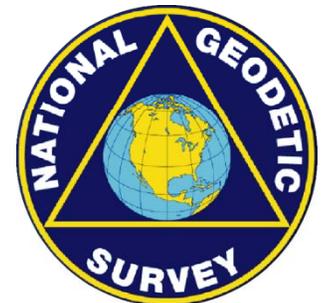


# STATUS OF IGS ORBIT MODELING & AREAS FOR IMPROVEMENT

- Earth radiation pressure (albedo) accelerations
  - see posters by C. Rodriguez Solano *et al.* (this afternoon)
- Spurious rotations & translations in AC solutions
  - compare Rapid & Finals daily orbits
  - check indirect AC orbit effects on polar motion, LOD, geocenter
  - study discontinuities between daily orbits
- Inconsistent AC yaw-attitude models
  - mostly affects clock estimates during eclipse season



**Jim Ray & Jake Griffiths**  
NOAA/National Geodetic Survey



EGU 2011, Session G2.4, Vienna, 8 April 2011

# Approaches to Study Orbit Errors

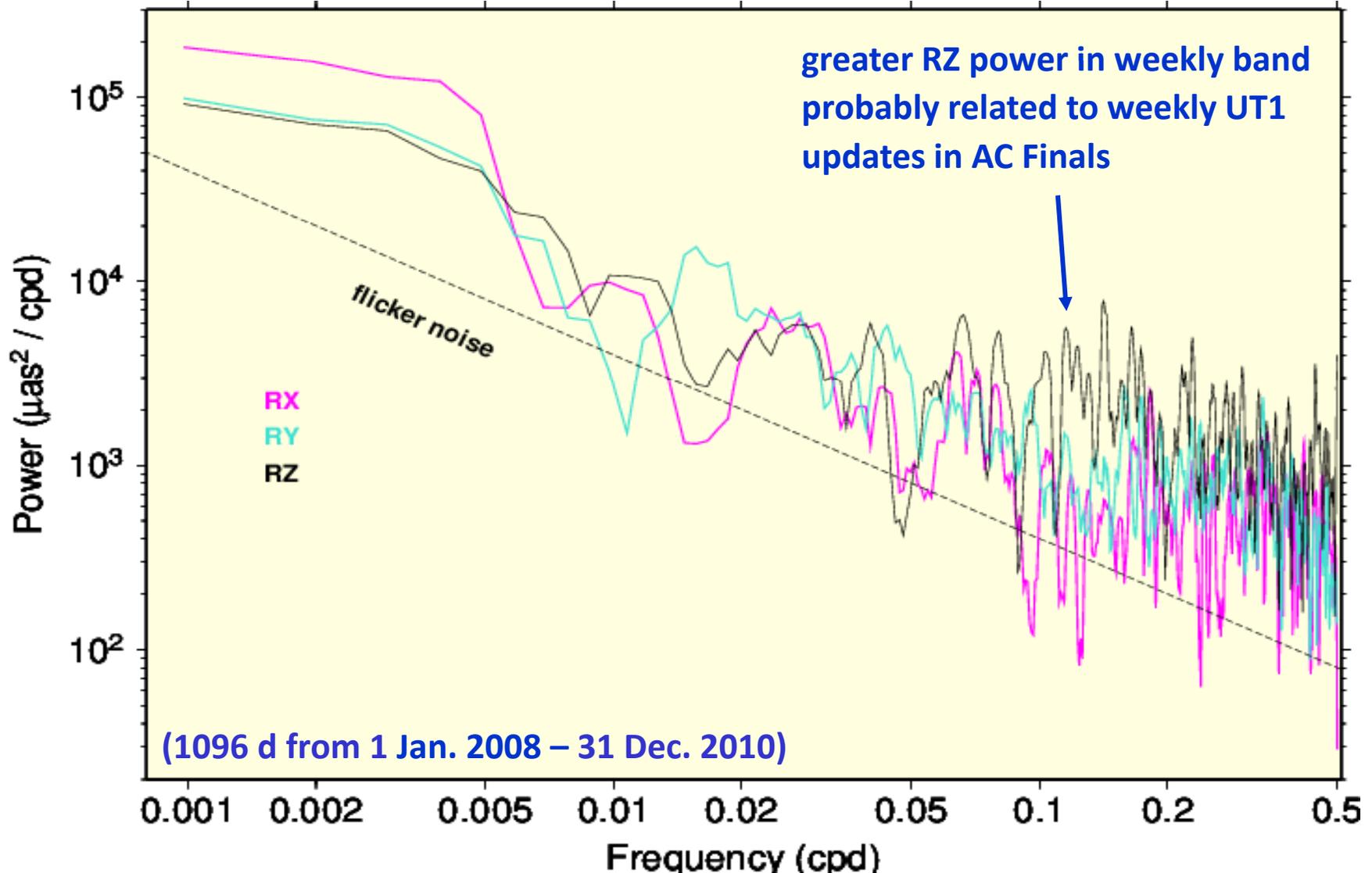
- **SLR ranging is only direct, independent method**
  - but just 2 old GPS Block IIA SVs with retro-reflectors (PRNs 05 & 06)
  - PRN05 was decommissioned in 2009
  - results suggest neglect of albedo shifts orbit origin few cm away from sun
  - not considered here → see posters by C. Rodriguez Solano *et al.*
- Or, can **check indirect effects on polar motion, LOD, & geocenter estimates**
  - net constellation rotations about RX & RY should ideally match polar motion offsets in PMy & PMx
  - LOD changes are indistinguishable from  $-dRZ/dt$ , net rate of satellite Right Ascensions (axial rotation rate)
  - compare LOD to independent multi-technique UT1+LOD combinations
  - compare geocenter motion to SLR & load models
- Can also **study discontinuities** between daily orbits at ~24:00
  - samples 1 point in orbit per day
  - aliases any subdaily harmonic orbit errors into longer-period features (except S1 & S2)

# IGS Rapid vs Final Orbit Differences (mm)

	DX	DY	DZ	RX	RY	RZ	SCL	RMS	WRMS	MEDI	TOTAL ERROR
mean	-0.2	0.1	-0.1	1.7	<b>-4.1</b>	-2.1	0.7	6.2	<b>5.9</b>	5.4	<b>8.2</b>
std dev	0.7	0.8	1.4	<b>5.0</b>	<b>4.7</b>	<b>4.6</b>	1.4	1.0	1.0	1.0	<b>(1D)</b>

- Compare 3 years of daily orbits: 1 Jan 2008 to 31 Dec 2010
- Net daily constellation **rotations are a leading orbit error**
  - must come mostly from modeling of satellite dynamics
  - note non-zero RY mean bias
- Implies **short-period orbit precision  $> 8.2/\sqrt{2} \approx 5.8$  mm**
  - this is **1D lower-limit** estimate  $\Rightarrow$  3D precision is  $>10.1$  mm
  - common-mode errors (e.g., subdaily EOP tide model) not visible here
- Other **common-mode IGR/IGS errors also not visible here**
  - long-period ( $> 1$  d) errors
  - e.g., due to Reference Frame or analytical form of empirical orbit model

# Spectra of (Rapid-Final) Orbit Rotation Differences

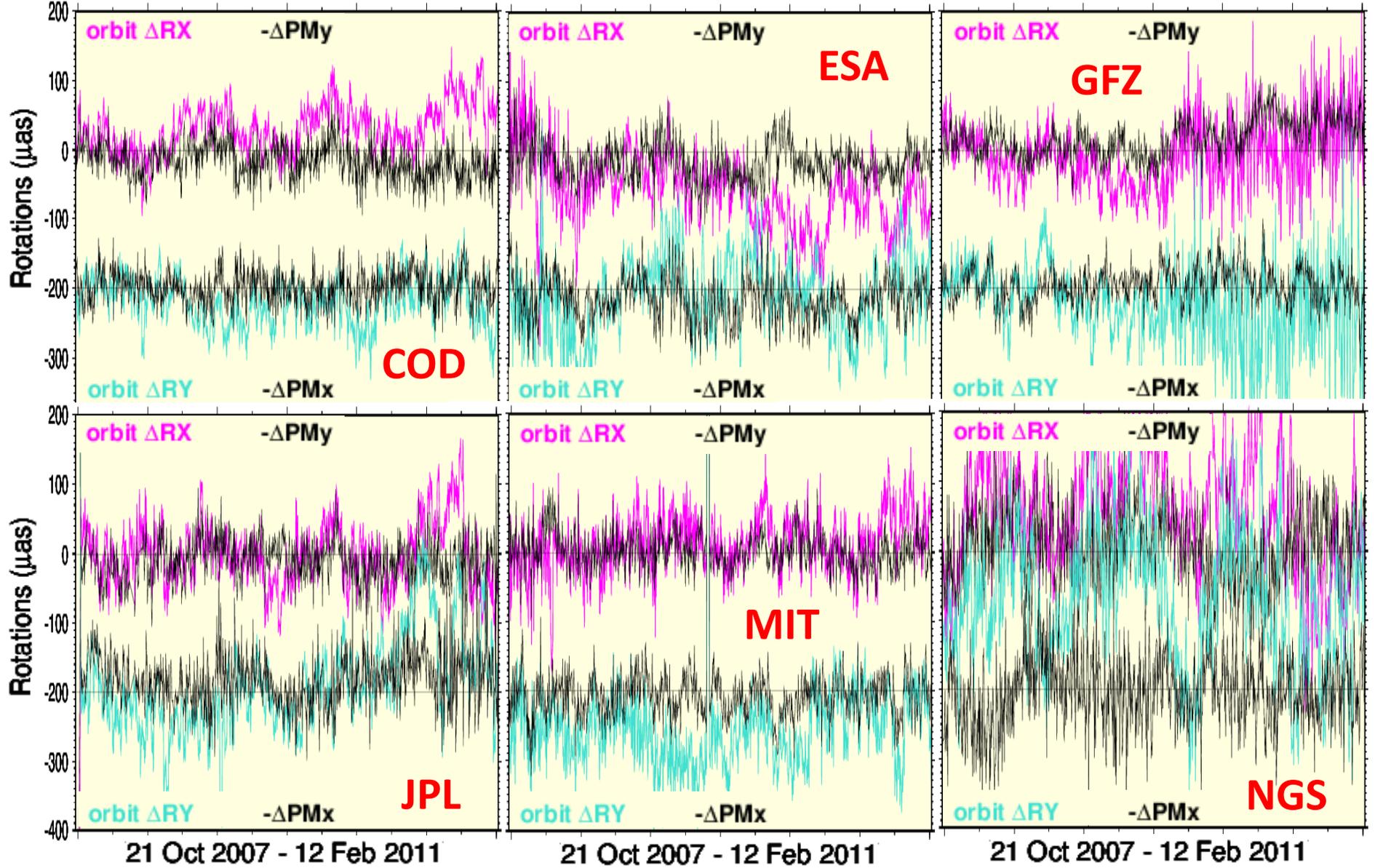


- Rotation differences nearly featureless
  - except for **background of flicker noise** down to sub-weekly periods

# AC Orbit & Polar Motion Consistency

- A constant rotational shift of TRF, e.g., should offset orbit frame & polar motion (PM) equally
  - expect: orbit  $R_X \approx \Delta PM_y$  & orbit  $R_Y \approx \Delta PM_x$
- But, a net diurnal sinusoidal wobble of orbit frame will alias entirely into a PM bias
  - does not equal any net rotational offset of orbit frame
- Likewise, prograde diurnal PM errors can alias into empirical once-per-rev (12-hr) orbit parameters
  - e.g., due to errors in  $\sim 24$ -hr terms of subdaily EOP tide model
  - net impact on orbit frame depends on geometry of orbit planes & SRP model terms
- So, check of orbit frame vs PM rotational consistency can provide insights into AC analysis weaknesses
  - note, though, that most ACs apply some over-constraints on orbit and/or PM variations (only ESA & NGS claim none; CODE has strongest)

# Rotational Self-Consistency of IGS Final Orbits/PM

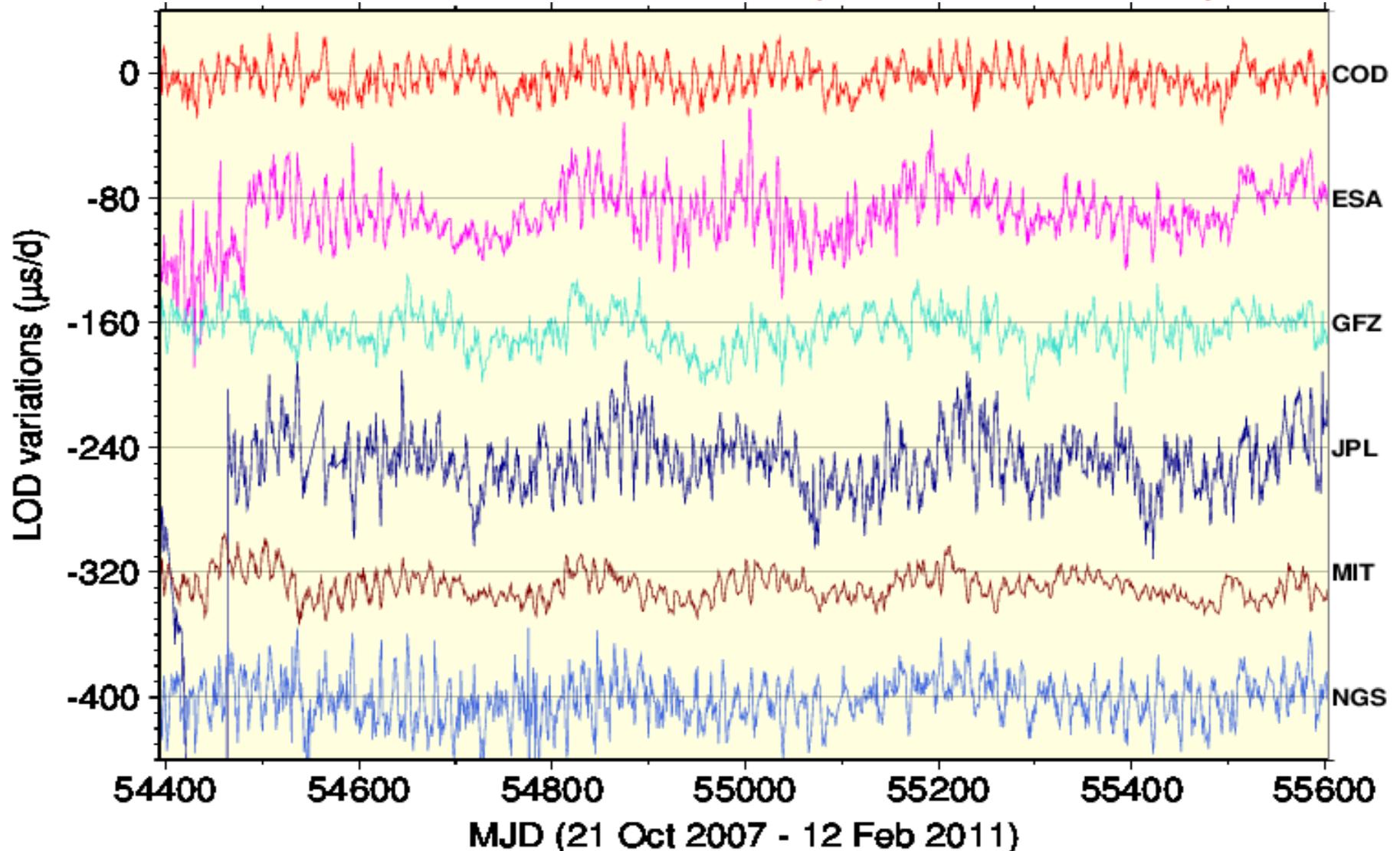


- Orbit rotations more variable than PM residuals for all ACs

# AC Orbit Modeling Differences

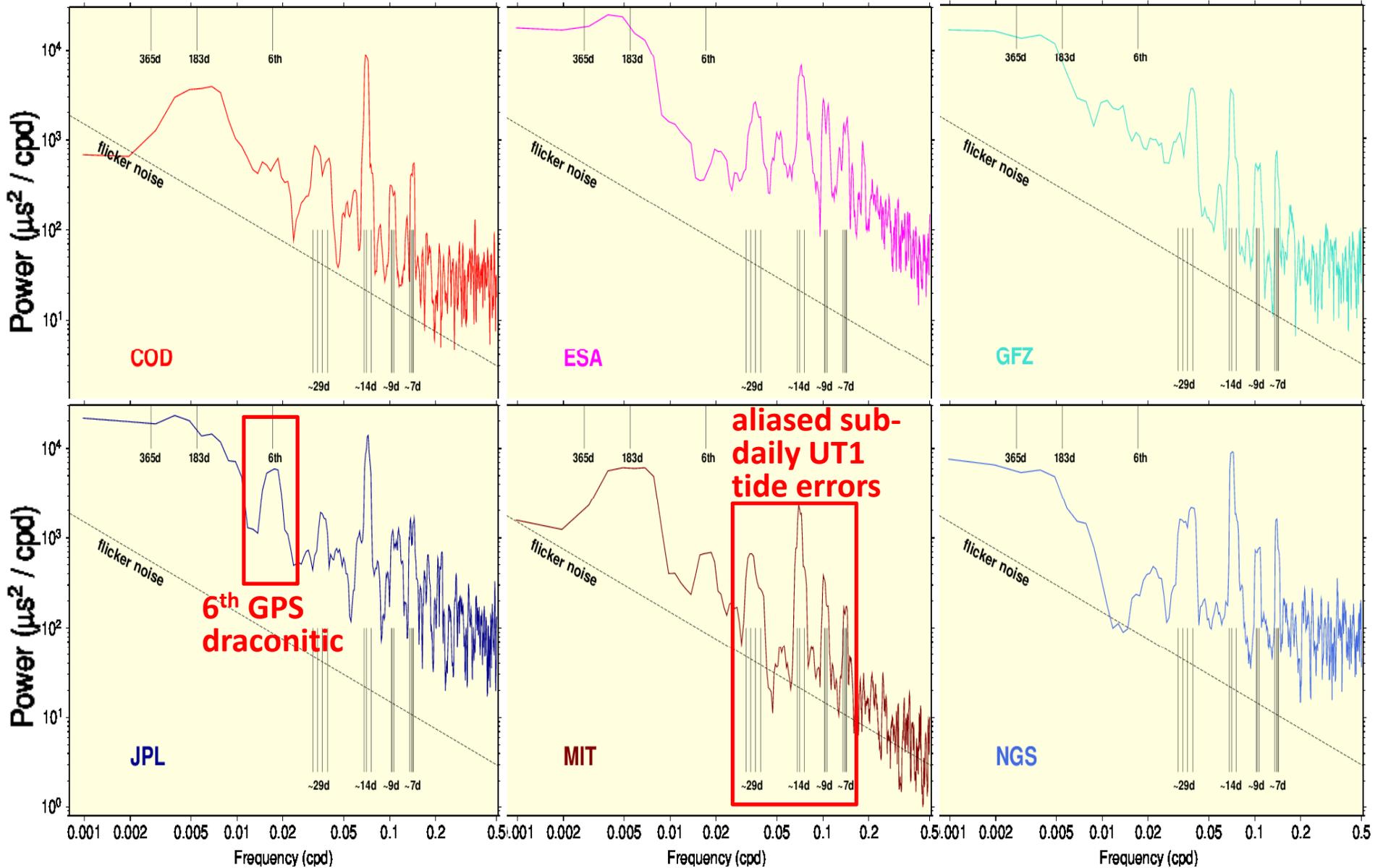
- **Most ACs use CODE Extended Orbit Model in some form, with empirical SRP parameters adjusted deterministically**
  - COD: D,Y,B scales + 1/rev in B + 12-hr velocity brks w/ constraints
  - ESA: D,Y,B scales + 1/rev in B + along-track offset & 1/rev
  - GFZ: D,Y,B scales + 1/rev in B + noon velocity brks
  - GRG: D,Y scales + 1/rev in D,B + velocity brks in eclipse
  - MIT: D,Y,B scales + 1/rev in D,Y,B w/ constraints
  - NGS: D,Y,B scales + 1/rev in B + noon velocity brks
  - SIO: D,Y,B scales + 1/rev in D,Y,B w/ constraints  
(frames oriented toward the Sun)
- **Except 2 ACs that use frame oriented toward the Earth with stochastic SRP estimation**
  - EMR: X,Y,Z scales + stochastic X,Y,Z
  - JPL: X,Y,Z scales + stochastic X,Y,Z
- **Geocenter & LOD estimates (among others) known to be sensitive to solar radiation pressure modeling**
  - especially Y & Z components of geocenter

# IGS Final LOD Residuals (AC – JPL KEOF)



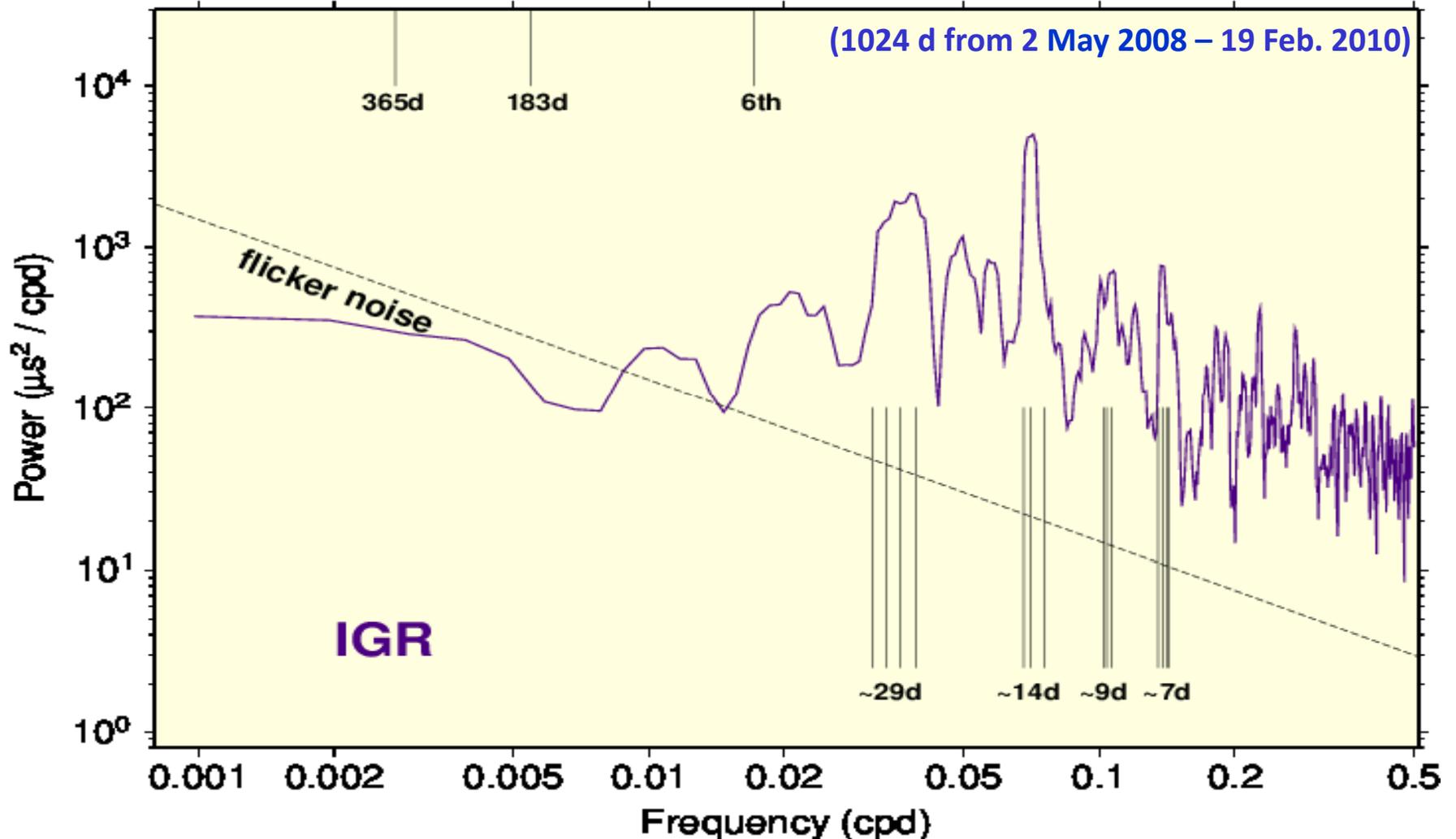
- Strong harmonic modulations visible for all ACs
  - but amplitudes vary among ACs

# Spectra of AC LOD Differences



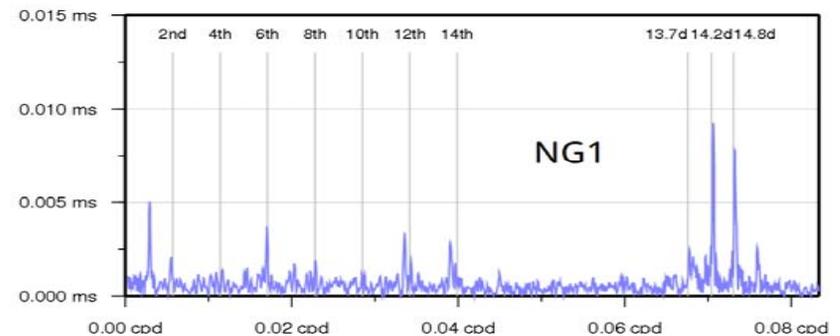
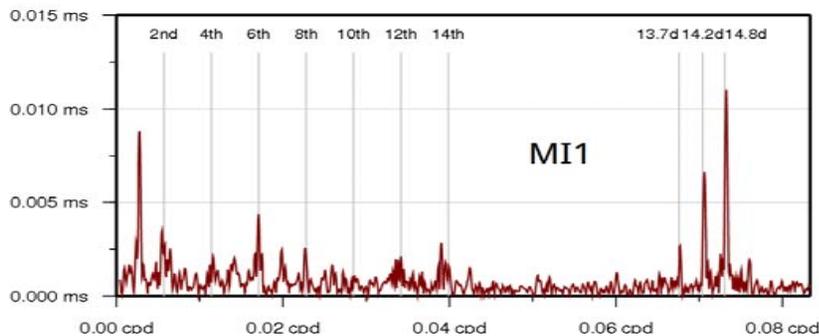
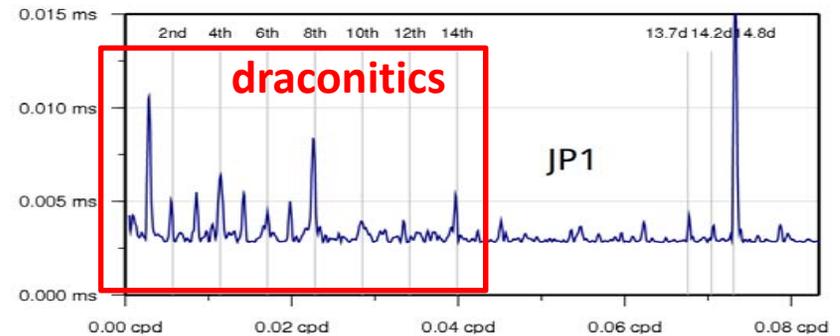
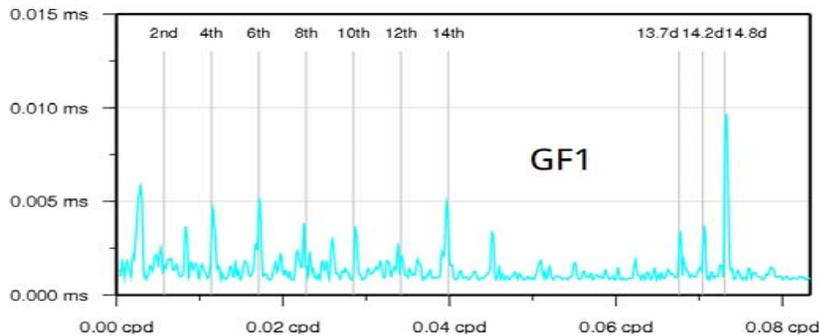
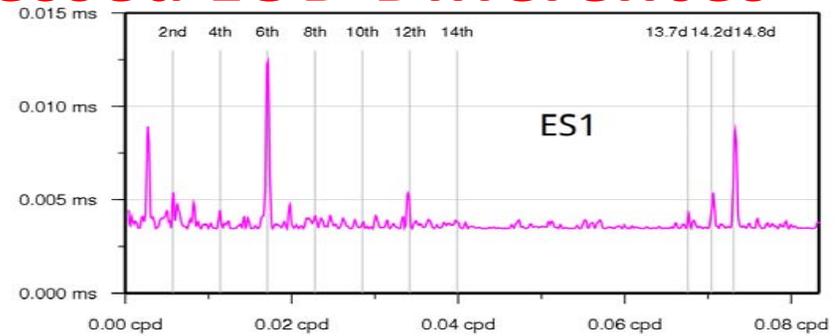
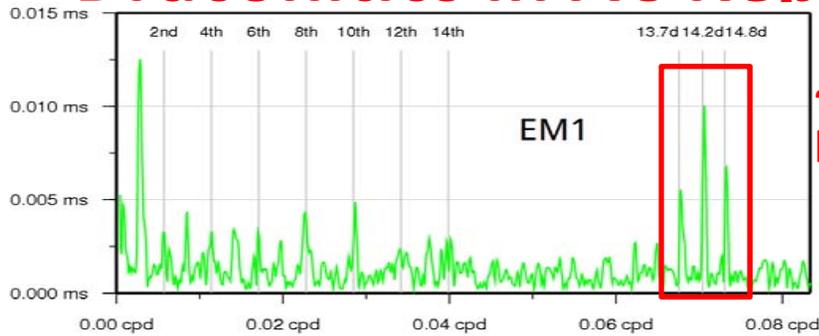
- Aliased subdaily UT1 errors, semi-annual, & 6<sup>th</sup> GPS draconitic

# Spectrum of IGS Rapid Combined LOD Differences



- IGS combination “calibrates” AC LOD biases by comparison with IERS Bulletin A over a 21-d sliding window
  - process seems effective at mitigating most LOD flicker & long-period noise

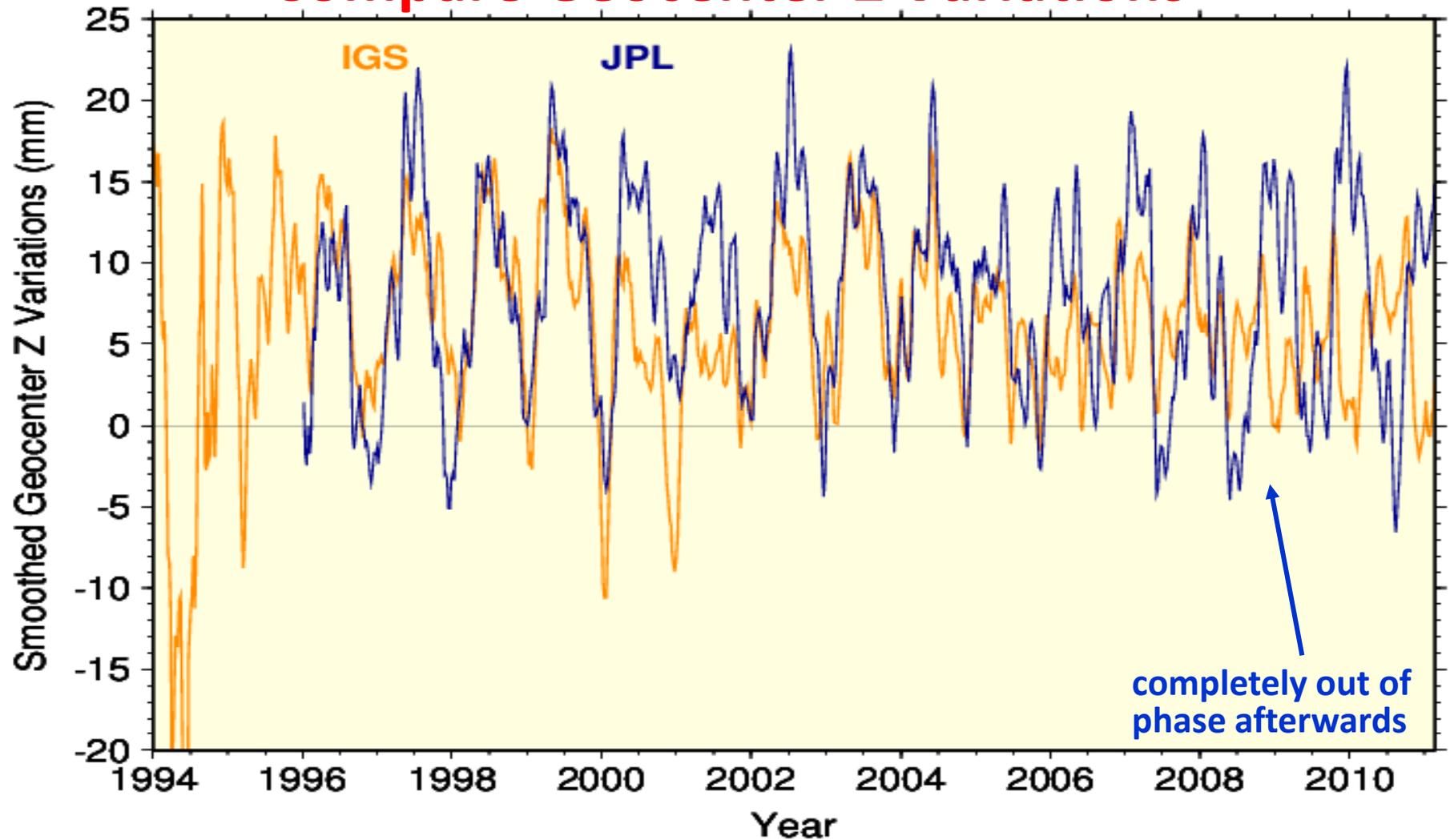
# Draconitics in AC Reprocessed LOD Differences



(from P. Rebischung, 2011)

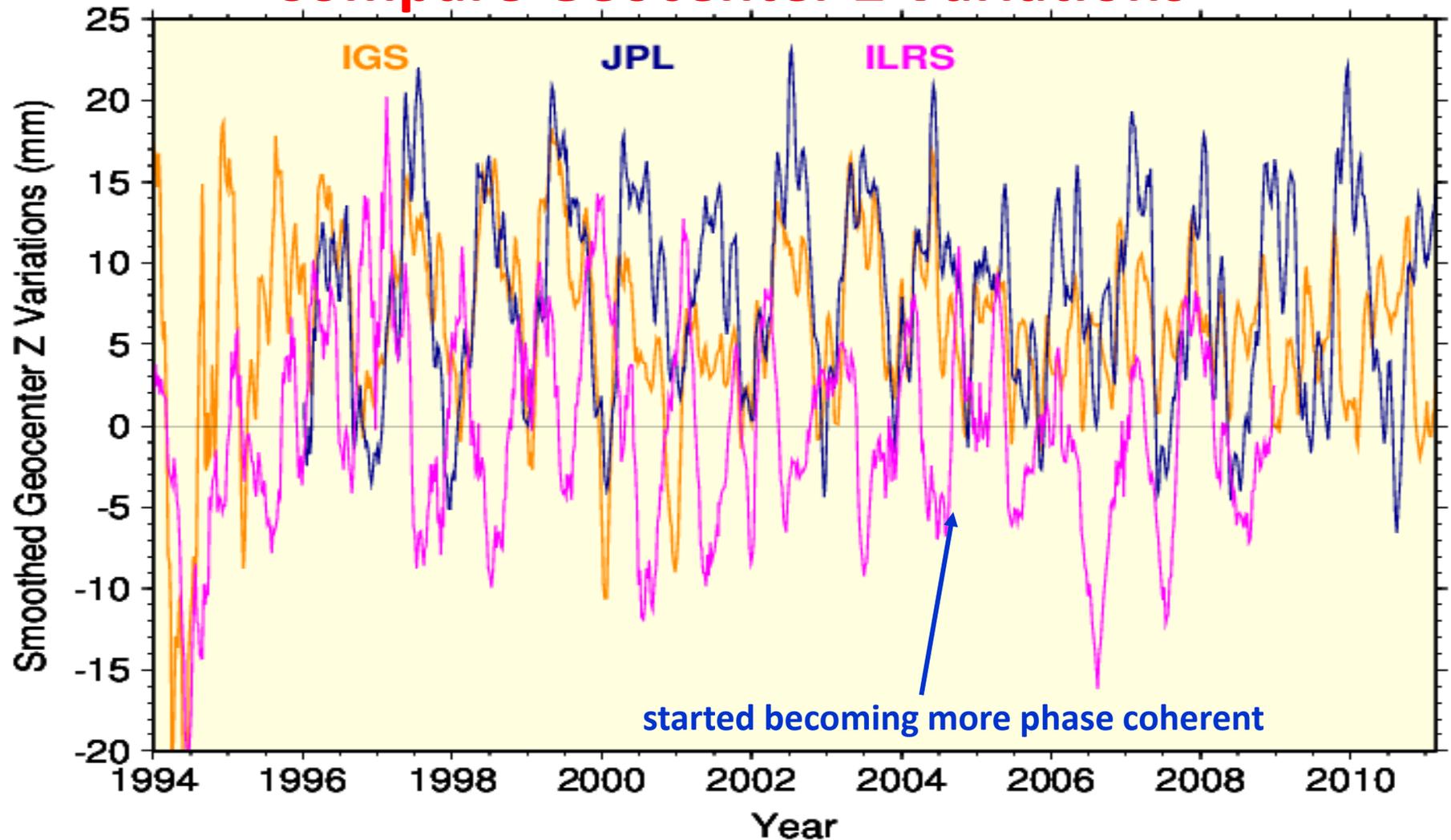
- Amplitude spectra from reprocessed years 1994/1998 - 2007
  - level of draconitics highly variable among ACs (but over long spans)

## Compare Geocenter Z Variations



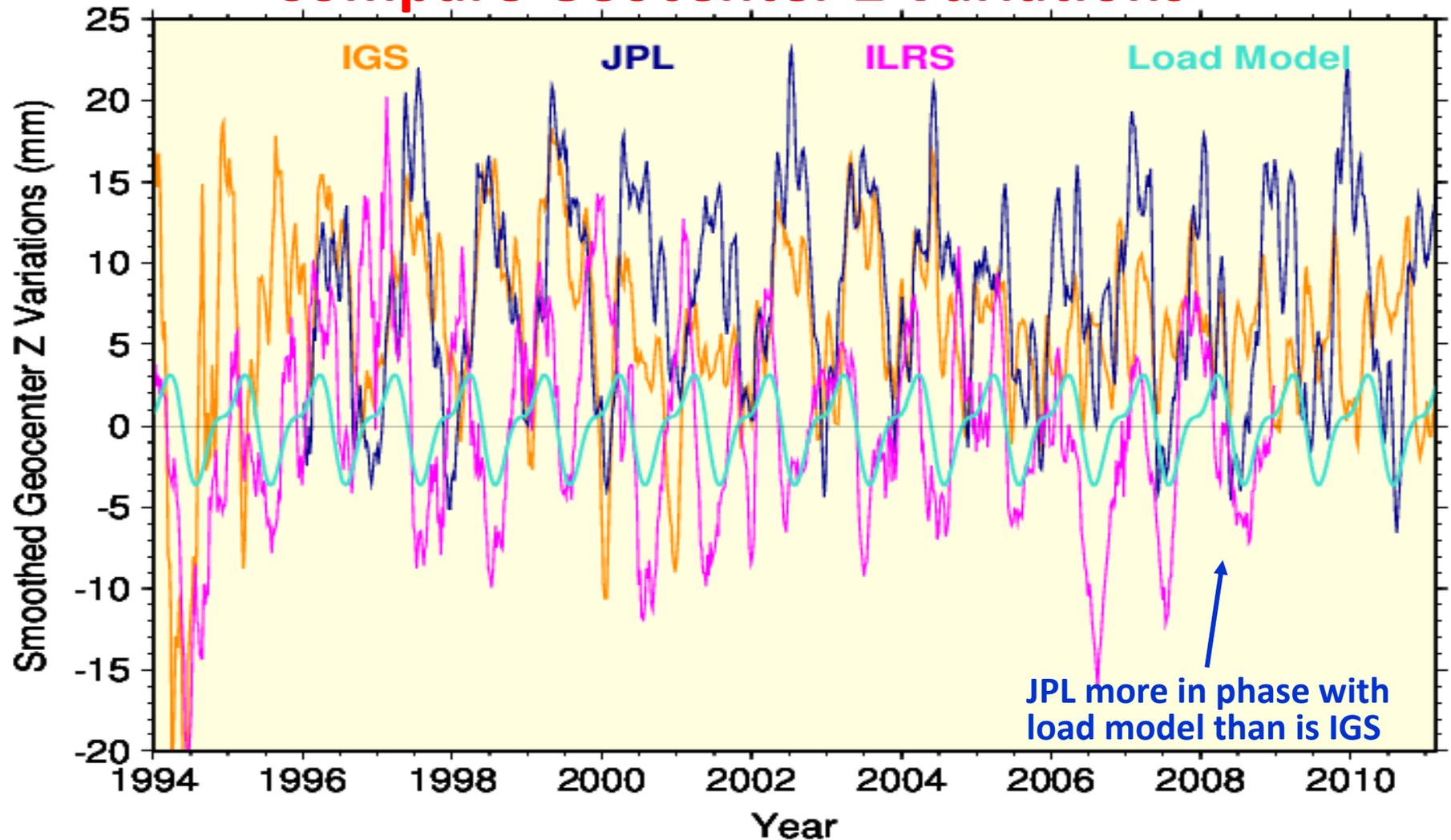
- IGS & JPL results from reprocessing + operations since 2007
  - out of phase with each other since ~2008.5

# Compare Geocenter Z Variations



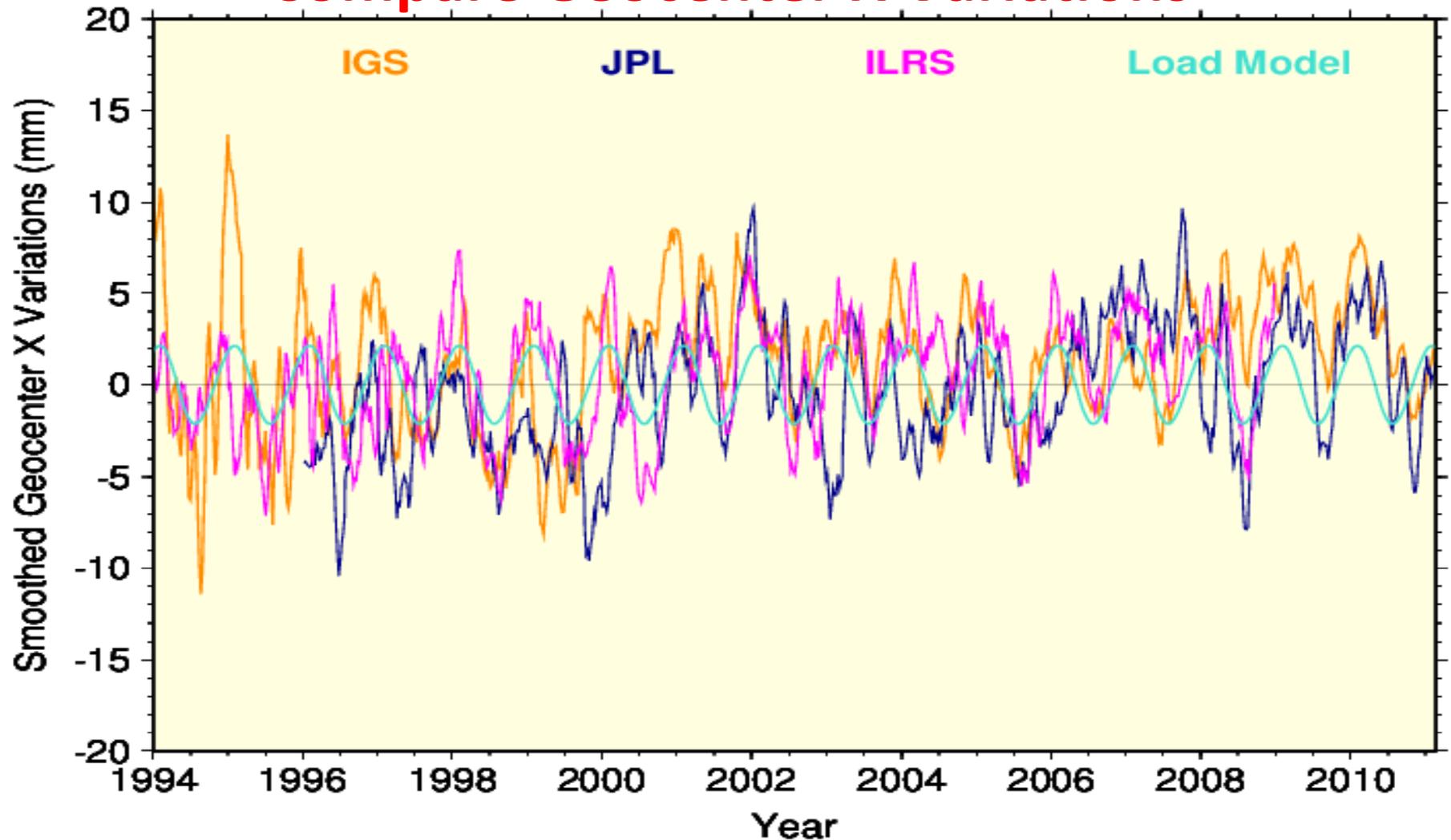
- ILRS results (from ITRF2008) mostly out of phase with IGS/JPL before ~2004.5
- IGS/JPL both show persistent bias

# Compare Geocenter Z Variations



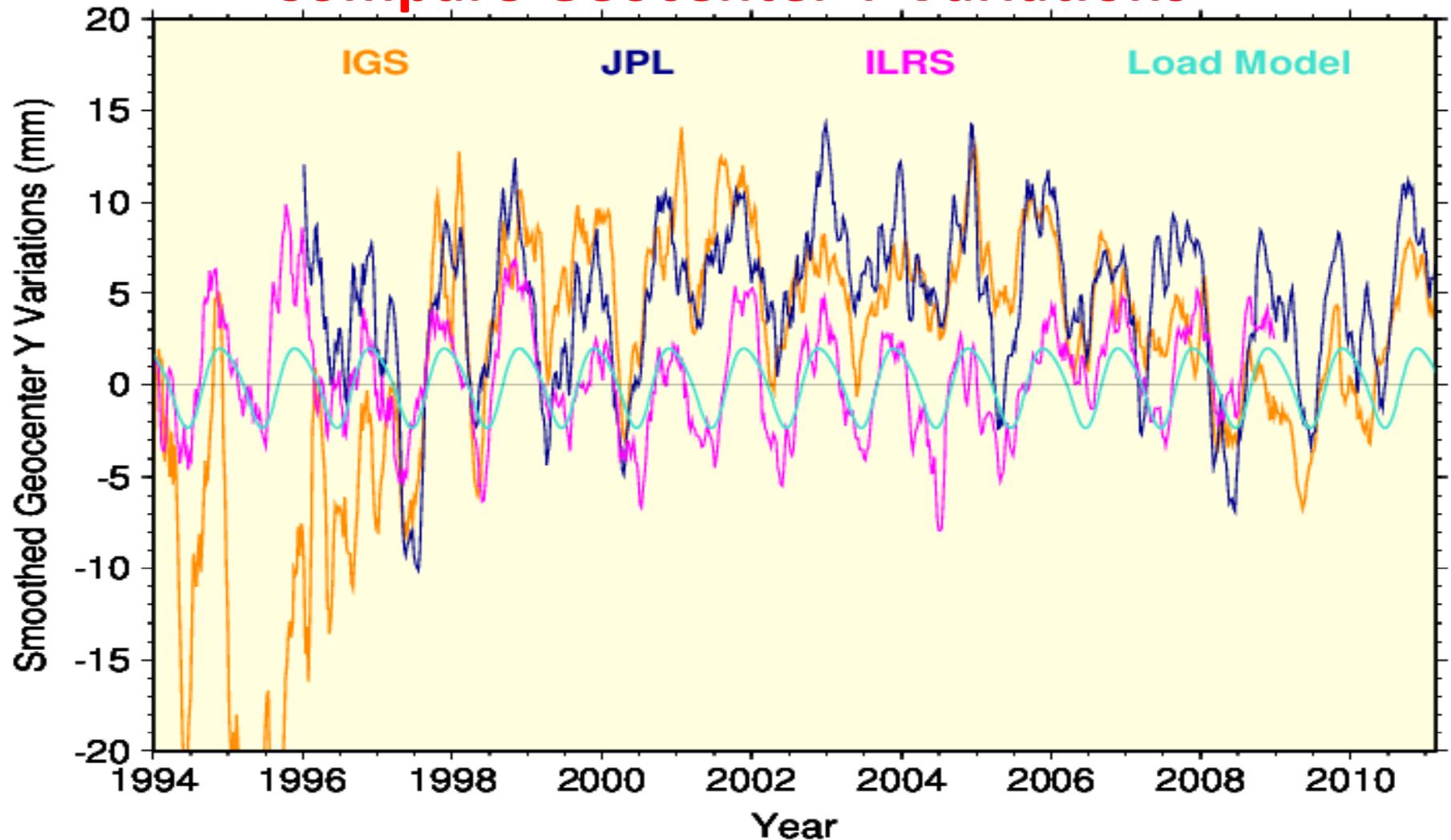
- **JPL Z geocenter more in phase with load model since ~2008**
  - recent IGS results are completely out of phase
  - may suggest recent JPL orbit modeling is better but amps are large

# Compare Geocenter X Variations



- **IGS & JPL agreement generally similar for X geocenter**
  - but IGS better at some times (e.g., 1999-2000 & 2003-2004)
  - long-term GNSS X origin less stable than ILRS or load model

## Compare Geocenter Y Variations

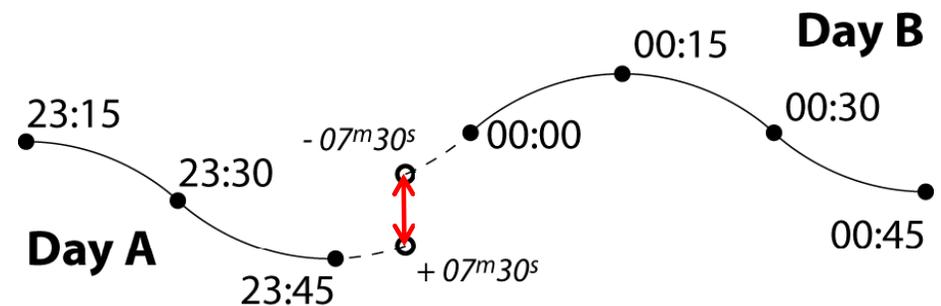


- IGS results strongly skewed before ~1998 for Y geocenter
  - both IGS & JPL poorly centered over most of span
  - probably mostly related to solar radiation pressure modeling

# Compute Orbit Discontinuities

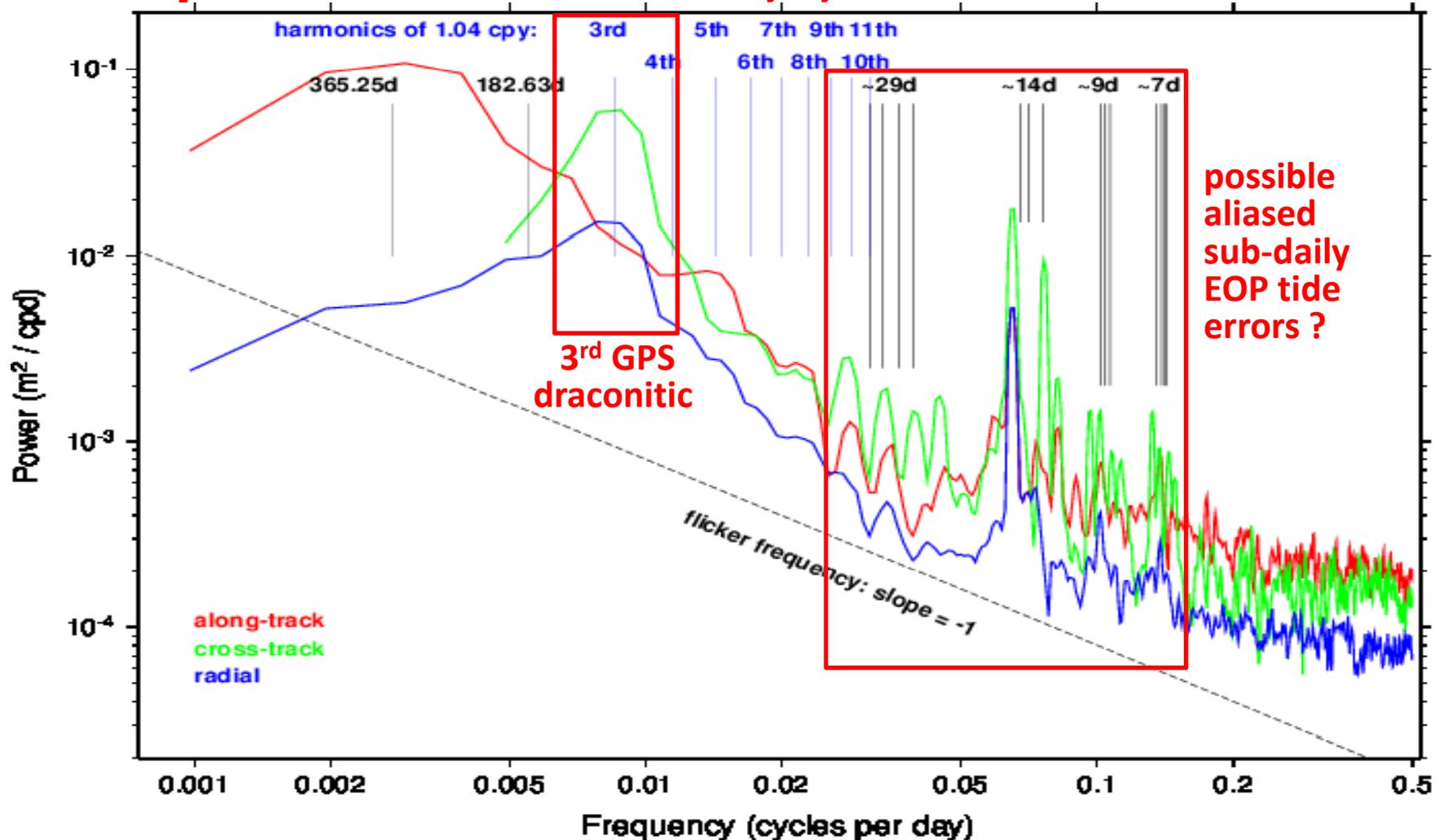
- Fit orbits for each day with BERNE (6+9) orbit model
  - fit 96 SP3 orbit positions for each SV as pseudo-observations for Day A
  - parameterize fit as  $X, Y, Z, \dot{X}, \dot{Y}, \dot{Z}$  plus 3 SRPs per SV component
  - propagate fit forward to 23:52:30 for Day A
  - repeat for Day B & propagate backwards to 23:52:30 of day before

- Compute A,C,R orbit differences at 23:52:30



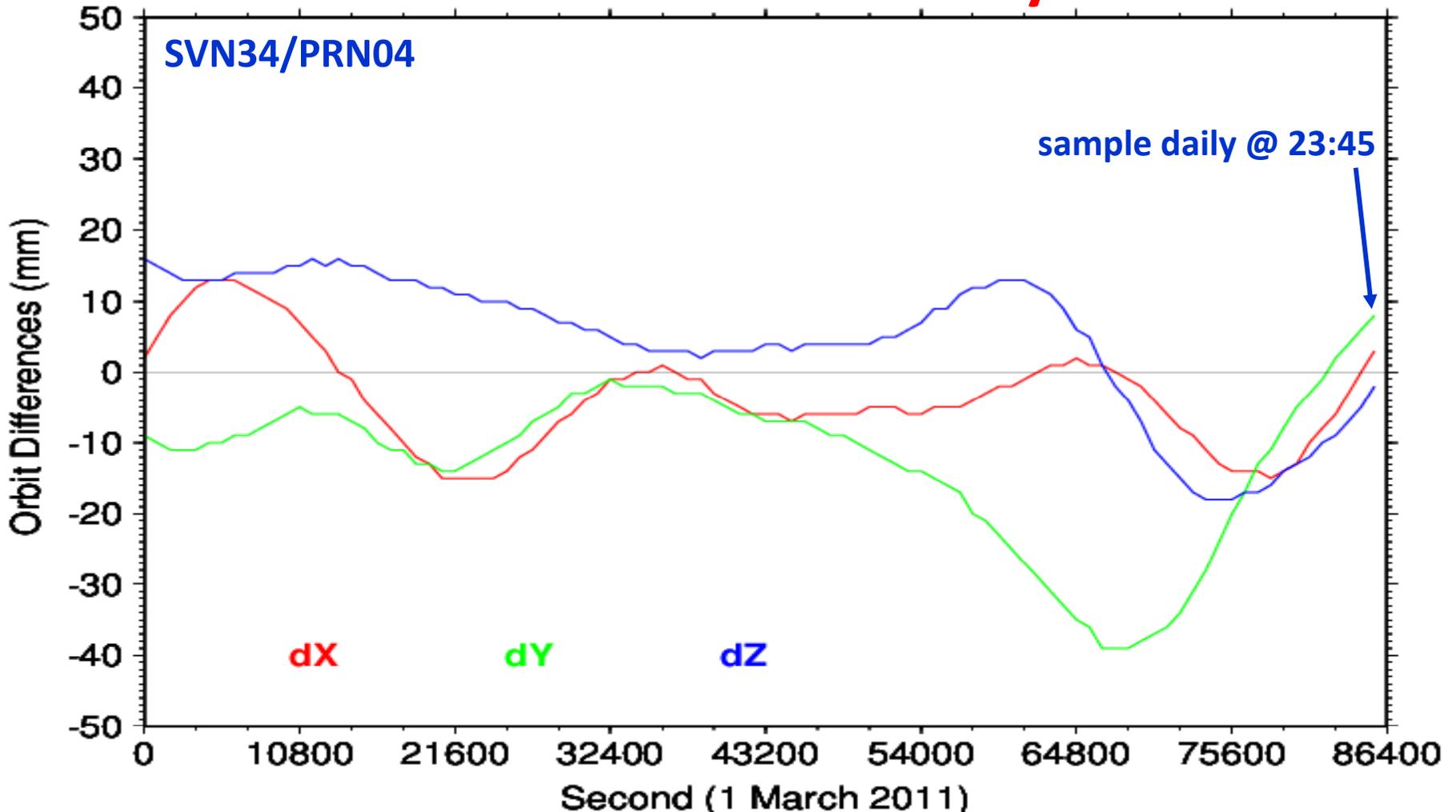
- Use 2049 d from 23 May 2005 thru 31 Dec 2010
  - spectra for all SVs stacked for each AC; data gaps linearly interpolated
  - sliding boxcar filter used to smooth across each 3 adjacent frequencies
  - previous procedures have been refined for improved results
- Power of fit/extrapolation error “calibrated” using similar test for observed values at 23:45

# Spectra of IGS Orbit A,C,R Discontinuities



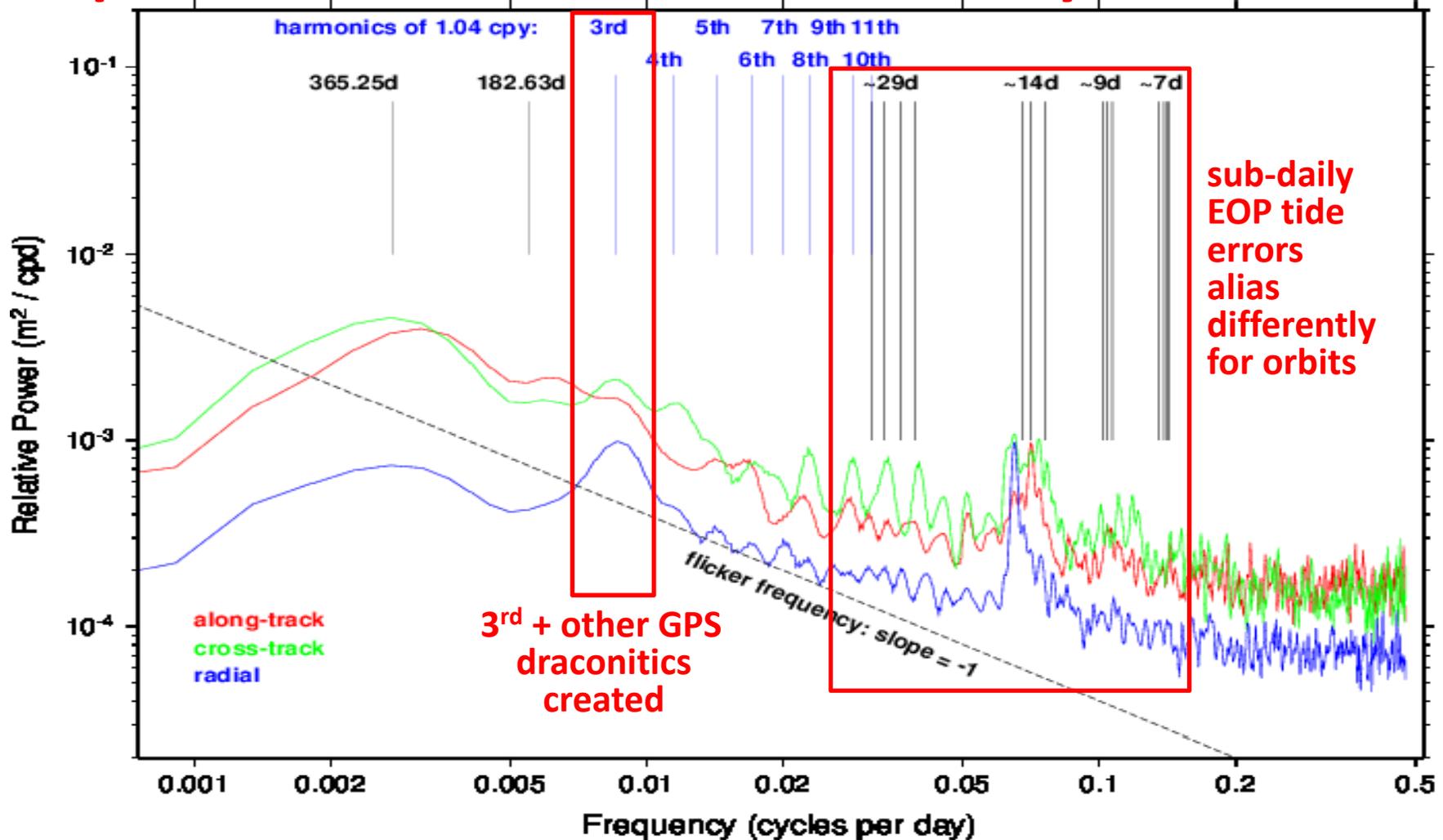
- Strong peaks near same **subdaily EOP alias lines** as LOD spectra
  - but **frequencies do not exactly match** aliases for 24-hr sampling
  - also effects differ for each A,C,R component
  - **3<sup>rd</sup> GPS harmonic** important in cross-track & radial components

# Simulate Orbit Errors from Subdaily EOP Model



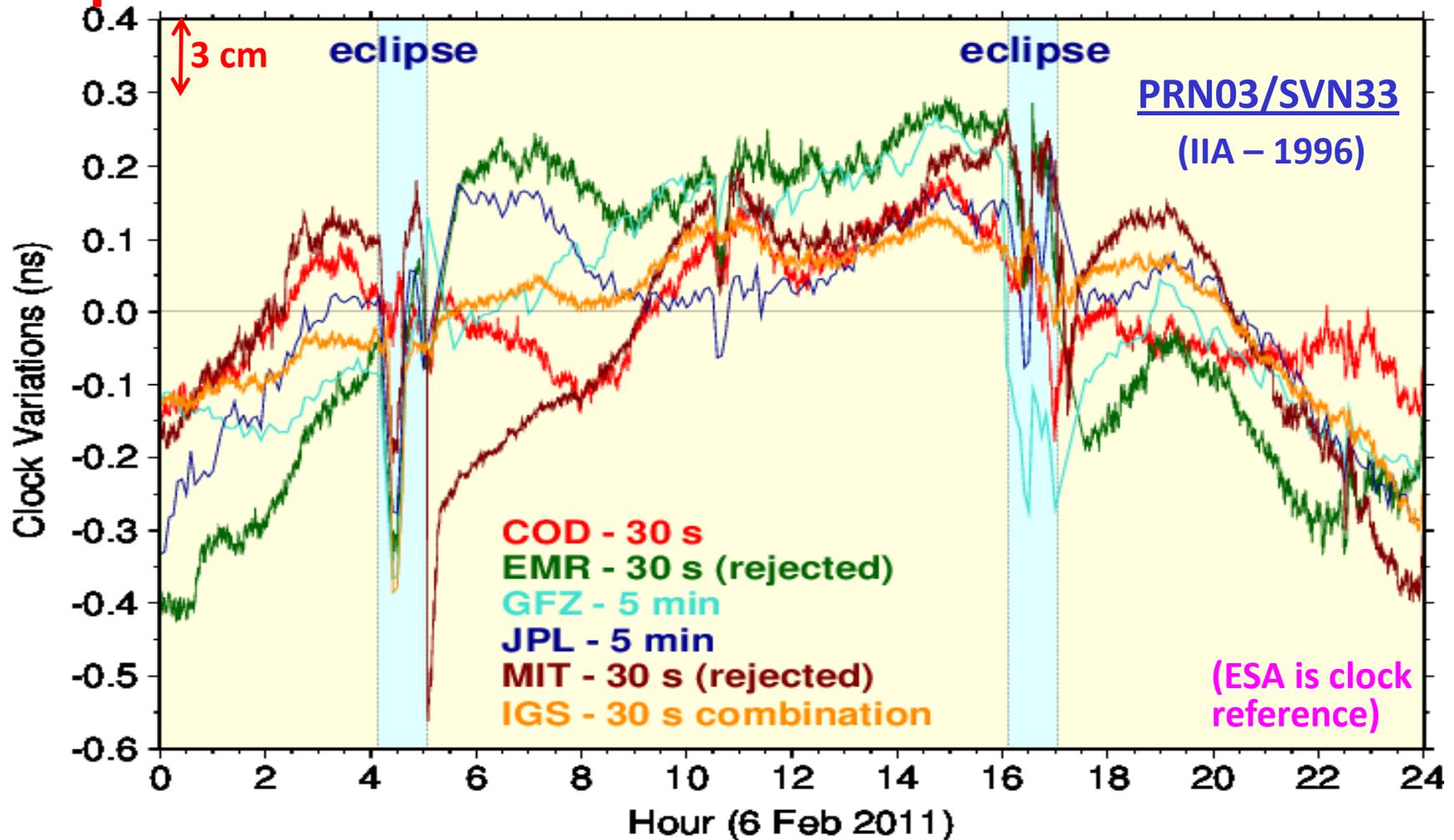
- Compare NGS orbits using IERS & **test subdaily EOP model**
  - for test EOP model, change tidal admittances by ~20%
  - sample daily differences at 23:45 & convert to A,C,R frame
  - subdaily periodic differences will alias to longer periods in spectra

# Spectra of Simulated A,C,R Subdaily EOP Errors



- Coupling of subdaily EOP errors into orbit parameters is complex
  - normal ~7, ~9, ~14, & ~29 d alias lines are split & frequency shifted
  - apparent **draconitic features created**, especially 3<sup>rd</sup> harmonic
  - large annual (K1 alias ?) signal but little semi-annual power

# Impact of AC Yaw-Attitude Models on GPS Clocks



- Diverse AC models for yaw-attitude variations during eclipse cause large clock discrepancies for older Block IIA GPS satellites
  - some ACs get rejected from clock combination
- **Must adopt a common yaw model** for ACs & PPP users

# Summary & Conclusions

- **Rotational variations are a leading IGS orbit error**
  - background spectrum shows flicker noise
  - probably is main source of flicker noise in station position time series
- **Larger variations in AC orbit frame rotations than polar motion**
  - cause is unclear but must be related to AC analysis methods
  - could be affected by *a priori* AC constraints
  - LODs show clear aliasing of subdaily EOP errors + 6<sup>th</sup> draconitic + semi-annual
- **Orbit discontinuities at day-boundaries reveal error details**
  - subdaily EOP tide errors alias very strongly into orbit parameters, especially in cross-track
  - but alias frequencies shifted & split compared to 1d sampling
  - annual or K1 tide alias errors important in along-track
  - 3<sup>rd</sup> & other draconitic harmonics created by subdaily EOP errors
- **Adoption of common model for yaw variations is mandatory**
  - otherwise combined SV clocks during eclipse are degraded