

# Analysis of the surface temperature distribution at Badain Jaran Desert using fully coupled hydro-thermal method

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# Contents

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**1. Introduction**

**2. Materials and methods**

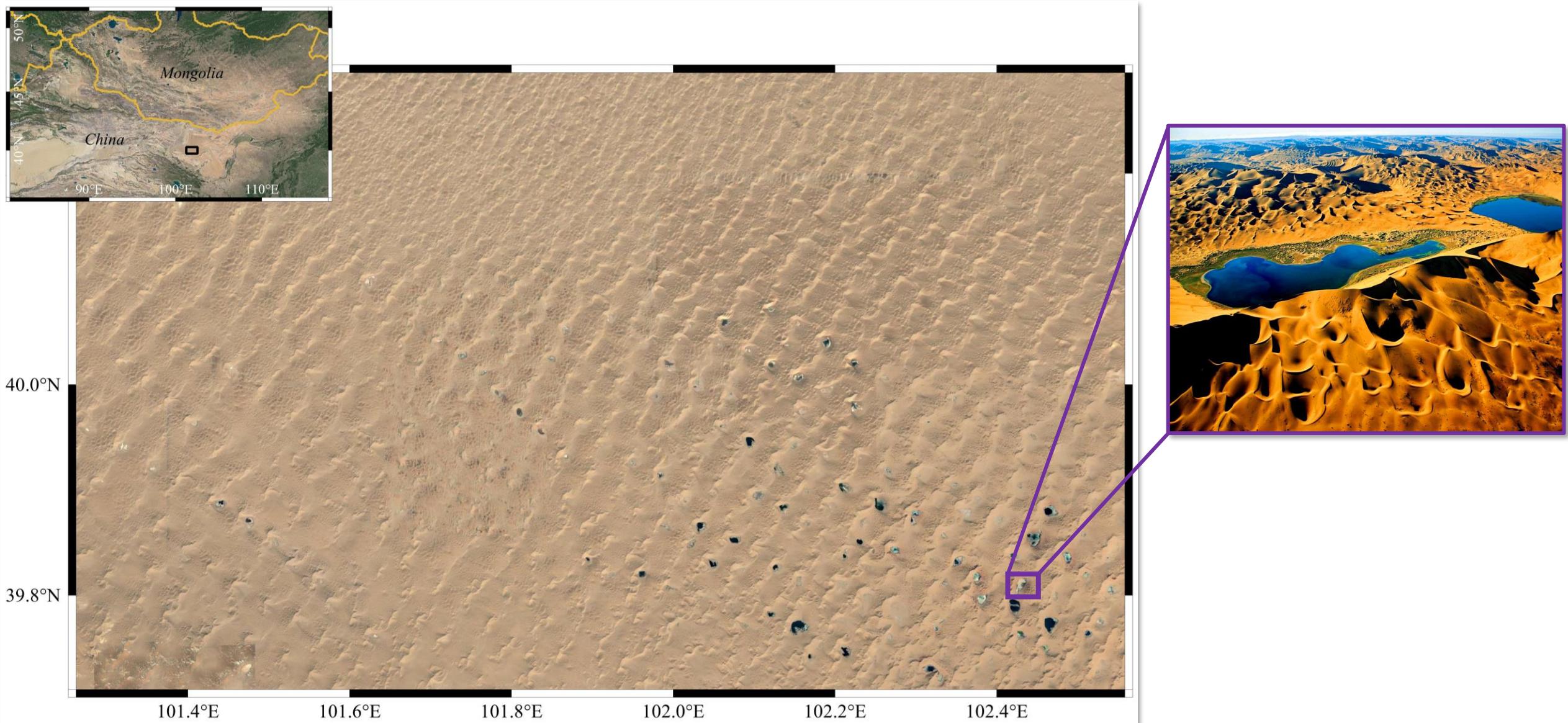
**3. Results**

**4. Discussion**

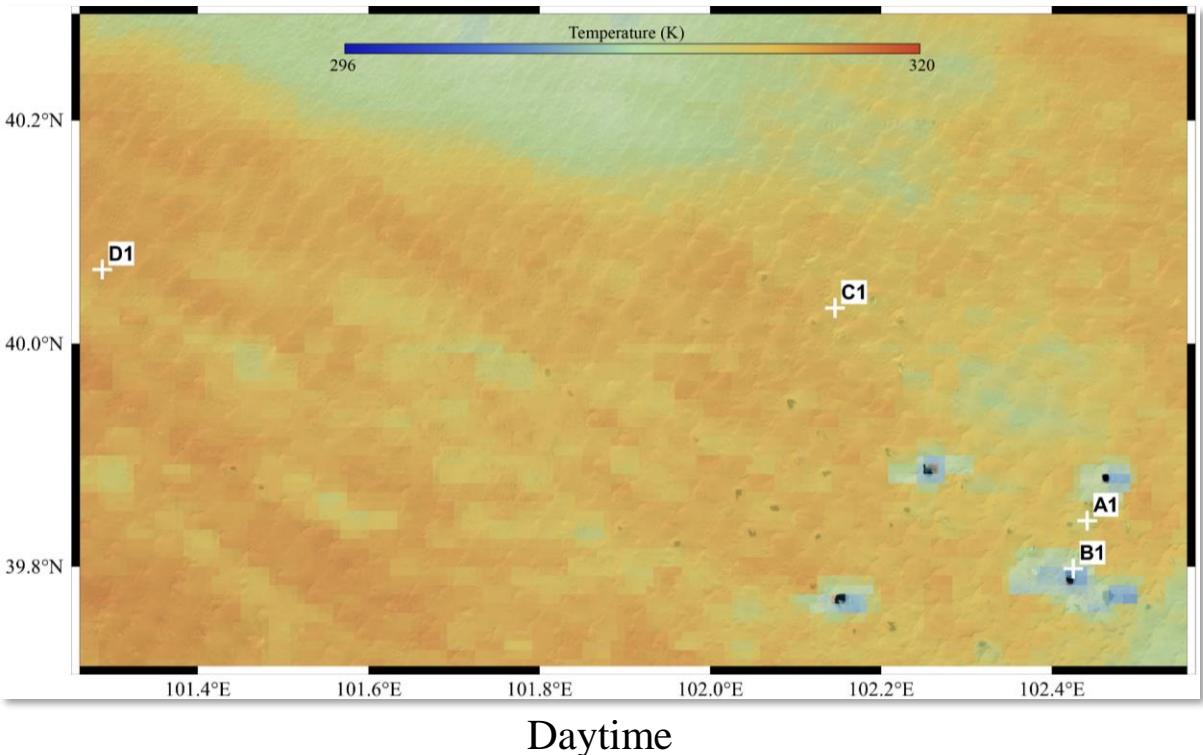
**5. Conclusions**

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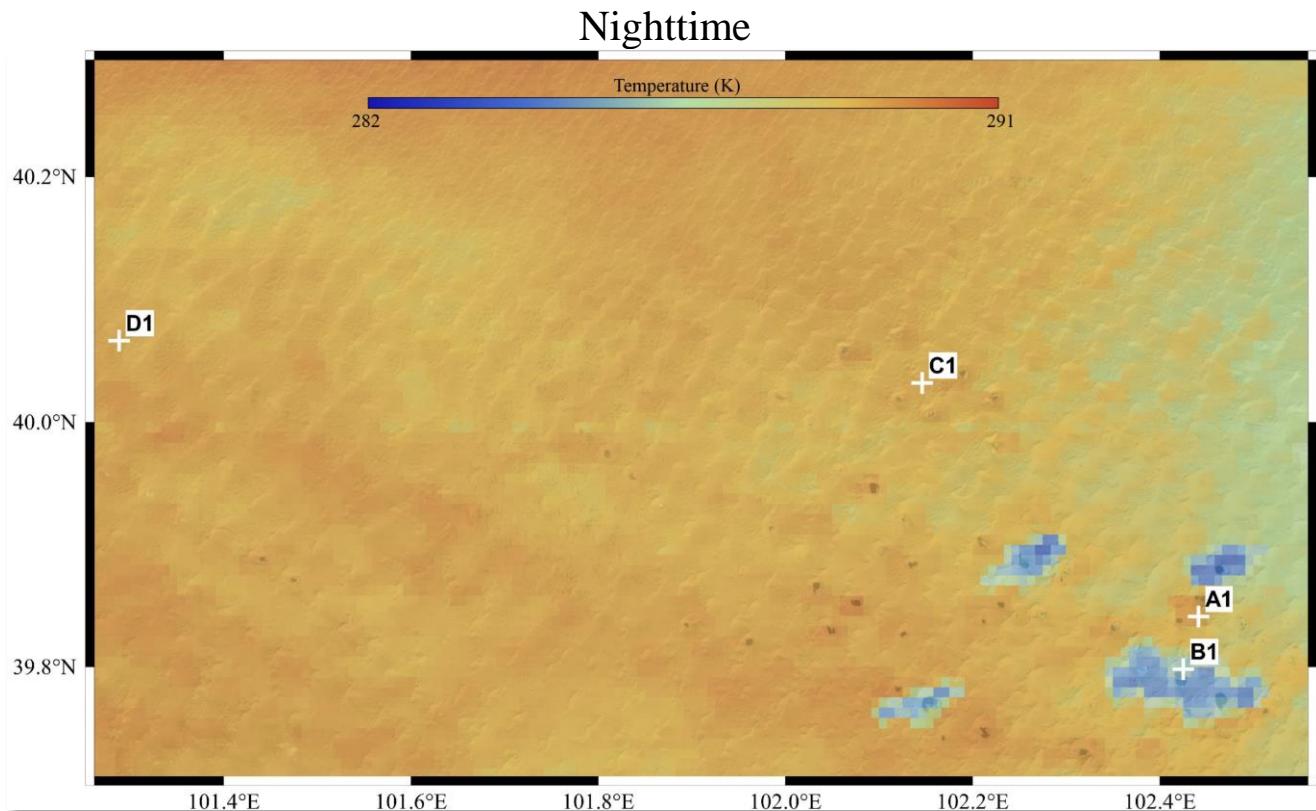
# Badain Jaran Desert site



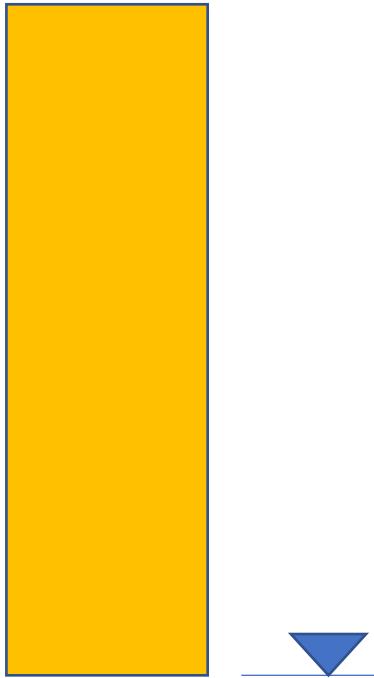
# Surface Temperature at the site



31st August 2008  
(MODIS TERRA)



# Motivation



Water table depth /m ← Surface temperature  $T_s$  ?

0.5

...

32

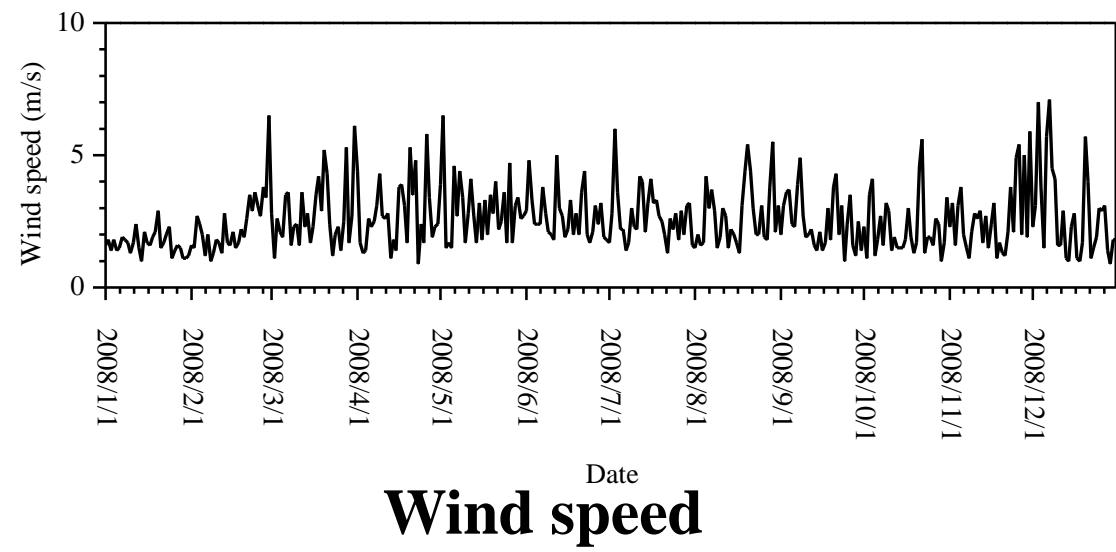
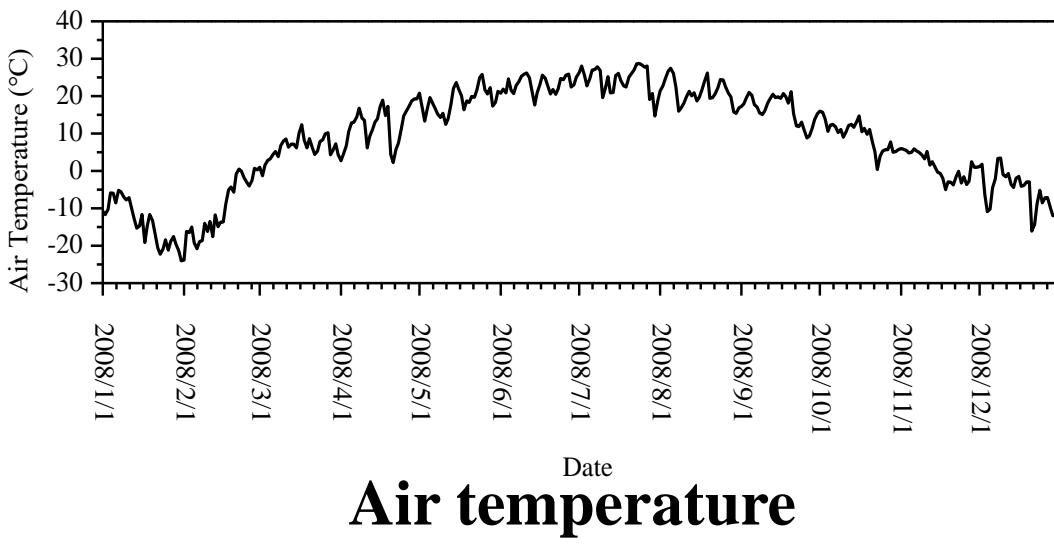
...

165

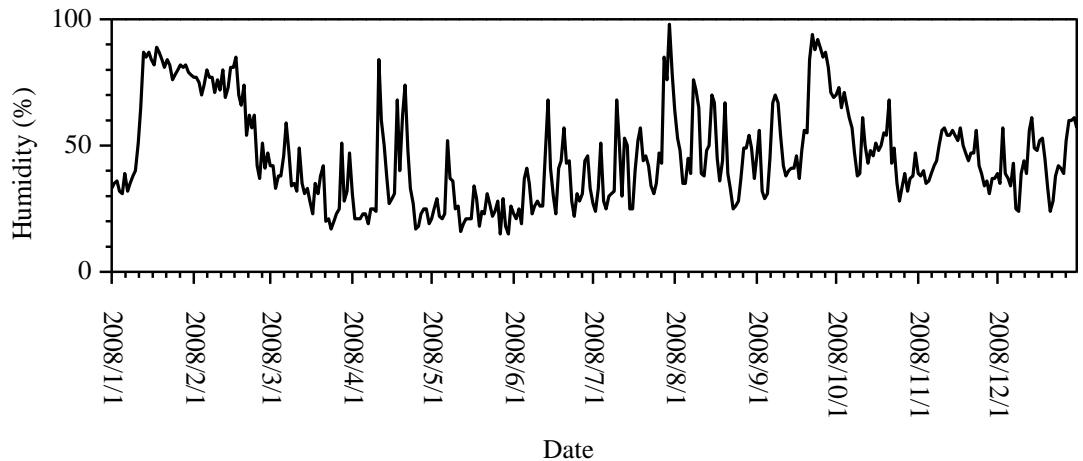
# Meteorological Data



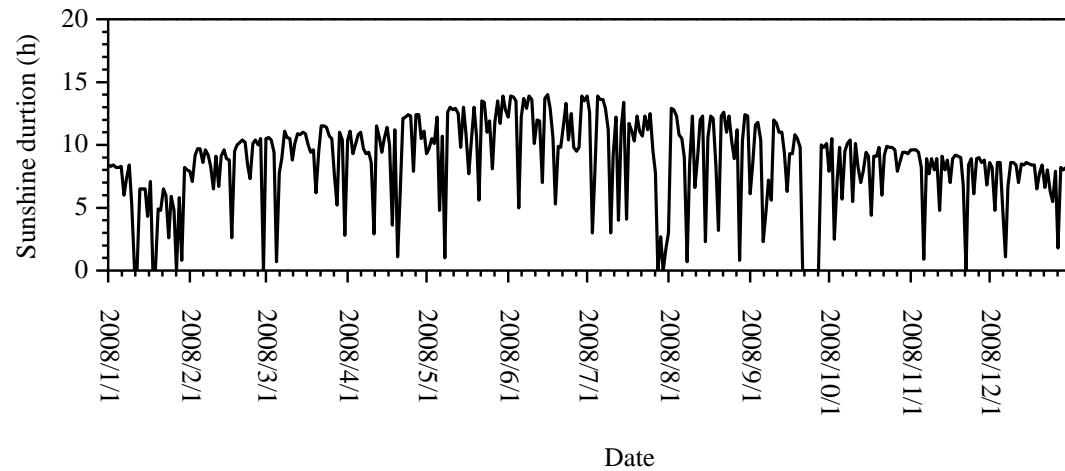
**Minqin station**



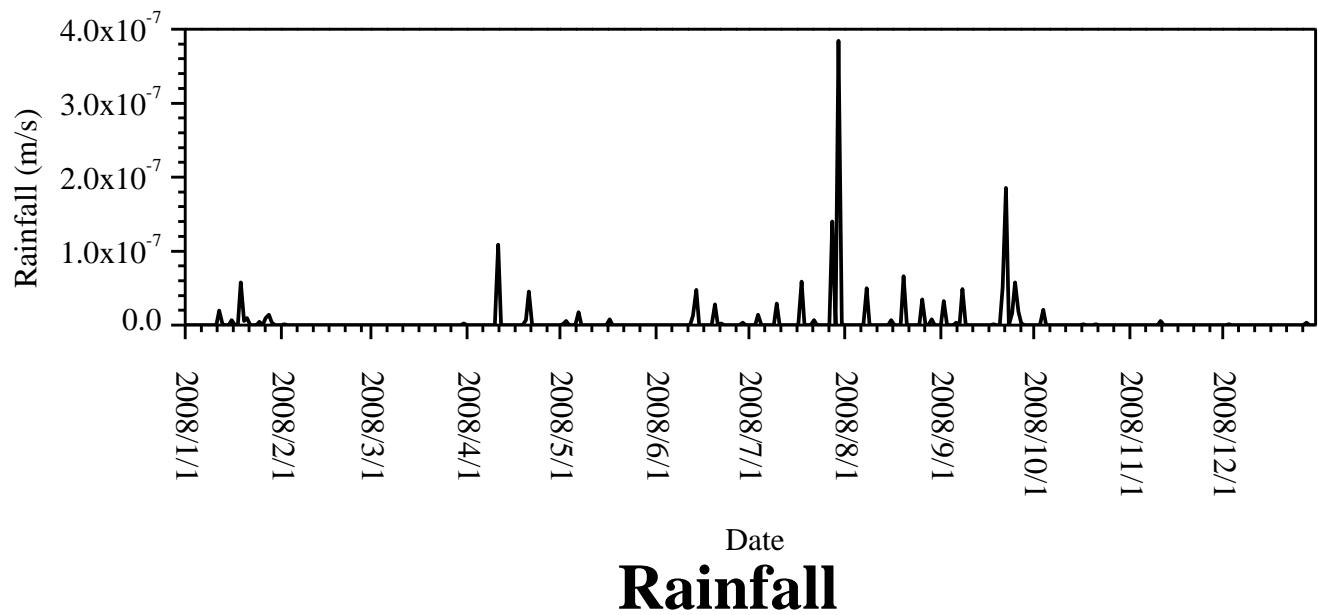
# Meteorological Data – Cont'd



**Humidity**

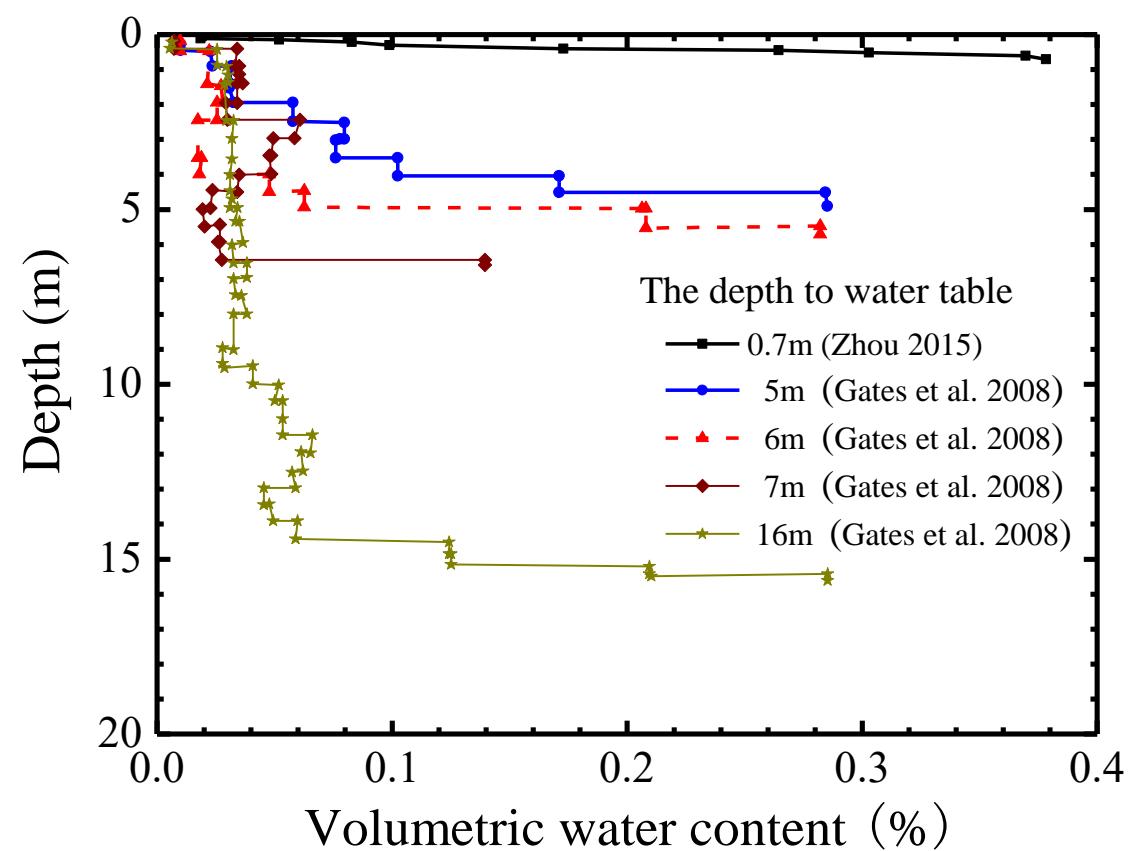


**Sunshine duration**

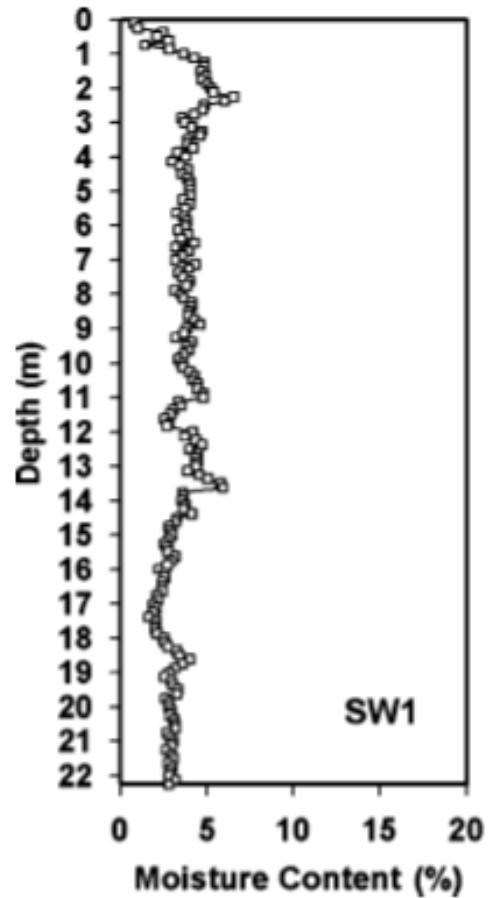


**Rainfall**

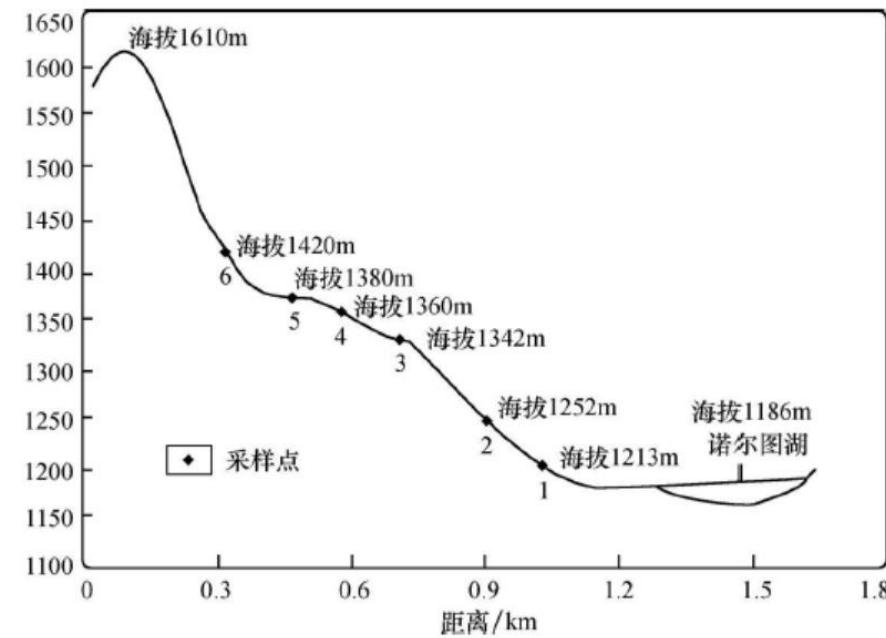
# Volumetric water content



Gates et al. (2008); Zhou (2015)



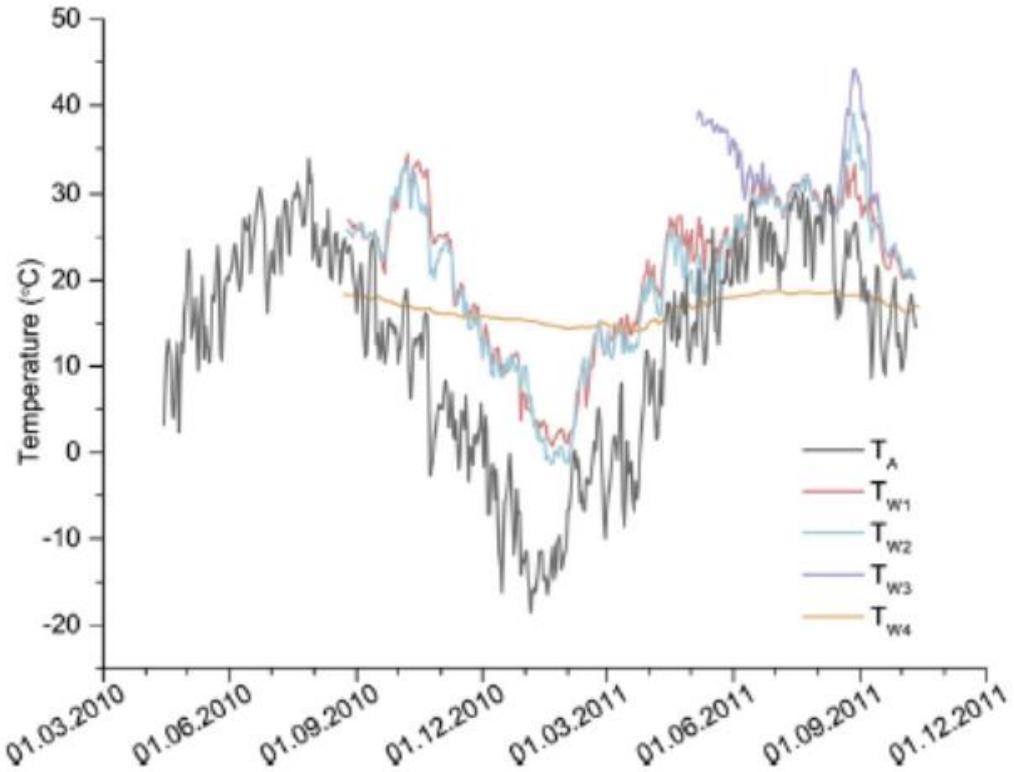
Ma and Eumunds  
(2006)



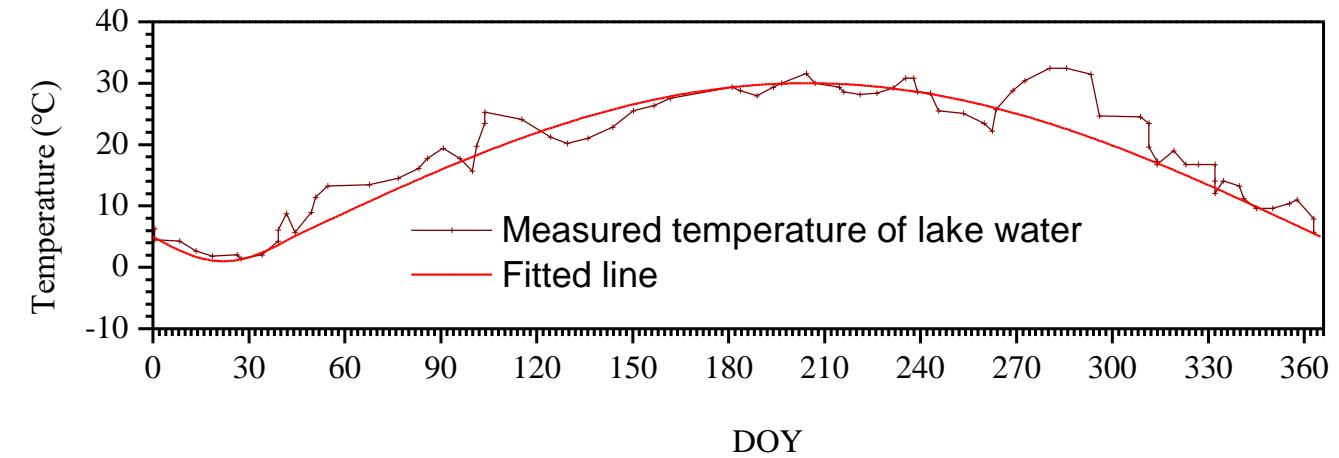
Surface: dry layer 35cm  
 $w < 0.5\% \approx 0.01\%$

Zhao et al. (2011)

# Lake water temperature



Dong et al. (2015)



$$T = \begin{cases} 5 - 4 \times \sin(\text{DOY}/44 \times \pi) & \text{DOY} \leq 44 \\ 5 + 25 \times \sin[(\text{DOY}-44)/322 \times \pi] & 44 < \text{DOY} < 366 \end{cases}$$

# Fully-coupled numerical method

(A1)

The fully coupled hydro-thermal method developed by Anni et al. (2017)

The governing equation of liquid and vapor water mass flow can be expressed as:

$$C_\varphi \frac{\partial \varphi}{\partial t} + C_{\varphi T} \frac{\partial T}{\partial t} = \nabla \cdot [K_\varphi \nabla \varphi] + \nabla \cdot [K_{\varphi T} \nabla T] + \rho_l \nabla K_w$$

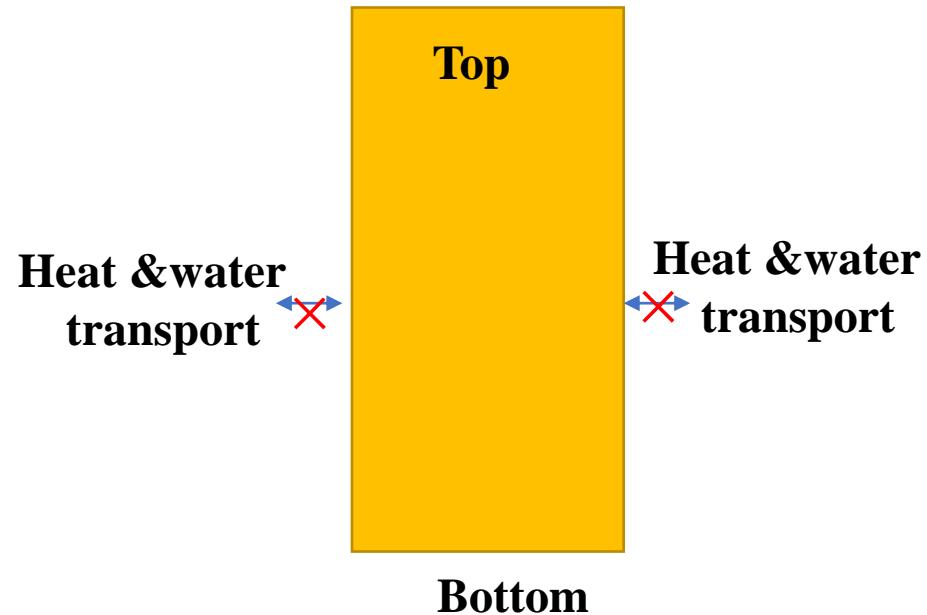
The governing equation of heat flow can be expressed as:

$$C_T \frac{\partial T}{\partial t} + C_{T\varphi} \frac{\partial \varphi}{\partial t} = \nabla \cdot [K_T \nabla T] + \nabla \cdot [K_{T\varphi} \nabla \varphi]$$

# Initial and boundary conditions

(A1)

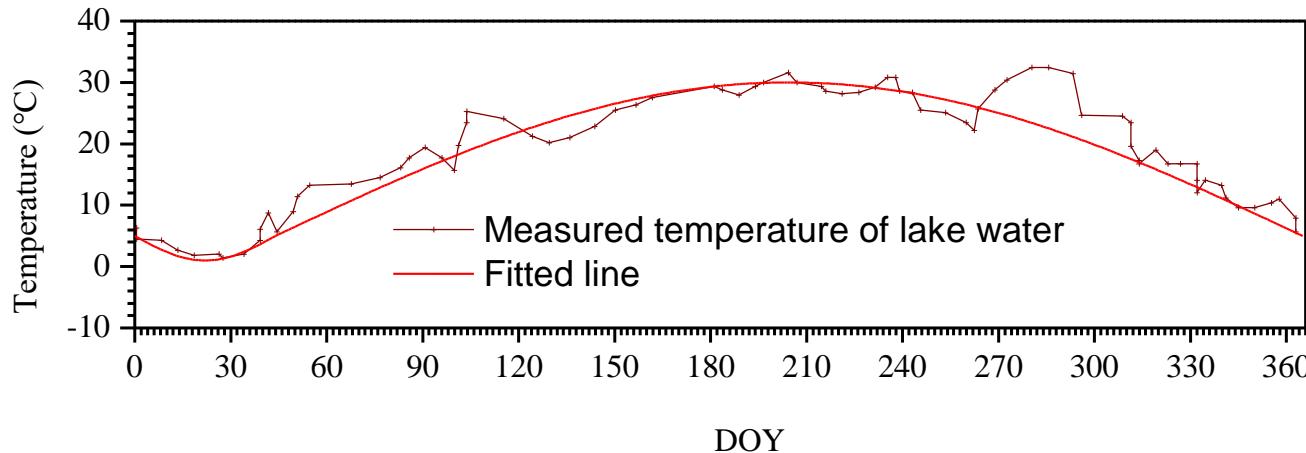
Initial temperature: 5°C Initial suction: hydrostatic equilibrium line



# Bottom boundary condition:

(A1)

## (1) Temperature at bottom



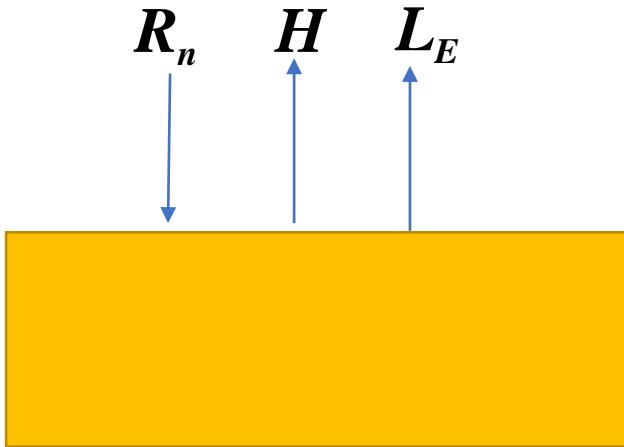
$$T = \begin{cases} 5 - 4 \times \sin(\text{DOY}/44 \times \pi) & \text{DOY} \leq 44 \\ 5 + 25 \times \sin[(\text{DOY}-44)/322 \times \pi] & 44 < \text{DOY} < 366 \end{cases}$$

## (2) Suction at bottom

$$\varphi = 0$$

# Heat flux at the top boundary

(A1)

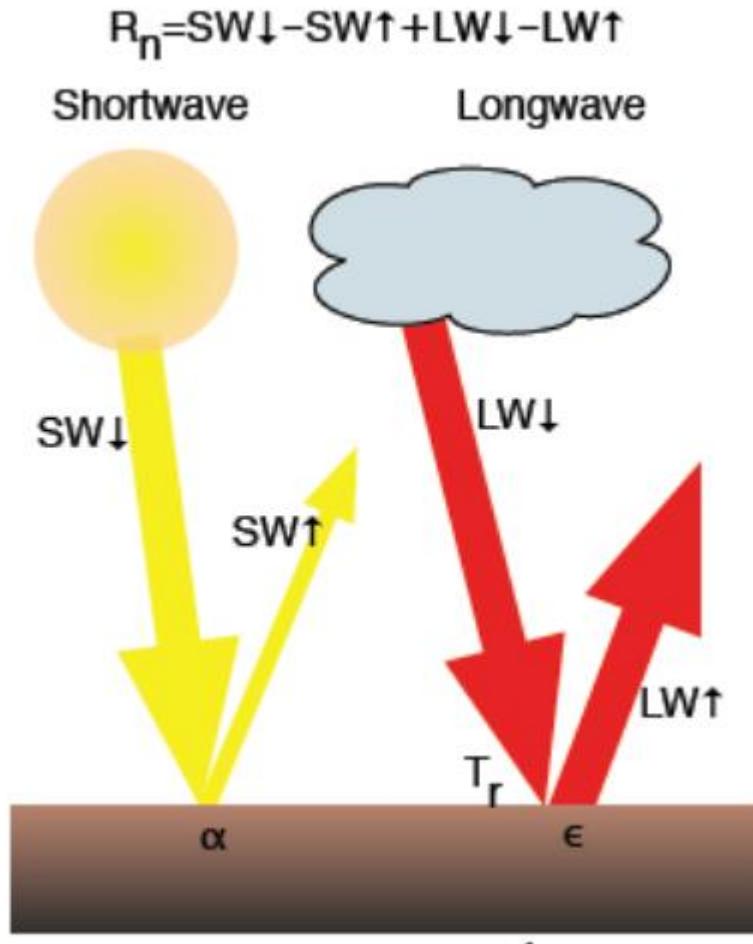


$$q_{htop} = -R_n + H + L_E$$

# The net solar radiation

(A1)

## The net solar radiation



$$SW \downarrow = \left( 0.25 + 0.5 \frac{n}{N} \right) R_{sa}$$

$$SW \uparrow = \alpha SW \downarrow$$

$$LW \downarrow = \varepsilon_a \sigma T_a^4$$

$$LW \uparrow = \varepsilon_s \sigma T_{surf}^4$$

# Sensible heat and latent heat

(A1)

## The sensible heat

$$H = \frac{\rho_a C_{pa} (T_s - T_a)}{r_a}$$

## The latent heat

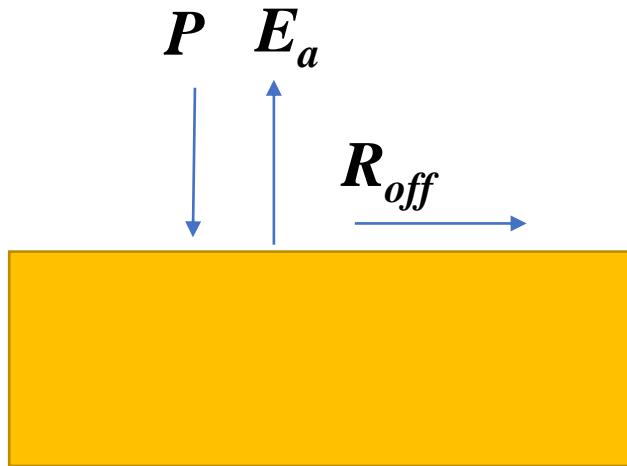
$$L_E = 1000 L_v E_a$$

$$\frac{E_a}{E_p} = \frac{e_0 - e_a}{e_s - e_a}$$

$$E_p = \frac{10^{-3}}{86400} (a + bu)(100 - h_a) \quad \text{Song (2015)}$$

# Water flux at the top boundary

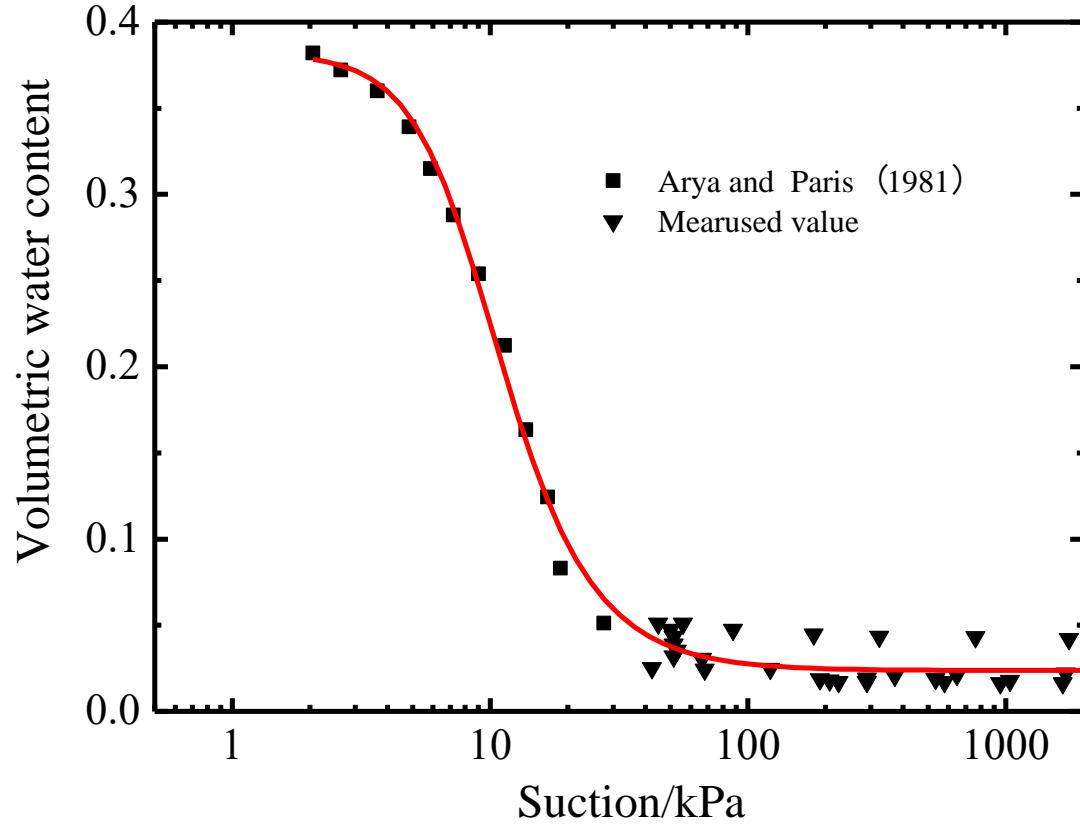
(A1)



$$q_{wtop} = E_a - (P - R_{off})$$

# Hydraulic property

(A1)



Water retention curve

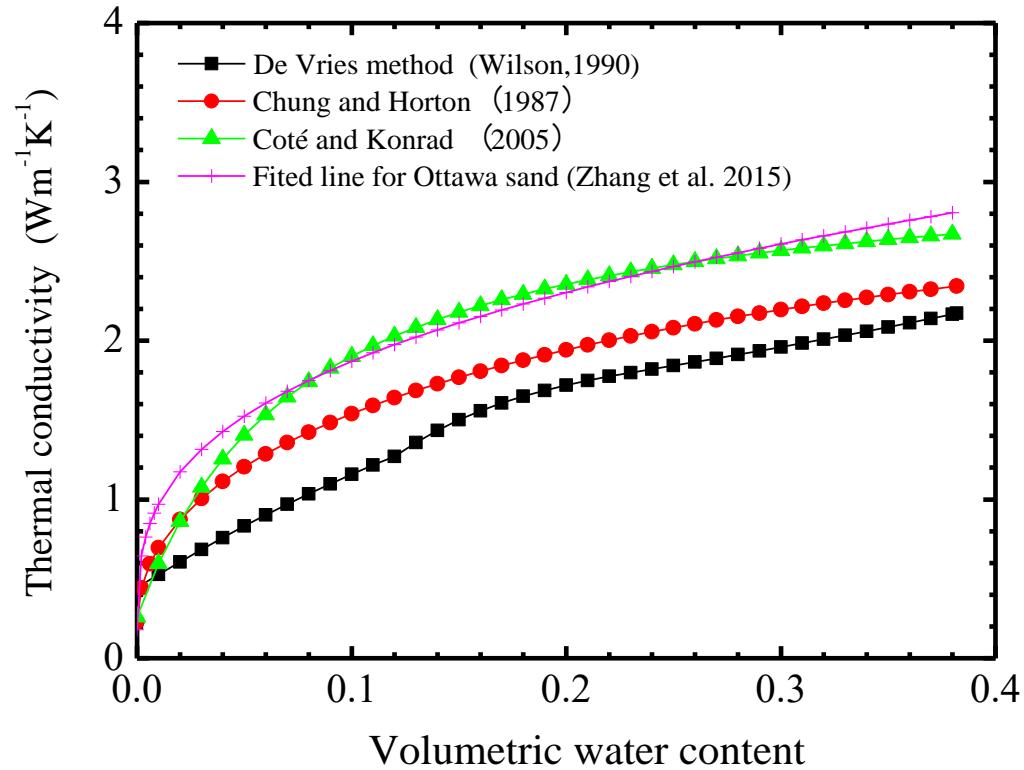
## VG model

Parameter	value
$a(\text{cm})$	88.3
$\theta_s$	0.382
$\theta_r$	0.0237
$n$	2.87
$k_s (\text{m/s})$	$1.06 \times 10^{-4}$

$$\theta = \theta_r + \frac{(\theta_s - \theta_r)}{\left(1 + \left(\frac{\psi}{a}\right)^n\right)^m}$$

$$k = k_s \Theta^{0.5} [1 - (1 - \Theta^{1/m})^m]^2$$

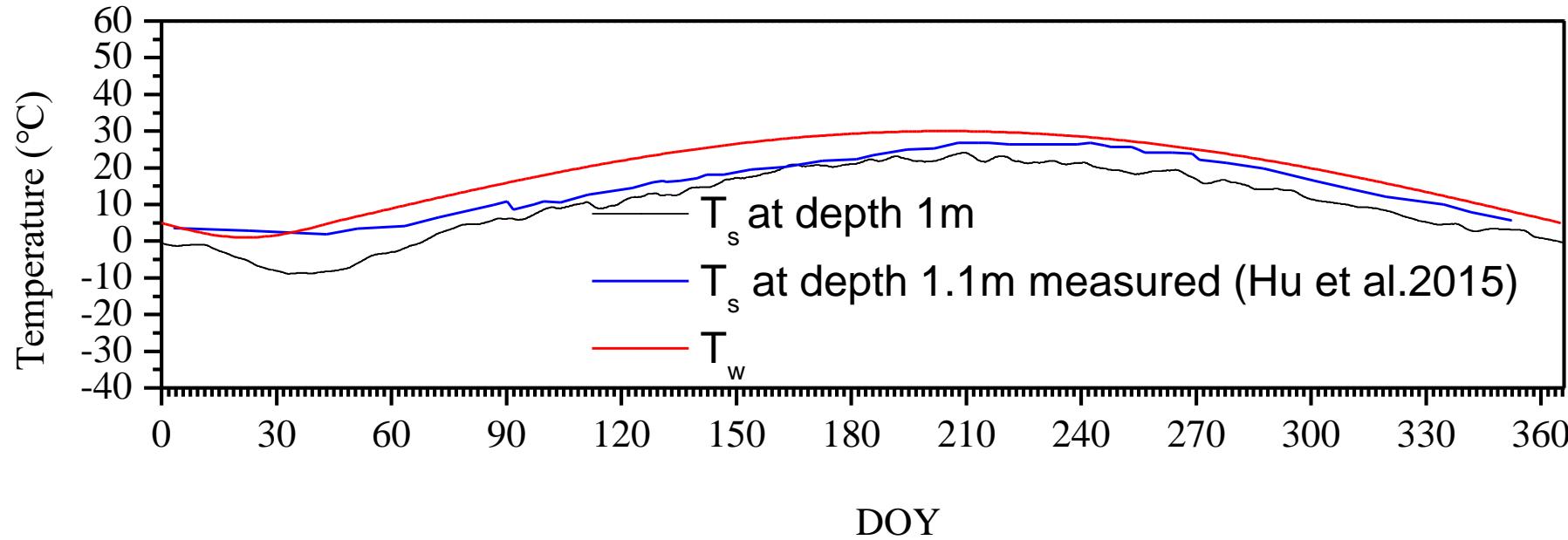
# Thermal property



$$\lambda = 0.18 + 3.61\theta^{0.33}$$

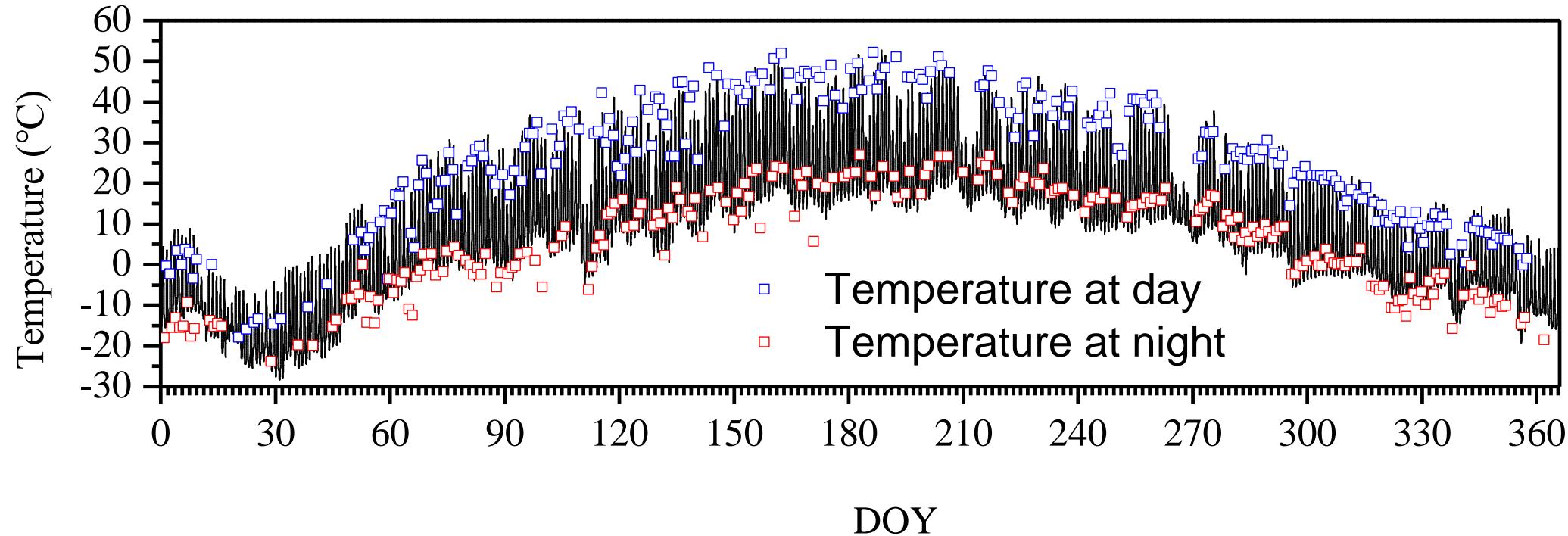
## Heat conductivity

# Calculation vs measurement at about 1 m depth

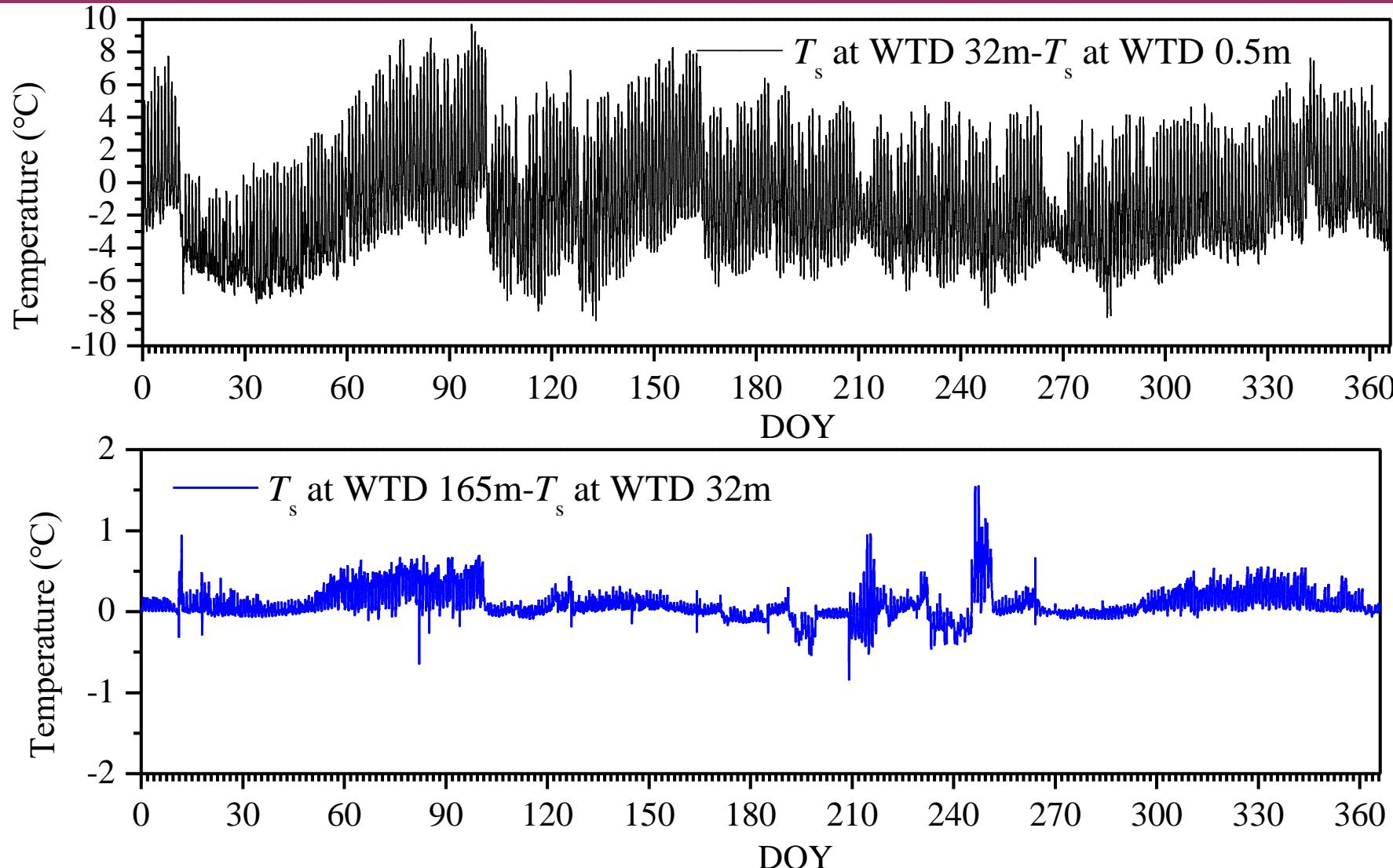


**Soil temperature at about 1m depth**

# Calculated and measured temperatures (B1)



# Surface temperature difference between different WTB depths



Surface temperature difference for different water table depth (WTD)

# Conclusions

- (1) The numerical approach can be used to correctly determine the soil surface temperature changes with varying water table depth.
- (2) The hydraulic and thermal parameters need to be refined to increase the calculation quality.
- (3) Slope direction seems to be important to be accounted for because it can greatly affect the solar radiation, wind speed etc.