

# Dansgaard-Oeschger events: bifurcations in the climate system.

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## Introduction

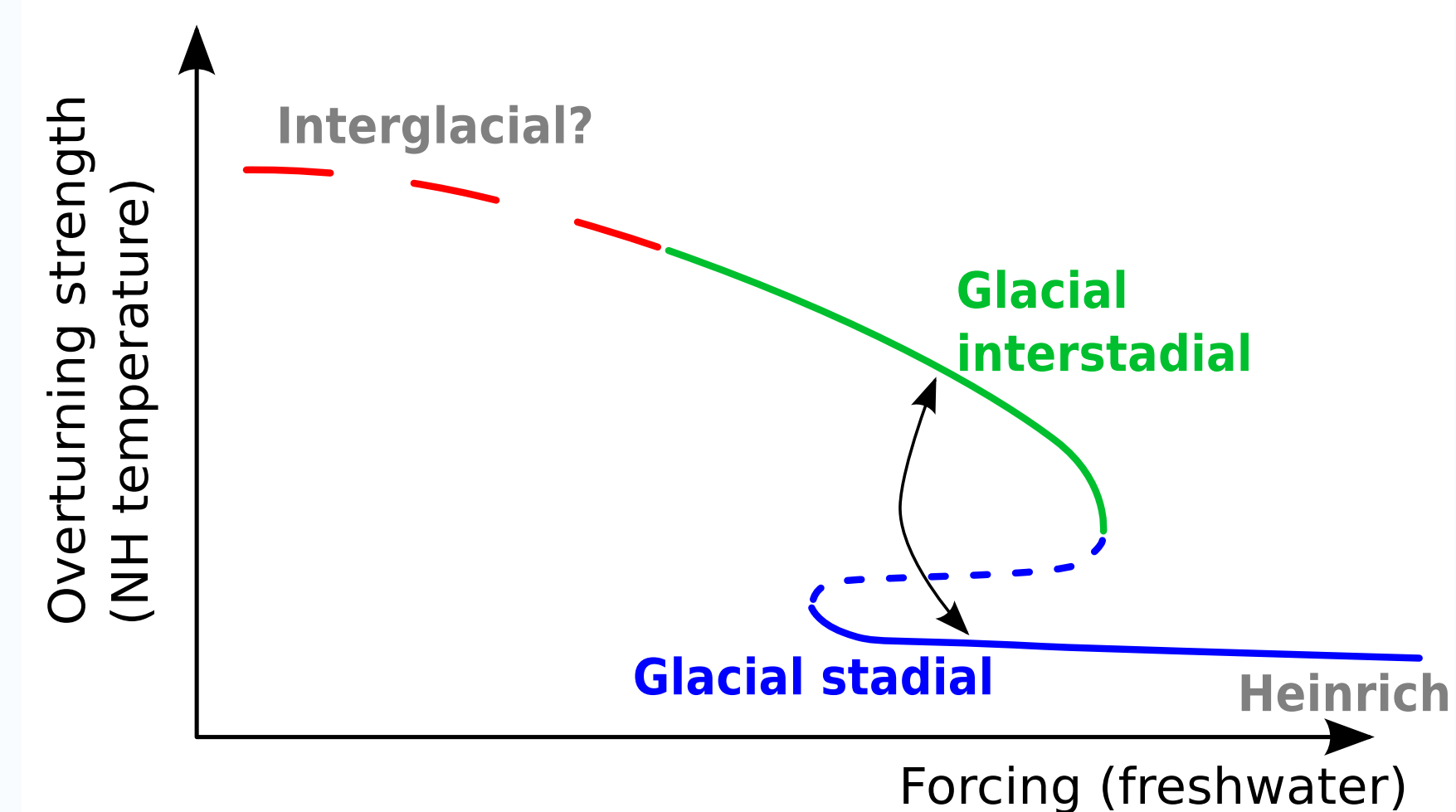
Dansgaard-Oeschger events represent the largest variability during last glacial age:

- Fast warming in the North Atlantic region (5–10°C in few decades)
- Slow cooling lasting hundreds to thousands of years
- Periodicity of approximately 1500 years

*Common hypothesis: connection with thermohaline circulation (THC).*

## Multiple equilibria

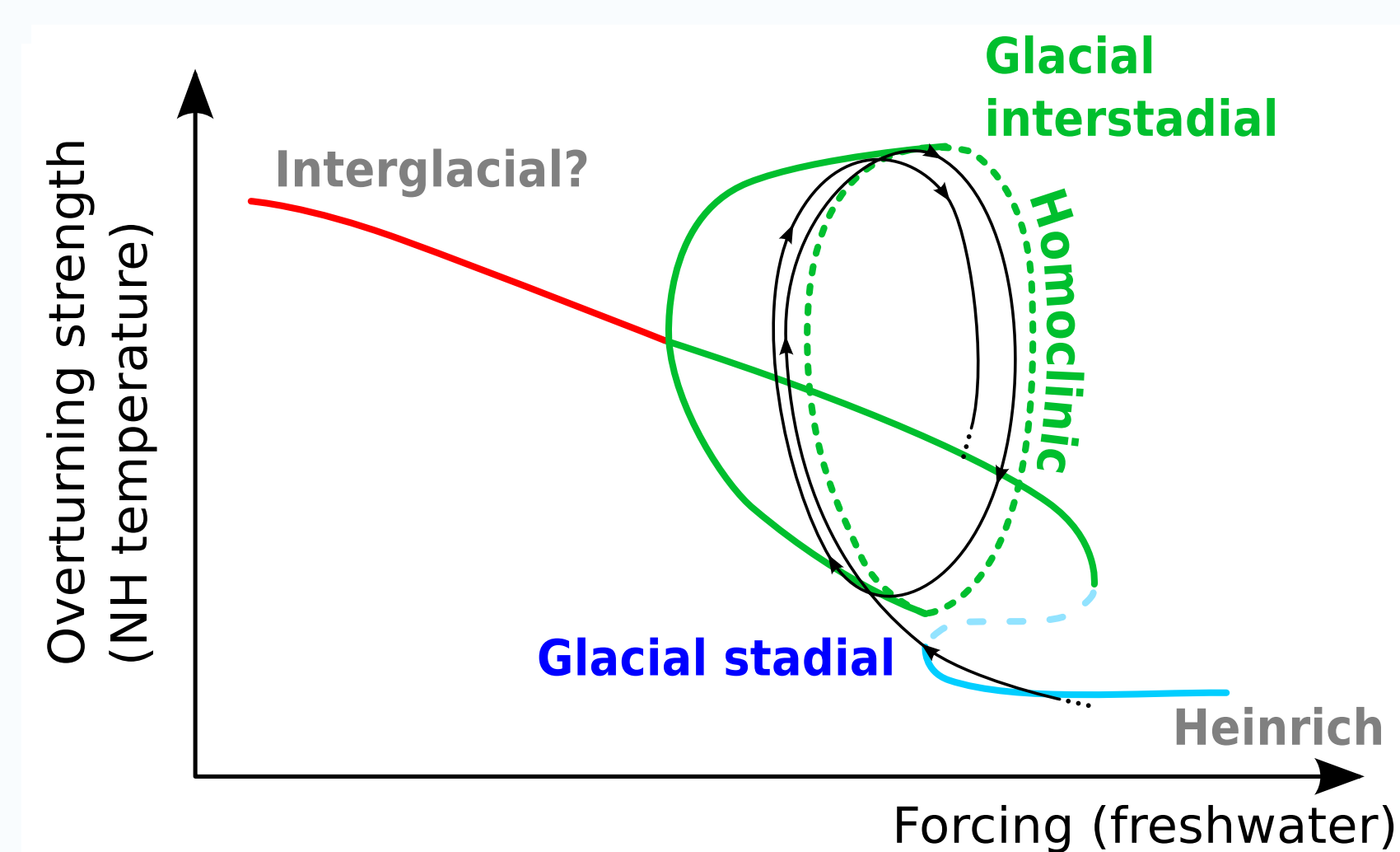
Response of THC (double saddle node structure) to an external forcing (noise+periodic component):



The basic mechanism is that of stochastic resonance [1].

## Periodic orbits

Interplay between THC and ice dynamics:



In connection with the presence of a fold-Hopf bifurcation, the system can undergo series of DO-events cycling close to a Homoclinic orbit [2].

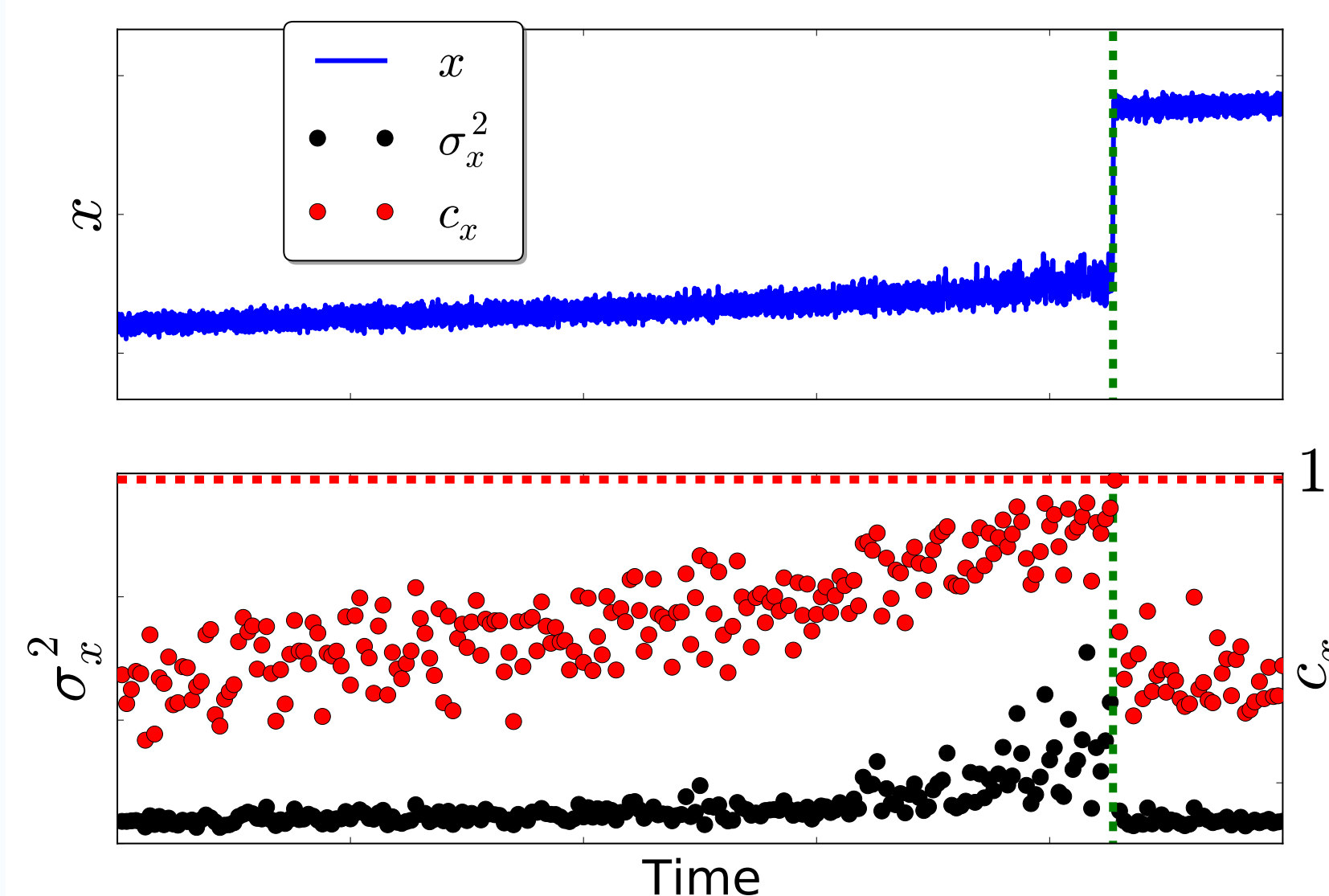
## From early warnings...

An approaching bifurcation can be associated with critical slowing down [3, 4].

- Slower decay of fluctuations = Increased autocorrelation  $c$  and DFA exponent  $\alpha$
- Larger fluctuations = Increased variance  $\sigma^2$

## ...to noise signatures...

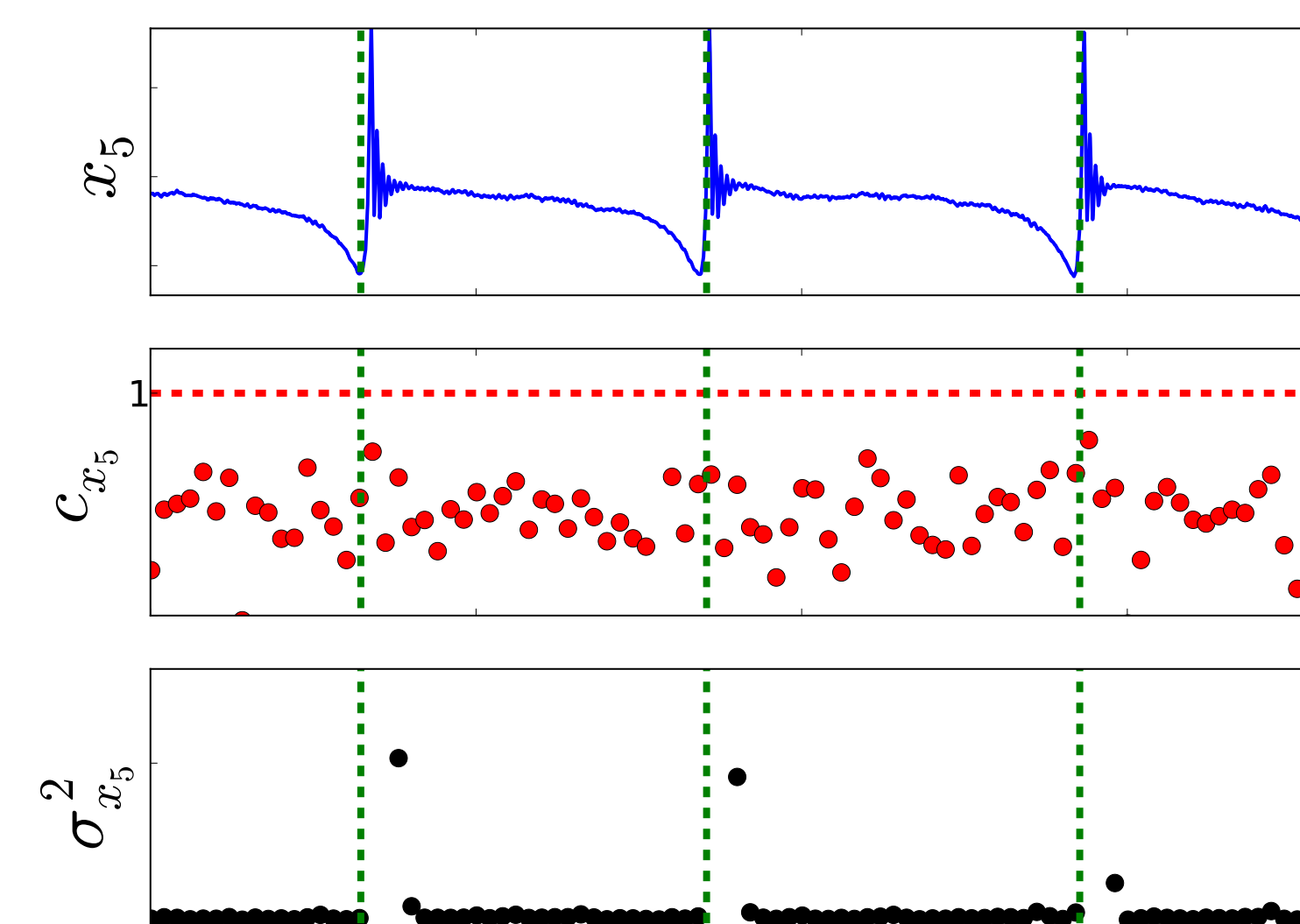
For a slowly changing parameter forcing a system to undergo a fold bifurcation we have a clear signature in the  $c$ ,  $\alpha$  and  $\sigma^2$ :



No such signal would be detected in the case of stochastic resonance!

## ...or no noise signatures

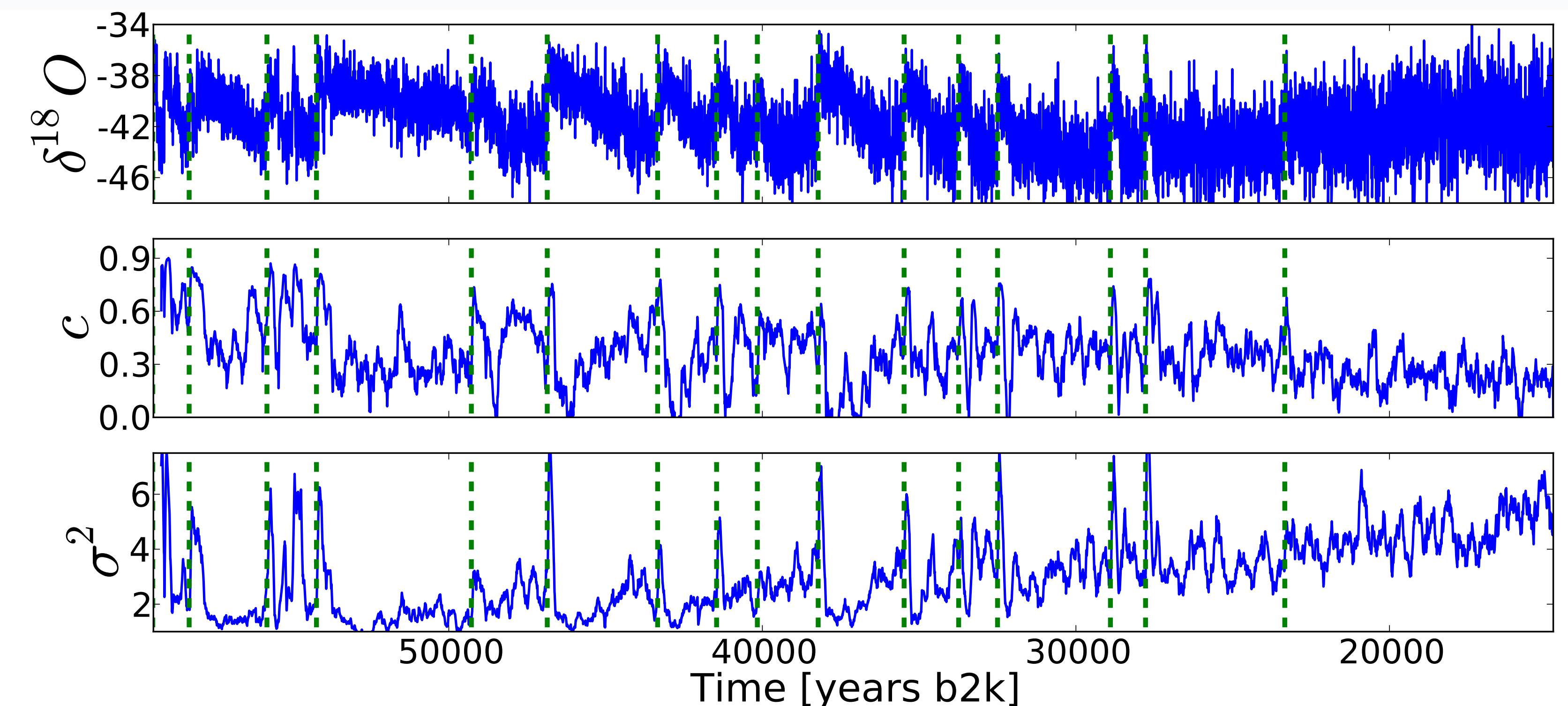
Abrupt transitions can take place with no early warning signal, for instance in the case of motion close to a homoclinic orbit (CD model [5]):



Consistent results with other "prototype models".

## Early warnings in ice core data

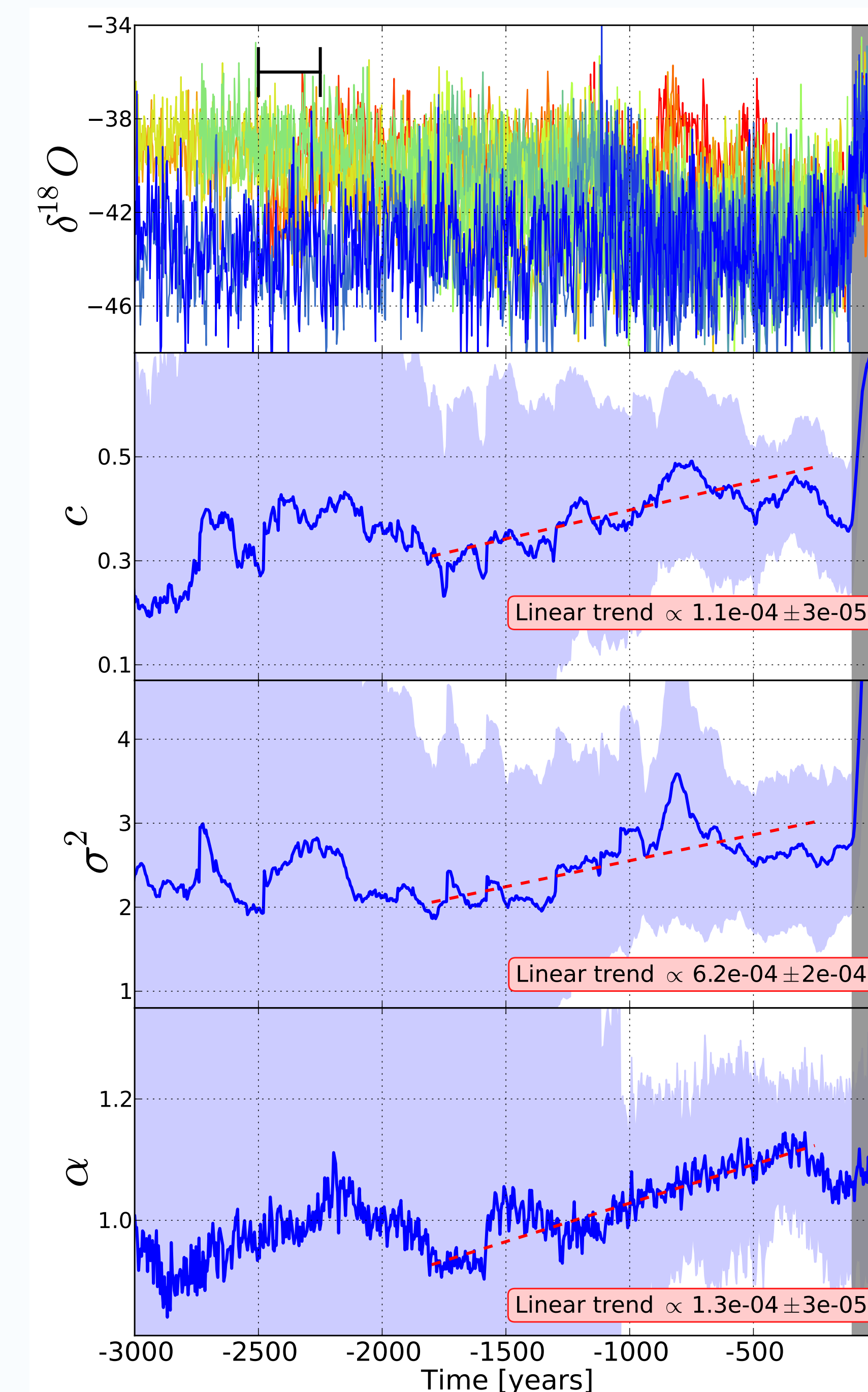
Noise signatures are computed for a high resolution  $\delta^{18}\text{O}$  paleoclimatic time series [6]:



Green lines mark DO events: *early warning signals* are visible only for some of the events.

## Ensemble behaviour

More reliable information is obtained when the ensemble of DO events is considered:



## Conclusions and Open Questions

*Statistical properties of fluctuations in the ensemble of DO events are consistent with the crossing of a (fold?) bifurcation point by climate system.*

- What is the forcing mechanism?
- Can we confirm these findings on other time series from last glacial age?
- Can we link the bifurcation to thermohaline circulation instability?

## References

- [1] A. Ganopolski and S. Rahmstorf. Abrupt Glacial Climate Changes due to Stochastic Resonance. *Phys. Rev. Lett.* 2002, **88**:038501
- [2] A. Timmermann *et al.* Coherent resonant millennial-scale climate oscillations triggered by massive meltwater pulses. *J. Clim.* 2003, **16**:2569
- [3] C. Kuehn. A mathematical framework for critical transitions. *arxiv:1101.2899*
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- [5] D. Crommelin *et al.* A mechanism for atmospheric regime behavior. *J. Atm. Sci.* 2004, **61**:1520
- [6] A. Svensson *et al.* A 60,000 year Greenland stratigraphic ice core chronology. *Clim. Past* 2008, **4**:47

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