

Natural convection instability during carbon dioxide storage into deep saline aquifers



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Processes

• Fluid mass balance equation of water and vapor

$$\frac{\partial[\phi(1-S_w)\rho_{gw}]}{\partial t} - \nabla \cdot \left[\rho_{gw} \frac{kk_{rw}}{\mu_g} \nabla p_g \right] - \nabla \cdot \left[\rho_g \frac{M_a M_w}{M_g^2} \mathbf{D}_{eff} \nabla \left(\frac{p_{gw}}{p_g} \right) \right] = - \frac{\partial[\phi S_w \rho_w]}{\partial t} + \nabla \cdot \left[\rho_w \frac{kk_{rw}}{\mu_w} \nabla p_w \right]$$

• Fluid mass balance equation of CO₂

$$\frac{\partial[\phi(1-S_w)\rho_{gs}]}{\partial t} - \nabla \cdot \left[\rho_{gs} \frac{kk_{rg}}{\mu_g} \nabla p_g \right] + \nabla \cdot \left[\rho_g \frac{M_a M_w}{M_g^2} \mathbf{D}_{eff} \nabla \left(\frac{p_{gw}}{p_g} \right) \right] = 0$$

• Energy balance equation

$$(\rho c_p)_{eff} \frac{\partial T}{\partial t} - \left[\rho_w c_{pw} \frac{kk_{rw}}{\mu_w} \nabla p_w + \rho_g c_{pg} \frac{kk_{rg}}{\mu_g} \nabla p_g \right] \cdot \nabla T - \nabla \cdot [\kappa_{eff} \nabla T] = \Delta H_{VAP} \left(\frac{\partial[\phi S_w \rho_w]}{\partial t} - \nabla \cdot \left[\rho_w \frac{kk_{rw}}{\mu_w} \nabla p_w \right] \right) \rightarrow \dot{m}_{vap}$$

$$(\rho c_p)_{eff} = \phi S_w \rho_w c_{pw} + \phi(1-S_w) \rho_g c_{pg} + (1-\phi) \rho_s c_{ps}$$

$$\kappa_{eff} = \phi S_w \kappa_w + \phi(1-S_w) \kappa_g + (1-\phi) \kappa_s$$

EOS

| Fluid Properties | Meaning | Ref | Unit |
|---------------------------------|--|-----|--|
| Water density | $\rho_w = \rho_{w0} [1 - \beta_T (T - T_0)]$ | | kg · m ⁻³ |
| Gas density | $\rho_g = \frac{M_a \cdot P_{gw} + M_s \cdot P_g}{R \cdot T}$ | | kg · m ⁻³ |
| Water viscosity | $\mu_w = a + b \cdot T + c \cdot T^2 + d \cdot T^3$ | | Pa · s |
| Gas viscosity | $\mu_g = X_{N_2} \cdot \mu_{N_2} + X_{CO_2} \cdot \mu_{CO_2}$ | | Pa · s |
| Water heat capacity | $c_{pw} = a + b \cdot T + c \cdot T^2$ | | J · kg ⁻¹ · K ⁻¹ |
| Gas heat capacity | $c_{pg} = X_{N_2} \cdot c_{pN_2} + X_{CO_2} \cdot c_{pCO_2}$ | | J · kg ⁻¹ · K ⁻¹ |
| Water conductivity | $\kappa_w = a + b \cdot T + c \cdot T^2$ | | W · m ⁻¹ · K ⁻¹ |
| Gas conductivity | $\kappa_g = X_{N_2} \cdot \kappa_{N_2} + X_{CO_2} \cdot \kappa_{CO_2}$ | | W · m ⁻¹ · K ⁻¹ |
| Enthalpy of vaporization | $\Delta H_{vap} = 2.6673 \cdot 10^7 \cdot (T_w - T)^{0.33}$ | | J · kg ⁻¹ |
| Saturated vapor pressure | $P_{gw} = P_{gw0} \cdot \exp \left[\frac{M_a \Delta H_{vap}}{R T_w} \left(\frac{1}{T} - \frac{1}{T_w} \right) \right]$ | | Pa |
| Vapor pressure | $P_g = P_{gw} \cdot \exp \left(\frac{M_s \Delta H_{vap}}{R T} \right)$ | | Pa |
| Effective diffusion coefficient | $D_{eff} = (1-S_w) \cdot 2.16 \cdot 10^{-10} \cdot \left(\frac{T}{T_w} \right)^{1.5}$ | | m ² · s ⁻¹ |
| Surface tension | $\sigma = 0.3258 \cdot \gamma^{1.258} - 0.3258 \cdot \gamma^{1.258} \cdot \chi^2 \left(1 - \frac{T}{647.3} \right)$ | | kg · s ⁻² |
| Vapor fraction | $X_{gw} = \frac{P_{gw}}{P_g}$ | | |

Numerical schemes

Weighted residuals for the weak form, spatially discretized based on Galerkin approach (hybrid monolithic/staggered scheme).

$$M_v \dot{\psi} + (A_v + K_v) \psi = f_v \quad \text{and} \quad M_T \dot{T} + (A_T + K_T) T = f_T$$

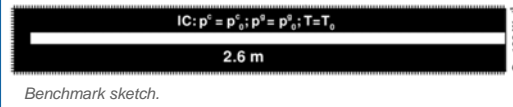
where $\psi = (p, p_c)^T$ stands for gas and capillary pressure unknowns at element nodes.

Generalized single step time discretization scheme.

$$[M + \theta \Delta t (A + K)] \xi^{m+1} = [M - (1-\theta) \Delta t (A + K)] \xi^m, \quad \text{With } \theta \geq 0.5$$

- Primary variables: gas pressure, capillary pressure and temperature
- Monolithic scheme for pressure and capillary pressure
- Staggered scheme for temperature
- Coupling terms calculated at each Gauss point by interpolating nodal values
- Picard linearization for nonlinear iterations

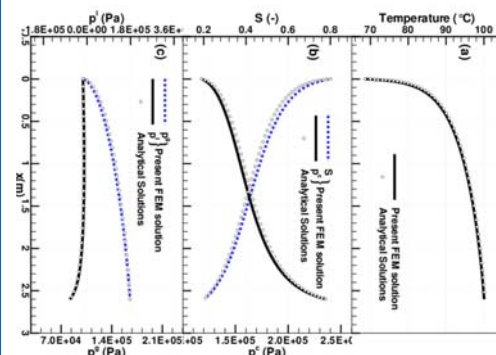
Benchmark



- The test benchmark problem for heat pipe effects is formulated in 1D column is filled with fluid subjected to heat flux $q_T=100$, at the right end where left end temperature maintained below to the saturation temperature
- Pressure gradients are derived for each phases in two-phase flow with heat transfer. Then obtained saturation gradient is integrated over two-phase regime. Two-phase zone is defined by imposing the limits of integration on saturation, i.e. $S=S_0$ at $x=0$ and $S=S_1$ at $x=L$. L is length of two phase zone.
- Decrease in vapour density is described by Kelvin equation and divergent form of temperature is obtained by using pressure gradients
- Coupled differential equations are integrated by using Euler method with following boundary conditions at $x=0$: $S=S_0$, $p_g=p_{g0}$, $p_c=p_{c0}$ and $T=T_{sat}$
- The scientific open source code OpenGeoSys for multi-phase flow is used for simulation

Geometry and material parameters.

| Meaning | Symbol | Value | Unit |
|----------------------------|------------|-----------------------|------------------------------------|
| Column length | L | 2.6 | m |
| Solid density | ρ_s | 2560 | kg m ⁻³ |
| Solid heat capacity | c_{ps} | 1200 | J kg ⁻¹ K ⁻¹ |
| Solid thermal conductivity | κ_s | 2.5 | W m ⁻¹ K ⁻¹ |
| Intrinsic permeability | k | 1.0×10^{-13} | m ² |
| Porosity | ϕ | 0.35 | - |
| Residual saturation | S_{rw} | 0.2 | - |
| Distribution index | λ | 2 | - |
| Entry pressure | p_d | Brooks Corey | Pa |
| Relative permeability | k_r | Brooks Corey | - |



Profiles of primary variable are compared with analytical solution for heat pipe example.

- Obtained solution for primary variables are well matched with the analytical solution
- Deviation at saturation distribution is due to saturation obtained by interpolating over gauss point
- The numerical model is implemented in the framework of the open source scientific software OpenGeoSys (OGS)
- OGS is based on object-oriented programming principles allowing model applications in various geotechnical areas

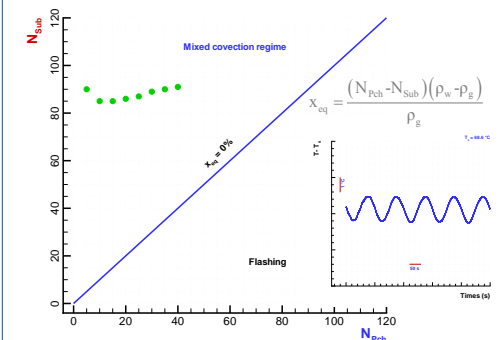
Application

- Two-phase natural convection and instability analysis by quality is presented for CCS into deep saline aquifers
- We assume that the aquifer is a partially saturated with CO₂ and water
- Potential two-phase flow instability, i.e. thermal oscillations is encountered. This is important for design and operation of CCS
- Structure and stability of the two-phase mixed convection process is characterized by N_{Sub} and N_{Pch}
- Identical N_{Sub} and N_{Pch} represent similar quality (x_{eq}) development of the flow.

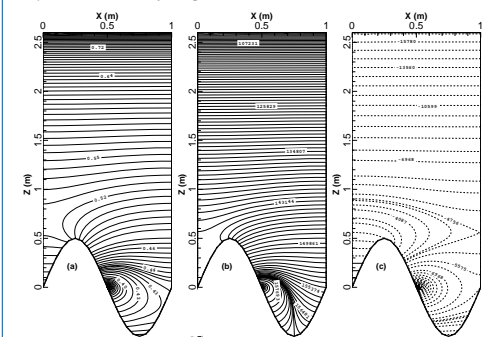
System geometry and boundary conditions.

Two numbers are defined as follow

$$N_{Pch} = \frac{(\rho_w - \rho_g) q_T}{\rho_g \dot{m}_{vap} \Delta H_{vap}} \quad \text{and} \quad N_{Sub} = \frac{(\rho_w - \rho_g) c_{pw} \Delta T}{\rho_g \Delta H_{vap}}$$



Operational stability diagram and thermal oscillations.



Distribution of the time averaged (a) saturation; (b) vapor pressure; (c) water pressure.

Conclusions

- Thermal oscillations occur at heat flux at $q_T=100 \text{ W m}^{-2}$, moreover its amplitude is depending on heat input
- Here, N_{Sub} and N_{Pch} are identical and quality $x_{eq} = 0\%$ showing stable two-phase flow.

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