

# When 1D Response Analysis Fails: Application of Earthquake HVSR in Site-Specific Amplification Estimation

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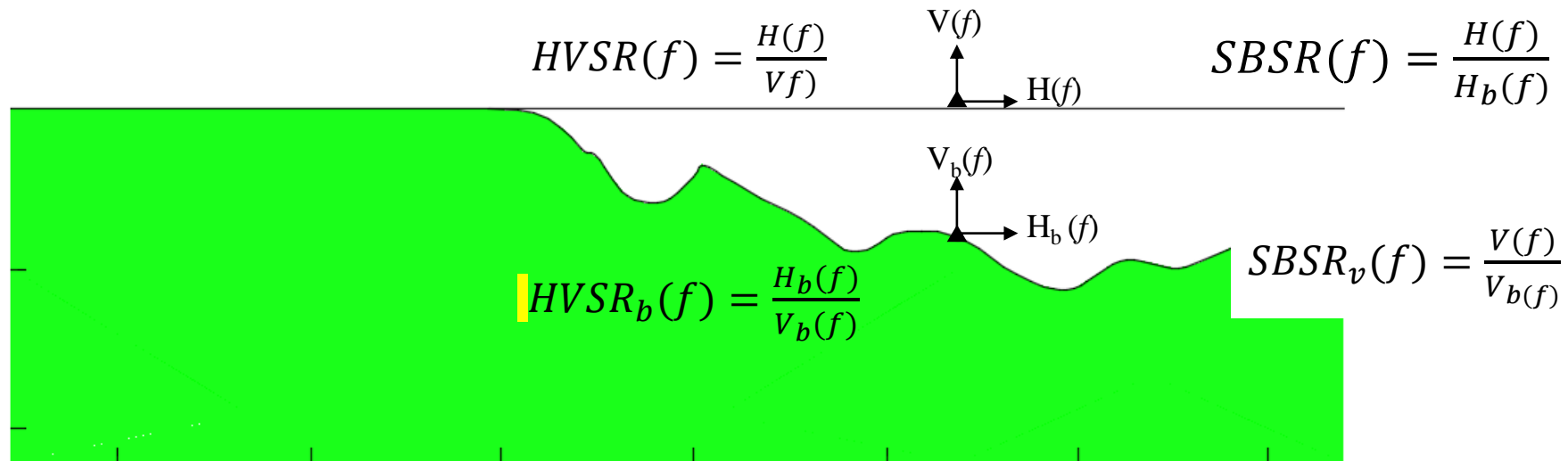
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# Empirical Correction to HVSR



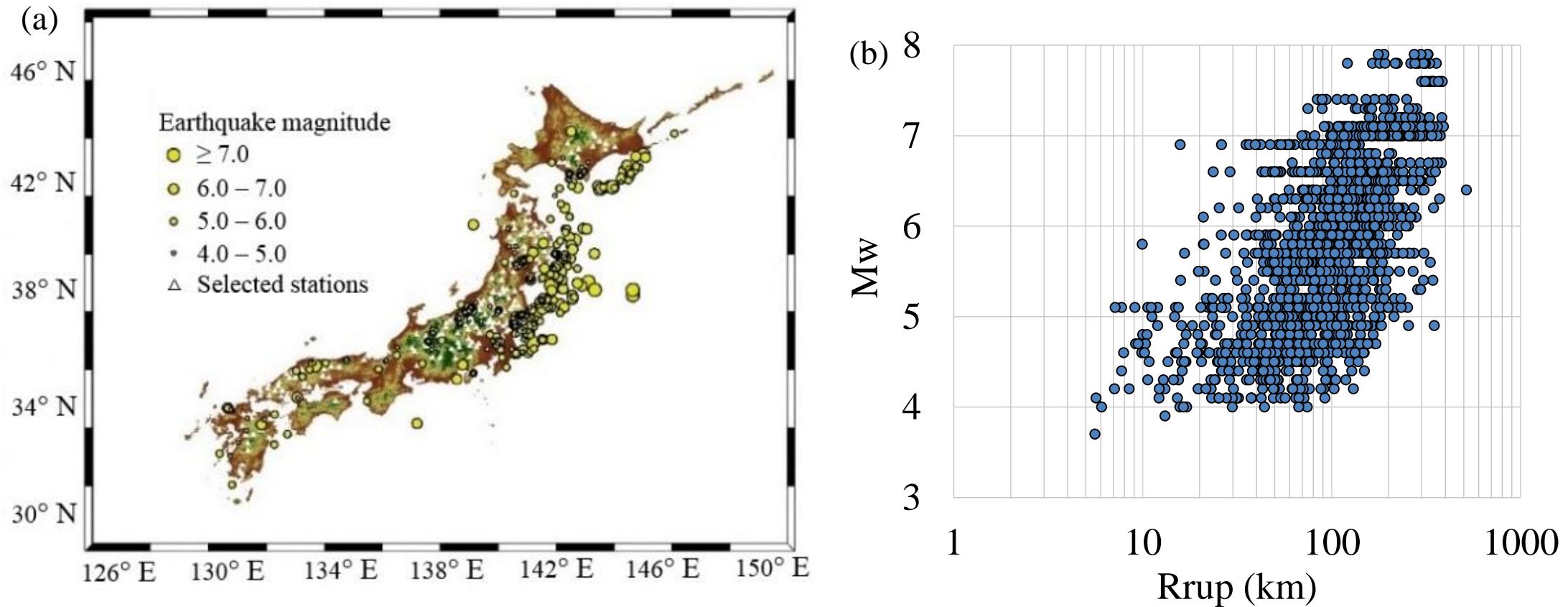
$$HVSR(f) = \frac{H(f)}{H_b(f)} \cdot \frac{H_b(f)}{V_b(f)} \cdot \frac{V_b(f)}{V(f)} = \frac{HVSR_b(f)}{SBSR_v(f)} \cdot SBSR(f)$$

$$H_b(f) = V_b(f) \text{ or } HVSR_b = 1.0$$

$$SBSR(f) = HVSR(f) \cdot SBSR_v(f)$$

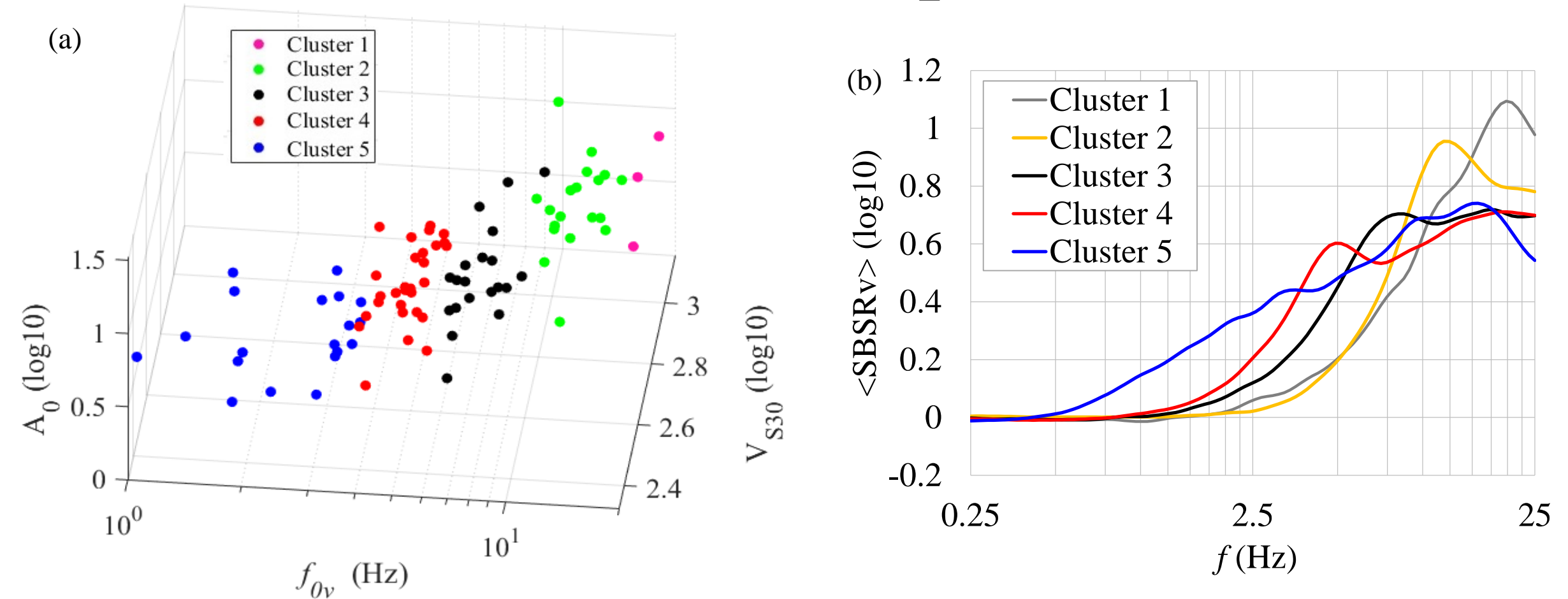
$$pSBSR(f) = HVSR(f) \cdot \langle SBSR_v(f) \rangle$$

# Data Selection



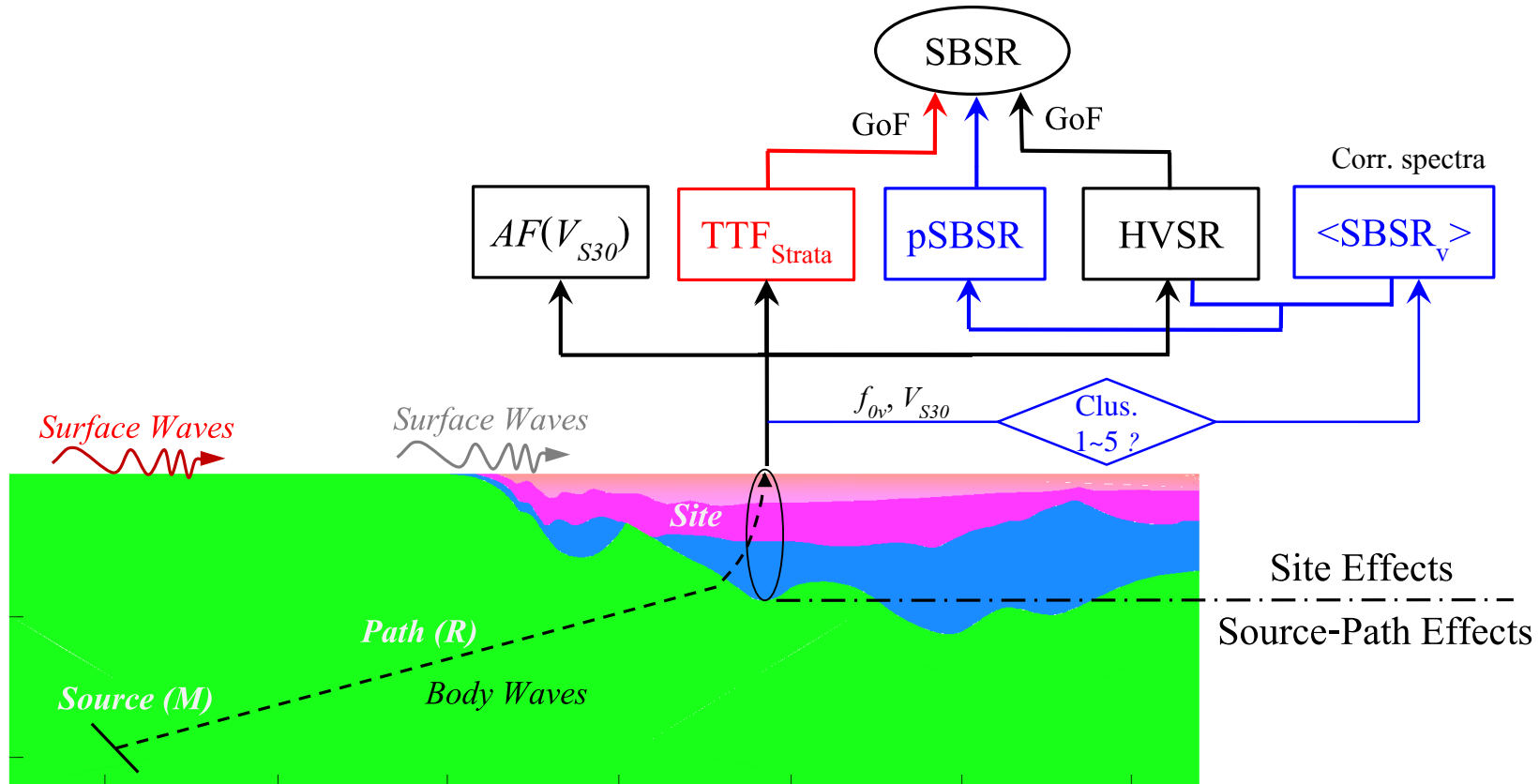
**Fig.** (a) Spatial distribution of earthquakes and 207 KiK-net stations used in this study, and (b)  $M_w$ -Rrup distribution of the 1840 selected earthquake recordings.

# Correction Spectra



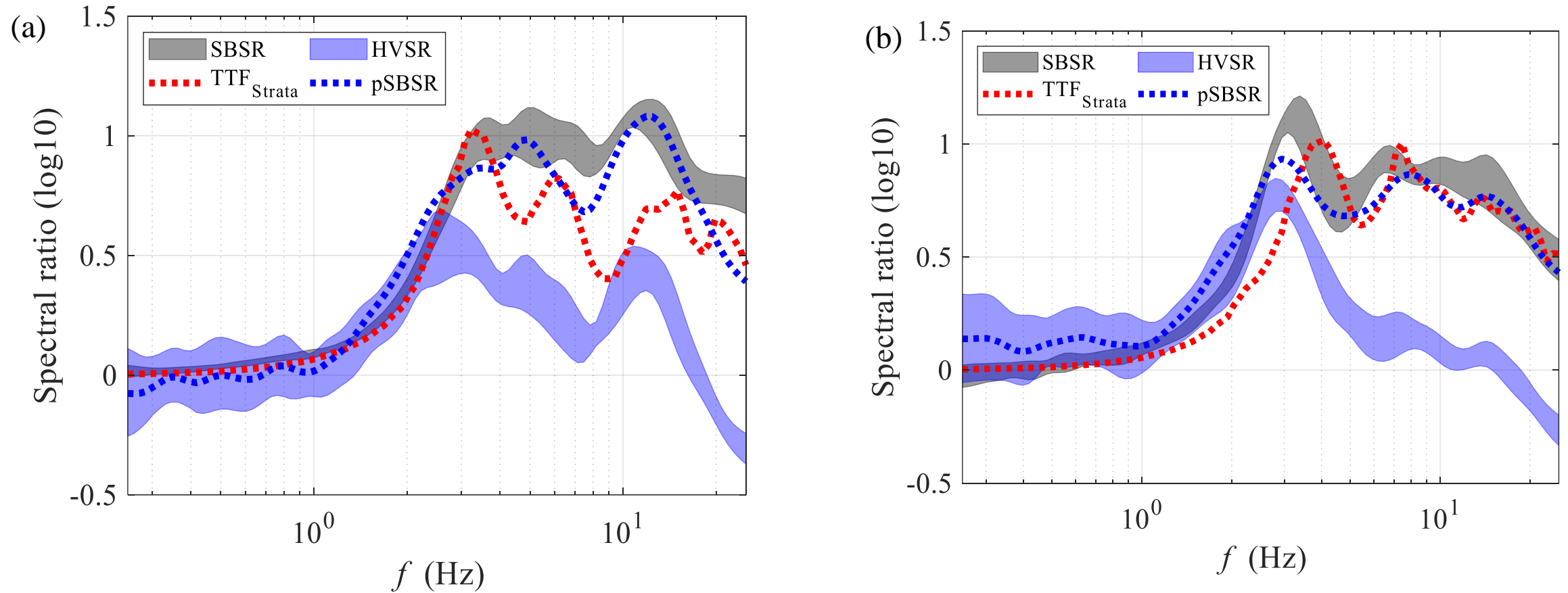
**Fig.** (a) k-means clustering of the 90 KiK-net sites, and (b) average SBSRv for each cluster, i.e.,  $\langle \text{SBSR}_v \rangle$ .

# Correction Spectra



**Fig.** Evaluation of techniques used in site effects quantification.

# pSBSR vs. TTF

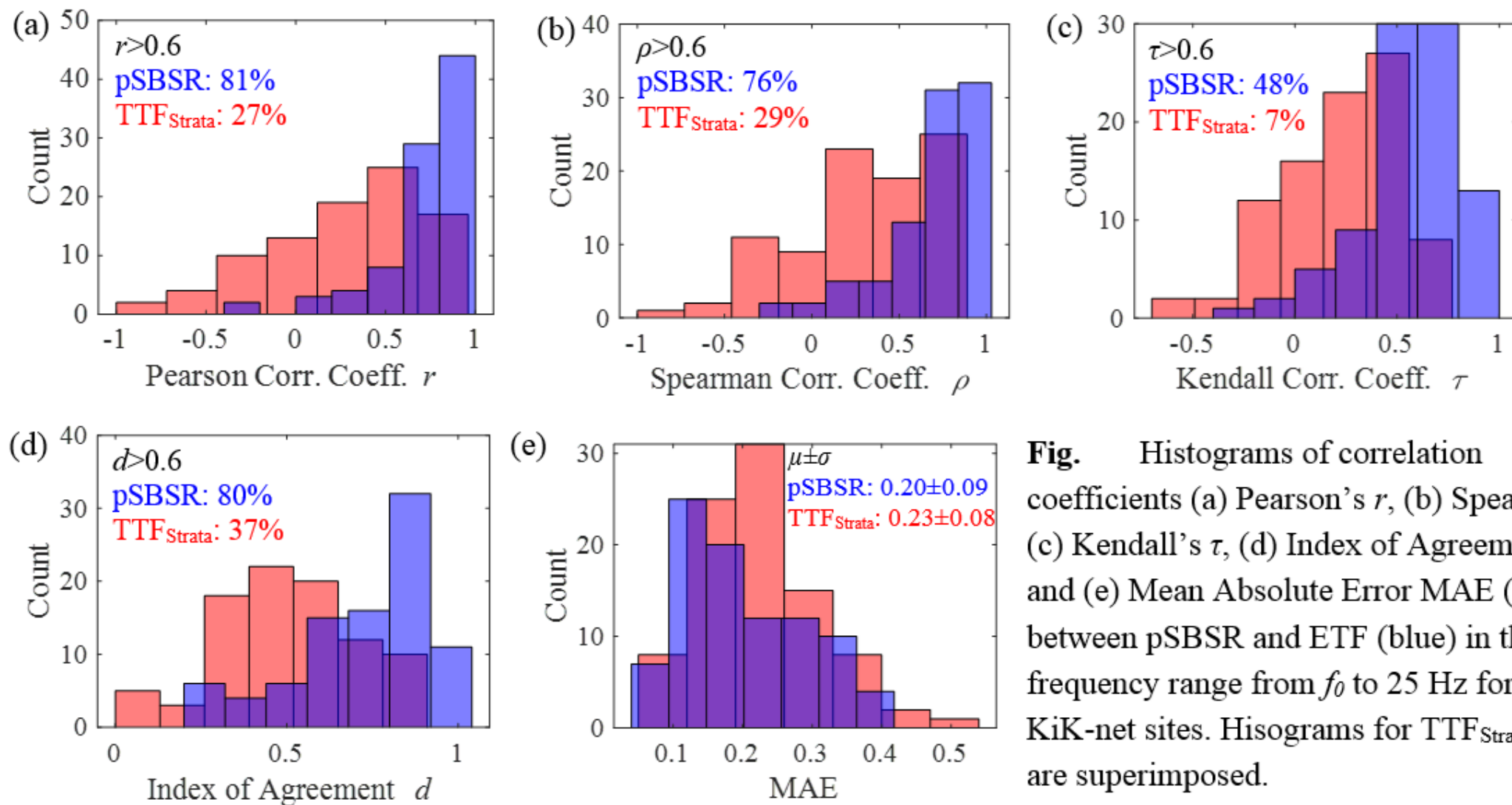


**Fig.** HVSR, TTF<sub>Strata</sub> and pSBSR at sites (a) TCGH07 and (b) IWTH04.

# Goodness-of-fit (GoF) metrics

Goodness-of-fit metric	Expression	Range	Measure	Interpretation
Pearson's r	$\frac{\sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})}{\sqrt{\sum_{i=1}^n (x_i - \bar{x})^2} \sqrt{\sum_{i=1}^n (y_i - \bar{y})^2}}$	[-1, 1]	Linear relationship	Measure the closeness in shape (alignment of peaks and troughs)
Spearman's $\rho$	$\frac{cov(r g_x, r g_y)}{\sigma_{r g_x} \sigma_{r g_y}}$	[-1, 1]	Ordinal relationship	
Kendall's $\tau$	$\frac{2[\sum_{i < j} sgn(x_i - x_j) sgn(y_i - y_j)]}{n(n - 1)}$	[-1, 1]	Ordinal relationship	
Index of Agreement d	$1 - \frac{\sum_{i=1}^n (x_i - y_i)^2}{\sum_{i=1}^n ( y_i - \bar{x}  +  x_i - \bar{x} )^2}$	[0, 1]	Degree of difference (relative)	Measure the difference in amplitude
Mean Absolute Error MAE	$\frac{\sum_{i=1}^n  y_i - x_i }{n}$	-	Degree of difference (absolute)	

# pSBSR vs. TTF



**Fig.** Histograms of correlation coefficients (a) Pearson's  $r$ , (b) Spearman's  $\rho$ , (c) Kendall's  $\tau$ , (d) Index of Agreement  $d$ , and (e) Mean Absolute Error MAE (log10) between pSBSR and ETF (blue) in the frequency range from  $f_0$  to 25 Hz for the 90 KiK-net sites. Histograms for TTF<sub>Strata</sub> (red) are superimposed.



# pSBSR vs. TTF

**Table.** Success rates of TTFStrata and pSBSR in reproducing SBSR under different definitions of “good match”

Estimation	$r>0.60$	$r>0.60$ $d>0.60$	$r>0.65$ $d>0.65$	$r>0.60$ MAE<0.25	$r>0.65$ MAE<0.20
TTF	27%	27%	18%	22%	14%
pSBSR	81%	76%	68%	62%	50%

# Summary

The empirical correction to HVSR is highly effective and achieves a “good match” in both spectral shape and amplitude at the majority of the 90 KiK-net sites, as opposed to less than one-third for the 1DSH modelling. In addition, the empirical correction does not require a ground model as GRA and thus has great potentials in seismic hazard assessments.

**Thank you very  
much!**