

Neural Supermodeling



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1. Supermodels (SUMOs): interactive ensemble of existing models

- Proposal to improve climate modeling[1]
- As an alternative to conventional noninteractive ensemble methods
- Models are good, but imperfect
- **Supermodel = Ensemble of dynamically coupled models**

Individual model dynamics

$$\dot{x}_\mu^i = f_\mu^i(x_\mu)$$

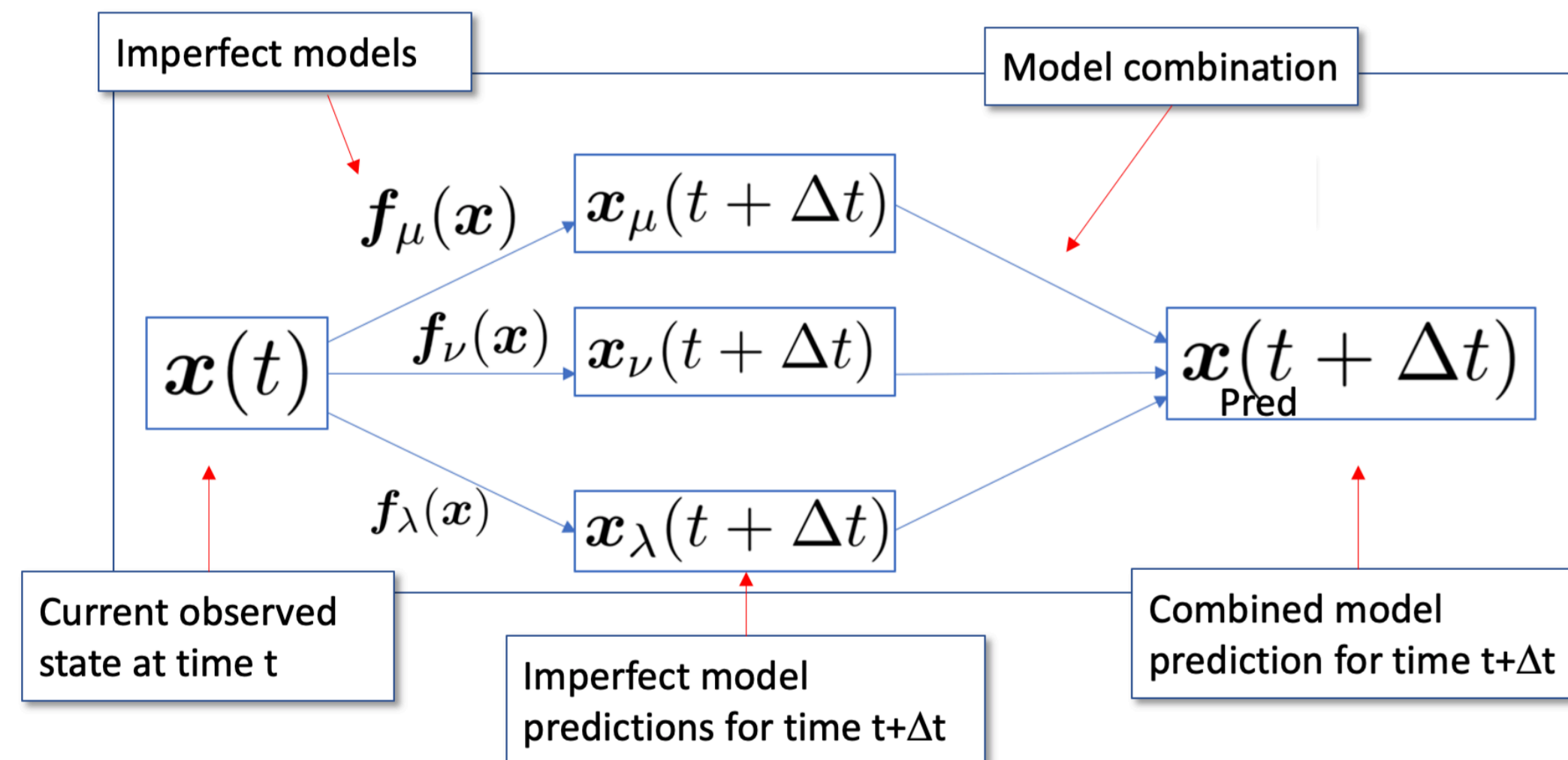
SUMO coupling by weighted averaging (see [2] and [3])

$$\dot{x}^i = \sum_\mu w_\mu^i f_\mu^i(x)$$

SUMO couplings need to be optimized

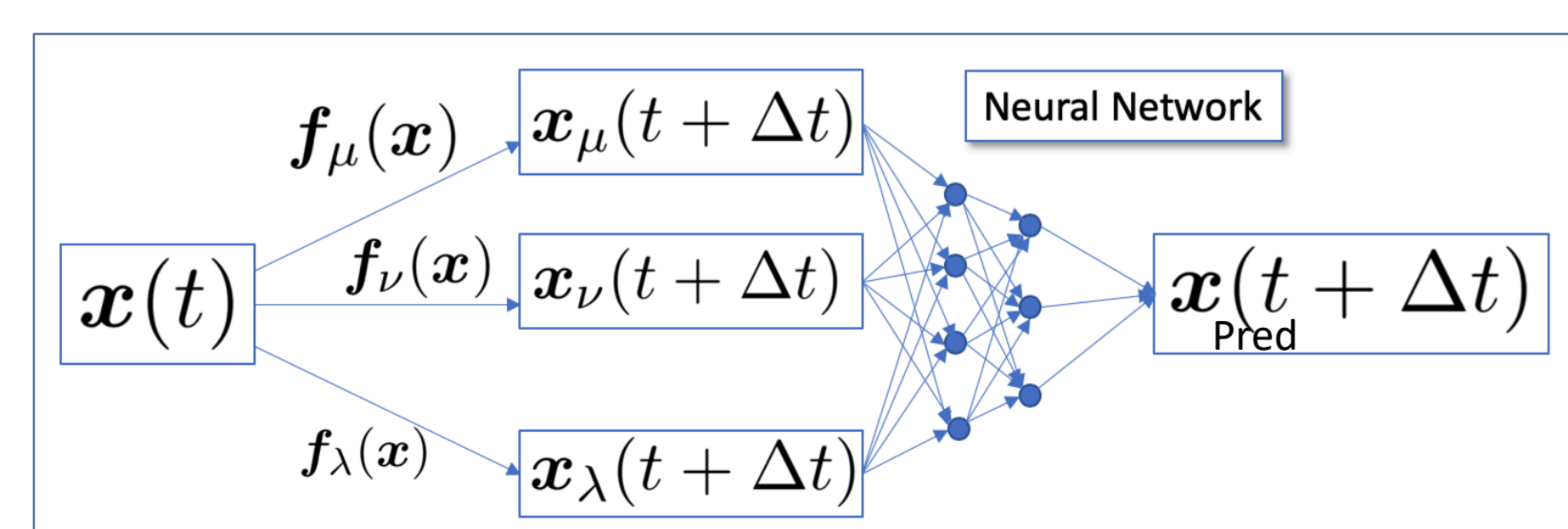
- e.g. by minimizing short term (Δt) prediction error E
- *Theoretical optimal if models are combined with $\Delta t \rightarrow 0$*
- *Works very good if Δt is small*
- *But this may be impractical*
- *We would like to work with larger Δt*

FOCUS of this poster: OPTIMIZING the combination of imperfect models for one step ahead prediction for given value of Δt



2. Neural model combination

Model combination can be done using linear models (such as e.g. weighted averaging), but also by a neural network.



3. Research Question

Can a convolutional neural network (CNN) improve linear / weighted averaging methods for model combination used in e.g. ensembles or SUMO?

Is this feasible? With so many variables involved and parameters to optimize? Based on limited amount of data?

First step: **proof of principle** with *artificial assumed ground truth* model and *artificial imperfect* models.

4. Experimental scenario

Three level quasi-geostrophic model T21 [4]

Simulates the wintertime atmospheric flow in the Northern Hemisphere quite realistically with a climatology with multiple weather regimes that are also found in observations.

Dynamical system for potential vorticity (PV)

$$\begin{aligned} \dot{q}_1 &= \mathcal{J}(\psi_1, q_1) - D_1(\psi_1, \psi_2) + S_1, \\ \dot{q}_2 &= \mathcal{J}(\psi_2, q_2) - D_2(\psi_1, \psi_2, \psi_3) + S_2, \\ \dot{q}_3 &= \mathcal{J}(\psi_3, q_3) - D_3(\psi_2, \psi_3) + S_3, \end{aligned}$$

Imperfect models

For benchmarking, we simulate four imperfect models by perturbing parameters of the Truth as in [3],

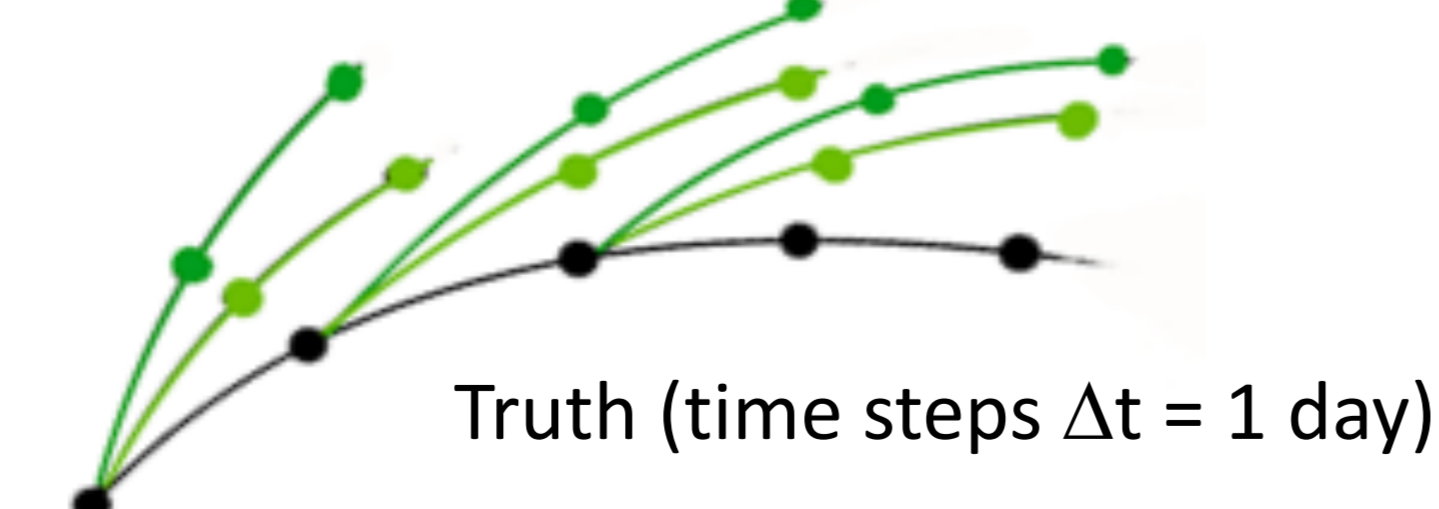
	τ_E	R_1	R_2	τ_E – timescale in days of the Ekman damping
Truth	2.0	0.1150	0.0720	
Model 1	1.5	0.1165	0.0705	R_1 – Rossby radius of deformation of the 200–500 hPa layer
Model 2	1.5	0.1130	0.0725	R_2 – Rossby radius of deformation of the 500–800 hPa layer.
Model 3	2.4	0.1130	0.0705	
Model 4	2.4	0.1165	0.0725	

Data set

Daily observations $q(x,y,z,t) \stackrel{\text{def}}{=} q(t)$ were simulated by running the *truth* from $t = 0$ until $t = 3000$ (t in days).

Starting from each daily observations, the four imperfect models predicted $\Delta t = 1 \dots 7$ days ahead. This yielded 2400 imperfect predictions $q_\mu(t+\Delta t; \mu)$ for $\mu=1..4$ and $\Delta t = 1 \dots 7$ days ahead (so $4 \times 7 \times 3000$ predictions).

Imperfect models, predict $\Delta t = 1, 2, \dots$ days ahead



4. Linear models and deep Convolutional Neural Network (CNN)

Input and output layer

- Input: $X*Y*M = 64*32*4$ variables to represent imperfect model predictions $q_\mu(x,y,z,t+\Delta t)$ at time $t+\Delta t$ and layer z .
- Output: $X*Y = 64*32$ variables to represent combined model prediction $q_{\text{pred}}(x,y,z,t+\Delta t)$ at time $t+\Delta t$ and layer z .
- Note: separate model trained for each z and each Δt

Linear models:

$$q_{\text{pred}}(x,y,z,t) = \begin{aligned} & \sum_\mu q_\mu(x,y,z,t+\Delta t)/4 \quad (\text{Average}) \\ & \sum_\mu w_\mu(z) q_\mu(x,y,z,t+\Delta t) \quad (\text{Global Linear}) \\ & \sum_\mu w_\mu(x,y,z) q_\mu(x,y,z,t+\Delta t) \quad (\text{Linear per Gridpoint}) \end{aligned}$$

Hidden layers (only for CNN)

- $64*32*4$ neurons per hidden layer
- Horizontal (X-direction) periodic boundary conditions
- Locally connected & nonlinear & weight sharing
- 4 nonlinear convolutional Layers
- 2 linear skip layers
- Hidden to output \rightarrow no weight sharing

Training

- Training set: first 2400 days
- Input is scaled $q \rightarrow q^s$ per layer
- Trained per layer
- Loss = Mean squared error per layer $\text{MSE}(q_{\text{pred}}^s(t+\Delta t), q_{\text{truth}}^s(t+\Delta t))$

Optimizer:

- linear algebra to solve w (linear models)
- gradient descent, 200 iterations (CNN)

Test

- Test set: last 600 days
- Data scaled using scaler from training set
- Loss = RMSE ($q_{\text{pred}}^s(t+\Delta t), q_{\text{truth}}^s(t+\Delta t)$) taking all layers into account

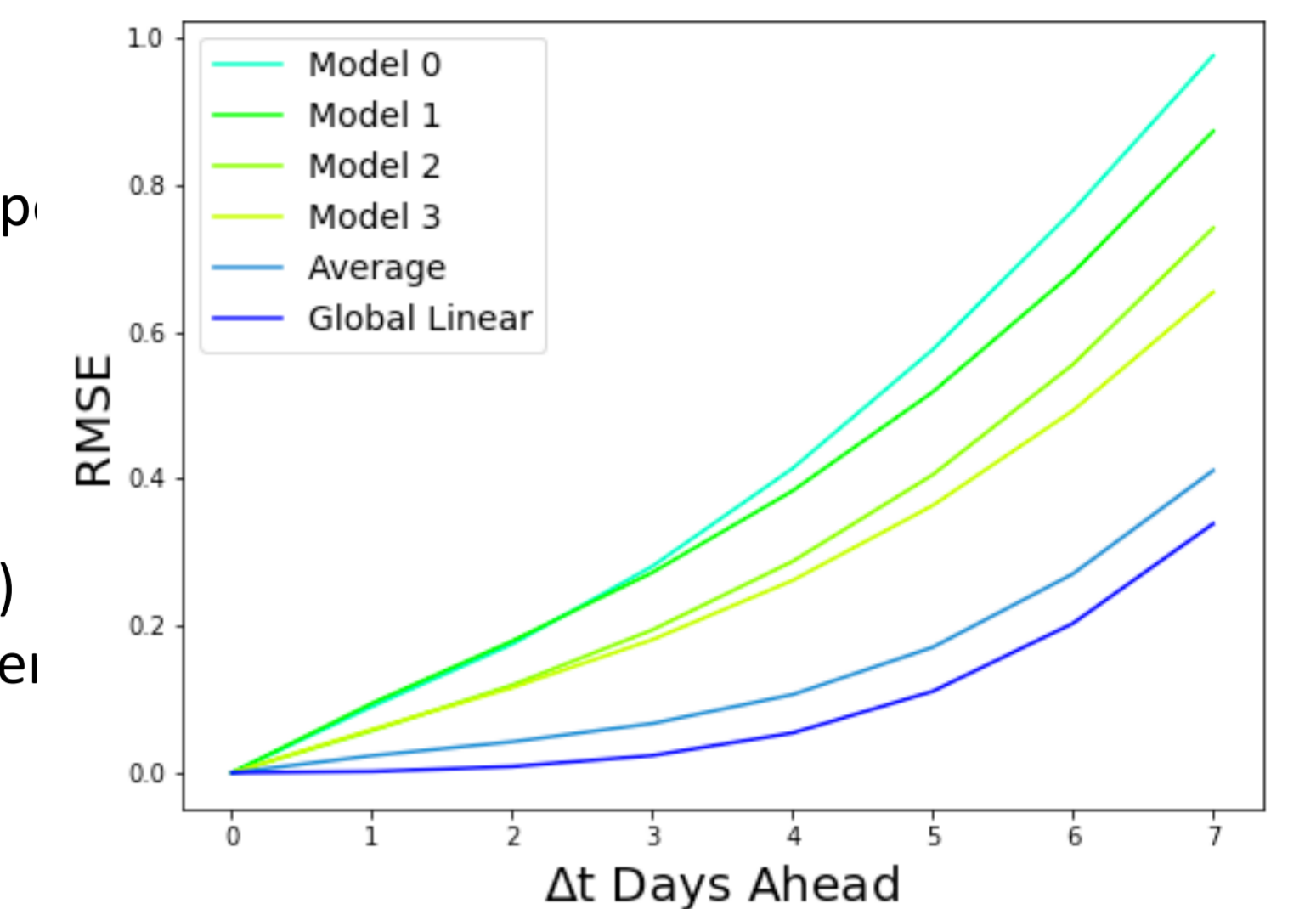
References

- [1] van den Berge, L. A., et al. A multi-model ensemble method that combines imperfect models through learning, Earth Syst. Dynam., 2, 161–177. (2011).
- [2] Wiegnerinck, et al. (2013). On the limit of large couplings and weighted averaged dynamics. In *Consensus and synchronization in complex networks* (pp. 257–275). Springer, Berlin, Heidelberg.
- [3] Schevenhoven FJ, Selten F. An efficient training scheme for supermodels. Earth System Dynamics. 2017;8(2):429–438
- [4] Marshall, John, and Franco Molteni. "Toward a dynamical understanding of planetary-scale flow regimes." *Journal of the atmospheric sciences* 50.12 (1993): 1792–1818.

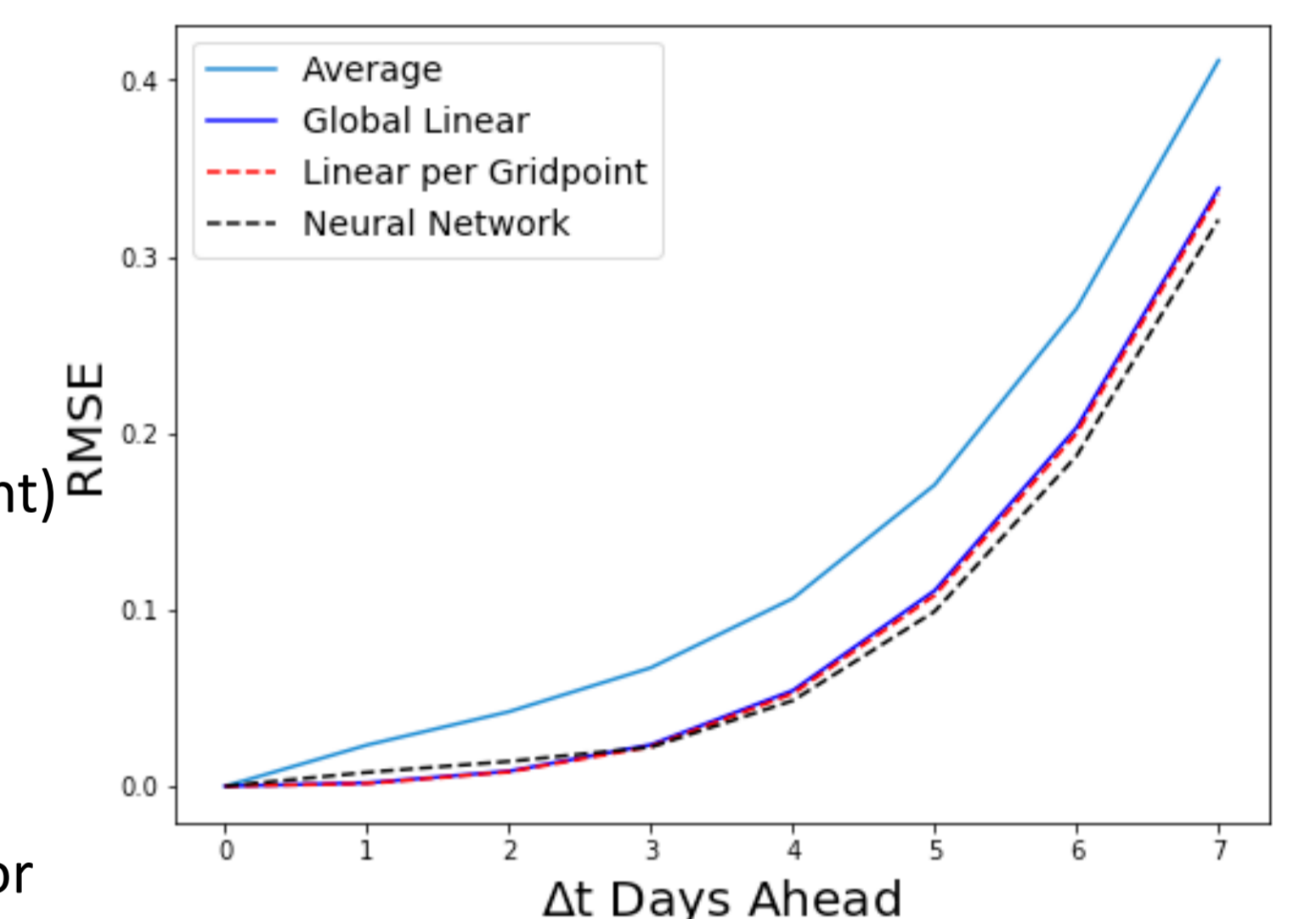
5. Experimental results

Figures show results on the test set.

Results in **top figure** confirm [3] that averaging improve upon individual imperfect model predictions and that global linear models (\cong weighted average) improves even further



Results in **bottom figure** show that in this case, the linear per gridpoint and neural network improve only marginally (but statistically significant) upon weighted average per layer.



For $\Delta t < 3$, linear methods are superior to neural networks.

6. CONCLUSIONS

- **A neural network (CNN) with imperfect model predictions as inputs, can improve linear models in short term prediction.**
- **However, in this model simulation,**
 - **improvements upon linear models are marginal**
 - **linear methods are superior for very short term predictions**
- **So far only proof of concept on artificial data of medium size atmospheric model.**