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# Models Bridging Subduction and Earthquake Dynamics Show Fault Strength as a Strain-average Quantity

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Ylona van Dinther

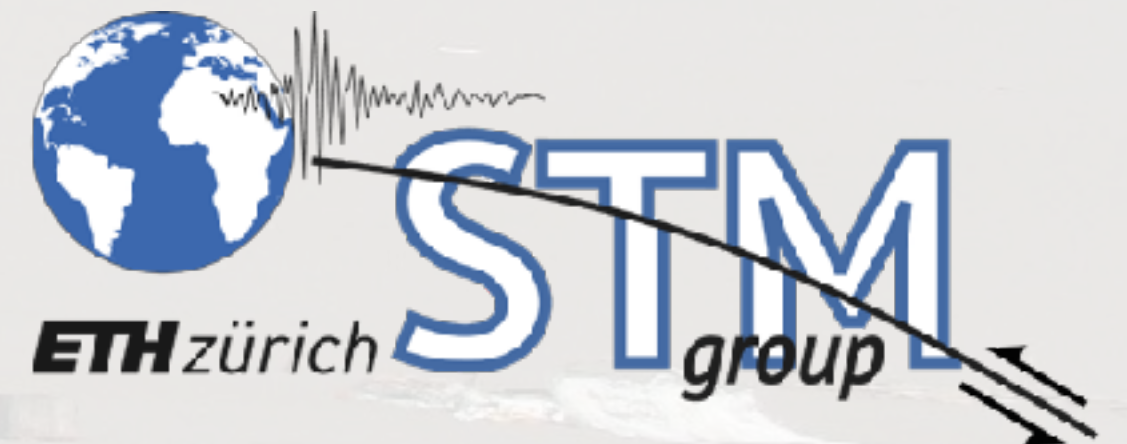
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Department of Earth Sciences, Utrecht University

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- **What strength / friction values are appropriate across various scales?**

- Geodynamic modelers interested in simulating subduction and plate tectonics:  $\mu_{\text{eff,static}} < \sim 0.05$
- Earthquake modelers interested in frictional sliding typically use Byerlee's friction ( $\mu \sim 0.6-0.85$ ):  $\mu_{\text{eff,static}} > \sim 0.5$

$$\mu_{eff} = 1 - \frac{Pf}{P} = 1 - \lambda$$

- Are these results as far apart as they seem? I show that
  - » Recent cross-scale and earthquake models converge perspectives
  - » Analytical considerations constrained by observations and laboratory experiments suggest  $\mu_{\text{eff,char}}$  is about **0.02 - 0.3**

# Long-standing debate: How weak or strong? Why?

- Absent local heat flow anomaly  
[e.g., Lachenbruch and Sass, 1992]

- Stress field rotation & z-indep. stress drop  
[e.g., Hardebeck, 2015]

- Differential stress estimates  
[e.g., Seno, 2009]

- Sustain subduction in models  
[e.g., Zhong et al., 1998; Duarte et al., 2015]

- ...

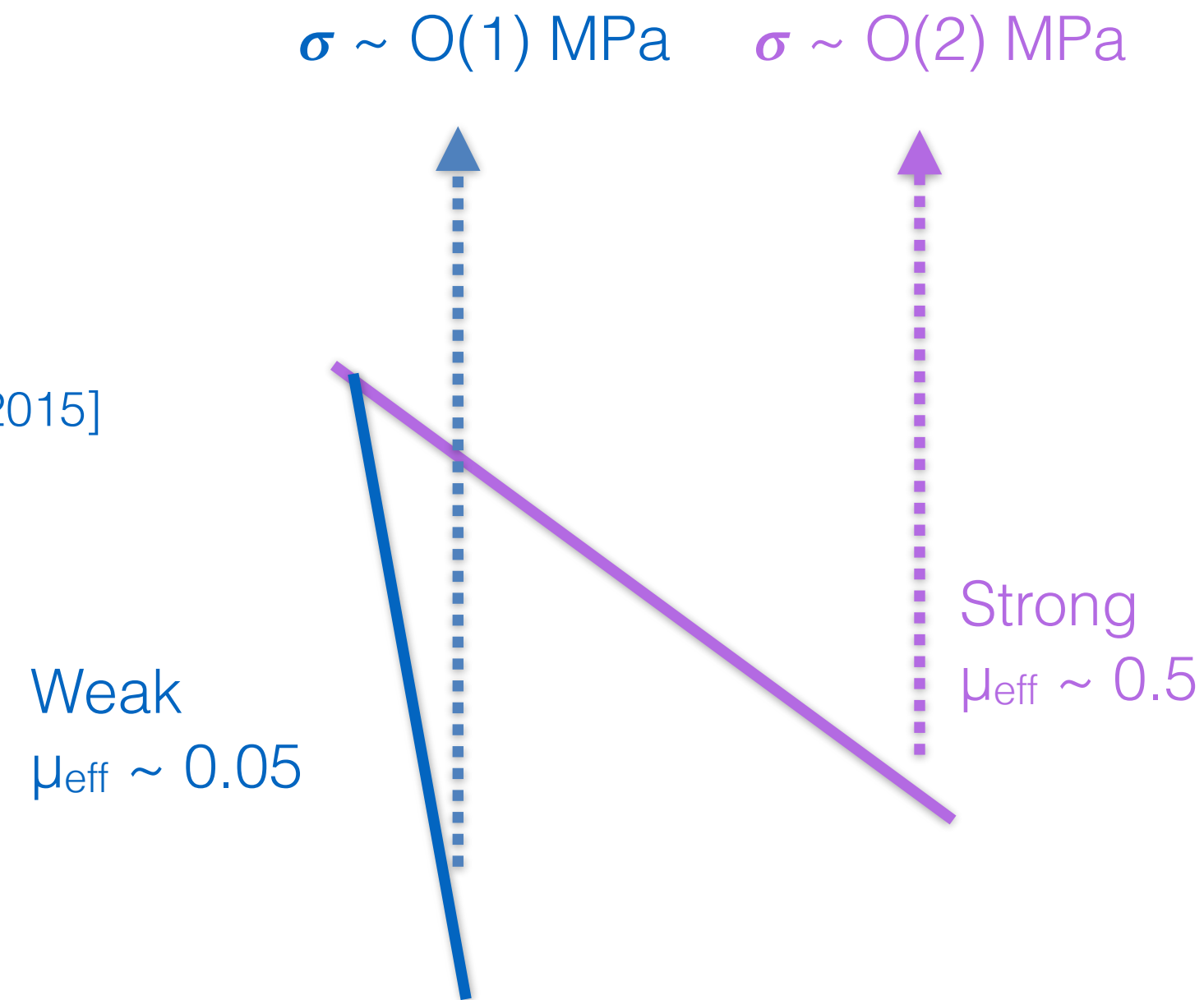
- Laboratory experiments  
(e.g., Byerlee, 1978)

- In-situ stress measurements  
(e.g., Brody et al., 1997)

- Dip orientation of earthquakes on (re-activated) faults  
(e.g., Sibson and Xie, 1998)

- Sustain mountains

- ...



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# I. Revisit arguments

- Absent local heat flow anomaly  
[e.g., Lachenbruch and Sass, 1992]

- Stress field rotation & z-indep. stress drop  
[e.g., Hardebeck, 2015]

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- **Sustain subduction in models**  
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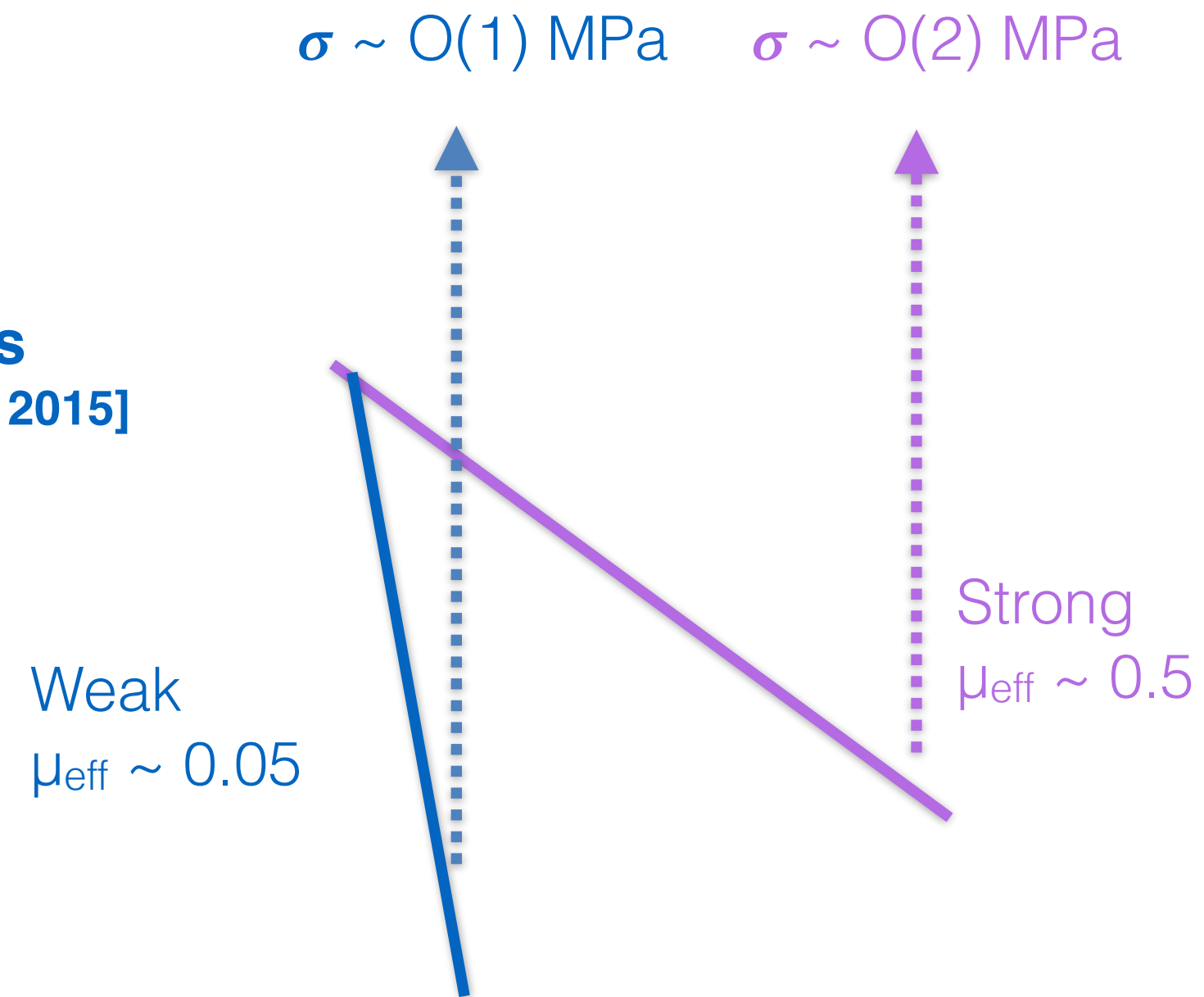
- **Laboratory experiments**  
(e.g., Byerlee, 1978)

- In-situ stress measurements  
(e.g., Brody et al., 1997)

- Dip orientation of earthquakes on (re-activated) faults  
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- **Sustain mountains**

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## II. Estimate what mechanisms are most important

- Absent local heat flow anomaly  
[e.g., Lachenbruch and Sass, 1992]

- Stress field rotation & z-indep. stress drop  
[e.g., Hardebeck, 2015]

- Differential stress estimates  
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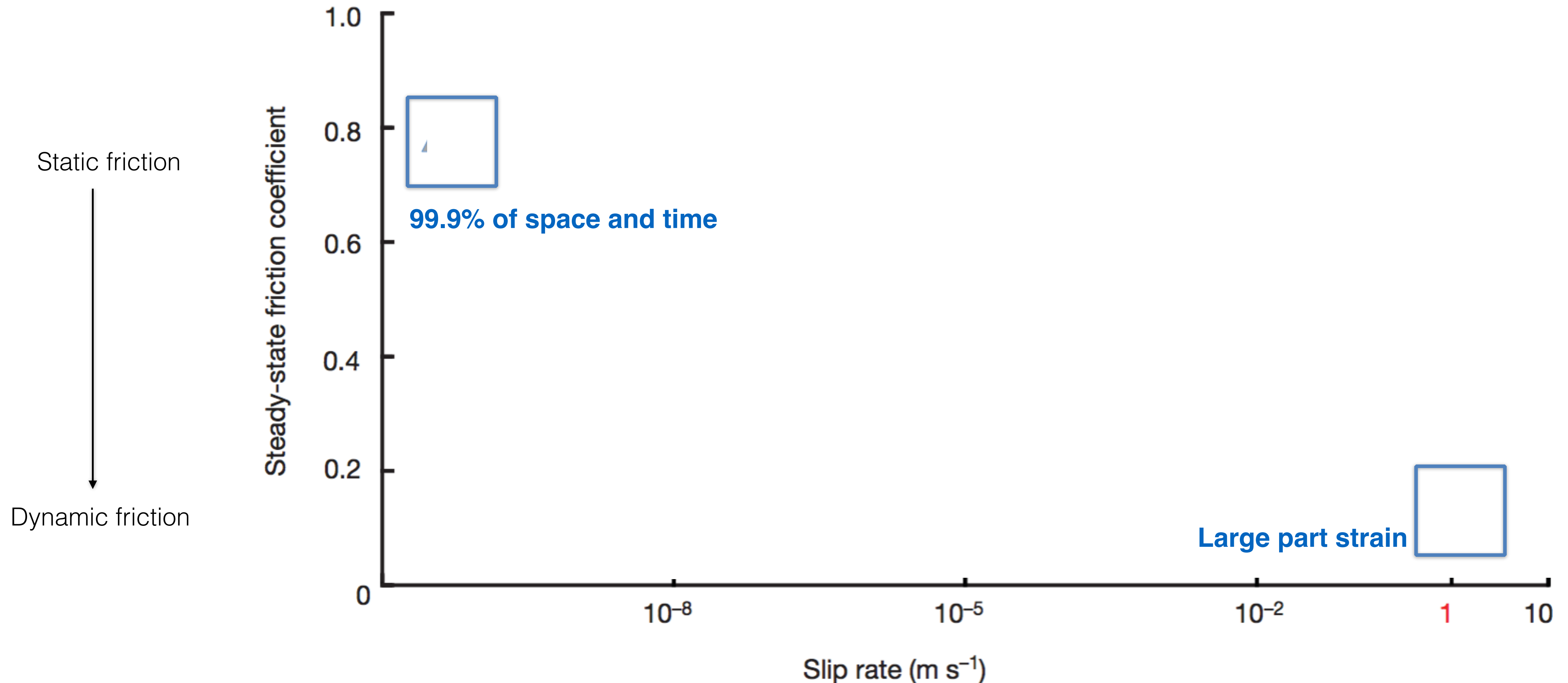
- What weakening mechanism is most important?

- High pore fluid pressures
- Low static friction
- Large dynamic earthquake weakening

## Rocks are almost always strong, but not at coseismic slip rates where most strain occurs

- High-speed lab experiments reveal enhanced dynamic weakening [e.g., Di Toro et al., Nature, 2011]

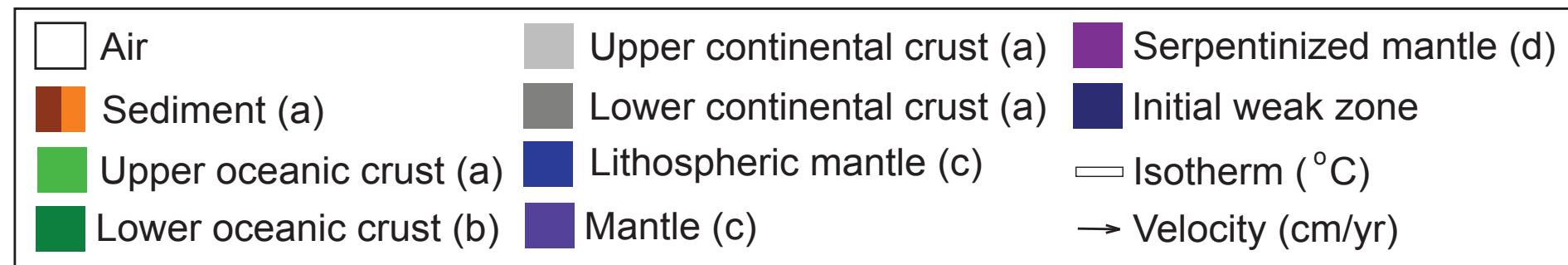
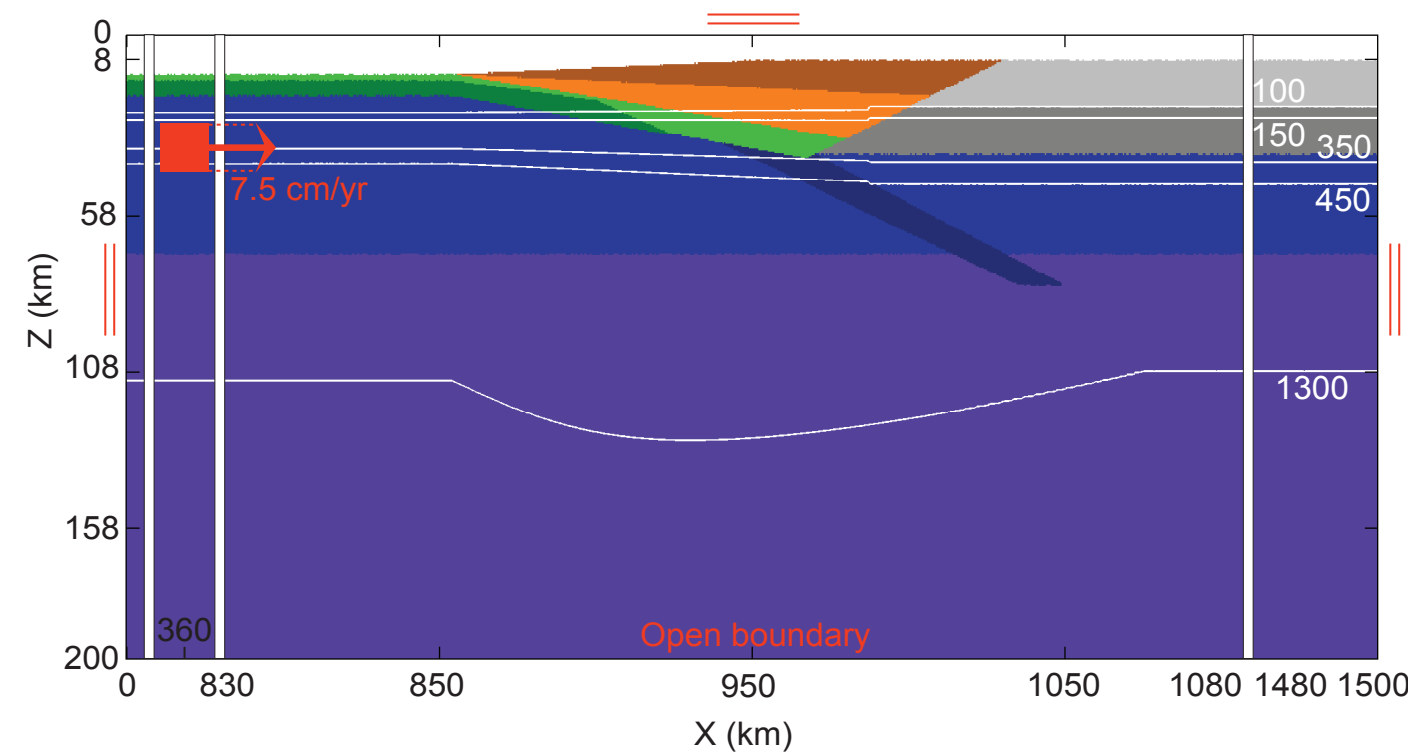
- Low slip rates  $\mu_{\text{eff}} \sim 0.7$
  - High coseismic slip rates  $\mu_{\text{eff}} \sim 0.15$
- } dynamic weakening  $\gamma \sim 0.79$        $\gamma = 1 - \frac{\mu_d}{\mu_s}$





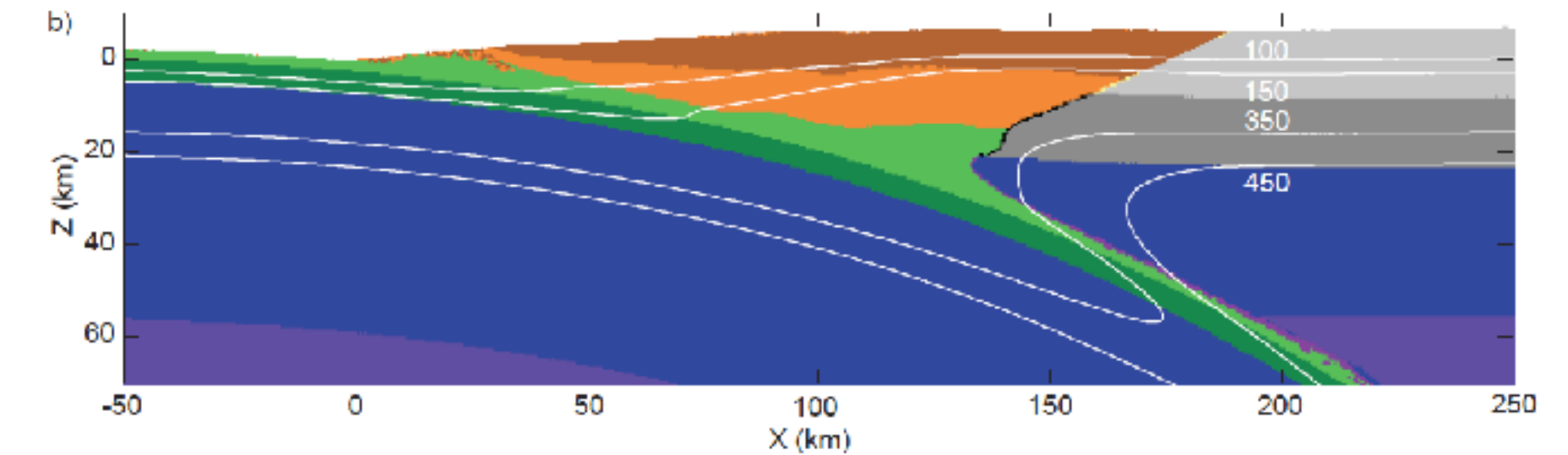
# Models simulating both long- and short-term dynamics

- Included dynamic weakening in geodynamic models [Seismo-Thermo-Mechanical; STM; van Dinther et al., 2013a,b]



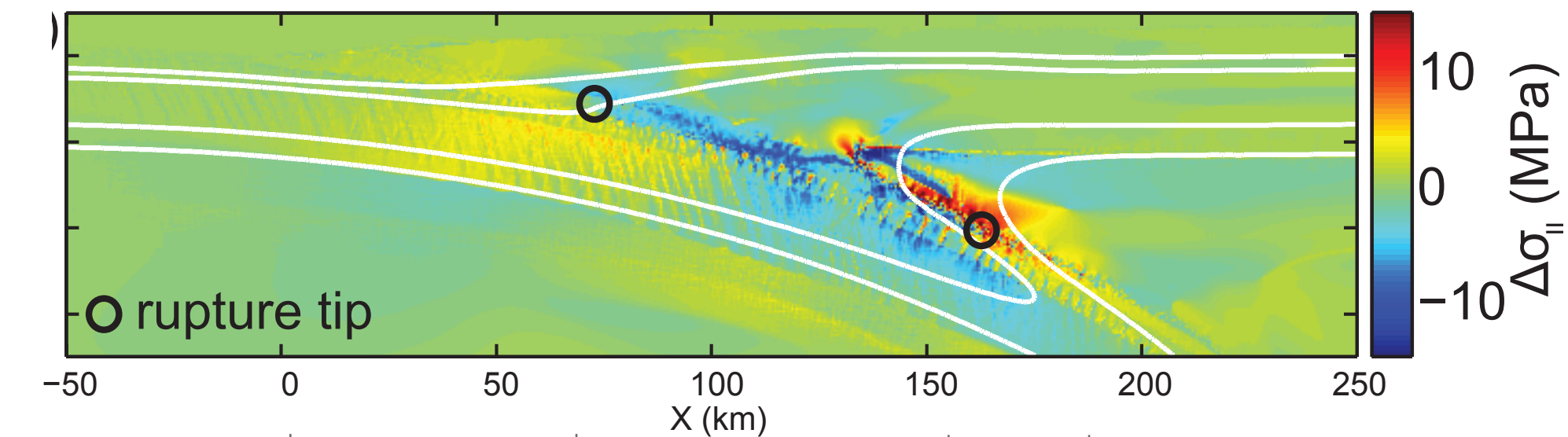
Conservation of mass,  
momentum and heat

Visco-elasto-plastic rheology



>> Spontaneous state and geometry  
e.g., stress, temperature, viscosity, fluid distribution

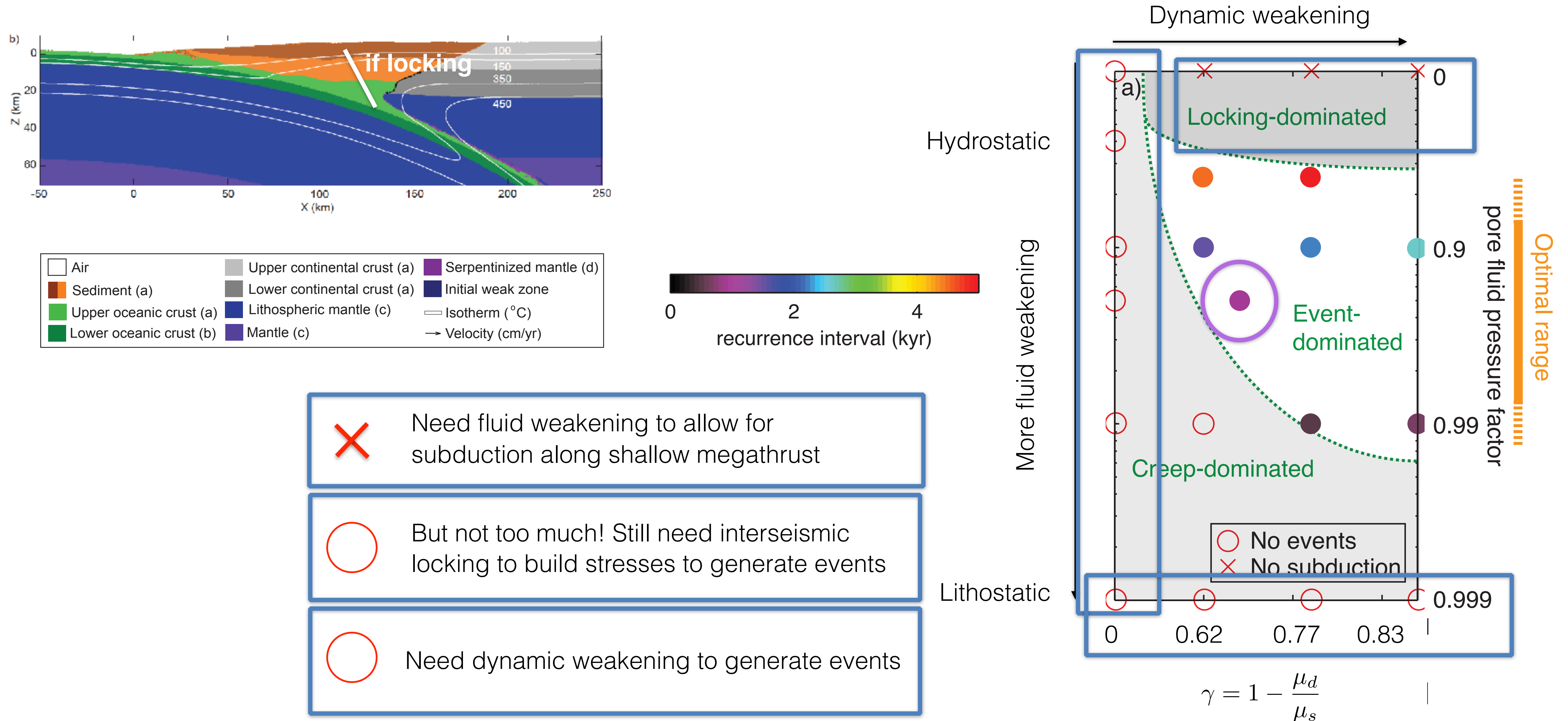
Small time steps  
+ rate-dep. friction  
+ inertia



>> Spontaneous rupture nucleation, propagation and arrest

# Need fluid and dynamic weakening in cross-scale models

- For subduction, mountain building, and reasonable earthquake characteristics need  $\sim 0.005 < \mu_{\text{eff, static}} < \sim 0.125$

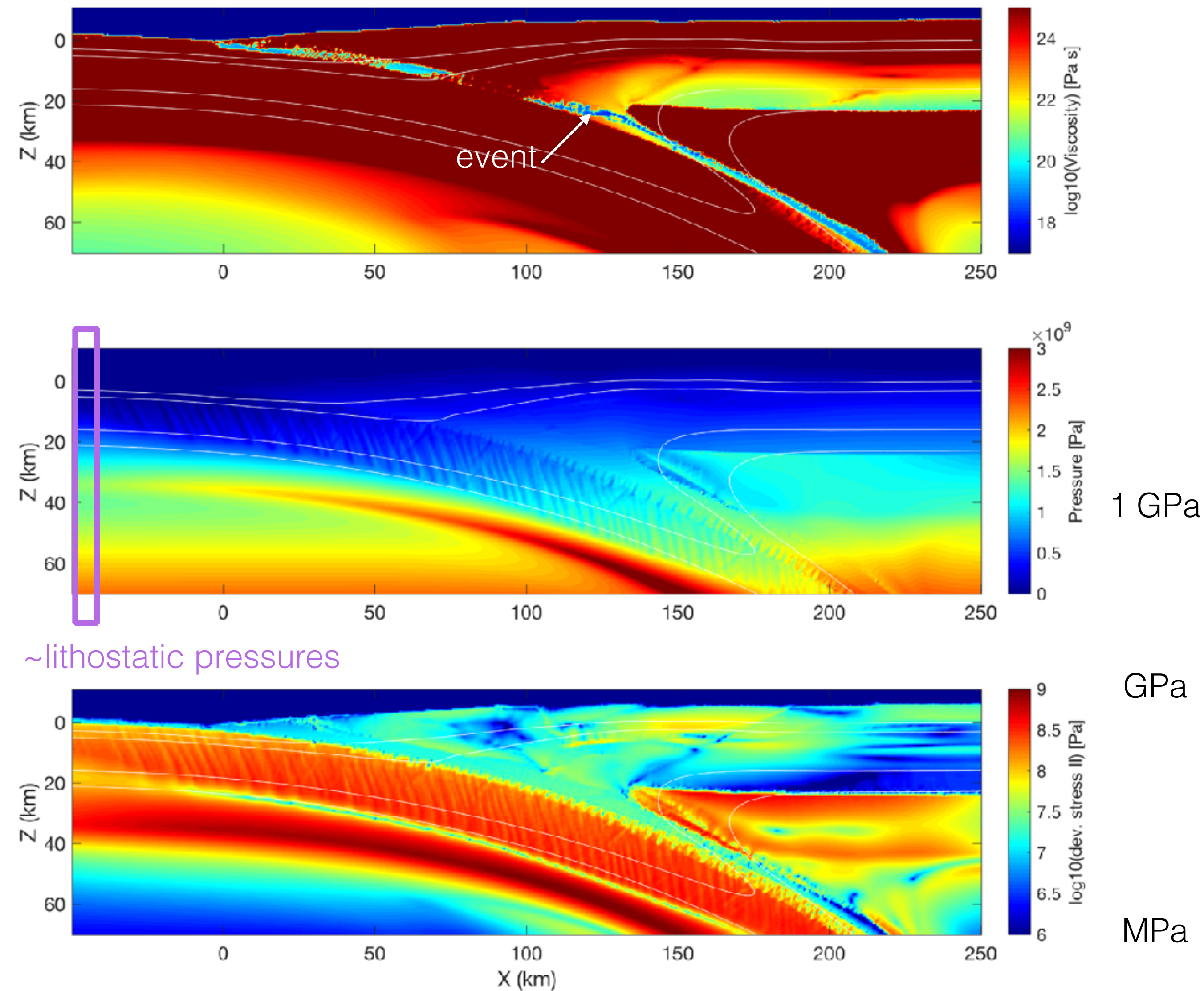




## Very weak @ very limited space or time does not mean weak throughout

- Temporarily weak ( $\sim 10$  MPa min.) and continuously overpressurized megathrust does not mean weak throughout lithosphere!

- Could still build mountains



max. megathrust  $\sigma'_{II} \sim 40$  MPa,  
but elsewhere still almost GPa

$$\mu_{\text{eff, static}} = 0.05$$

- » Rocks are “always” strong, but weak during dynamic slip, where most strain occurs → How do we account for that in long-term models?
- Consider friction as a strain-average quantity:
- Time-integrated mechanical energy dissipation

For equations I refer to van Dinther, in prep.

>> Derive constraints from observations and laboratory experiments



## Long-term fault strength as a strain-average quantity

- » Rocks are “always” strong, but weak during dynamic slip, where most strain occurs → How do we account for that in long-term models?
- Consider friction as a strain-average quantity, since

$$H = \int \sigma_{ij(d)} \dot{\epsilon}_{ij(d)} dt + \int \sigma_{ij(s)} \dot{\epsilon}_{ij(s)} dt$$

- Mechanical consistency of energy and strain for unresolved **d**ynamics requires

$$\sigma_{II(c)} = \frac{\epsilon_{II(d)}}{\epsilon_{II(d)} + \epsilon_{II(s)}} \sigma_{II(d)} + \frac{\epsilon_{II(s)}}{\epsilon_{II(d)} + \epsilon_{II(s)}} \sigma_{II(s)}$$

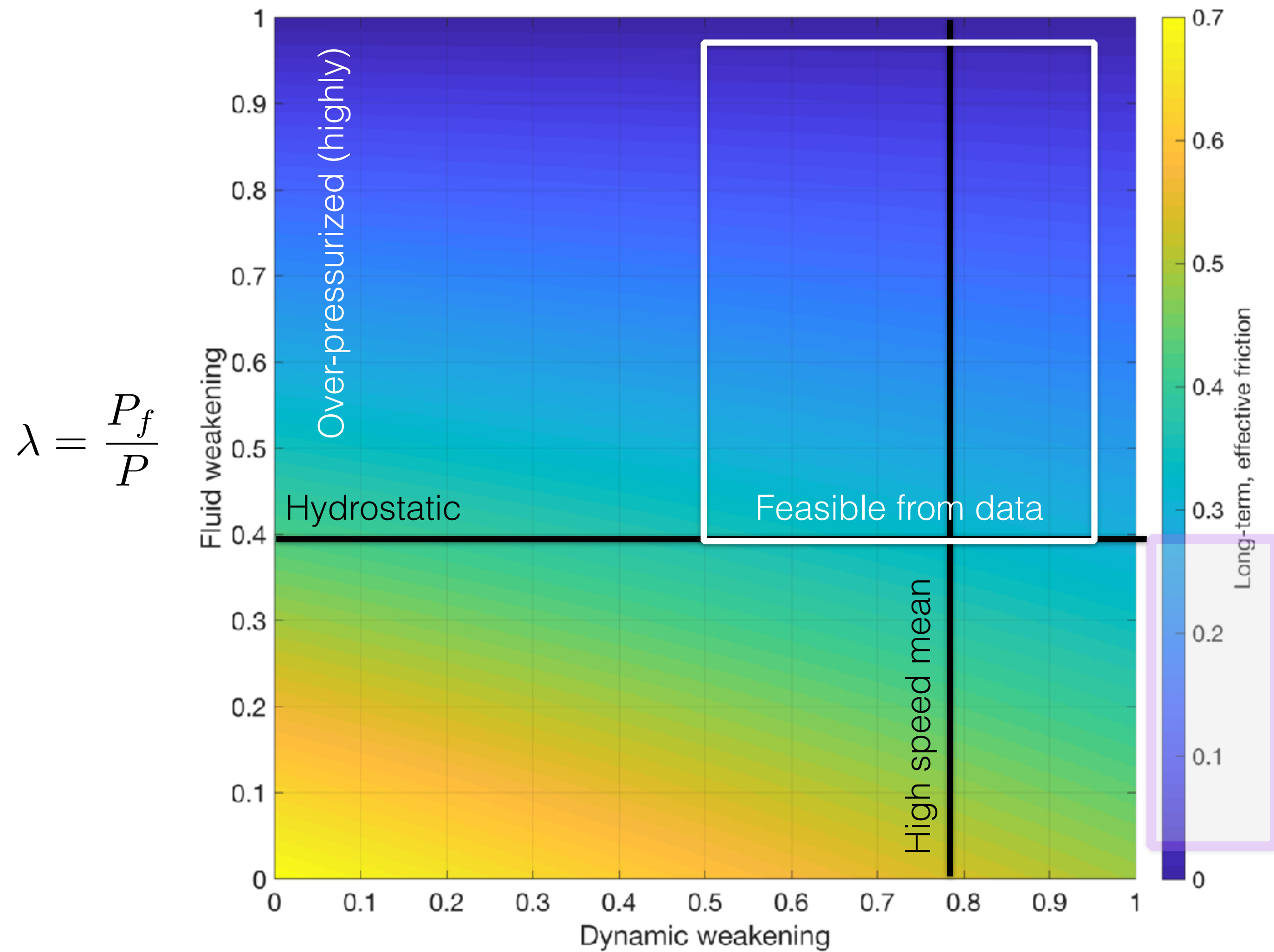
- With stress limited by strength (parameters) and

$$\boxed{\text{seismic coupling}} \quad \chi = \frac{M_0^\Sigma}{M_{0e}} \quad \boxed{\text{pore fluid pressure ratio}} \quad \lambda = \frac{P_f}{P} \quad \boxed{\text{dynamic weakening}} \quad \gamma = 1 - \frac{\mu_d}{\mu_s}$$

- Long-term average, effective friction is strain-averaged as

$$\mu_{eff(c)} = \chi(1 - \lambda)(1 - \gamma) \boxed{\mu_{(s)}} + (1 - \chi)(1 - \lambda) \mu_{(s)}$$

>> Derive constraints from observations and laboratory experiments



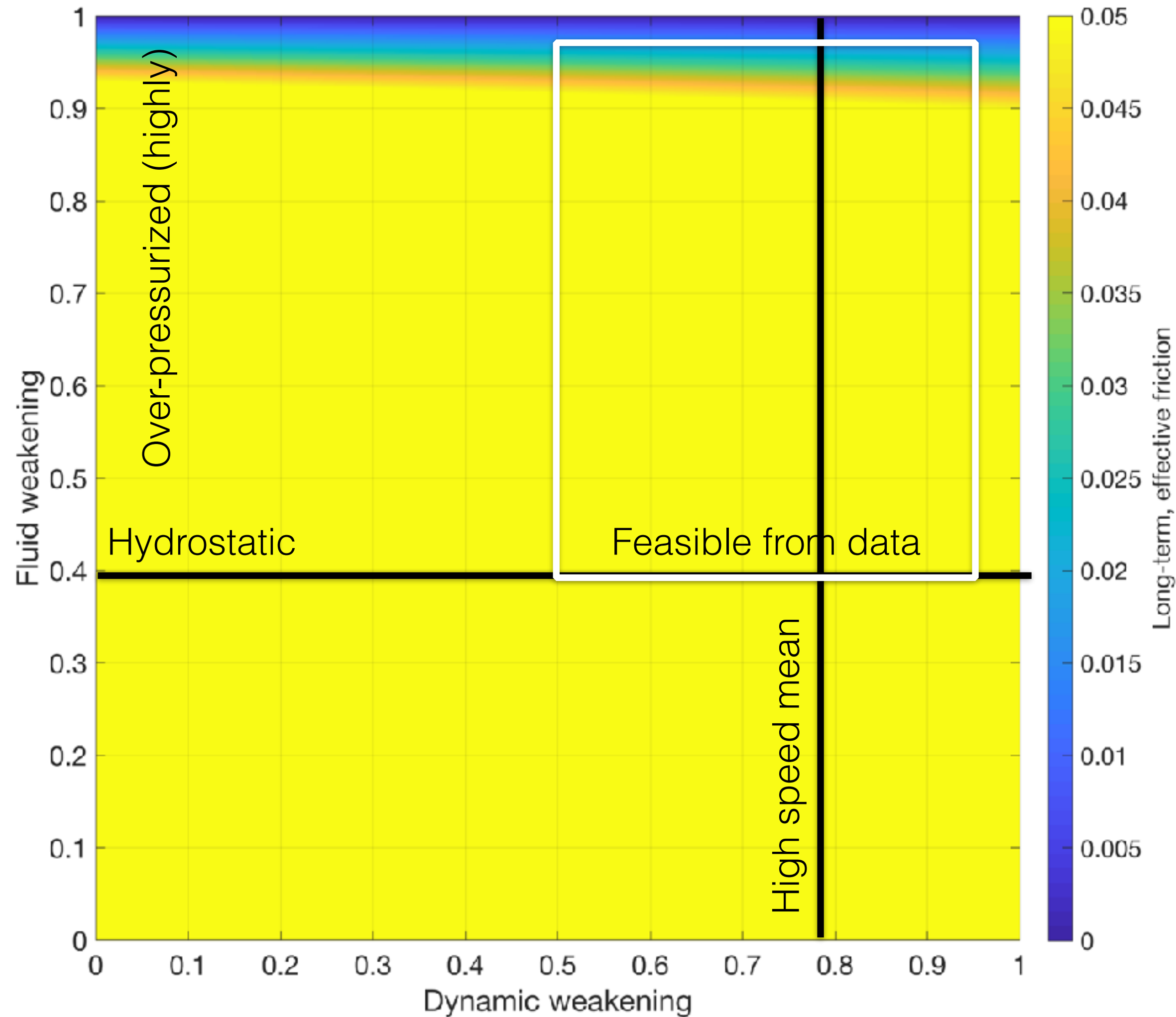
- Best guess:
- $\mu_s = 0.7$  [e.g., DiToro et al., Nature, 2011]
- $\chi = 0.3$  [e.g, McCaffrey, BSSA, 1997]

$$\gamma = 1 - \frac{\mu_d}{\mu_s}$$



## What do we need for long-term weak faults ( $\mu_{\text{eff},c} < 0.05$ )?

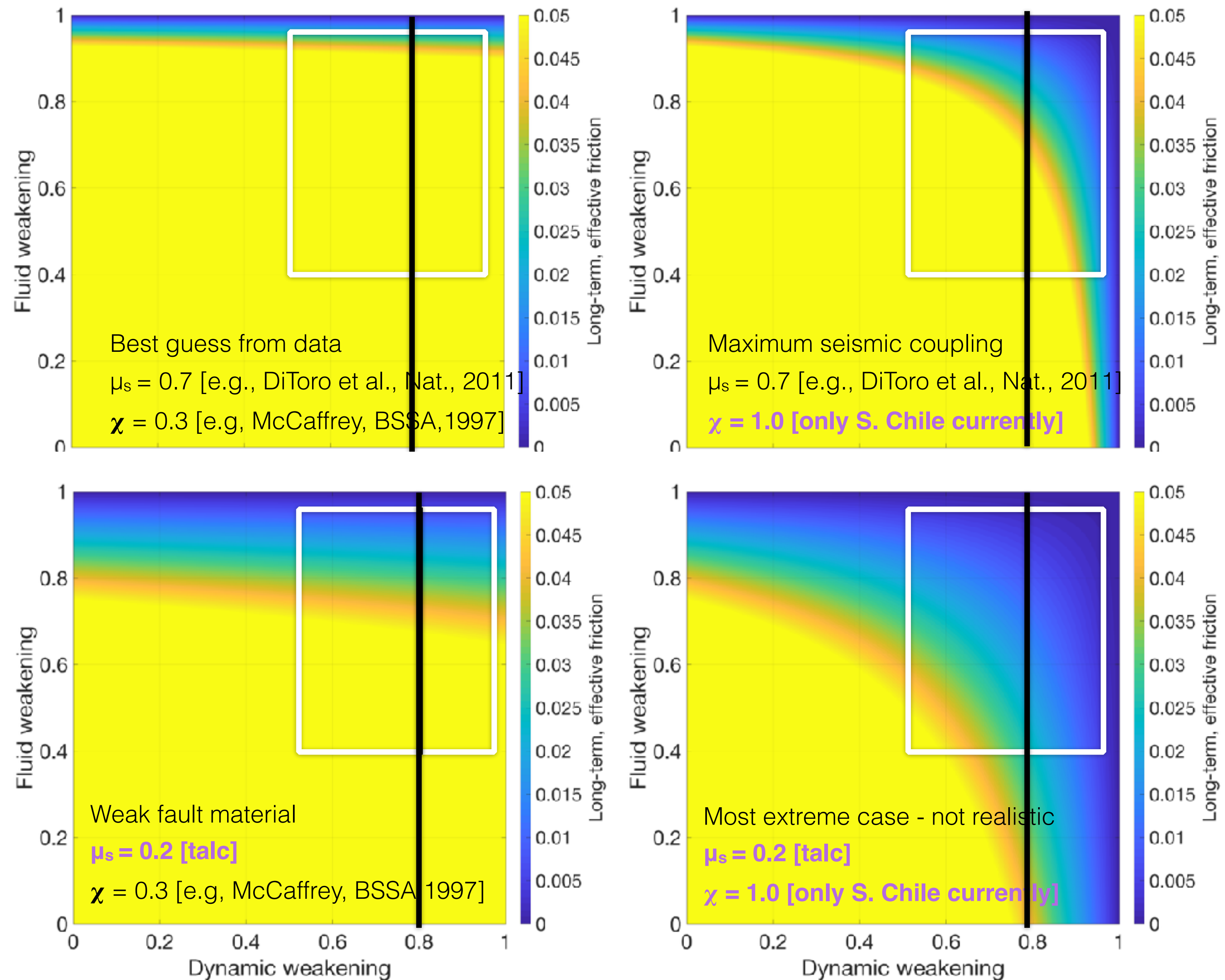
- What is needed for subduction to occur in geodynamic models? (i.e.,  $\mu_{\text{eff},c} < 0.05$ ; e.g., Zhong et al., 1998; Buiter et al., 2001; Sobolev & Babeyko, 2005; Duarte et al., 2015)
  - » Dynamic weakening can bring pore fluid pressures in more acceptable range, but still **requires largely over-pressurized megathrust**



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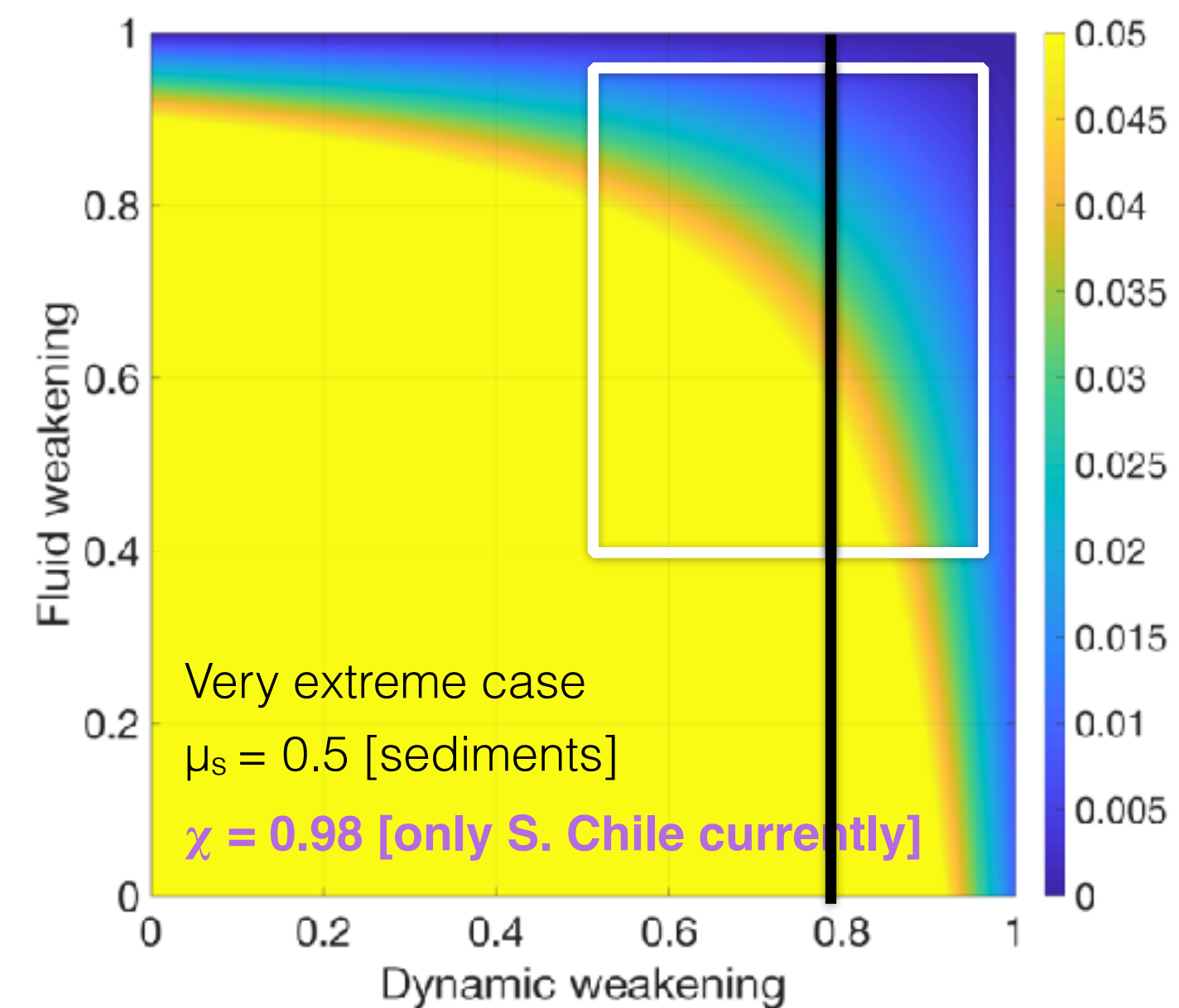
» Dynamic weakening can bring pore fluid pressures in more acceptable range, but still **requires largely over-pressurized megathrust**





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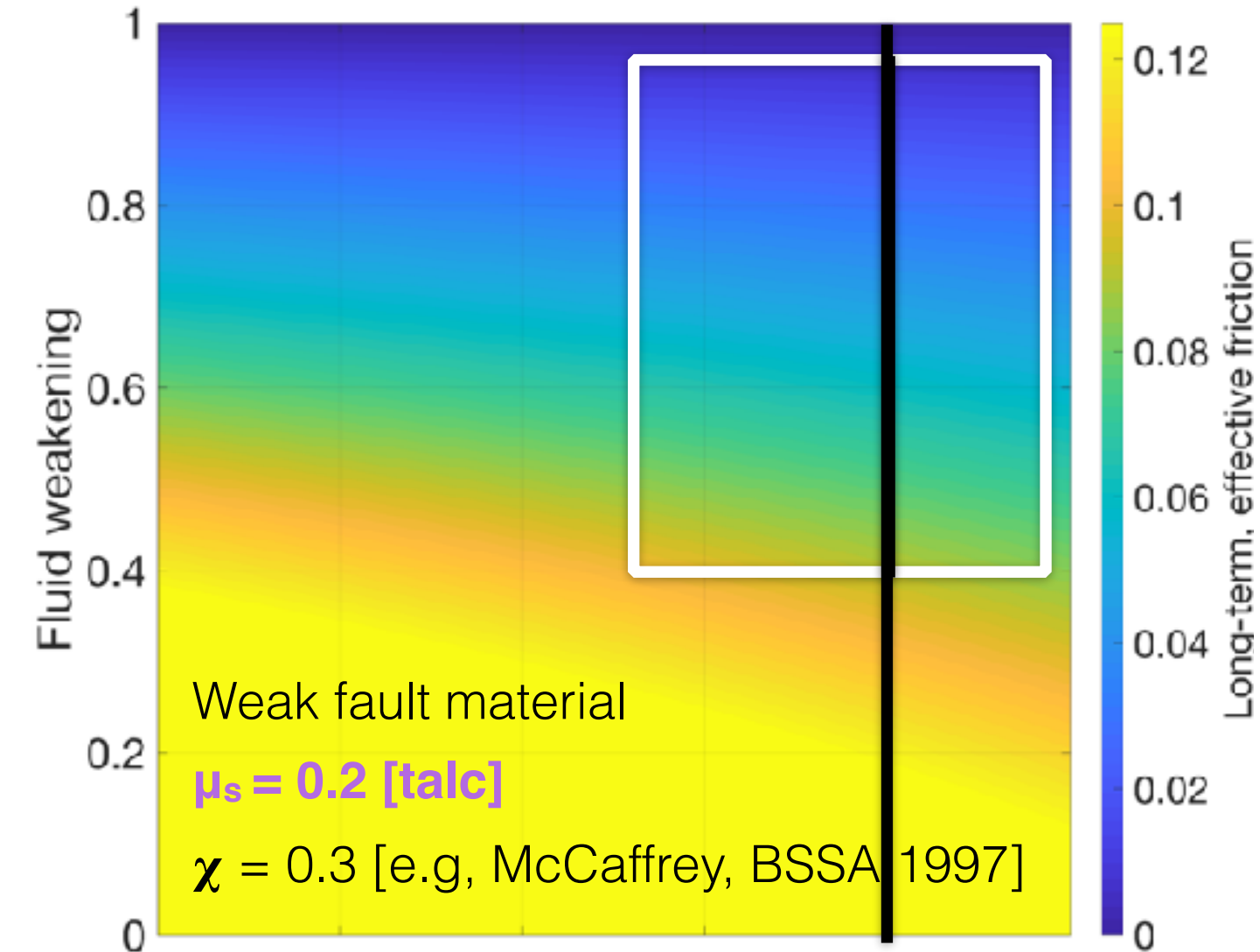


**highly over-pressurized faults**  
~~unless full seismic coupling~~

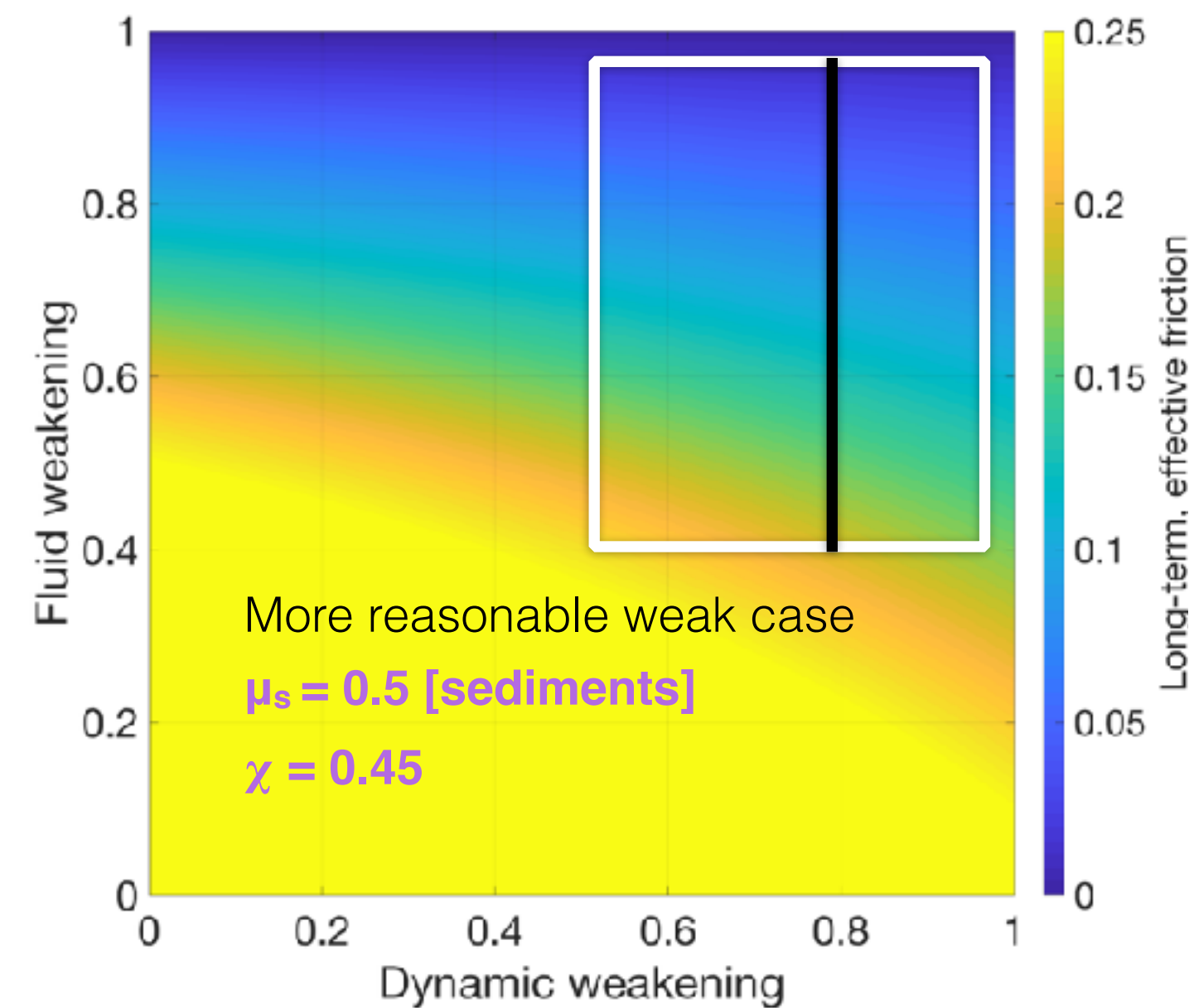
( or a different weakening  
mechanism is missing )

( or long-term models incorrect )

» IF subduction with realistic characteristics can occur in long-term geodynamic models for



$\mu_{\text{eff}, c} \sim 0.1$  for statically very weak megathrust (too weak)



$\mu_{\text{eff}, c} \sim 0.2-0.3$  for weak, but potentially reasonable megathrust

» I have not seen this

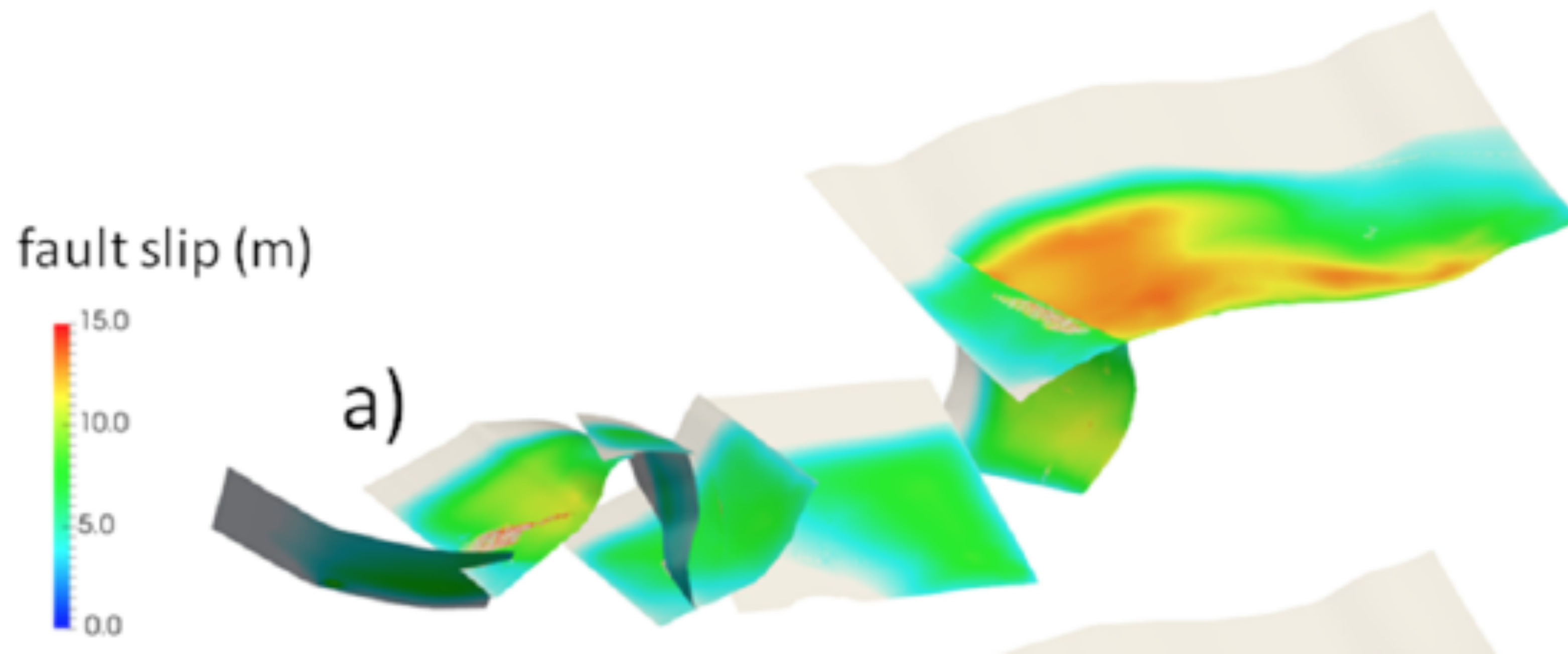


» Most effective way to remove highly over-pressurized faults remains reducing static friction (not earthquake slip)

Double	Reduces $\mu_{\text{eff (char)}}$ at reference values by	Reduces $\mu_{\text{eff (char)}}$ at full seismic coupling by
1. pore fluid pressure	67%	
2. static friction	50%	
3. seismic coupling	47%	
4. friction drop	20%	50%

## Apparently weak faults also work better for dynamic earthquake ruptures (DR)

- Lab-observed large strength drops allowed in slip/rate-weakening DR models through distinctly increased pore fluid pressures
- 2016 M7.8 KAIKOURA earthquake only jumps for large fluid pressures ( $\lambda \sim 0.66$ )



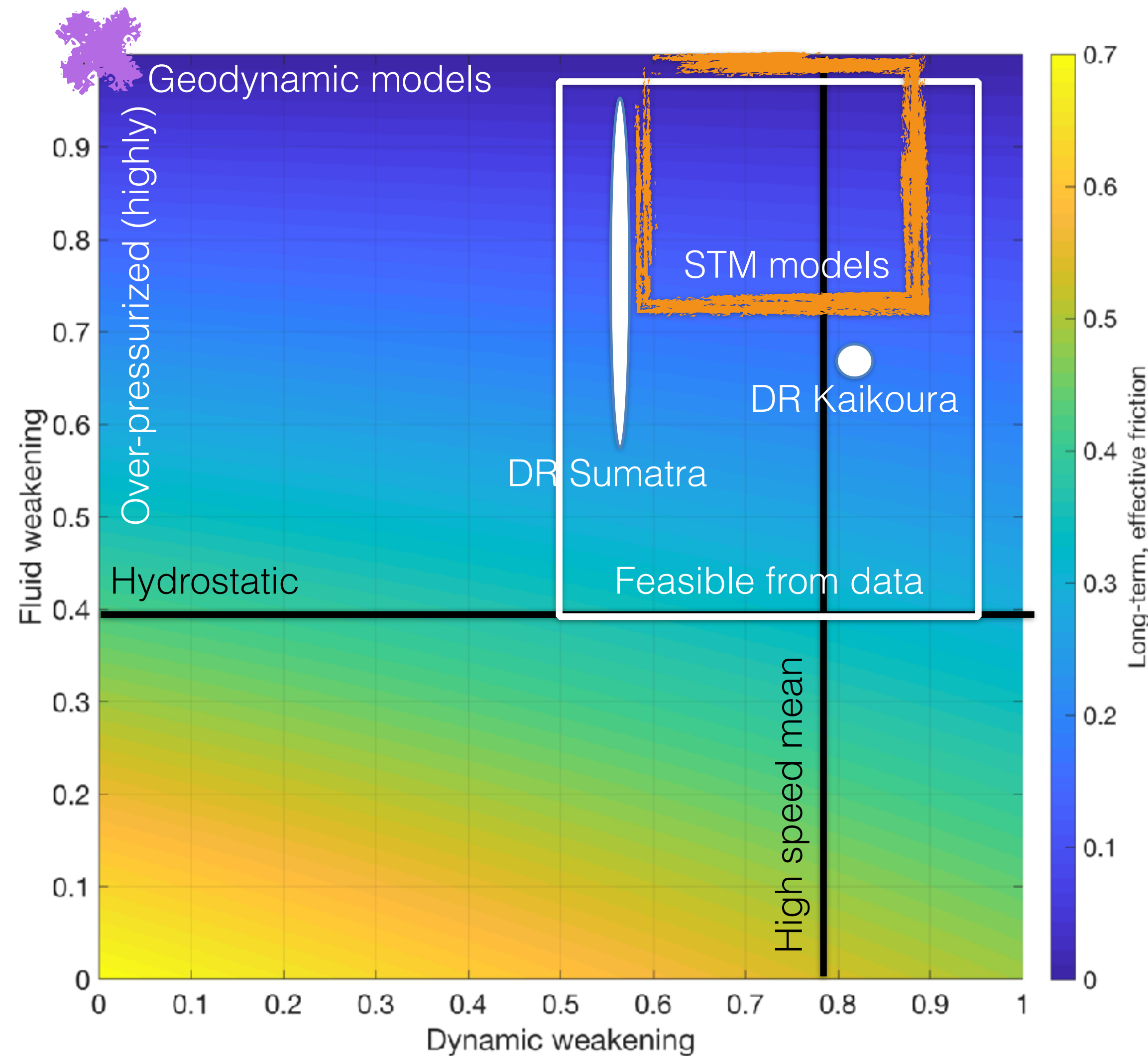
Ulrich et al., Nat. Comm., 2019  
Strongly rate-dep. friction,  $\gamma \sim 0.8$

$$\Delta\tau \sim (\mu_s - \mu_d)(1 - \lambda)$$

» Strain occurs around  $\mu_{\text{eff}} \leq 0.1$

# Models across scales support weak(er) megathrusts

» Recent modeling results show that long- and short-term results are not so far apart as they seem



DR Sumatra: Madden et al., AGU, 2018

**Feasible long-term friction values from models:**  
 $\mu_{\text{eff,c}} \sim 0.02 - \sim 0.20$

- Best guess:
- $\mu_s = 0.7$  [e.g., DiToro et al., Nature, 2011]
- $\chi = 0.3$  [e.g, McCaffrey, BSSA, 1997]



- Models at, and across, all time scales support (somewhat) weak megathrusts
  - »  $\mu_{\text{eff,c}} \sim \mathbf{0.02 \text{ to } 0.2}$
- Long-term strength is a strain-average quantity
  - Described by pore fluid pressure ratio, static friction, seismic coupling, and dynamic friction
- Analytical considerations constrained by data and laboratory experiments support (somewhat) weak megathrusts
  - »  $\mu_{\text{eff,c}} \sim \mathbf{0.02 \text{ to } 0.3}$
- Megathrusts are mainly weak due to distinctly to highly over-pressurized pore fluids
  - » Geodynamic models not resolving earthquake dynamics are within their right within **bold** range (and can justify choice)