

# SHORT-TERM PHOTOVOLTAIC GENERATION FORECASTING USING HETEROGENOUS SOURCES OF DATA BASED ON AN ANALOG APPROACH



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**Research center :**  
PERSEE  
Centre for processes, renewable  
energies and energy systems



Industrial partner :



- I. Objectives of PV forecasting
- II. Proposed approach
  - I. A multi-inputs approach
  - II. A conditioned learning
- III. Models definition / Case study
- IV. Outcomes and analysis
- V. Conclusions

## Weather dependence

- Production **variability**, limited **controllability**, **uncertainties**...
- ... leads to **large-scale integration problems**

## New challenges to meet

- Management of the distribution **network** (balance, reserve, ...)
- Optimization of **maintenance** scheduling
- Trading on electricity **market**

## What we propose:

- **Short-term** forecasting model (i.e. few minutes up to 6h ahead)
- A statistical approach
- A **seamless** model (i.e. a unique model suitable for large range of horizons)
- A **simple** model with **good performances**

# A multi-inputs approach – State of the art

## State-of-the-art

- Production measurements
- Numerical Weather Prediction (NWP)
- Satellite images
- Sky images

## Inputs complementarity

- Due to their temporal & spatial resolutions, each approach observes specific phenomena

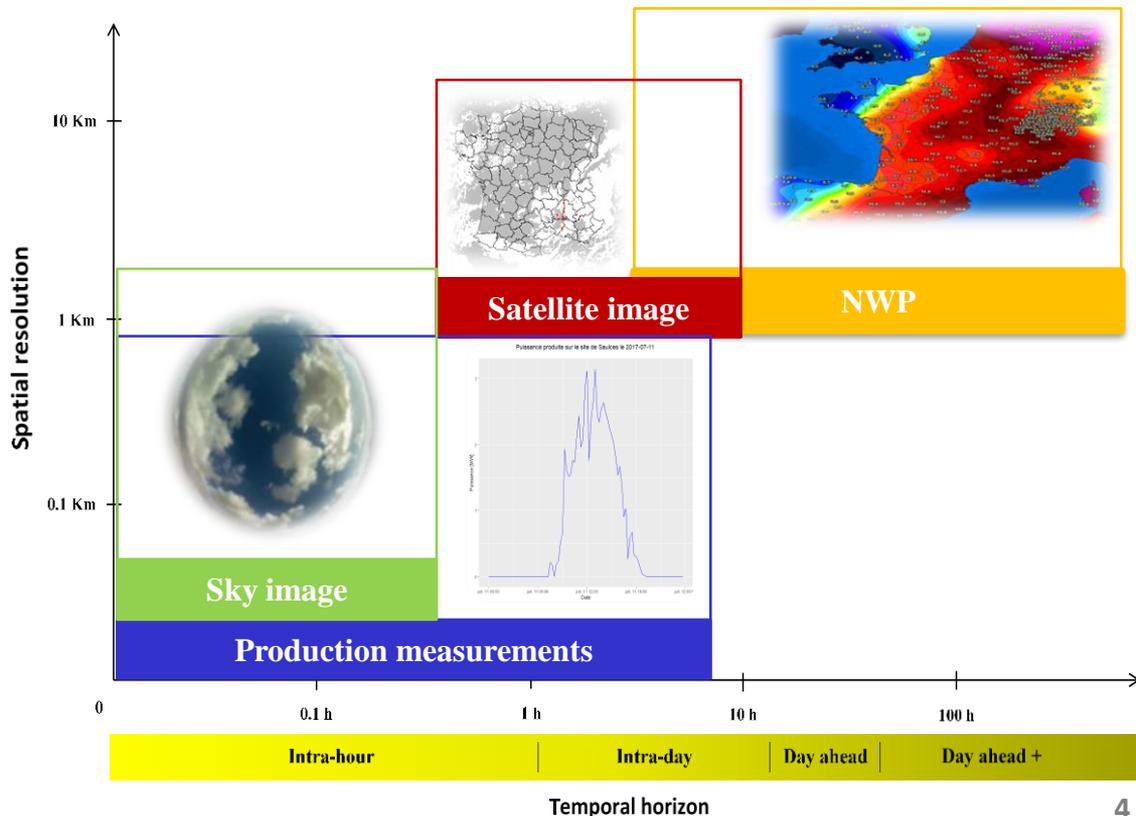
## Inputs combination

- Improvement of forecasting performance for short-term horizons (Aguiar 2016, Vallence 2018)

### Classification of inputs used for PV production forecasting.

Adapted from (Antonanzas, 2016) and (Diagne 2013).

Photo credits: (Météo-France, meteociel.fr, (Cañadillas, 2018), CNR)



# The Spatio-Temporal approach

## Description

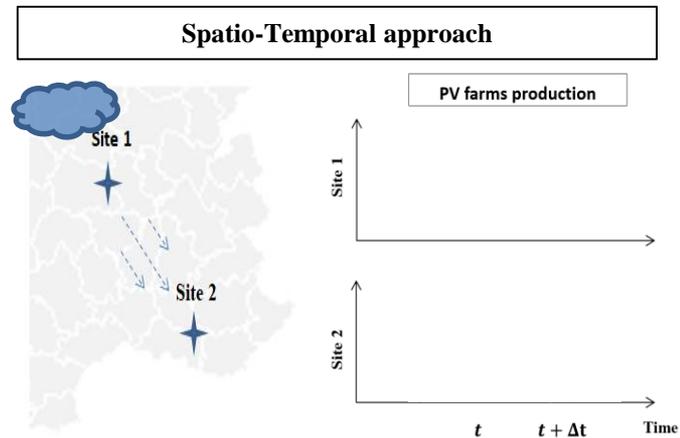
- Exploits the spatial and temporal correlations between the production data of spatially distributed PV sites
  - Idea: a set of neighbouring PV plants is affected by the same clouds
- Short-term horizons (Bessa 2015)

## Interests

- Data easily **available** (provided real time data logging)
- Improve forecasting performance **up to 10%** (Bessa 2015, Agoua 2018)

## Limitations

- PV sites **spatial distribution** (low density)
- **Quality** of time series (converter shutdown, ...)



## Weather variability

- **Variability in cloud cover** leads to variability in PV production
- Models need to operate on a **wide range of weather conditions** (from sunny to overcast skies)
- An **adaptative model** is more **accurate** than a static model (*Bacher, 2009*)

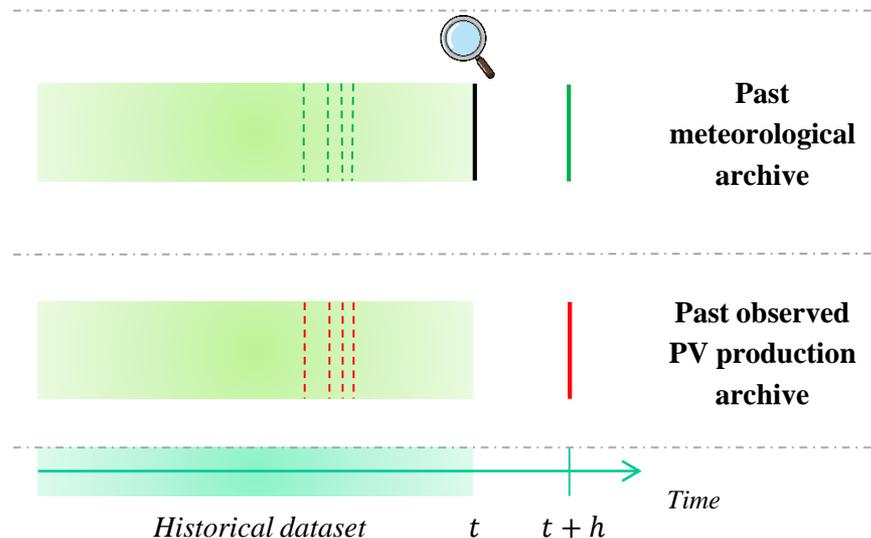
## Proposed approach

- Hypothesis: **similar PV production dynamics** are observed under **similar weather conditions**
- Thus, fitting a model on all past PV observations can **drown relevant information**
- It seems wise to **sample the learning set** to obtain a **weather coherent** PV production observations **subset** in regard with the future weather state
- To do so, an **analogy based approach** is implemented

# A conditioned learning

## An analog based approach:

- Construction of **2 past records** for the same period
  - Meteorological archive
  - Observed PV production archive
- Retrieve **forecast** of analog predictors **at time  $t + h$**
- Compute the **analogy score** between the target meteorological situation and all the candidate situations from the meteorological archive.
- Each **meteorological situation** is **ordered** from the most similar to the less one.  **$N$  best meteorological situations** are selected.
- The  **$N$  associated PV production observations** are selected to **train the forecasting model**.
- **Forecast of PV production at time  $t + h$ .**



### Legend

— Target meteorological situation

- - Analogous meteorological situation

— Target PV production to forecast

- - PV production observation used to fit models

Which leads to an **adaptive learning**

# An analog based approach

## Analog variable

- **Geopotential field** is chosen as an **analog predictor**
- Geopotential field is considered as a **wind driver**

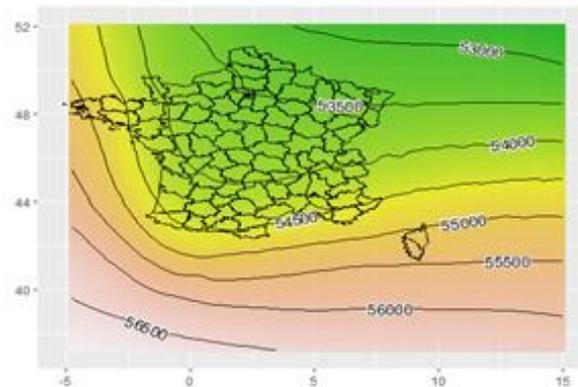
## Analog metric

- Need to take into account the predictor **spatial distribution**
- Score **S1** is used to **measure similarity** between the target and the candidate situations
  - (Teweless and Wobus 1954, Obled, 2002)

## Data integration

- **Perfect prognosis** mode
  - Regarding target situation, reanalysis data are used instead of predictions
  - Quantify the interest of using geopotential field as an analog predictor

## Geopotential height fields



$$S_1 = 100 \frac{\sum_{i=1}^{I-1} \sum_{j=1}^J \left| \Delta_{i,j}^{i,Target} - \Delta_{i,j}^{i,Candidate} \right| + \sum_{i=1}^I \sum_{j=1}^{J-1} \left| \Delta_{i,j}^{j,Target} - \Delta_{i,j}^{j,Candidate} \right|}{\sum_{i=1}^{I-1} \sum_{j=1}^J \max \left( \left| \Delta_{i,j}^{i,Target} \right|, \left| \Delta_{i,j}^{i,Candidate} \right| \right) + \sum_{i=1}^I \sum_{j=1}^{J-1} \max \left( \left| \Delta_{i,j}^{j,Target} \right|, \left| \Delta_{i,j}^{j,Candidate} \right| \right)}$$

Terms are defined in the [annex](#) section

# Data Stationarization

## Inputs stationarity



- ARIMA process requirement
- Get time series more « easily » forecastable

## PV production variability

- Deterministic component: sun's path
- Stochastic component: clouds, aerosol, ...

Taken into account by stationarity procedure

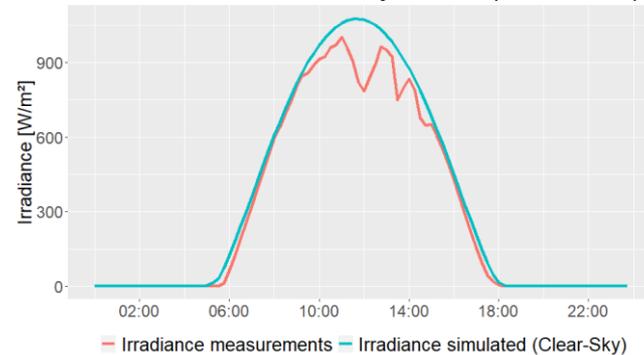
## Methods

- Clear-sky normalization (*Bacher, 2009*), (*Agoua, 2018*)
- Seasonal decomposition (*Cleveland, 1990*), (*Yang, 2012*)
- ...

## Clear sky model used:

- McClear model (*Lefèvre, 2013*)

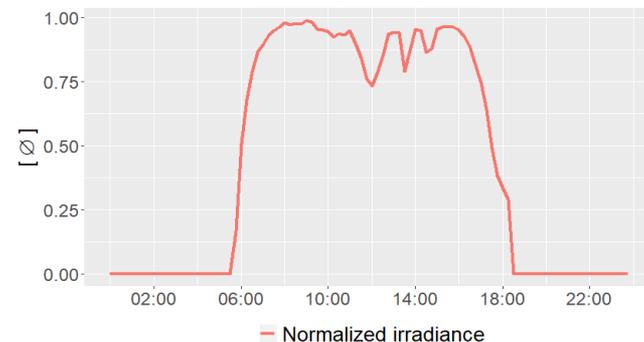
Observed irradiance and clear-sky irradiance (McClea model)



Normalization

$$p^{stat}(t) = \frac{p^{obs}(t)}{p^{clear-sky}(t)}$$

Normalized irradiance



# Models definition

## Performance evaluation

Score	Skill Score
$RMSE = \sqrt{\frac{1}{N} \sum_{t=1}^N (\hat{P}_t - P_t)^2}$	$SS(h) = 1 - \frac{RMSE_{Model}(h)}{RMSE_{Reference}(h)}$

## Reference model: smart persistence

$$\hat{P}_{t+h|t}^x = \begin{cases} \bar{P}_t^x & \text{if } \bar{P}_t^x \neq 0 \text{ (i.e. daytime)} \\ \bar{P}_{t+h-24H}^x & \text{if } \bar{P}_t^x = 0 \text{ (i.e. nighttime)} \end{cases}$$

## Auto-Regressive (AR) model

$$\hat{P}_{t+h|t}^x = \hat{\beta}_h^0 + \sum_{l=1}^L \hat{\beta}_h^l \bar{P}_{t-l}^x$$

## A two steps conditioned learning approach (CAR model)

- First, the learning set is sample according to the **hour of the day (CAR-T)**
- Then, the previous subset is sample again in respect to the **synoptic situations** using the analogy based method (**CAR-T.An**)

### Conditioned Auto-Regressive (CAR-T.An)

$$\hat{P}_{t+h|A_{t+h}}^x = \hat{\beta}_h^0 + \sum_{l=0}^L \hat{\beta}_h^l f_{A_{t+h}}(\bar{P}_{t-l}^x)$$

On-site observations

### CAR-T.An + Spatio-Temporal data (CARST-T.An)

$$+ \sum_{l=0}^L \sum_{y \in X} \hat{\beta}_h^{l,y} f_{A_{t+h}}(\bar{P}_{t-l}^y) \\ + \sum_{i=1}^N \hat{\beta}_{i,h}^{Sat} f_{A_{t+h}}(\overline{Sat}_t^i)$$

+ nearby sites observations  
+ satellite images

### CARST-T.An + eXogenous inputs (CARXST)

$$+ \hat{\beta}_h^{NWP} f_{A_{t+h}}(\overline{NWP}_{t+h}^x)$$

+ NWP

Terms are defined in the [annex](#) section

## Least Absolute Shrinkage and Selection Operator (LASSO)

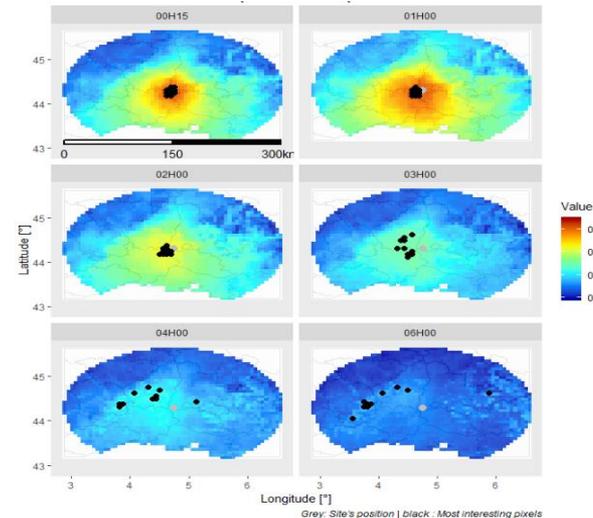
- To provide a **seamless model**, variable selection is carried out on each horizon to keep most **informative features**

$$\hat{\beta}_h^{LASSO} = \underset{\beta_h}{\operatorname{argmin}} \left\{ \frac{1}{2} \operatorname{RSS}(\beta_h) + \lambda |\beta_h| \right\}$$

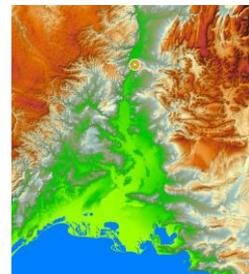
## Satellite pixels selection

- To avoid a too large number of variables, we limit our approach to the **10 most informative pixels**
- To quantify the correlation between the stationarized PV production and the stationarized satellite data for various lags, the **Mutual Information Criterion** is used (Carriere, 2020).
- The correlation area is highly influenced by the Rhône valley topography.
- The shorter the horizon, the closer the most relevant pixels.
- For horizon higher than 3H00 ahead, most informative points are located westward.
  - In this region, main wind seems to be **westerly wind** (see [annex](#))

Location of the 10 most informative pixels



Rhône valley topography



# Case study

## Production measurements



- 9 PV plants
- $D \in [7.3 ; 133]$  km
- $\bar{P}_t = \frac{P_t}{P_{nom}}$ , with  $P_{nom} \in [1.2 ; 12]$  MWp
- $\Delta t = 15'$

## Satellite images



- Helioclim-3 (Blanc, 2011)
- Stationarized GHI
- $\Delta t = 15'$

## NWP (exogenous inputs)

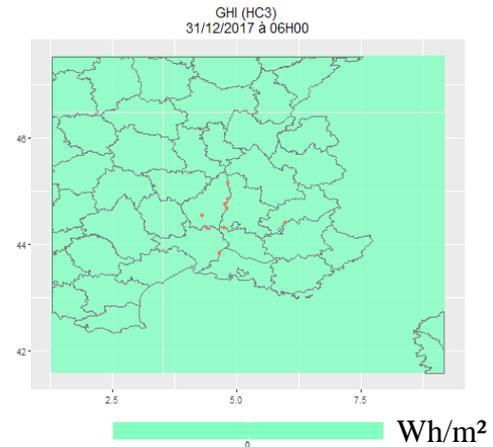
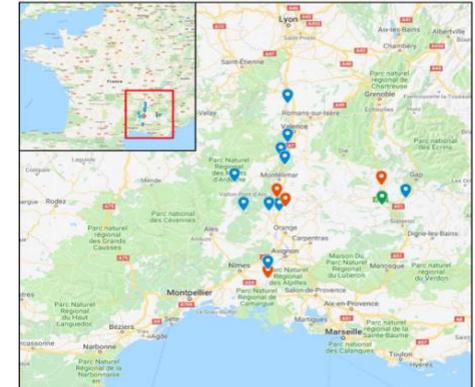


- ARPEGE – Météo France
- Operational forecasting conditions
  - Dissemination schedule
- Stationarized GHI
- $\Delta t = 1H$  interpolated to  $\Delta t = 15'$

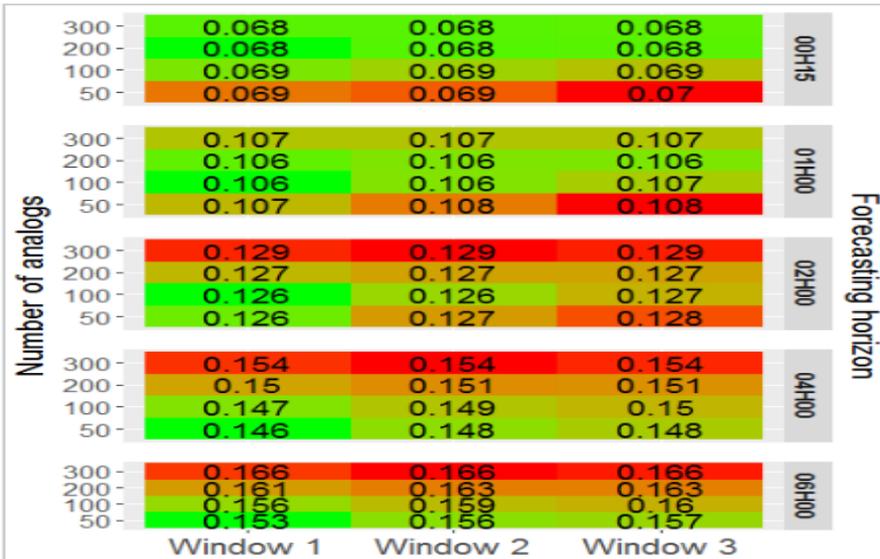
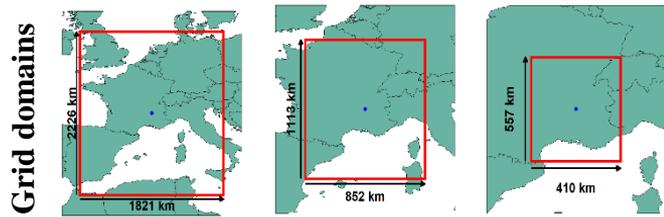
## Analog predictor



- ERA5 – ECMWF – Reanalysis
- *Perfect prognosis* mode
- Geopotential field at 500 & 925hPa
- $\Delta t = 1H$



# Sensibility analysis



## Parameters of the sensibility analysis

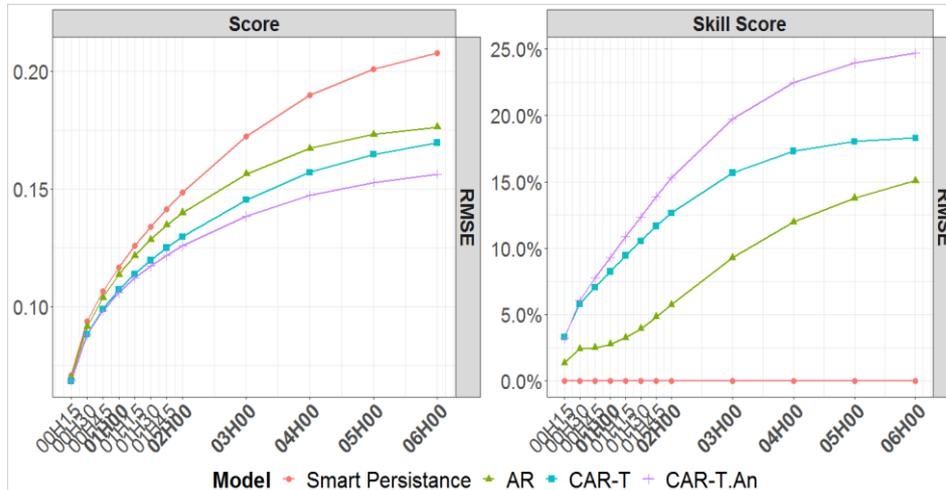
- Grid domains of the analog spatial window
  - 3 regions centered over the Rhône valley region
- Number of analogs situations to train the models
  - From 50 up to 300 analogs situations

## Conclusions

- Grid domains
  - The larger spatial window exhibits better performances.
- Number of analogs
  - For very short-term horizons (i.e. from 15' up to 1H ahead), the more analogs, the better the performances,
  - For longer horizons (i.e. from 2H up to 6H ahead), better performances are achieved with less analogous situations.
  - **100 analog situations seems a good compromise.**

# Influence of the conditioned approach over performances

## Performance evaluation of the proposed conditioning approach over the reference model



Model names are defined in the [annex](#) section

## Conclusions

### ■ AR model

- AR model outperforms the persistence up to ~15% for a 6H horizon.

### ■ CAR-T model

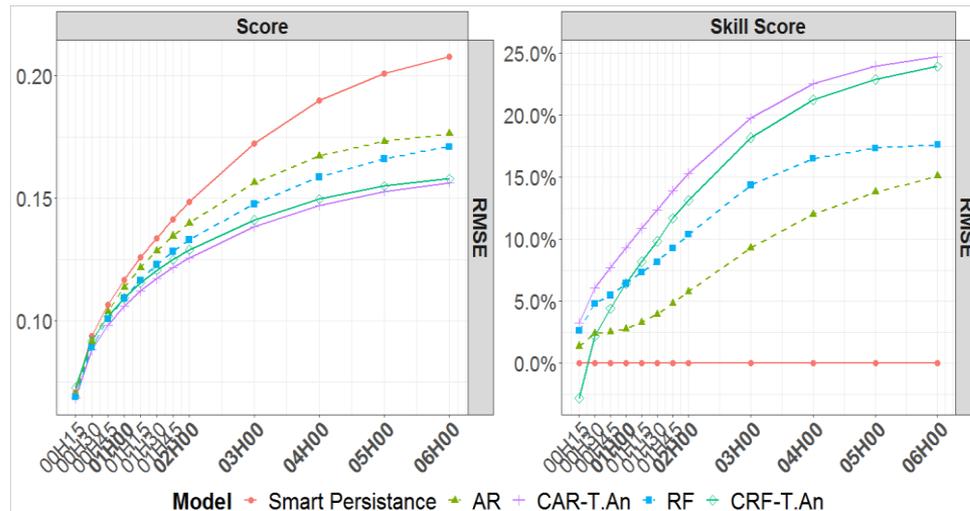
- Conditioning of the learning set to the hour of day, improves performances in comparison with the AR model
- This phenomenon can be explained by:
  - The stationnarisation procedure is not perfect, especially for dawn times (Agoua, 2018)
  - The PV production dynamics varies according to the time of the day

### ■ CAR-T.An

- The CAR-T.An model outperforms both the previous models. Compared to persistence model, improvement can reach ~24% for a 6H lead time
- Better performances** are obtained when forecast model **depends on the weather situation**

# Comparison with a more advanced model

## Performance evaluation of the proposed conditioning approach with the Random Forest model (RF)



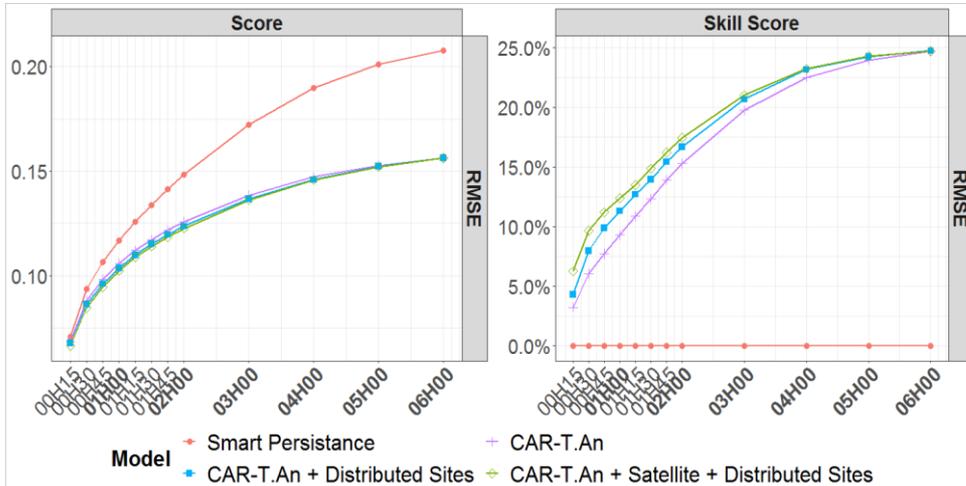
Model names are defined in the [annex](#) section

## Conclusions

- **AR model**
  - The RF approach outperforms the AR model regardless of the considered forecasting horizon
- **CAR model**
  - The proposed conditioning approach outperforms the RF and CRF models.
  - Bad performances from CRF for very short times are supposed to result from over fitting

# Spatio temporal inputs – CARST model

## Performance evaluation of the CAR model with ST inputs



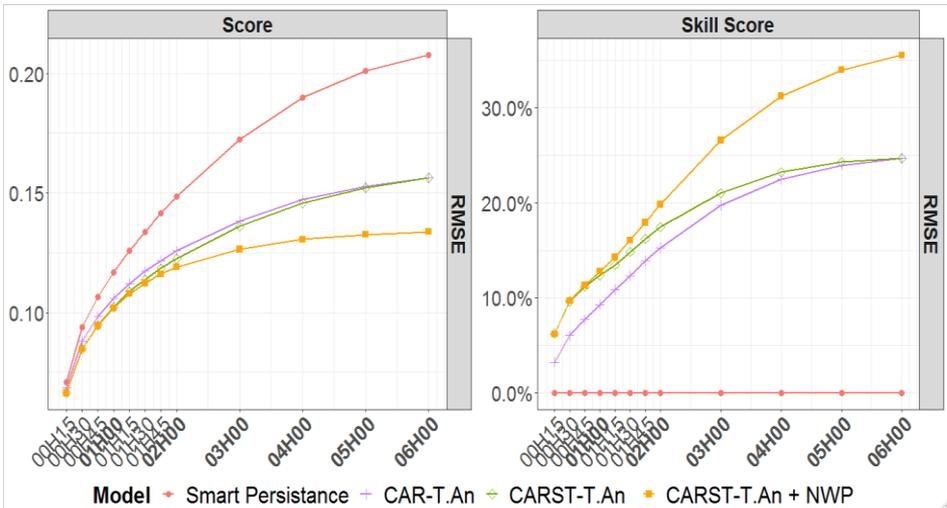
Model names are defined in the [annex](#) section

## Conclusions

- ◆ CARST-T.An Model
  - **ST inputs** (i.e. distributed sites and satellite pixels) **improves performances** for horizons below 6H00 ahead.
  - **Improvement** are higher for 30' horizon and **decrease with time**
  - At **6H00** horizon, the **influence of ST is neglectable**

# NWP inputs – CARXST model

## Performance evaluation of the proposed models



Model names are defined in the [annex](#) section

## Conclusions

- **CARST-T.An Model**
  - For horizon ranging from 15' up to 45', performances **improvement** result from **ST data**
- **CARXST-T.An Model**
  - From 1H up to 6H ahead horizon, the main source of performance **improvement** is due to **NWP**.



**Seamless way to integrate capacity of NWP outputs to extend forecasting horizon**

## Conclusion

- The proposed **conditioned learning improve performances up to 25%** in comparison with a persistence model for a **6H ahead horizon**
- **ST data improve performances for horizon below 6H ahead,**
  - By ~4% for a 30 min horizon
  - Improvement decrease progressively to become neglectable for a 6H horizon
- Combining the proposed conditioning approach with ST and NWP inputs, performances reach ~35% for a 6H lead time in regards with the persistence model
- The **LASSO** features selection enable to propose a **seamless approach**

## Perspectives

- Operational framework: consider NWP of geopotential fields rather than reanalysis
- Improve ST data integration by considering Cloud Motion Vector (CMV) approach

Thanks for your attention.





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Abbreviation	Definition
AR	Auto Regressive
CAR	Auto Regressive model with <b>C</b> onditioned learning
CARST	Conditioned <b>A</b> uto Regressive model with <b>S</b> patio-Temporal inputs
CARXST	Conditioned <b>A</b> uto Regressive model with <b>S</b> patio-Temporal and <b>eX</b> ogenous inputs
CMV	Cloud <b>M</b> otion <b>V</b> ector
CNR	Compagnie <b>N</b> ationale du <b>R</b> hône
GHI	<b>G</b> lobal <b>H</b> orizon Irradiance
LASSO	Least <b>A</b> bsolute <b>S</b> hrinkage and <b>S</b> election <b>O</b> perator
NWP	<b>N</b> umerical <b>W</b> eather <b>P</b> redictions
PV	<b>P</b> hoto <b>V</b> oltaic
ST	<b>S</b> patio <b>T</b> emporal
SS	<b>S</b> kill <b>S</b> core
RF	Random <b>F</b> orest

# Model name definition

Abbreviation	Definition
<b>AR</b>	Auto <b>R</b> egressive model considering all available PV production observations
<b>RF</b>	Random <b>F</b> orest model considering all available PV production observations
<b>CAR</b>	Auto <b>R</b> egressive model with <b>C</b> onditioned learning
<b>CAR-T</b>	<b>AR</b> model <b>C</b> onditioned to the <b>T</b> ime of the day
<b>CAR-T.An</b>	<b>AR</b> model conditioned to the <b>T</b> ime of the day and the synoptic state through an <b>A</b> nalog based method
<b>CRF-T.An</b>	<b>RF</b> model conditioned to the <b>T</b> ime of the day and the synoptic state through an <b>A</b> nalog based method
<b>CARST-T.An</b>	<b>C</b> onditioned <b>A</b> uto <b>R</b> egressive model with <b>S</b> patio- <b>T</b> emporal inputs
<b>CARXST-T.An</b>	<b>C</b> onditioned <b>A</b> uto <b>R</b> egressive model with <b>S</b> patio- <b>T</b> emporal and <b>eX</b> ogenous inputs

# S1 score

## Definition of the S1 score

$$S_1 = 100 \frac{\sum_{i=1}^{I-1} \sum_{j=1}^J \left| \Delta_{i,j}^{i,Target} - \Delta_{i,j}^{i,Candidate} \right| + \sum_{i=1}^I \sum_{j=1}^{J-1} \left| \Delta_{i,j}^{j,Target} - \Delta_{i,j}^{j,Candidate} \right|}{\sum_{i=1}^{I-1} \sum_{j=1}^J \max \left( \left| \Delta_{i,j}^{i,Target} \right|, \left| \Delta_{i,j}^{i,Candidate} \right| \right) + \sum_{i=1}^I \sum_{j=1}^{J-1} \max \left( \left| \Delta_{i,j}^{j,Target} \right|, \left| \Delta_{i,j}^{j,Candidate} \right| \right)}$$

$$\begin{cases} \Delta_{i,j}^{i,X} = V_{i+1,j}^X - V_{i,j}^X \\ \Delta_{i,j}^{j,X} = V_{i,j+1}^X - V_{i,j}^X \end{cases} \quad X \in \{Target, Candidate\}$$

### Where:

- $\Delta_{i,j}^i$  – The east-west geopotential gradient
- $\Delta_{i,j}^j$  – The north-south geopotential gradient
- $V_{i,j}$  – The geopotential field at grid node (i,j)

# Models parameters definition

## Parameters definition

- $\bar{P}_t^x$  – Observed stationarized PV production at time  $t$  for plant  $x$
- $\hat{P}_{t+h}^x$  – Predicted stationarized PV production at time  $t+h$  for plant  $x$
- $A_{t+h}$  – Synoptic weather situation expected at time  $t+h$
- $f_{A_{t+h}}$  – Conditioning approach based on synoptic situation and time of the day
- $\hat{\beta}$  – Regression coefficients
- $L$  – Maximum lag of PV production observations (here, 2H)
- $X$  – Neighbouring sites (here, 5 closest sites are considered)
- $\overline{Sat}_t^i$  – Stationarized GHI observed at pixel  $i$  and time  $t$
- $\overline{NWP}_{t+h}^x$  – Stationarized GHI forecast obtained from NWP output at plant  $x$  and time  $t+h$

## Skill score definition

$$SS(h) = \frac{RMSE_{Model}(h) - RMSE_{Reference}(h)}{\underbrace{RMSE_{Perfect\ model}(h)}_{=0 \forall h} - RMSE_{Reference}(h)}$$

# Main wind in the Rhône valley

## Principal Component Analysis (PCA)

- **PCA** is performed on 1 years of hourly reanalysis (ERA 5) of wind velocity at 750hPa
- The first Principal Component (PC) is represented at the opposite graph
- **Westerly wind** are observed

