

# Simplified evaporation method for determining soil hydraulic properties: a reinvestigation of linearization errors

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## Introduction

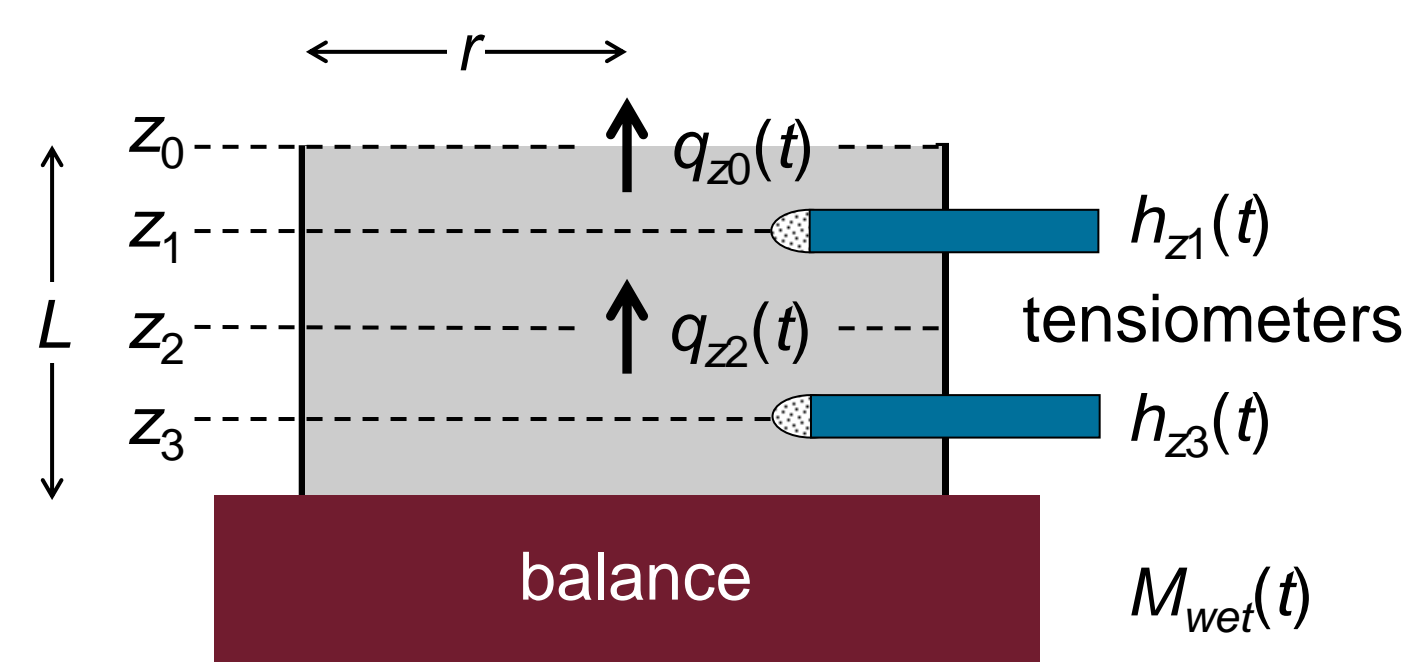
- In the simplified evaporation method of Schindler (1980, Arch. Acker- u. Pflanzenbau u. Bodenk., 24:1-7), the soil hydraulic properties are derived as:

$$\theta(t) = \frac{M_{\text{wet}}(t) - M_{\text{dry}}}{\rho \pi r^2 L}$$

$$K(t) = \frac{q_{z2}(t)}{\nabla H_{z2}(t)}$$

$$q_{z2}(t) \approx \frac{q_{z0}(t)}{2} = -\frac{L \Delta \theta(t)}{2 \Delta t}$$

$$\nabla H_{z2}(t) \approx \frac{h_{z3}(t) - h_{z1}(t)}{z_3 - z_1} + 1$$



- Peters and Durner (2008, J. Hydrol., 356:147-162) evaluated this method using a process model that considers liquid water flow in capillaries only and found that it gives reliable results.
- In this study, we reinvestigate the simplified evaporation method using a more realistic process description that includes liquid water flow in films and water vapor flow. We treat the following questions:
  - Are the conclusions of Peters and Durner (2008) still valid when film and vapor flow is taken into account?
  - Does the kind of averaging of pressure heads affect the accuracy of the method?
  - Is the accuracy of the method dependent on the flow rate and length scale of the sample?

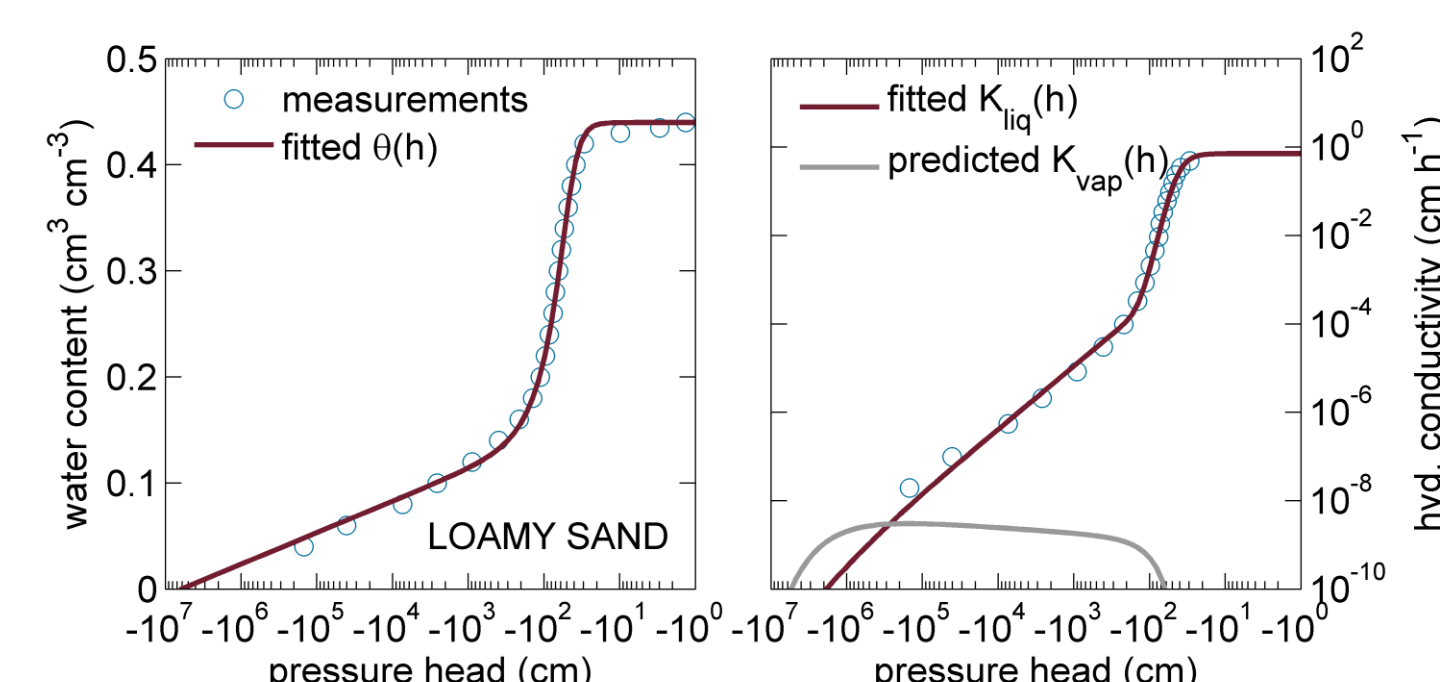
## Methods

- We simulated evaporation experiments using an extended form of the Richards equation that includes isothermal vapor flow.
- Synthetic data from simulated evaporation experiments were evaluated with the simplified evaporation method. For calculating the mean pressure head, we used two different approaches:

arithmetic mean:  $\bar{h}(t) = \frac{h_{z3}(t) - h_{z1}(t)}{2}$

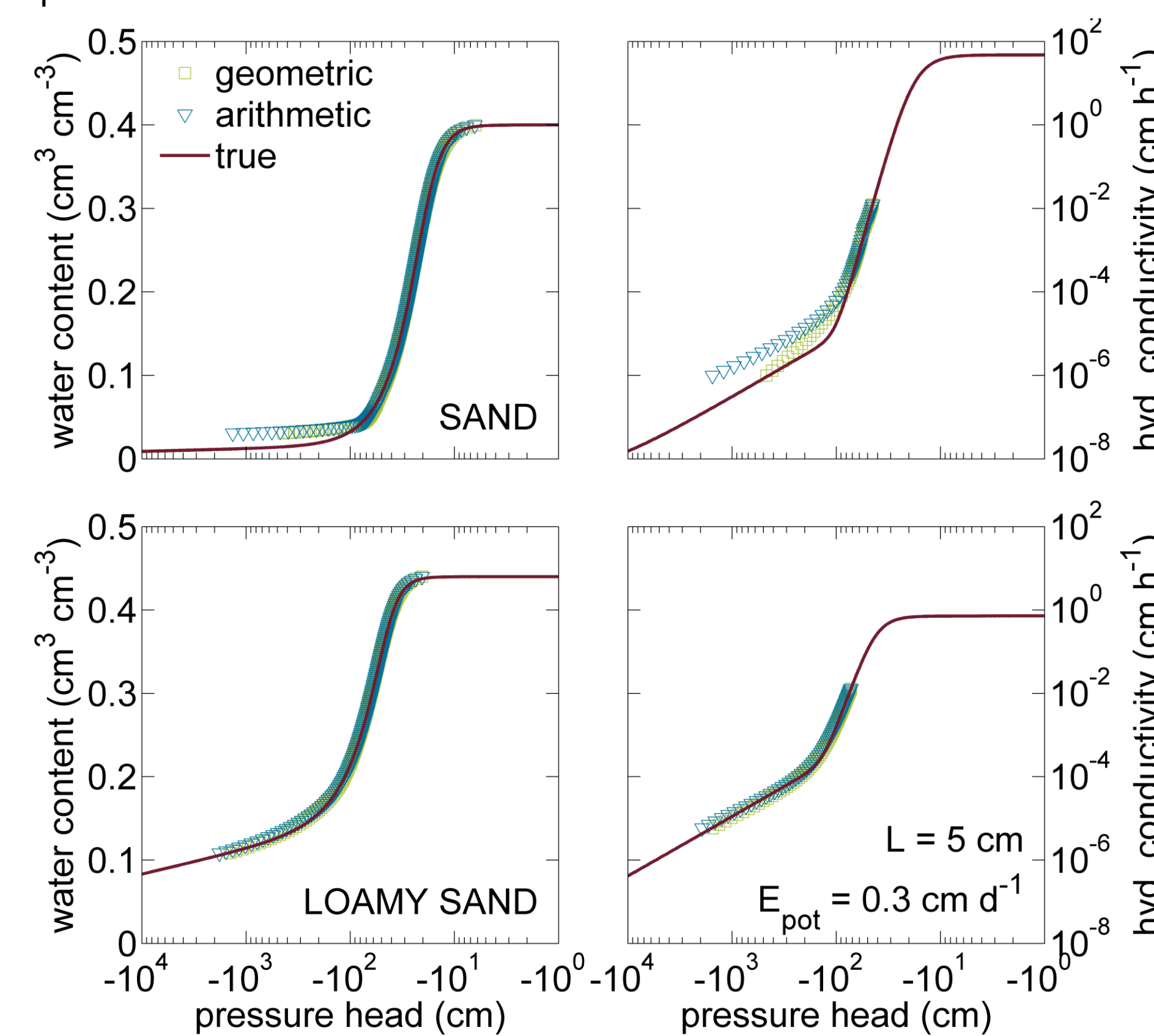
geometric mean:  $\bar{h}(t) = \sqrt[3]{h_{z1}(t)h_{z3}(t)}$

- Soil hydraulic properties of a loamy sand (shown below) and a sand were derived from data reported in the literature and parameterized using the model of Lebeau and Konrad (2010, Water Resour. Res., 46:W12554), which includes a film flow component in the hydraulic conductivity function.



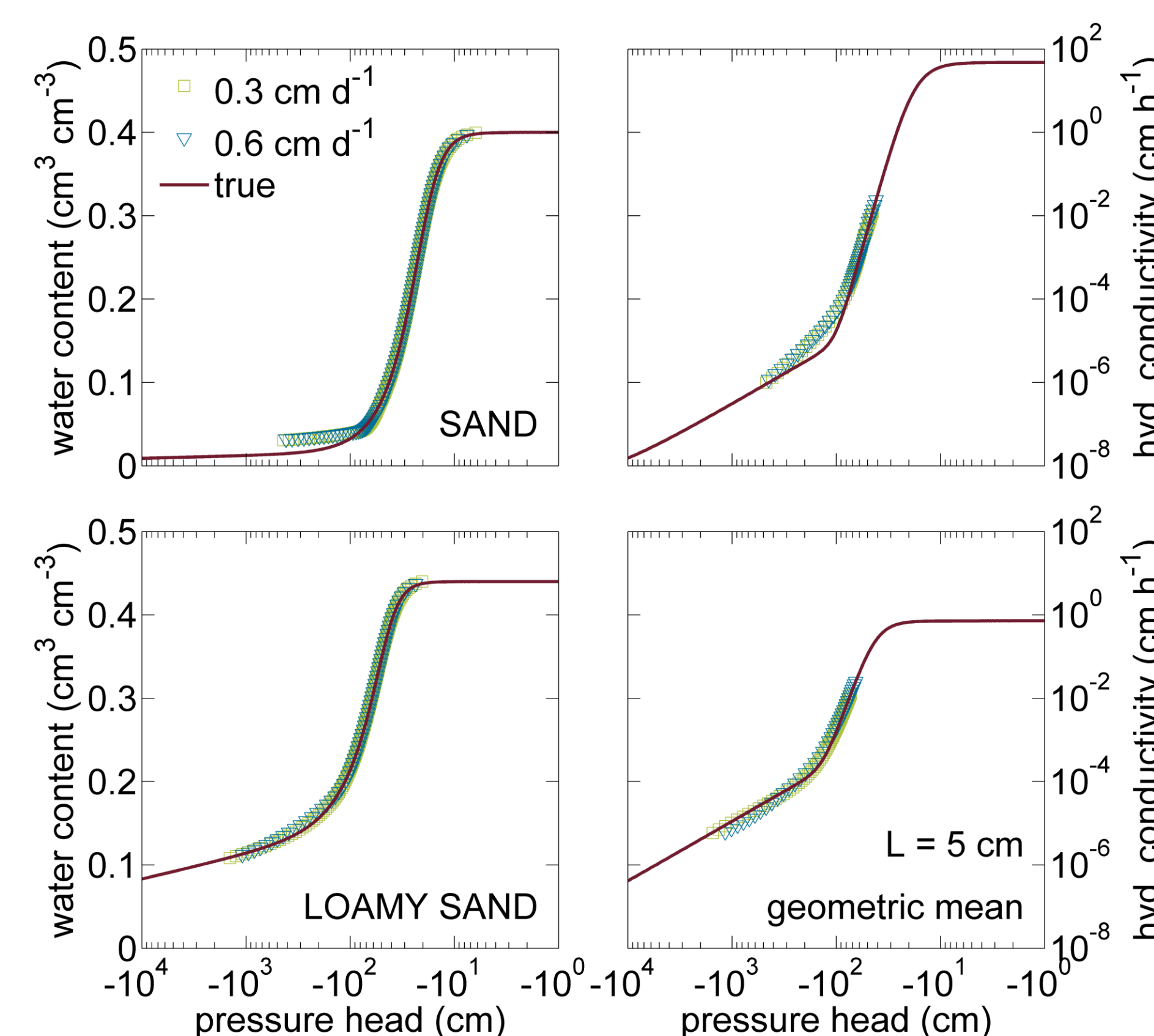
## Results 1: Arithmetic vs. geometric mean

For medium-textured soils, both the arithmetic and the geometric mean give almost identical results. For coarse-textured soils, the geometric mean gives results that are closer to the true hydraulic properties.



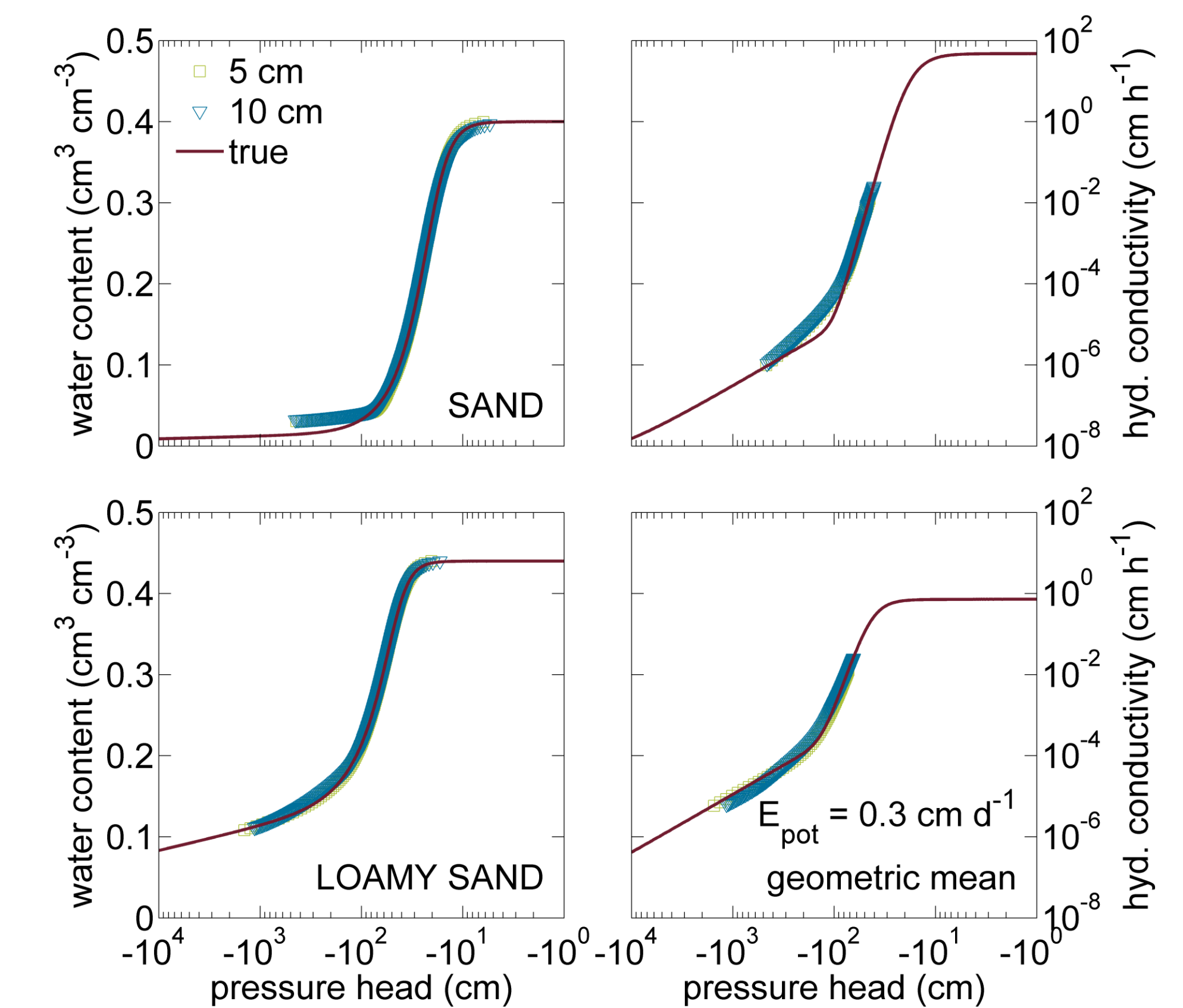
## Results 2: Flow rate dependency

In general, deviations from the true hydraulic properties increase with increasing flow rate (potential evaporation rate). This effect is more pronounced for medium-textured soils.



## Results 3: Length scale dependency

The accuracy of the simplified evaporation method decreases with increasing sample length. Again, this effect is more pronounced for medium-textured soils.



## Conclusions

- The simplified evaporation method gives quite accurate results for medium-textured soils. Deviations from the true hydraulic properties are more pronounced for coarse-textured soils, especially in the medium to dry range.
- The use of the geometric mean for calculating the mean pressure head is preferable to the arithmetic mean.
- The accuracy of the derived soil hydraulic properties increases with decreasing flow rate. Our results indicate that a potential evaporation rate of 0.3 cm d⁻¹ or less is generally acceptable.
- The accuracy of the derived soil hydraulic properties depends on the length of the sample. Our results indicate that samples should not be substantially longer than 5 cm.

## Acknowledgements

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