Solute Spreading in Variably Saturated Spatially Heterogeneous Formations: The Role of Water Saturation and Soil Texture

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1. Background
Solute transport in near-surface geological formations is considerably affected by the heterogeneity in the hydraulic properties (HP) of the formations. The latter may be characterized by a relatively complex correlation structure. In the approach adopted here, the spatial arrangement of distinct geological materials (e.g., sand or clay deposits) is replaced by a single, composite material whose properties are bimodal and statistically homogeneous. The composite heterogeneous formation, in turn, is viewed as a mixture of two populations (background soil and embedded soil) of differing spatial structures.

2. Purpose of the Presentation
(i) To employ first-order, Lagrangian-stochastic framework of vadose zone transport in order to investigate the combined effect of the embedded soil’s texture and the mean pressure head (i.e., water saturation) on solute spread and breakthrough in a composite, bimodal, heterogeneous, variably saturated formations, and,
(ii) To test the applicability of the results of the first-order analyses (FOA) to more realistic conditions.

3. Theoretical Considerations
Consider the vadose zone of the composite formation. The mean flow takes place normal to its strata. The composite formation is variably saturated and its flow parameters depend on water saturation in a manner which is highly dependent on the texture of the two distinct soil materials that constitute the formation. It is assumed here that the constitutive relationships for unsaturated flow for the i-th soil material of the composite formation are given by the 2-parameter Gardner-Russo model, i.e., K_i and q_i=1,2. Quantification of the vadose-zone transport is based on a two-stage approach which combines:
(i) a first-order perturbation approximation of the 3-D steady-state unsaturated flow equation; and
(ii) a general Lagrangian description of the motion of an indivisible particle of a passive solute carried by a steady-state flow.

4. Results - First Order Analyses
Results of the FOA (Russo, 2004; 2010) suggest that in variably saturated, bimodal heterogeneous formations, logK variance, $\sigma^2_i$, is a concave function of the mean pressure head, $H=\bar{E}[\psi]$. The concave nature of the $\sigma^2_i(H)$ relationships stems from the basic differences between the local K-ψ relationships associated with coarse-textured soils and their counterparts associated with fine-textured soils. Consequently, the magnitude of the principal components of the time-dependent macrodispersion tensor (Fig. 1) are also concave functions of H.

5. Numerical Simulations
The stringent assumptions of the FOA may oversimplify the processes occurring in realistic variably saturated flow systems. The applicability of the results presented here to more realistic situations, is briefly analyzed. A series of numerical analyses of flow and transport in a hypothetical, yet realistic, 3-D variably saturated heterogeneous, bimodal formations were conducted (Russo, 2010). Two different flow regimes were considered. The first is a relatively simple, steady-state (SS) flow, pertinent to the flow conditions assumed in the FOA. The second is a transient (TR) flow, pertinent to realistic situations involving periodic forcing conditions at the soil surface and water uptake by plant roots.

6. Conclusions
In SS flows, features of transport associated with the two different formations exhibit a crossover behavior at intermediate water saturations. This explains why in TR flows associated with active root zone, the response of the different formations is essentially independent of the texture of the embedded soil.}

**Literature Cited**