



Mathematical models of erosion have to obey mathematical rules with respect to both the units and the values of the parameters involved. Some modifications of the Universal Soil Loss ignore these rules.

The USLE operates on the basis that the primary physical model is represented by the “unit” plot, a bare fallow area 22 m long on a 9 % slope with cultivation up and down the plot.

The soil loss from the unit plot is determined by the product of R and K and both of these parameters have units. The units for R are MJ mm ha<sup>-1</sup> h<sup>-1</sup> y<sup>-1</sup> and for K, t h MJ<sup>-1</sup> mm<sup>-1</sup> so that their product is soil loss with units t ha<sup>-1</sup>. The remaining 4 factors have no units and are used to modify the value of the soil loss from the unit plot (A<sub>1</sub>) to predict soil loss from areas that are different for the unit plot. The model operates in two steps

$$A_1 = R K \quad (1)$$

$$A = A_1 L S C P \quad (2)$$

The units for R are derived from the fact that in the USLE, and subsequent valid revisions and improvements, the event erosivity factor (R<sub>e</sub>) is given by the product of storm kinetic energy (E) and the maximum 30-minute intensity. K is in effect the regression coefficient in the relationship between R<sub>e</sub> and the soil loss from runoff producing events on the unit plot. **If the event erosivity factor is changed from EI<sub>30</sub> then K cannot be used.**

## Invalid modifications of the USLE event erosion equation

( A<sub>e</sub> = soil loss for an event)

$$A_e = EI_{30} K_e L S C_e P_e \quad \text{VALID} \quad (3)$$

## The MUSLE

$$SY_e = 11.8 (q_e q_{pe})^{0.56} K L S C_e P_e \quad \text{INVALID} \quad (4)$$

SWAT uses the MUSLE

## APEX

$$SY_e = X_e K L S C_e P_e \text{ (ROKF)} \quad (5)$$

$$X_e = EI_{30} \quad \text{VALID} \quad (6a)$$

$$X_e = 1.586((q_e q_{pe})^{0.56} DA^{0.12}) \quad \text{INVALID} \quad (6b)$$

$$X_e = 0.65EI_{30} + 0.45 (q_e q_{pe})^{0.33} \quad \text{INVALID} \quad (6c)$$

$$X_e = 2.5 (q_e q_{pe})^{0.5} \quad \text{INVALID} \quad (6d)$$

$$X_e = 0.79(q_e q_{pe})^{0.65} DA^{0.009} \quad \text{INVALID} \quad (6e)$$

$$X_e = b_1 q_e^{b_2} q_{pe}^{b_3} DA^{b_4} \quad \text{INVALID} \quad (6f)$$

Estimates of R produced by another means must produce the same numerical values as if based on EI<sub>30</sub> values

$$F_M = \sum_{i=1}^{12} \frac{P_i^2}{P} \quad P_i = \text{month } i \text{ rain, } P = \text{annual rain}$$

$$R = 0.739 F_M^{1.847} \quad , \text{ USA (Renard and Freimund, 1994)} \quad (7)$$

$$R = 3.82 F_M^{1.41} \quad , \text{ Australia (Yu, 1996)} \quad (8)$$