

PCA study of the interannual variability of GPS heights and environmental parameters

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Objective

- To identify and analyze principal modes of variability of
 - GPS heights
 - Environmental parameters

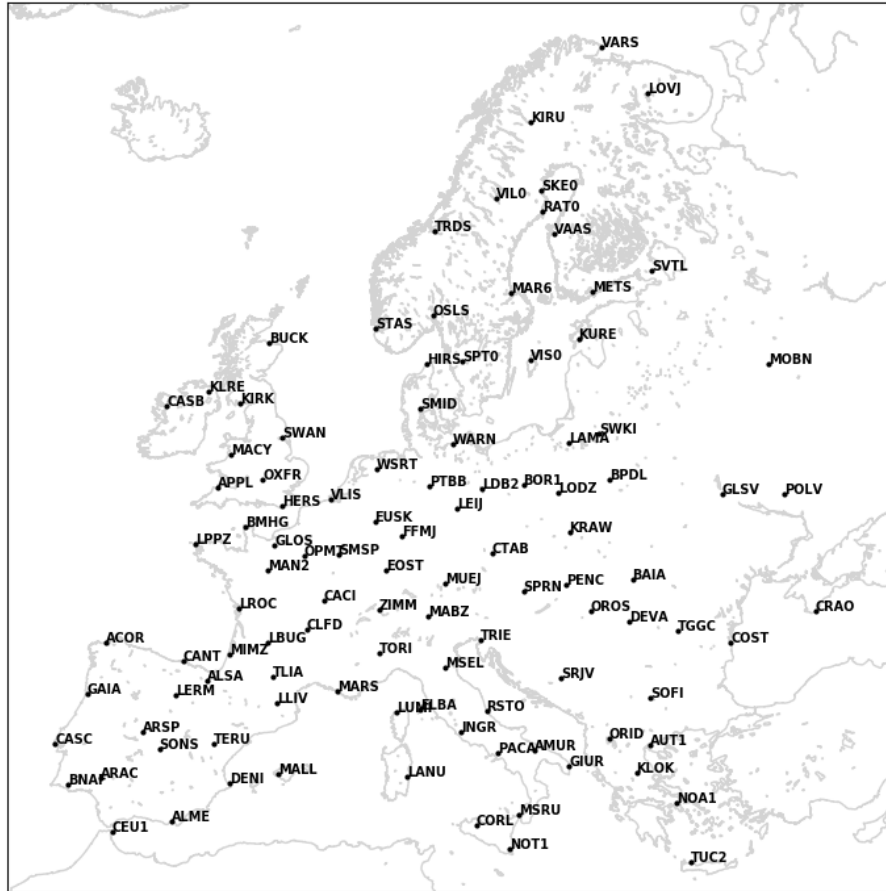
and

- To study the coupled variability of these parameters

Parameters

- GPS heights
- Surface atmospheric pressure (AP)
- Terrestrial water storage (TWS)
- Climate indices (NAO, EA, SCAND, AO, TNA, MEI)

Study area and GPS stations



107 GPS stations selected according to

- Length of the time series of the daily coordinates
- Completeness of the time series
- Spatially uniform coverage

Datasets

Daily time series covering the period

June 9, 2010 – September 5, 2018

- **GPS** heights (Nevada Geodetic Laboratory, <http://geodesy.unr.edu/>)
- **AP** (National Center for Environmental Prediction, <https://www.esrl.noaa.gov/psd/data/gridded/data.ncep.html>)
- **TWS** (NASA Data and Information Services Center, <https://disc.gsfc.nasa.gov/>)

Data pre-processing

- Detrending
- Deseasoning
- Estimate of weekly mean values
- Standardization
- Spatial interpolation in the case of AP and TWS

Principal Component Analysis (PCA)

To identify principal modes of variability of a dataset



Principal Component Analysis (PCA):

modes of variability



spatial patterns



time components

PCA theory

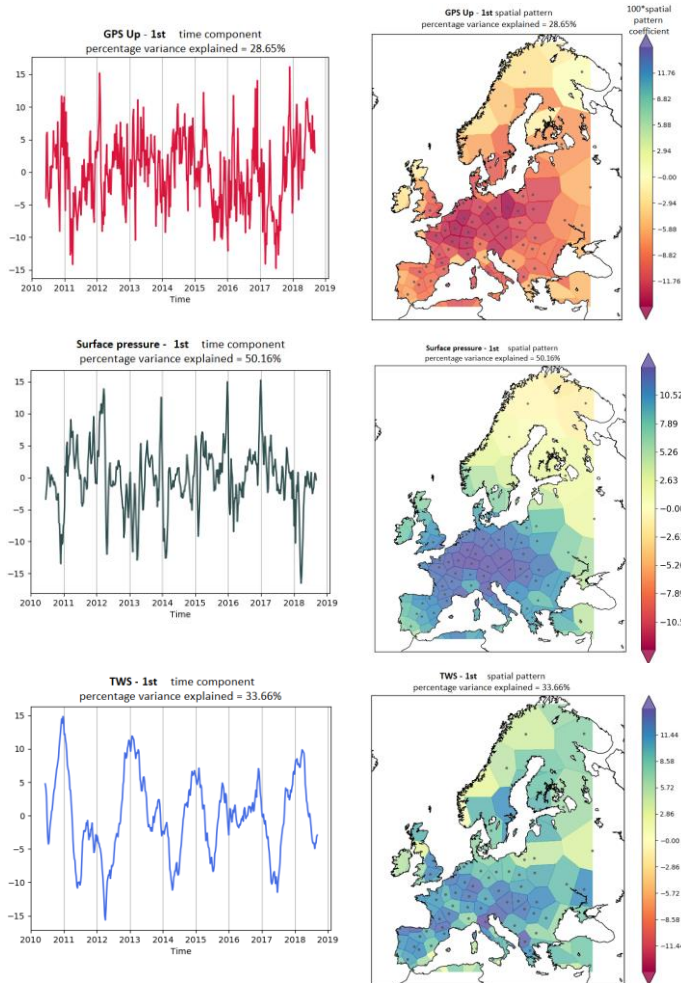
$$F_{ij} = \begin{bmatrix} f(t_1, x_1) & \cdots & f(t_1, x_p) \\ \vdots & \ddots & \vdots \\ f(t_n, x_1) & \cdots & f(t_n, x_p) \end{bmatrix} \rightarrow R = \frac{F^T F}{n-1}$$

- eigenvector c_i of $R \rightarrow$ spatial pattern of the i -th mode
- vector $a_i = Fc_i \rightarrow$ time component of the i -th mode
- eigenvalue l_i of $R \rightarrow$ variance explained by the i -th mode

Each mode explains part of the total variability of the dataset

Percentage of variance explained			
Mode	GPS Height (%)	AP (%)	TWS (%)
1	28.65	50.16	33.66
2	11.60	21.86	12.91
3	9.07	10.80	11.04
4	4.17	4.67	7.19
Total	~ 50	~ 90	~ 65

Example: 1st mode of variability



- Change of slope between the end of 2010 and the beginning of 2011
 - Change of slope at the beginning of 2018
- ↕
- Heavy rainfalls characterized the second half of 2010 over Europe
 - A drought period started in spring of 2011
 - Anomalous cold and low pressure characterized the beginning of 2018

All 3 parameters are spatially coherent

Singular Value Decomposition (SVD)

To identify common modes of variability between pairs of variables



Singular Value Decomposition (SVD)
common modes of variability



2 spatial patterns



2 time components

Pair of variables studied:

- GPS height-AP → first 3 modes = 70% of total covariance
- GPS height-TWS → first 3 modes = 50% of total covariance

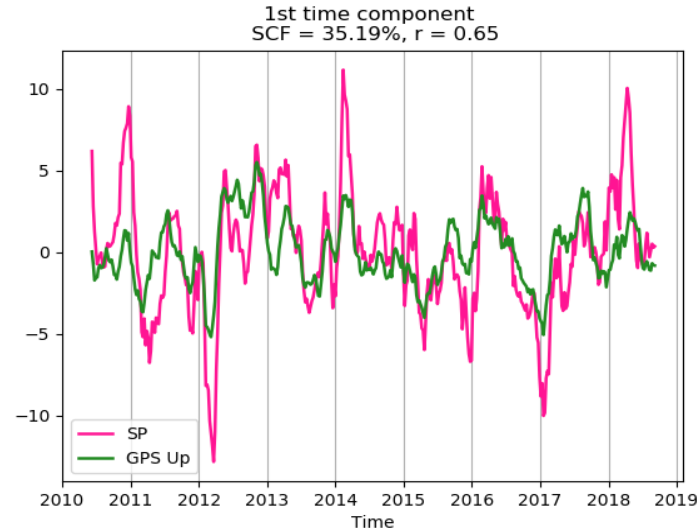
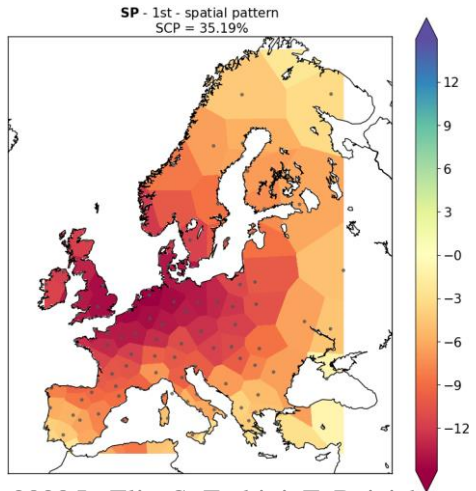
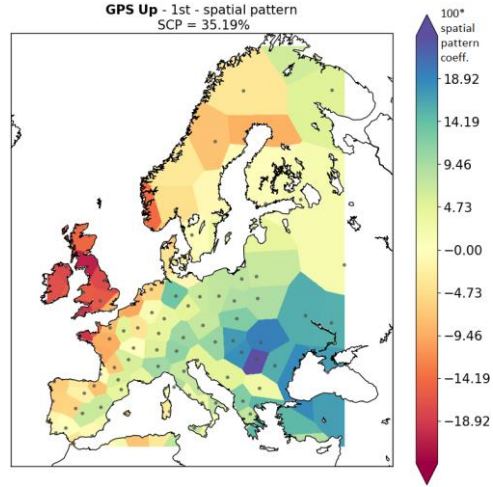
SVD theory

F_1 and F_2 : matrices of the two variables

$$R_{cross} = F_1^T F_2 = ULV^T$$

- Columns u_i of U and v_i of $V \rightarrow$ spatial pattern of the i -th mode of covariability of F_1 and F_2
- vectors $a_i = F_1 u_i$ and $b_i = F_2 v_i \rightarrow$ time component of the i -th mode of covariability of F_1 and F_2
- Values l_i of $L \rightarrow$ covariance explained by the i -th mode

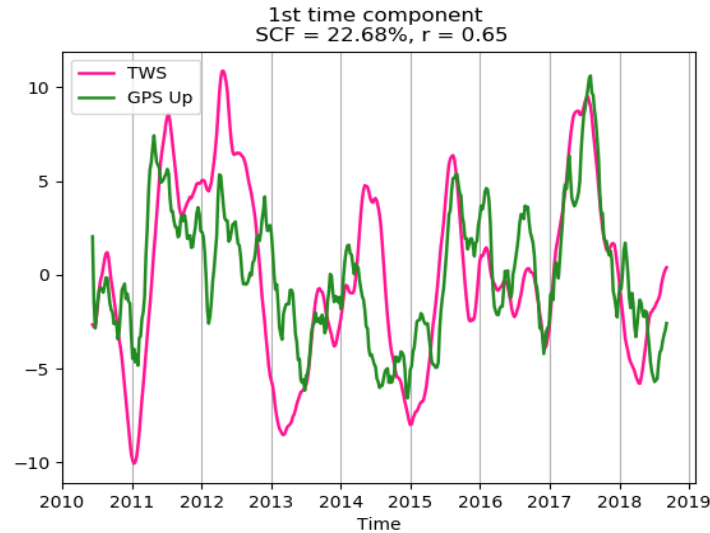
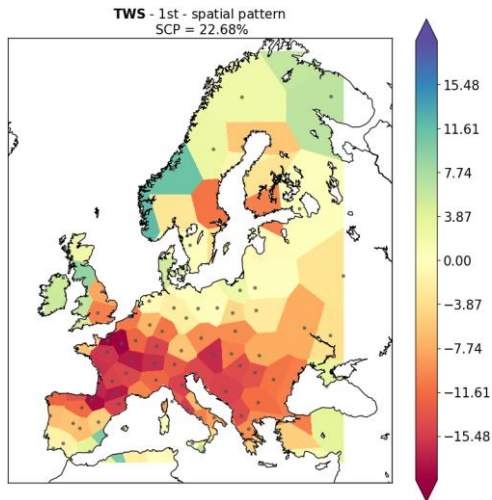
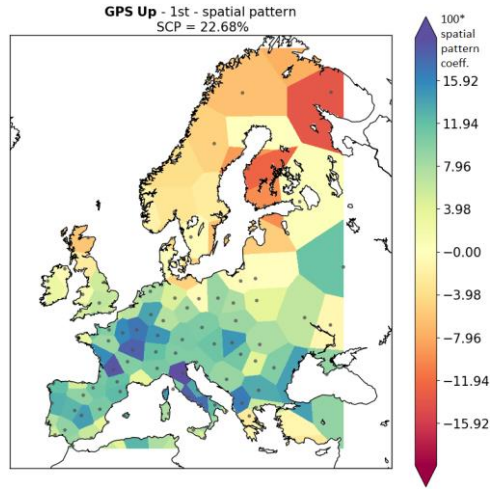
SVD GPS height-AP



First mode of covariability:

- ~ 35% covariance
- AP: spatial pattern coherent over Europe and the Mediterranean area
- GPS height: spatial pattern coherent, except for the British Isles
- General anticorrelation of the spatial patterns → **loading mechanism**

SVD GPS height-TWS



First mode of covariability:

- ~ 23% covariance
- General anticorrelation of the spatial patterns of GPS height and TWS → **loading mechanism**

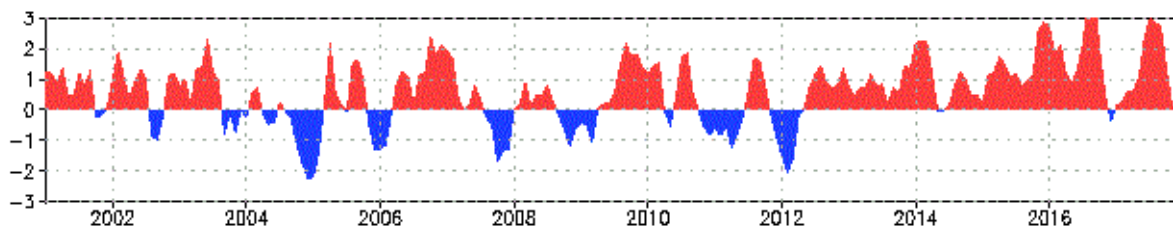
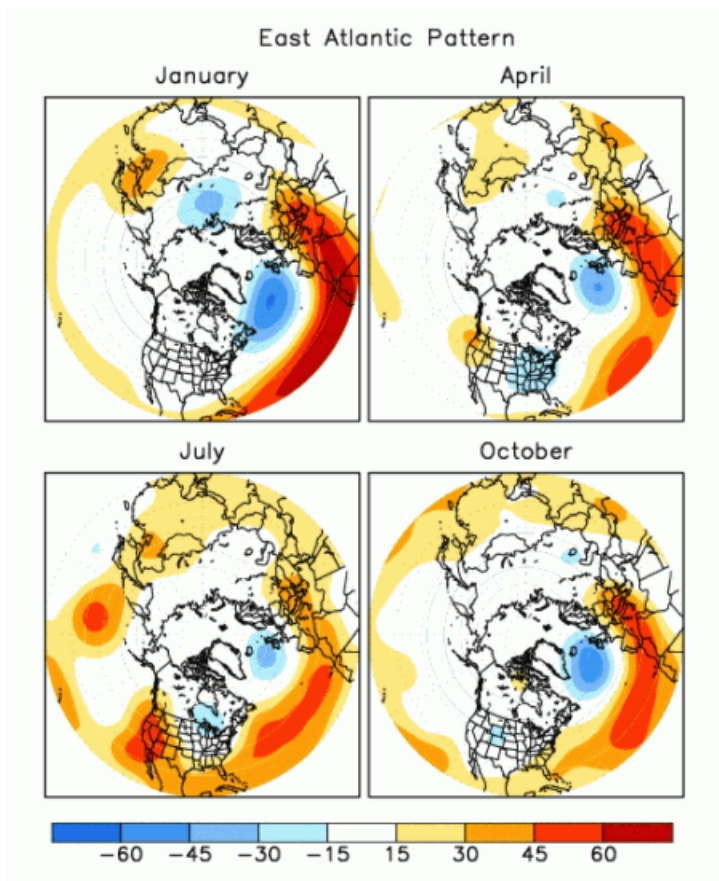
Climate indices

Climate indices NAO, EA, SCAND, AO, TNA, MEI
compared to



- Monthly means of the first four time components of the GPS height
- Monthly means of the “*dimensionality reduced*” time series of the GPS height

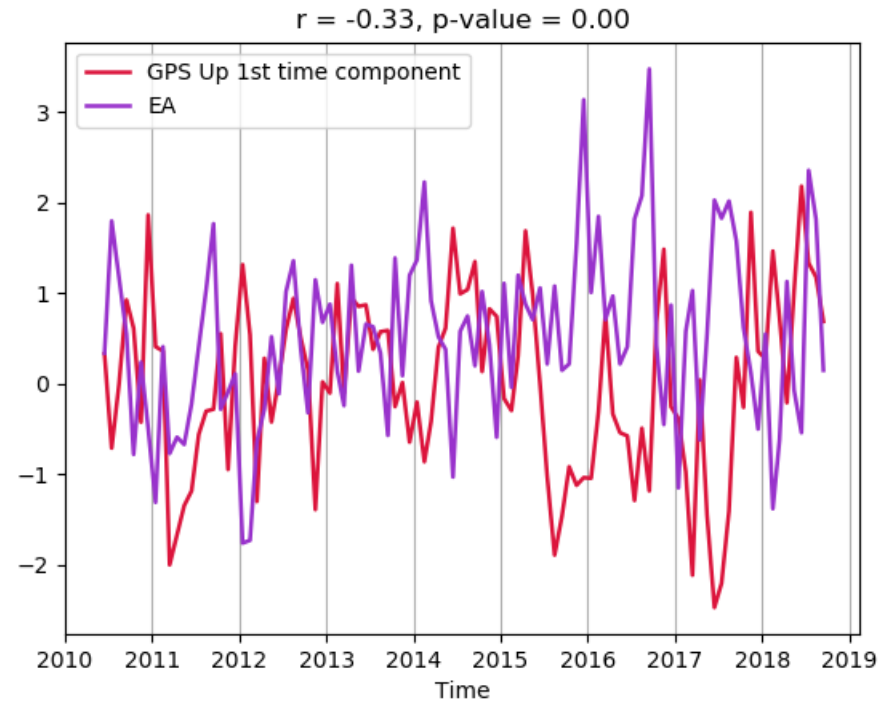
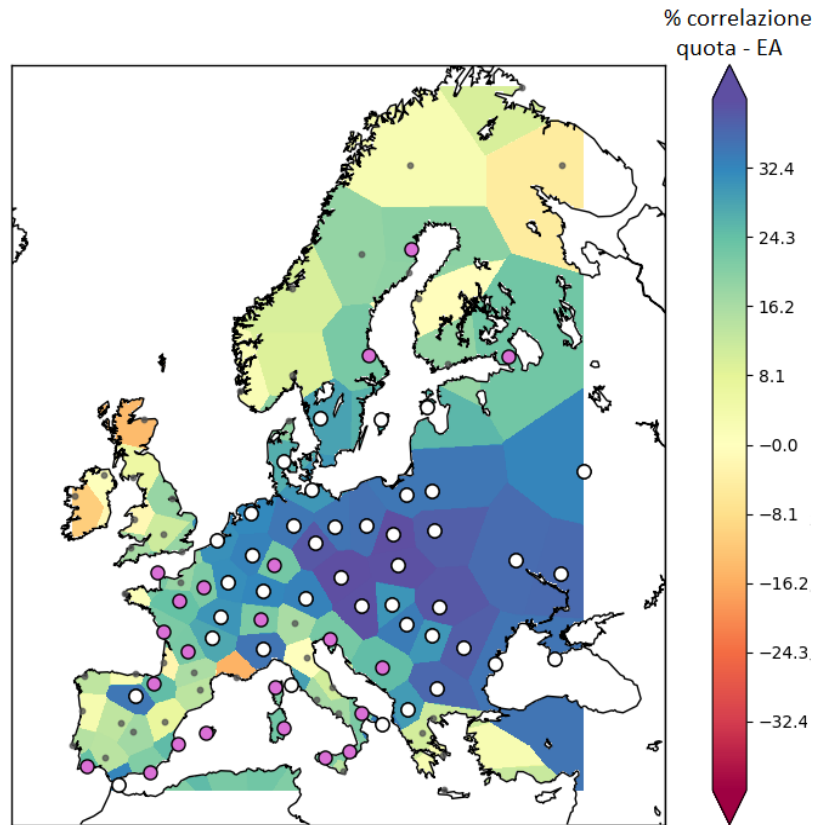
East Atlantic (EA)



Features of the positive phase

- Above-average precipitations in Northern Europe and Scandinavia
- Below-average precipitations in Southern Europe

Correlation map EA-GPS height



Variance explained by the 1st mode 28.65%

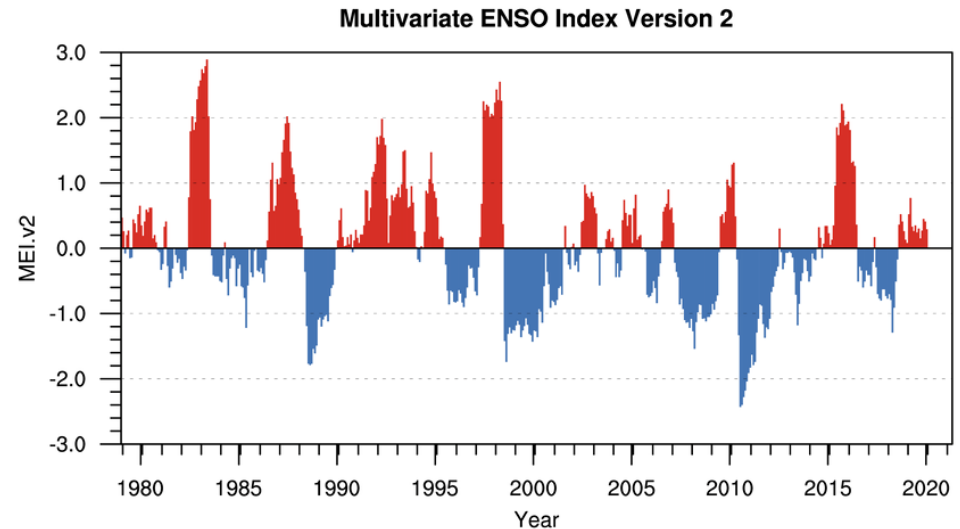
Lilac points: GPS site showing correlation with EA index larger than 10% and significance level larger than 95%

White points: GPS sites showing correlation with EA index larger than 10% and significance level larger than 99%

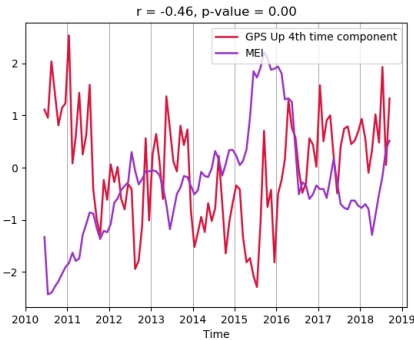
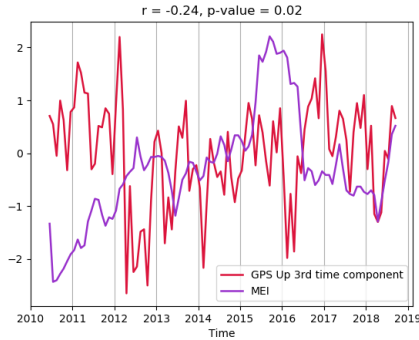
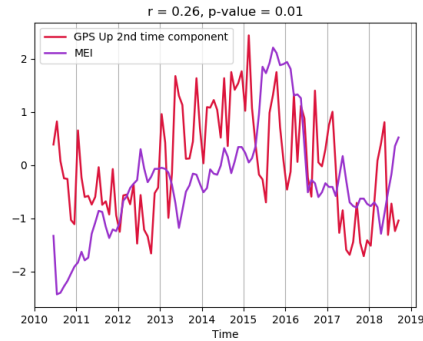
Multivariate ENSO Index

MEI provides an assessment of the **El Niño Southern Oscillation** and is based on 5 main variables related to the Equatorial Pacific:

- Sea level pressure
- Sea surface temperature
- Zonal and meridional components of the surface winds
- Outgoing longwave radiation



Correlation map MEI-GPS height

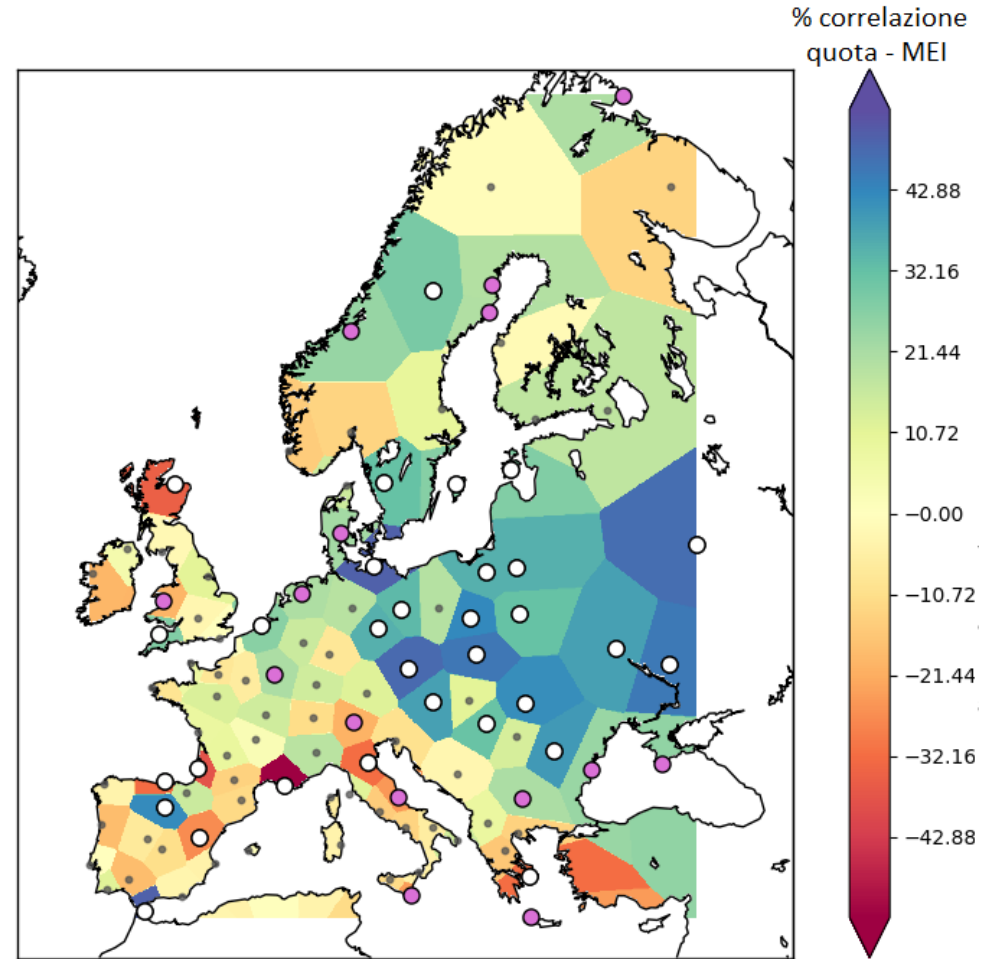


Variance explained by:

- 2nd mode 11.60 %
- 3rd mode 9.07 %
- 4th mode 4.17 %

Lilac points: GPS sites showing correlation with MEI index larger than 10% and significance level larger than 95%

White points: GPS sites showing correlation with MEI index larger than 10% and significance level larger than 99%



Conclusions

PCA analysis

- Principal modes of variability of GPS height, AP, TWS
- Relationship with climatic events

SVD analysis

- Common modes of variability between the pairs GPS height-AP and GPS height-TWS
- Loading mechanism at continental scale

Climate indices comparison

- Relationship between climate patterns and vertical deformation of the Earth crust at continental scale

Outlook

- Tracing fingerprints of climatic events
- Extension of the investigated time period