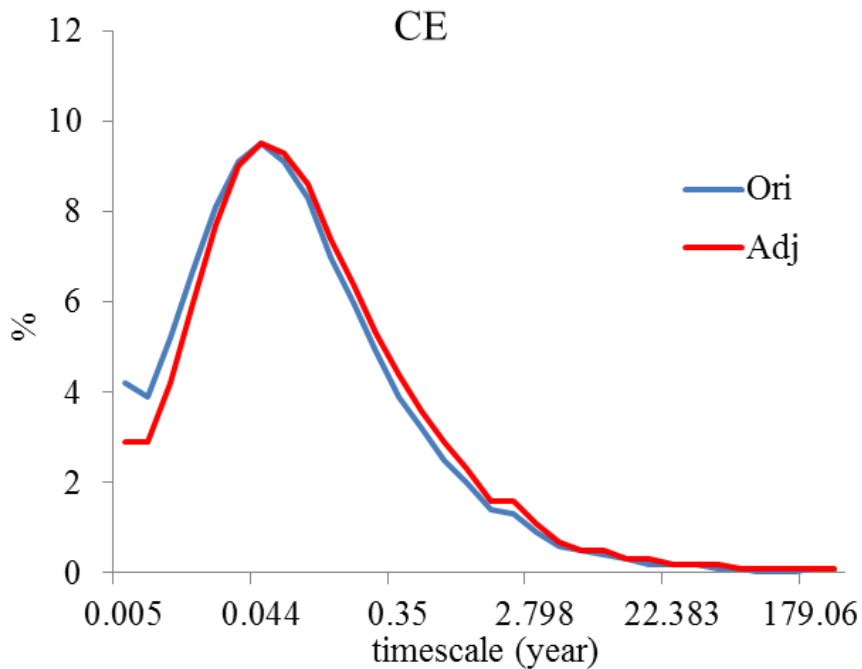
wavelet analysis of CET

– after the 1931 inhomogeneity has been adjusted

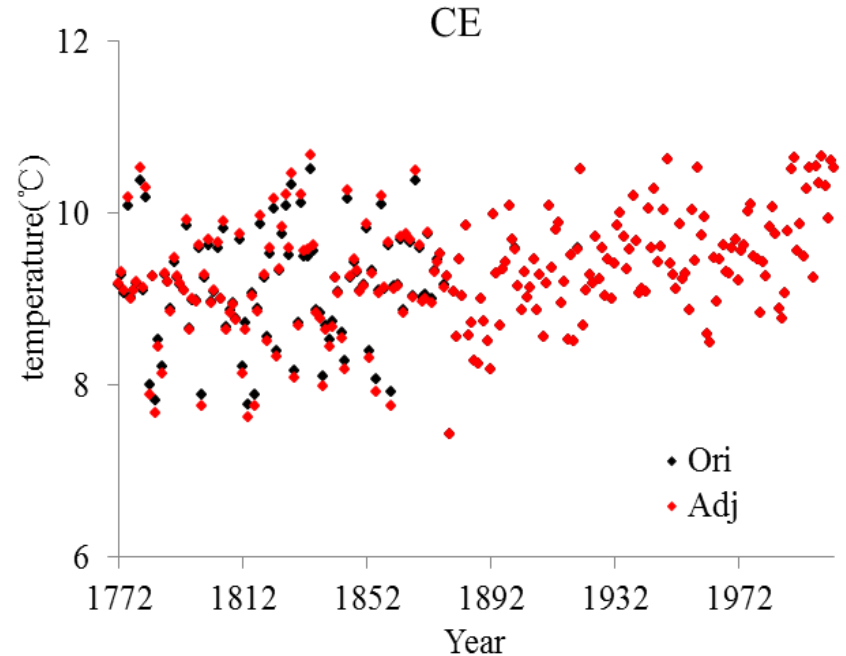


Annual wavelet power (red dots) of bands 1-3 adjusted series, and corresponding moving t-test and the 0.001 significance thresholds (blue lines).

Comparing wavelet power spectra and **annual mean temperature** between original and adjusted CET



Average wavelet power for daily mean temperature anomaly series 1772-2003 at CE



The annual mean temperature in original and adjusted series 1772-2003 at CE

Potential for adjusting inter-annual and longer-term variability if reference series are available

Influences on trends of mean temperature and extremes in CET

		annual	winter	summer
Mean	Ori	0.034*	0.055*	0.009
	Adj	0.034*	0.056*	0.008
Hot day	Ori	0.331*	0.090*	0.086*
	Adj	0.348*	0.119*	0.070
Cold day	Ori	-0.873*	-0.206*	-0.101
	Adj	-0.883*	-0.216*	-0.109*
		annual	summer-half year	winter-half year
Heat wave	Ori	0.053*	0.031*	0.023*
	Adj	0.027*	0.016*	0.012
Cold surge	Ori	-0.105*	-0.037*	-0.069*
	Adj	-0.142*	-0.052*	-0.092*

Linear trends in original and adjusted annual and seasonal mean temperature and extreme series 1772-2003 at Central England.

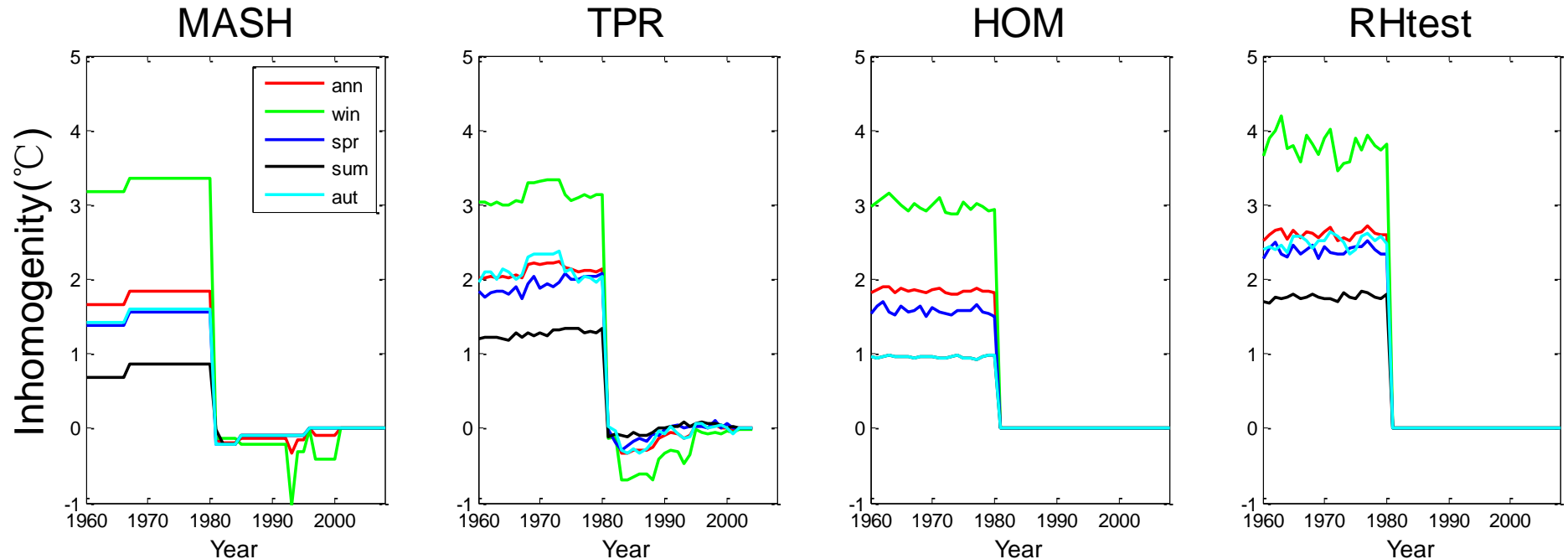
(* denotes the linear trends significant at $\alpha = 0.05$)

Results

Case 2: Henan (HN) station

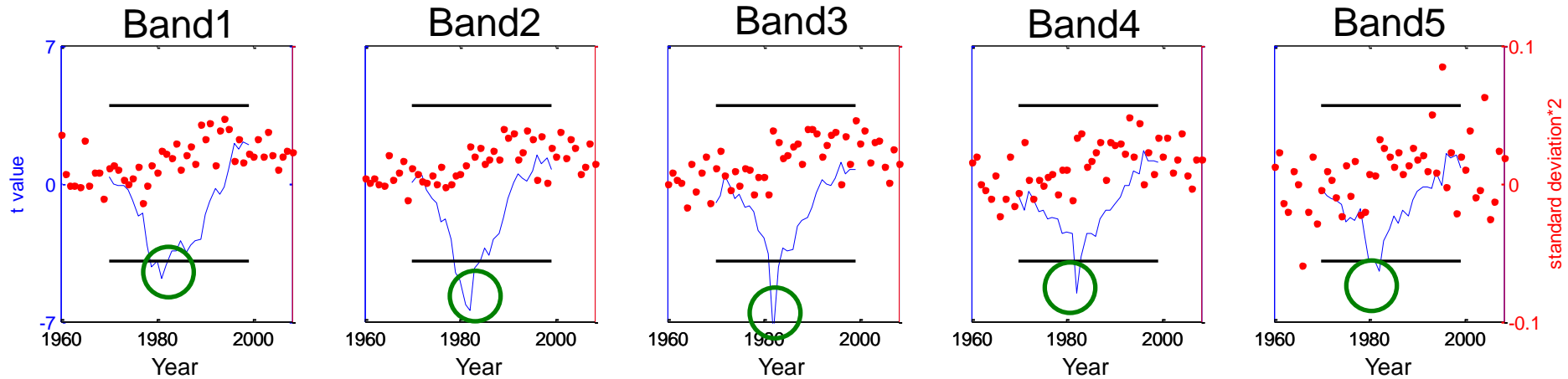
Inhomogeneities estimated by different methods

There is a relocation on 1 January 1981 with a change in elevation from 1974.4m to 3414.1m.



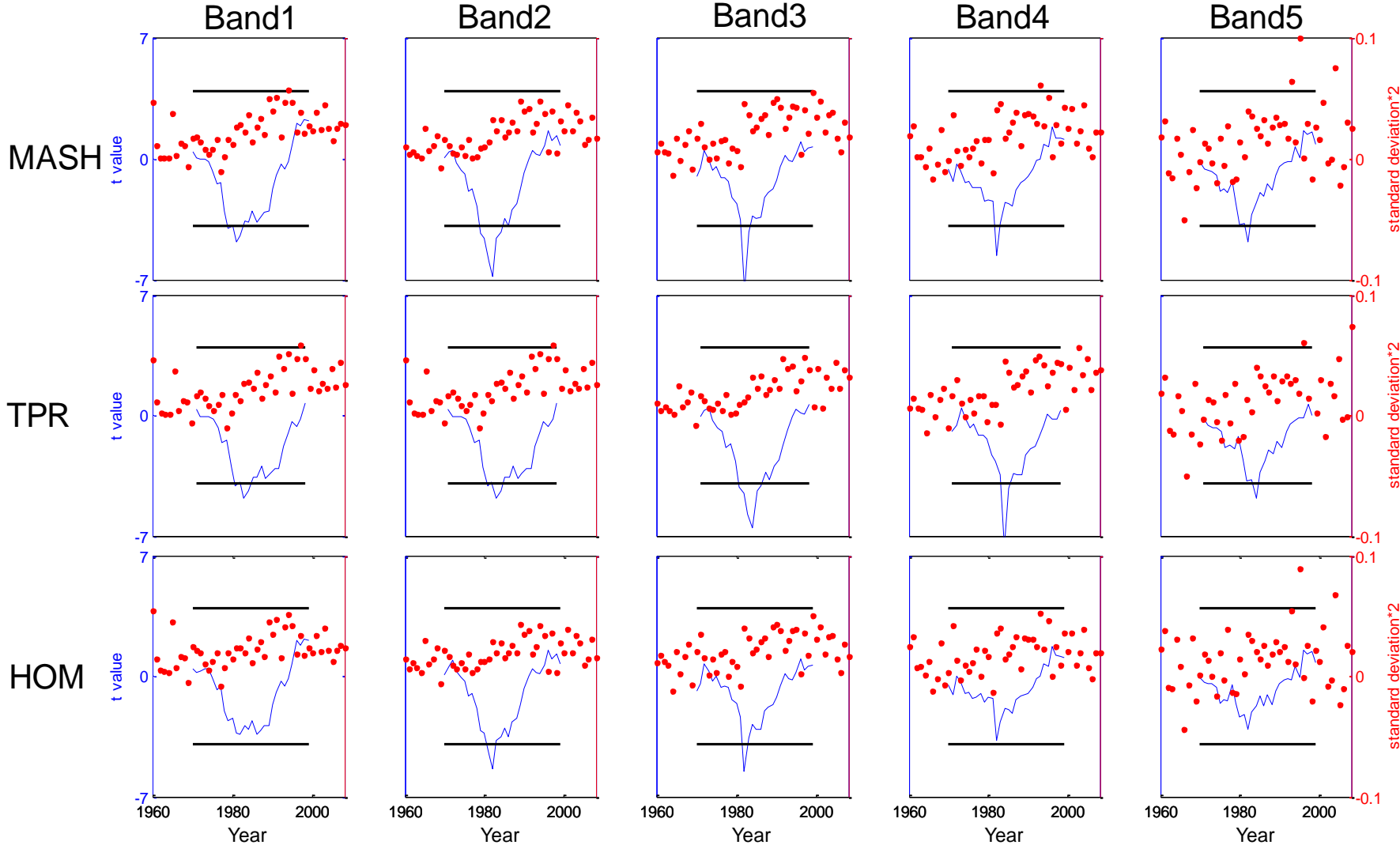
The annual and seasonal inhomogeneities estimated by MASH, TPR, HOM and RHtest at HN

wavelet analysis at HN – for original series



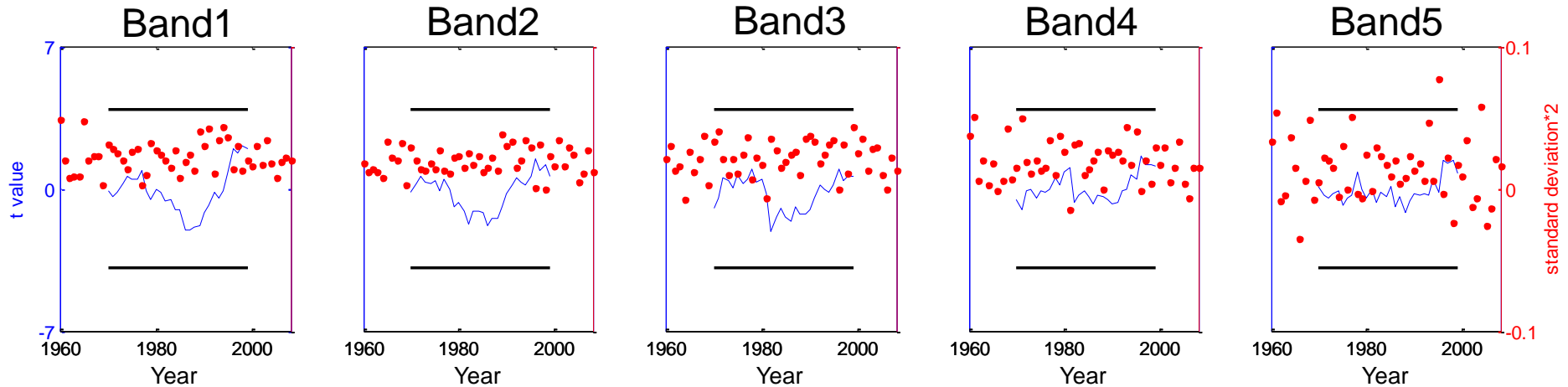
The difference of winter mean wavelet power (bands 1-5) (red dots) between HN and HJL and corresponding moving-t test with the 0.001 significance thresholds (blue line).

wavelet analysis at HN – For conventionally adjusted series



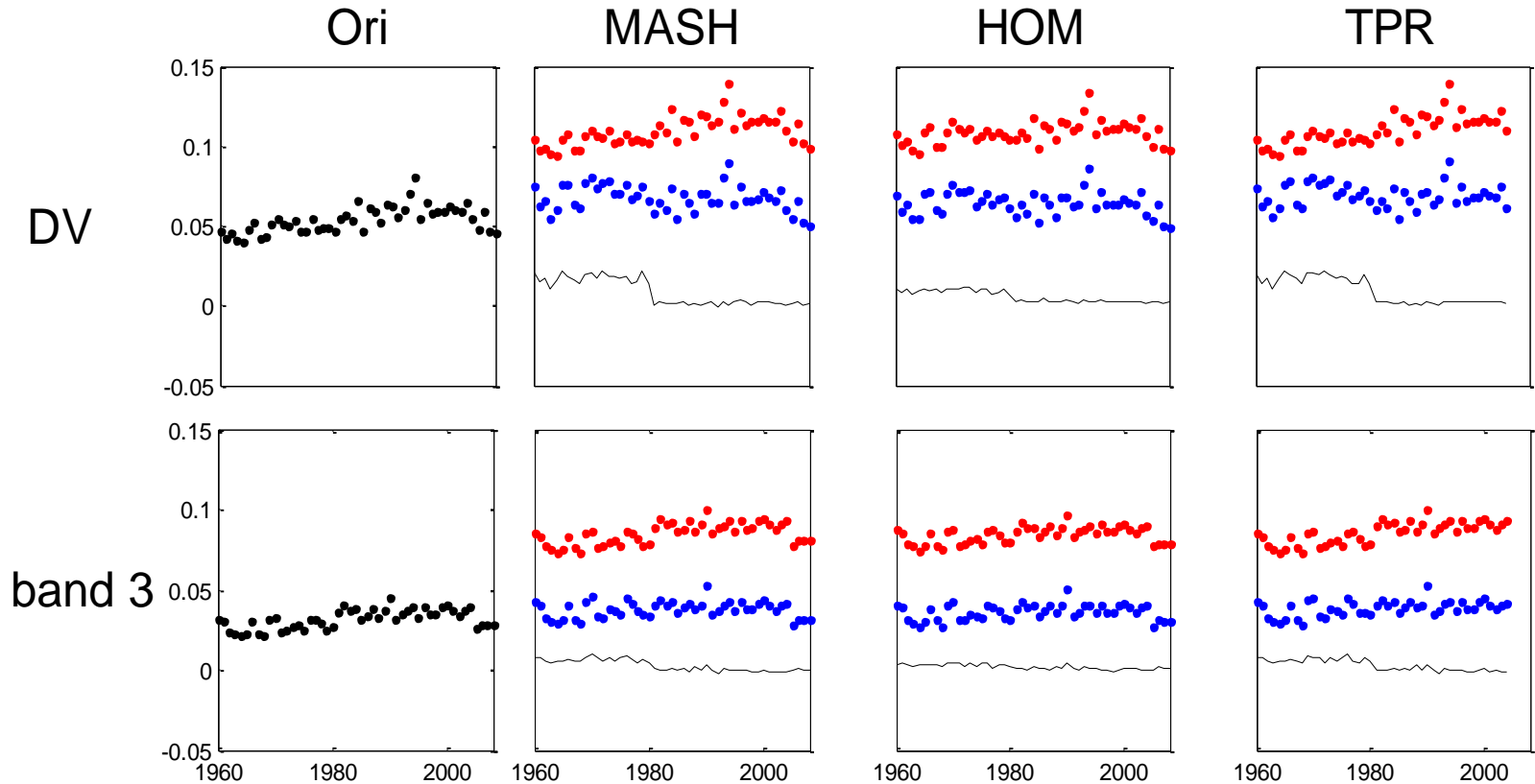
The inhomogeneities in 1981 are still obvious, especially for the homogenized series based on MASH and TPR.

wavelet analysis at HN – For adjusted series by RHtest



Rhtest tends to have improved the wavelet power spectra regarding inhomogeneity hidden in DV and WV (bands 1-5).

Comparing annual wavelet power of DV and band3 for the original and various homogenized series

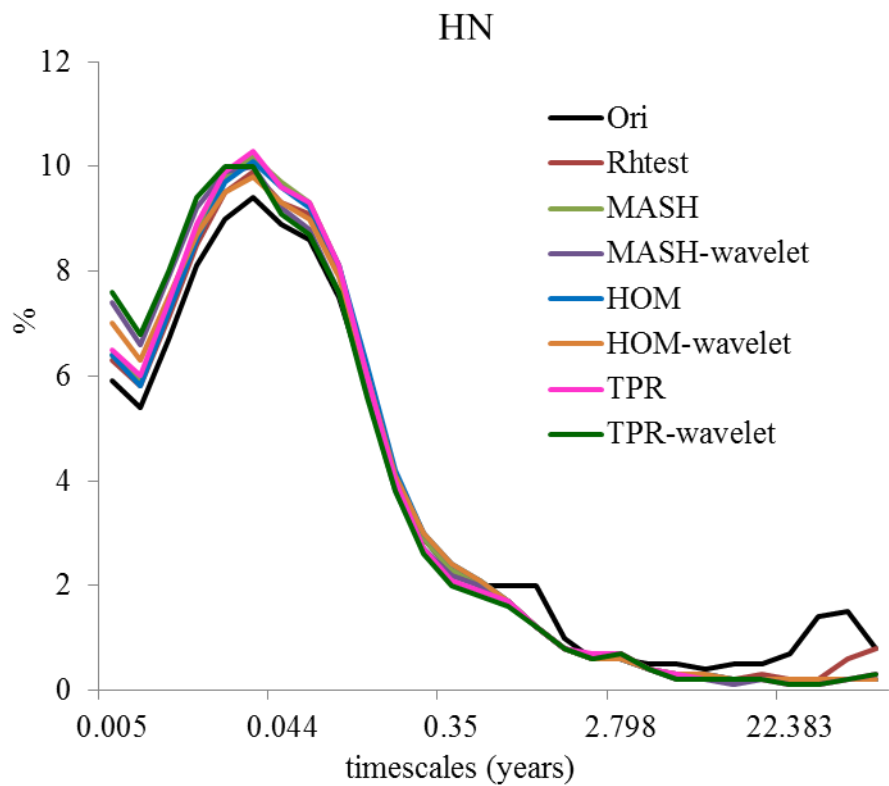


Original: black dots; Previously homogenized: red dots;

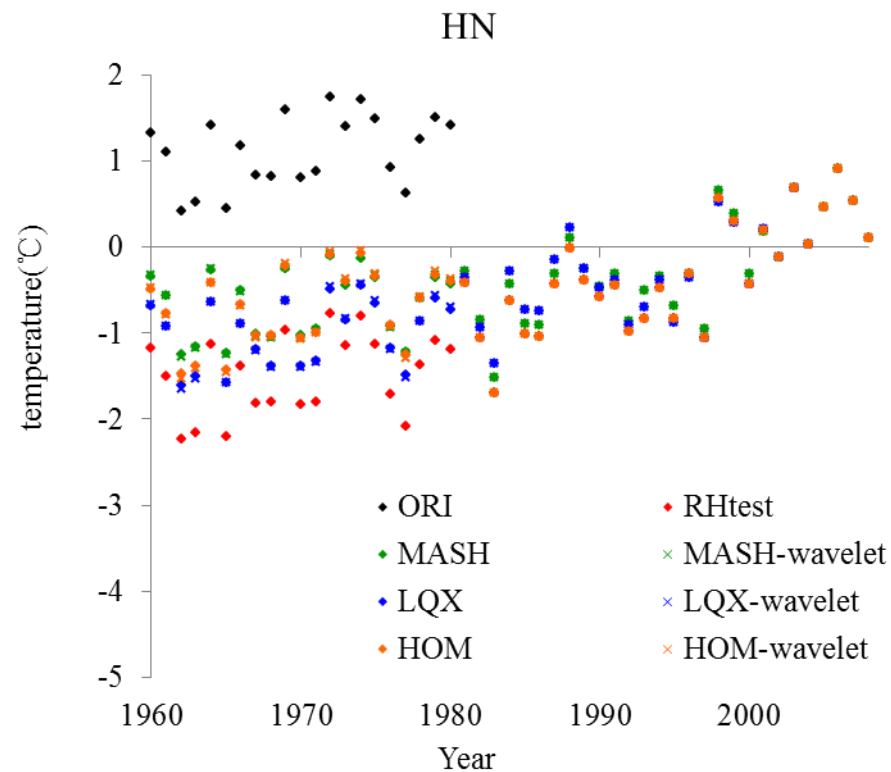
Present adjusted: blue dots;

differences between the present and previously homogenized series: black line).

Comparing wavelet power spectra and annual men temperature between the original and various homogenized at HN



Average wavelet power for the daily mean temperature anomaly series 1960-2008(1960-2004 for TPR) at HN



The annual mean temperature in original and various homogenized series 1960-2008 (1960-2004 for TPR) at HN

Influences on trends of mean temperature and extremes at HN

	Mean	Hot day	Cold day	Heat wave	Cold surge
Original	-0.273*	-4.73*	2.92*	-0.76*	0.23
MASH	0.240*	3.44*	-1.19	0.26*	-0.25
MASH-wavelet	0.241*	3.25*	-1.41	0.30*	-0.23
TPR	0.289*	3.70*	-2.13*	0.33*	-0.39*
TPR-wavelet	0.290*	3.36*	-2.13*	0.35*	-0.32
HOM	0.251*	3.33*	-1.90*	0.28*	-0.31*
HOM-wavelet	0.252*	3.17*	-2.02*	0.32*	-0.28*
RHtest	0.476*	4.21*	-8.67*	0.45*	-1.12*

Linear trends in original and various homogenized annual mean temperature and climate extreme series since 1960 at HN.

(* denotes the linear trends significant at $\alpha = 0.05$)

Conclusion

- Most of current methods adjust inhomogeneities mainly regarding the mean levels, but hardly identify those hidden in variability of different timescales.
- The wavelet-analysis-based method by this study adjusts those inhomogeneities unsolved with conventional approaches.
- The wavelet adjustments do not influence on estimating trends in mean temperature; but do on estimating climate extremes and changes.