

# *On the Multi-Technique Combination with Atmospheric Ties*

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# Motivation

- ❑ Regardless of space geodetic observing system (GNSS, VLBI, SLR, and DORIS) estimates of
  - ❑ plate tectonics,
  - ❑ satellite orbits,
  - ❑ Earth's rotation, and
  - ❑ atmospheric state

should –in principle- differ only within measurement error bounds, e.g., Krügel et al. (2007), Thaller et al. (2007), Thaller (2008), Nilsson et al. (2015)

- ❑ Multi-technique combination facilitates distinction of ***genuine geophysical signals*** from ***technique-specific artefacts***, e.g., Rothacher (2002)
- ❑ Improvements in ground co-location (more sites with more systems)

## In this presentation

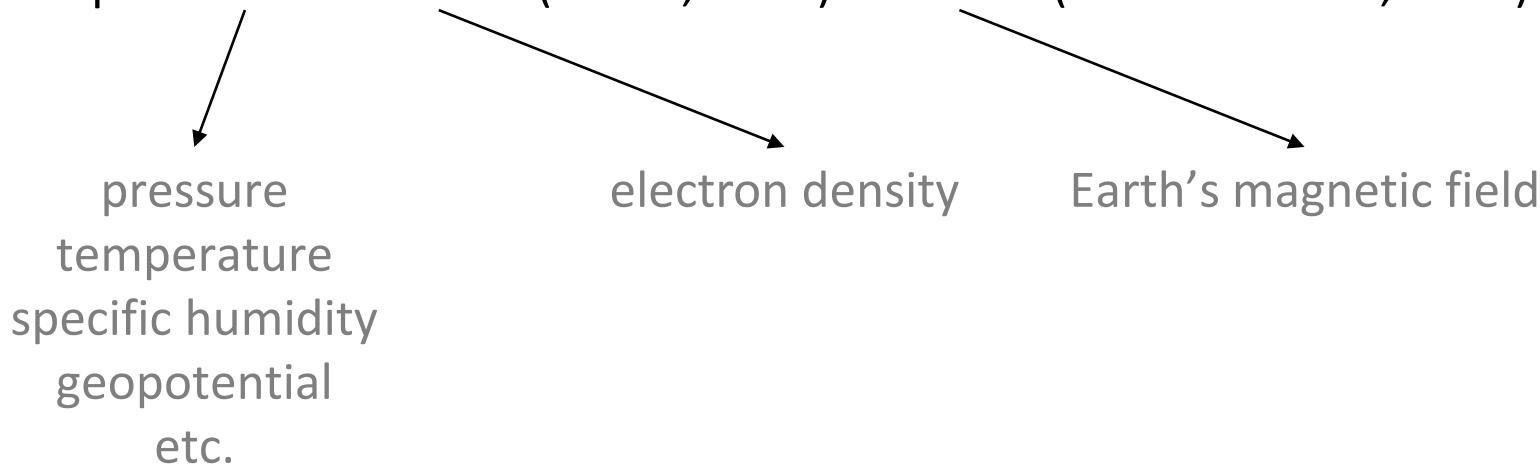
- ❑ Atmospheric ties from a *modeller's* perspective
- ❑ Atmospheric ties from a *geodesist's* perspective

# Chapter 0

## Ray-Tracing

# How Are the Atmospheric Delays Calculated?

- In-house GFZ's **ray-tracing software**: Direct Numerical Simulation (DNS) Tool by Zus et al. (2014)
- Input: **ERA5 + IRI2016** (Bilitza, 2018) + **IGRF12** (Thébault et al., 2015)



# Chapter I

## Definition of Atmospheric Ties

# What Are Atmospheric Ties?

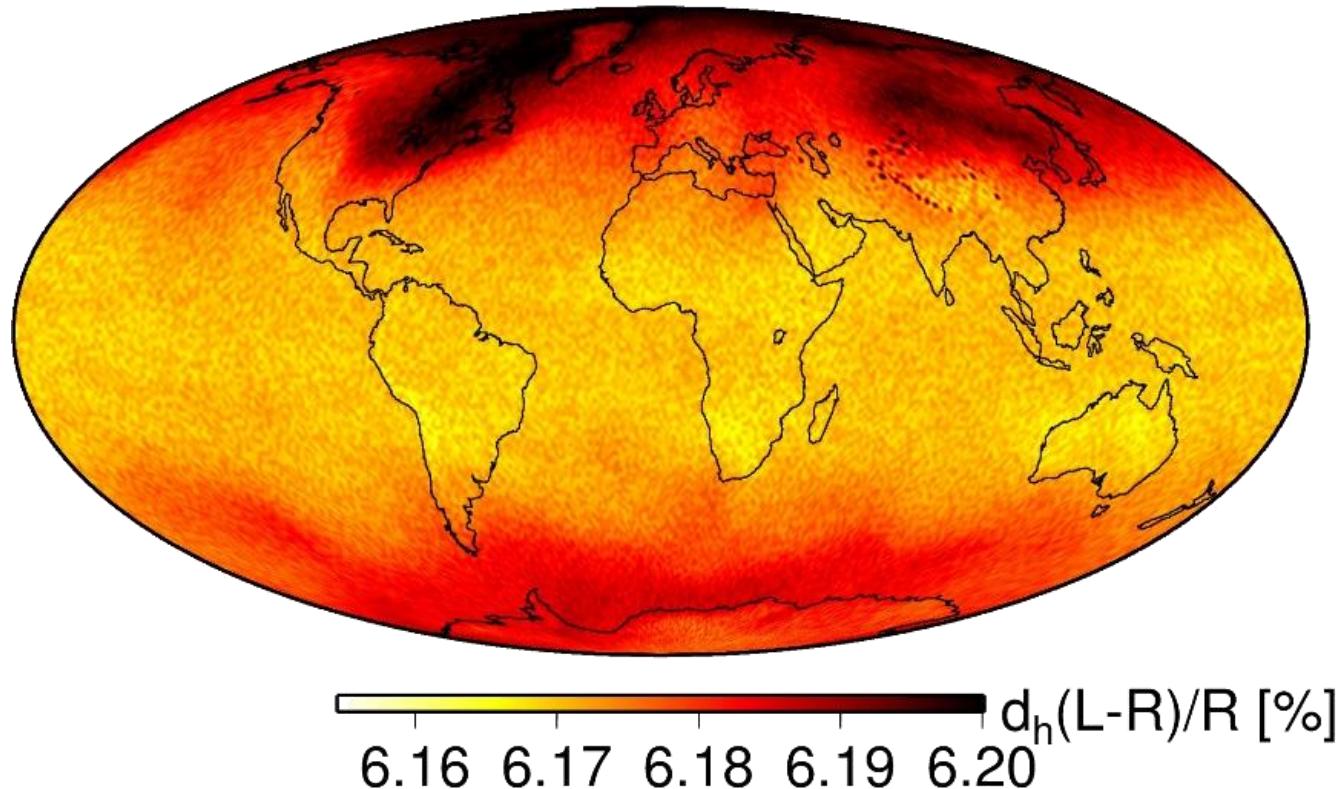
- Expected differences between atmospheric parameters at co-locations obtained *independently* of space geodetic methods
- Useful for intra- and inter-technique combination (e.g., Krügel et al., 2007; Thaller, 2008)
- Systematic discrepancies due to:
  - **frequency** difference (microwave, optical);
  - **position** difference (mainly height); and
  - **observing system** differences (technique, geometry, hardware)
- IAG JWG Tropospheric Ties (Heinkelmann et al., 2016)  
... continued for a second term by Kyriakos Balidakis & Daniela Thaller

# Chapter II

## Frequency-Induced Differences

# Zenith Hydrostatic Delays

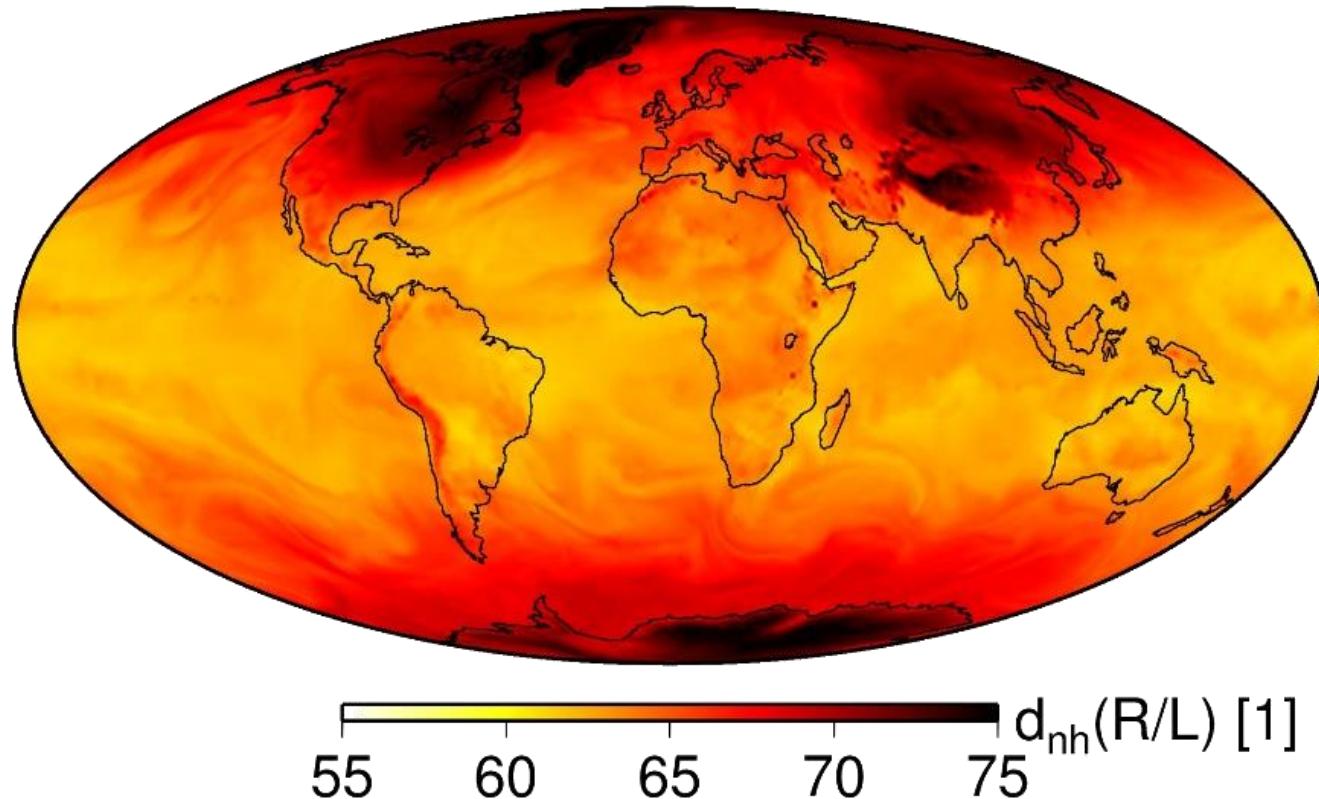
- SLR@532nm **6% larger** than VLBI/GNSS/DORIS



Balidakis (2019)

# Zenith Non-Hydrostatic Delays

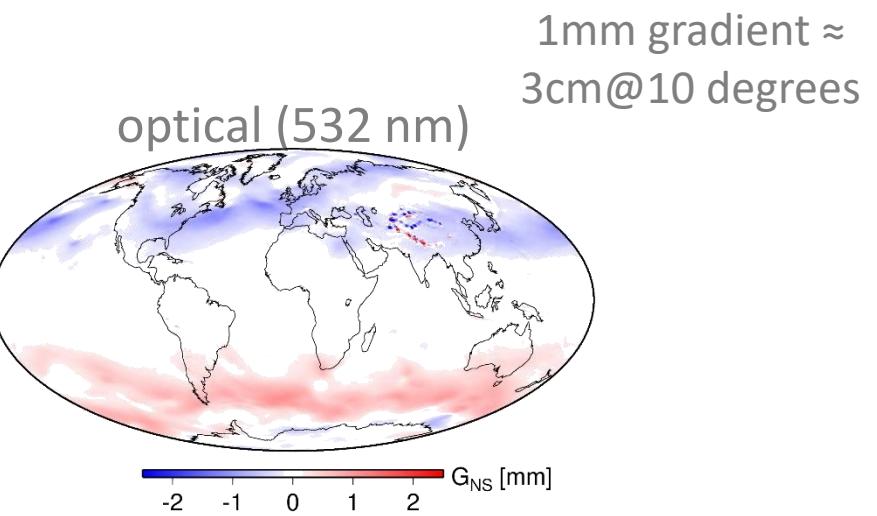
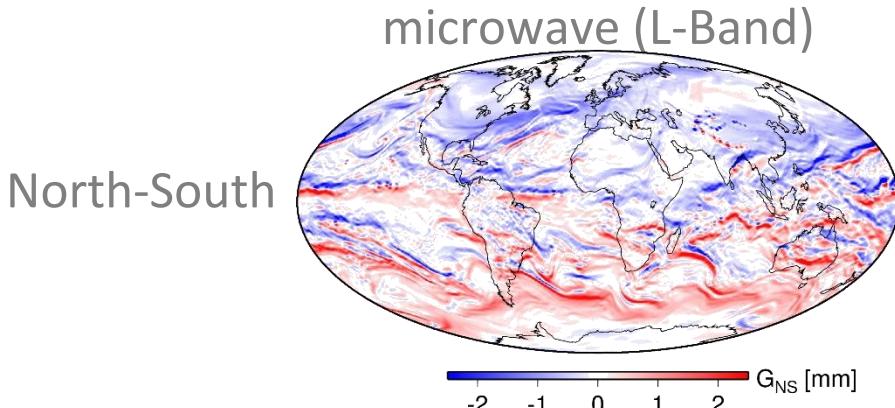
- SLR@532nm **66 times smaller** than VLBI/GNSS/DORIS



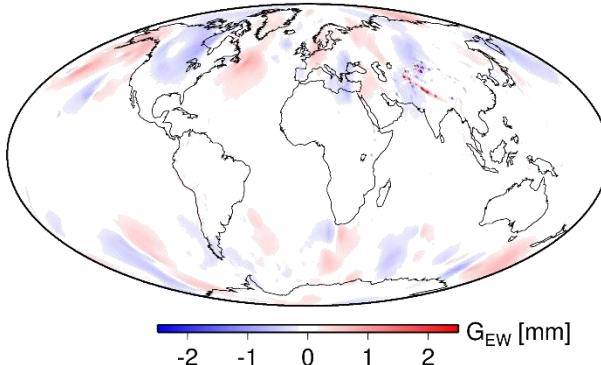
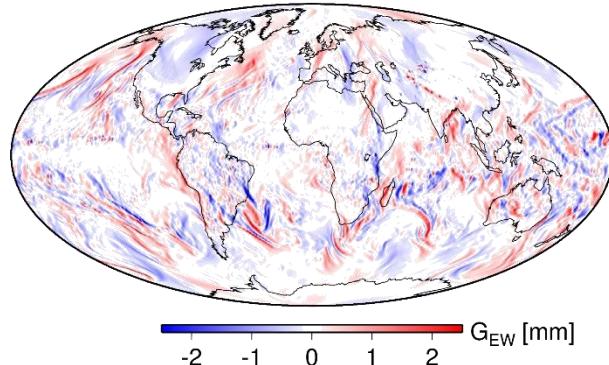
Balidakis (2019)

# Asymmetric Delays I

- Linear gradient components



East-West



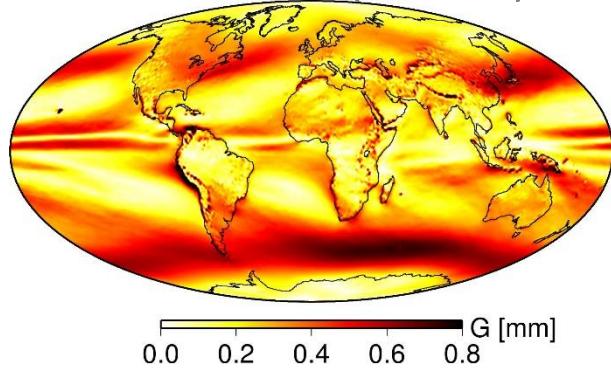
- Spatio-temporally noisy for microwave, smooth for optical

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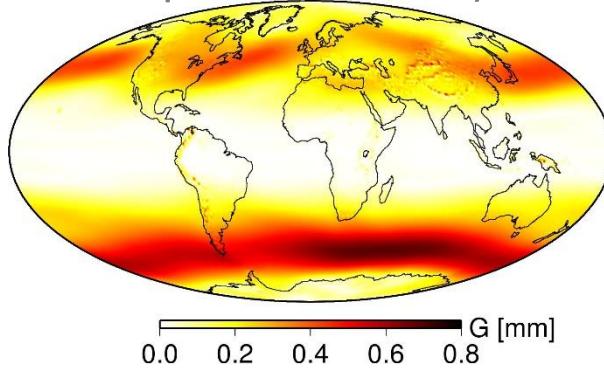
# Asymmetric Delays II

- 40-year average asymmetric delay amplitude

microwave (L-Band)

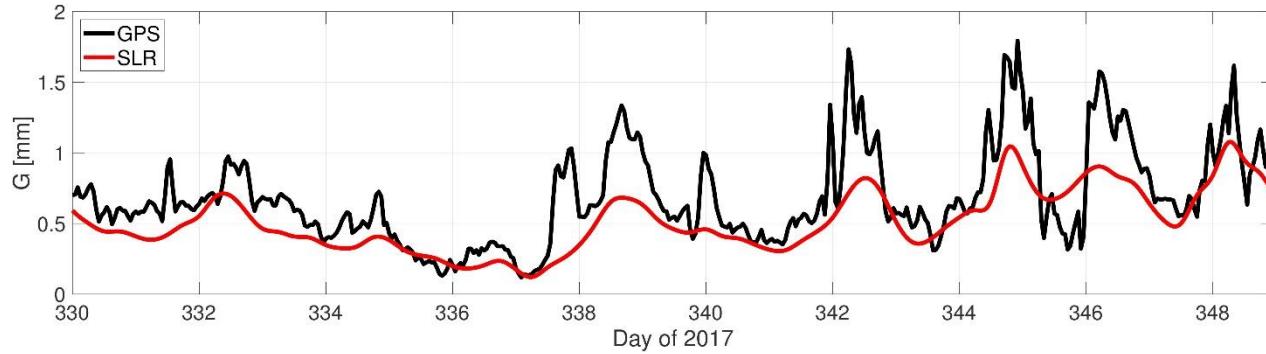


optical (532 nm)



$$G = \sqrt{G_{NS}^2 + G_{EW}^2}$$

- Hourly gradient estimates from ERA5 at Wettzell during CONT17

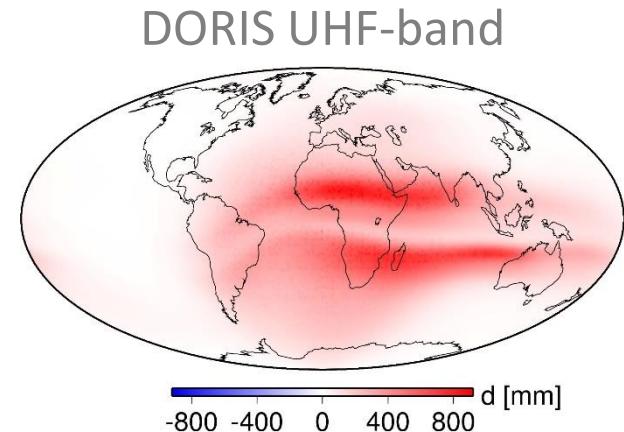
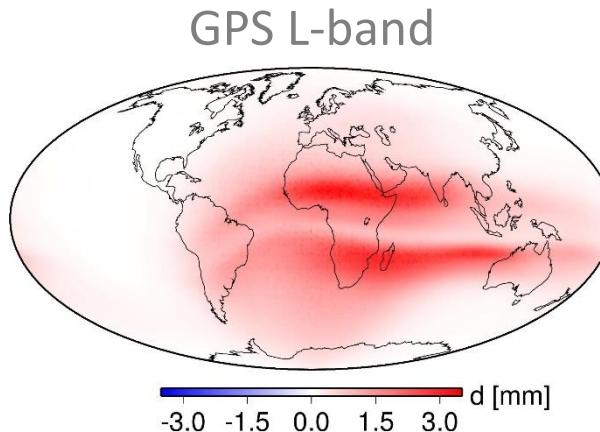
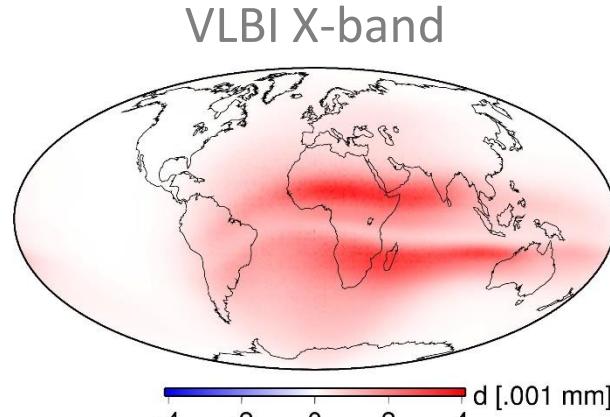


# Ray-Bending due to Ionospheric Refraction

Based on ERA5, IRI2016, IGRF2014,  $\varepsilon = 3^\circ$ ,  $\alpha = 0^\circ$

$$\int (1 + 10^{-6}N) ds_i - \int (1 + 10^{-6}N) ds_\infty$$

$N$ : refractivity,  $s_i$ : arc length,  $s_\infty$ : arc length in the hypothetical absence of ionosphere



expected  $\delta H \approx 0.4 \mu\text{m}$

expected  $\delta H \approx 0.4 \text{ mm}$

expected  $\delta H \approx 100 \text{ mm}$

Note the different colour scales!

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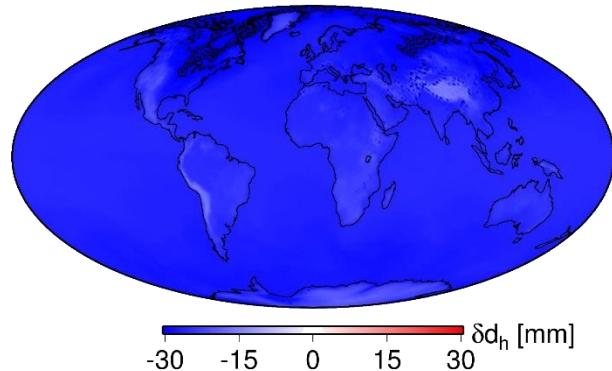
# Chapter III

## Position-Induced Differences

# Height-Related Differences

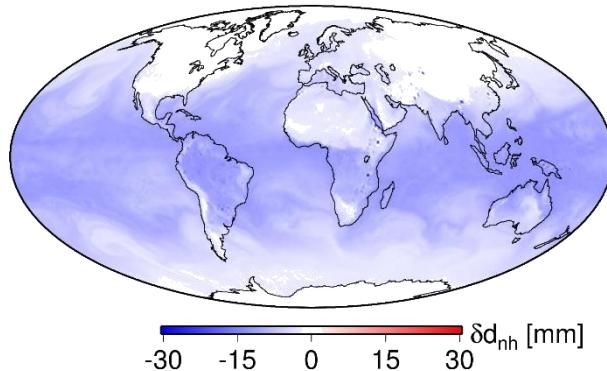
- 100 m height difference (Galileo)

Zenith hydrostatic delay



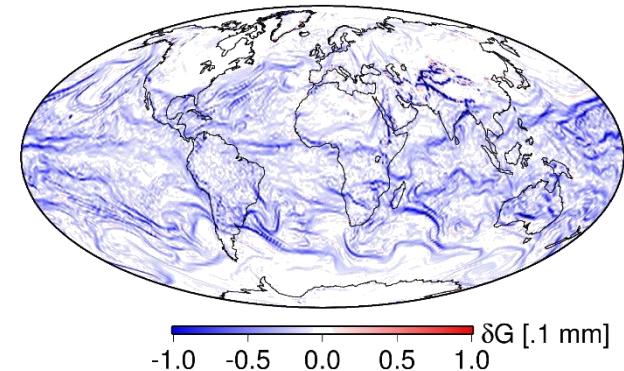
-27 mm on average

Zenith non-hydrostatic delay



-3 mm on average

Gradient amplitude

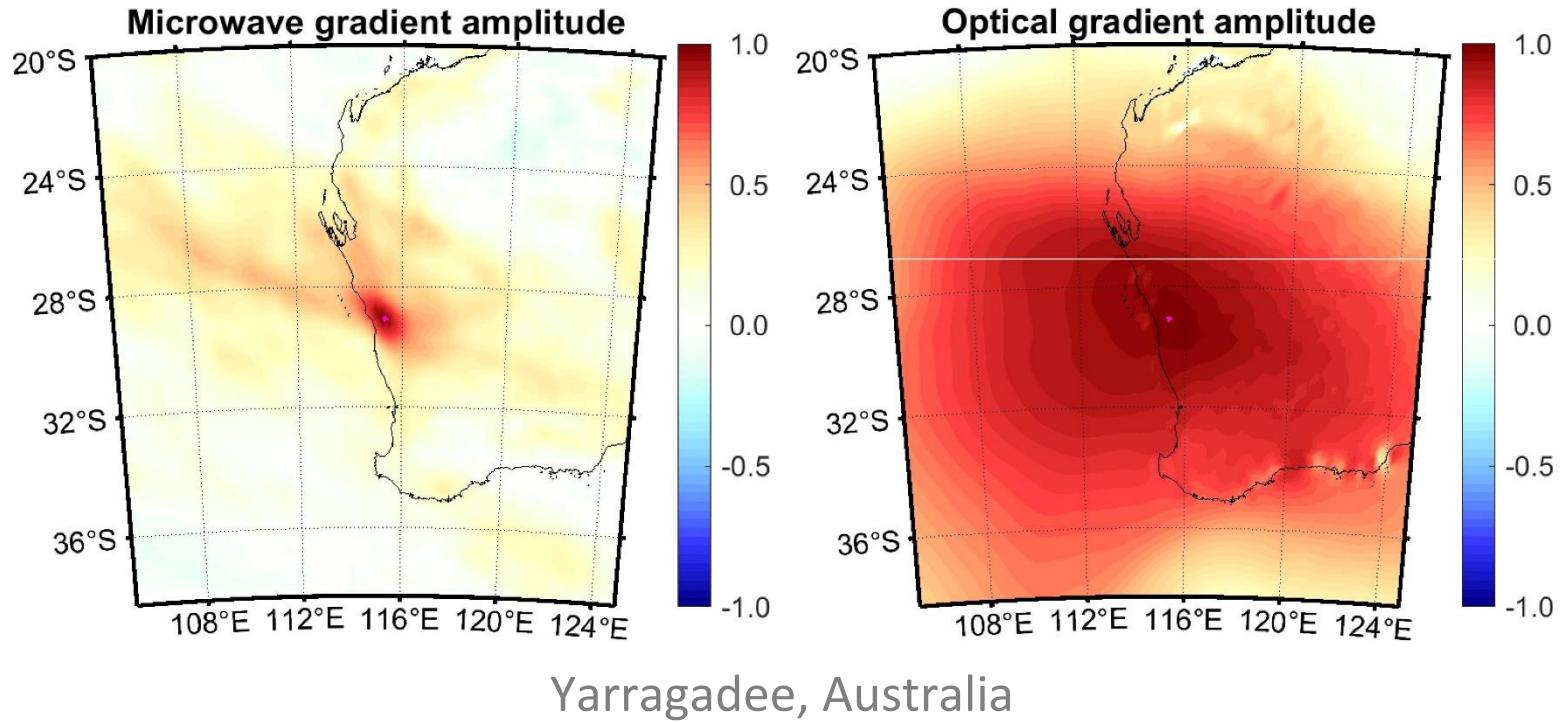


$$G = \sqrt{G_{NS}^2 + G_{EW}^2}$$

-0.06 mm on average  
or -3 mm@7°  
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- Symmetric/asymmetric delay decreases upwards

# Spatial Correlation



- ☐ Microwave gradients decorrelate very fast → difficult to predict

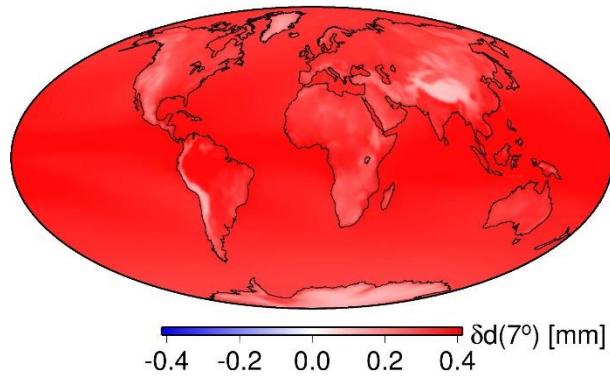
Balidakis (2019)

# Chapter IV

## Observing System-Induced Differences

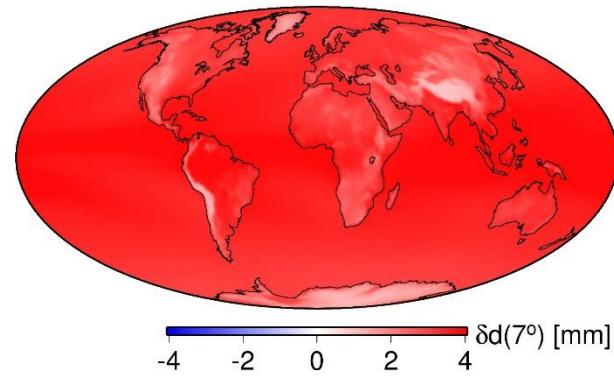
# Mapping Functions Depend on the Orbital Altitude

GNSS minus VLBI



expected  $\delta H \approx 0.2$  mm

DORIS minus VLBI



expected  $\delta H \approx 2$  mm

## □ Mapping factor magnitude ranking

$$mf^L < mf_{h,nh}^R < mf_{h,nh}^P < mf_{h,nh}^D$$

L: SLR, R: VLBI, P: GNSS, D: DORIS

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# Chapter V

## Simulation of Space Geodetic Observations

# Space Geodetic Adjustment

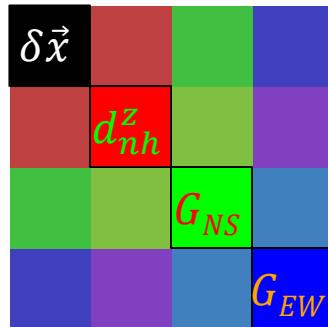
- ❑ Assumption: everything perfectly understood except for non-tidal station motion, atmospheric refraction, and frequency standards' stability
- ❑ Weighted least-squares, statistical tests for outliers, loose relative constrains, no absolute constrains, etc.

$$o - c = mf_{nh} d_{nh}^z + mf_g [G_{NS} \cos(\alpha) + G_{EW} \sin(\alpha)] + clk + \delta \vec{x}$$

estimated parameters

$o$ : observed,  $c$ : computed,  $mf_{nh}$ : non-hydrostatic mapping factor,  $mf_g$ : gradient mapping factor,  $\alpha$ : azimuth

- ❑ NEQs for combination

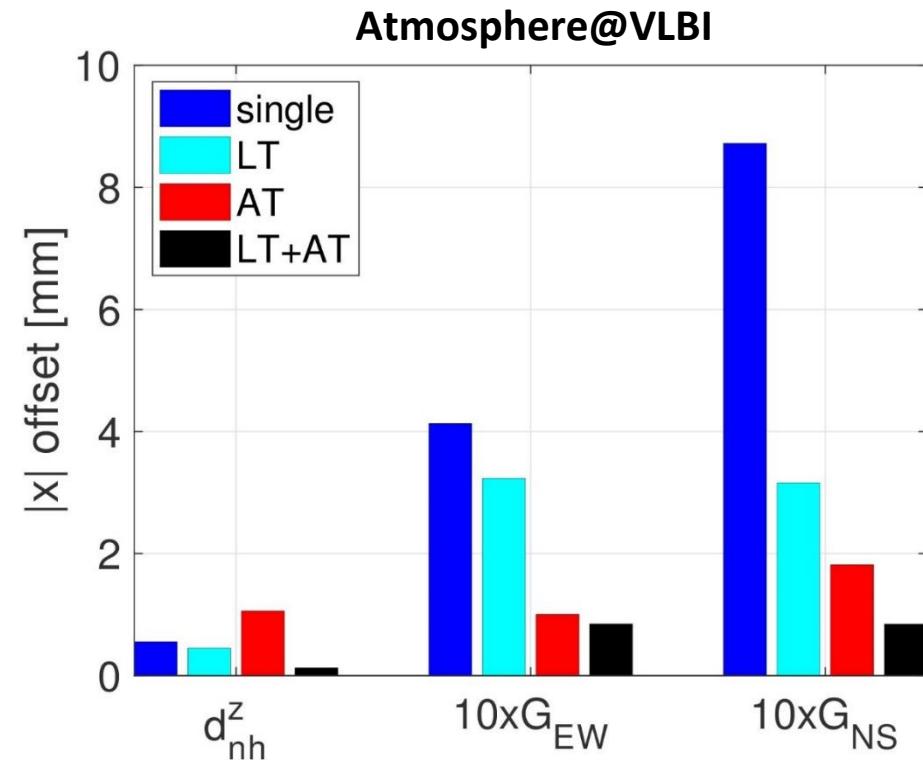
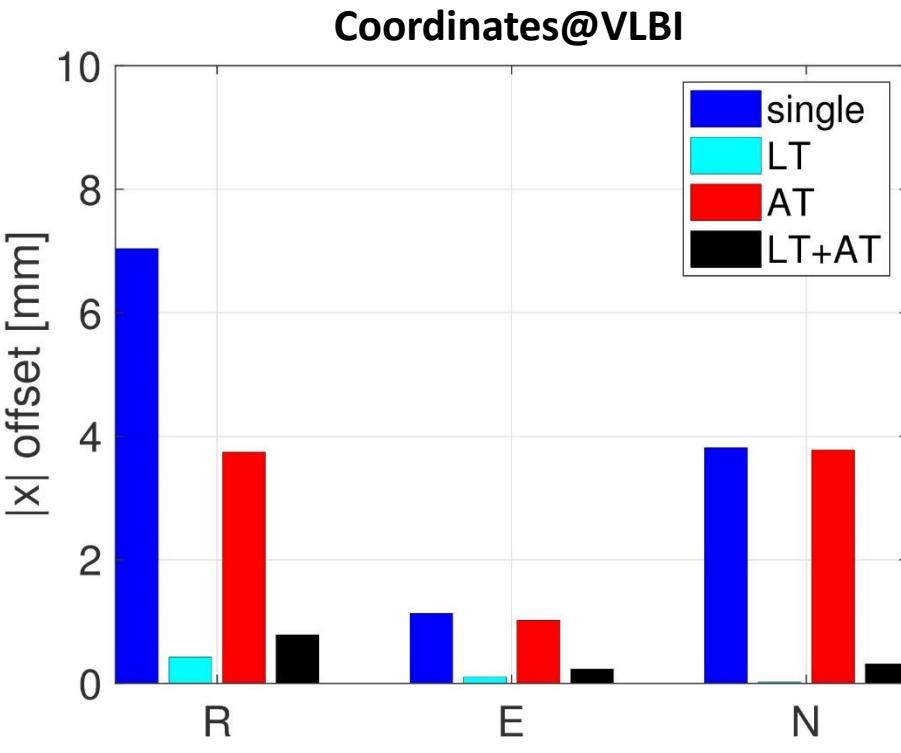


# Chapter VI

## Multi-Technique Combination

# ... Introducing Local + Atmospheric Ties

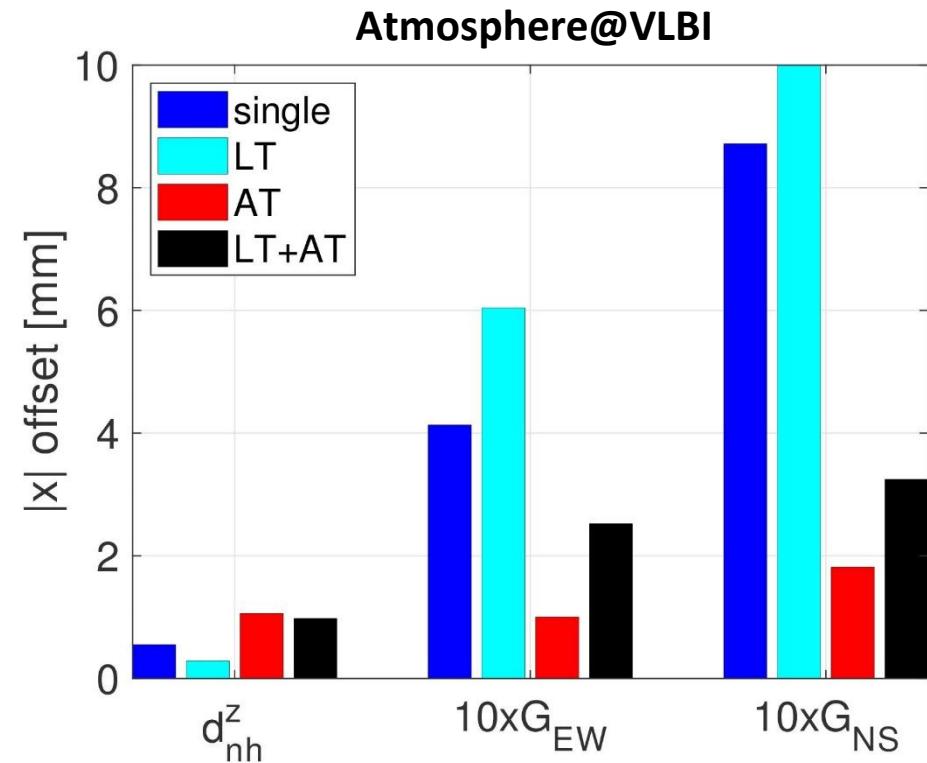
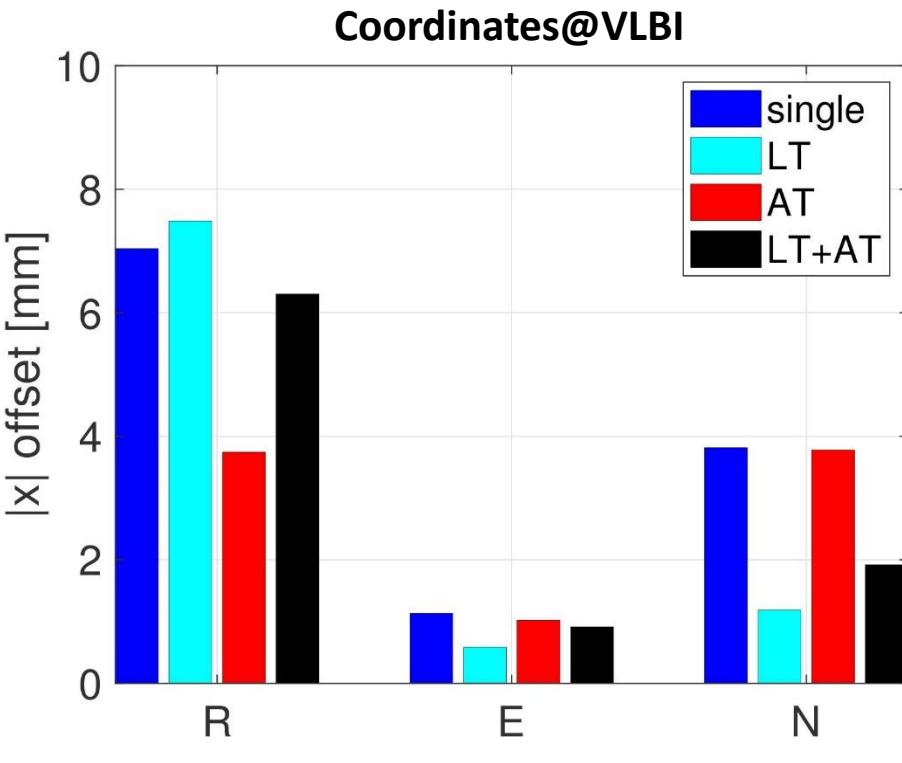
- Imp. for coordinates/troposphere → offset/scatter reduction



47% and 66% reduction in zenith delay and gradient scatter resp.

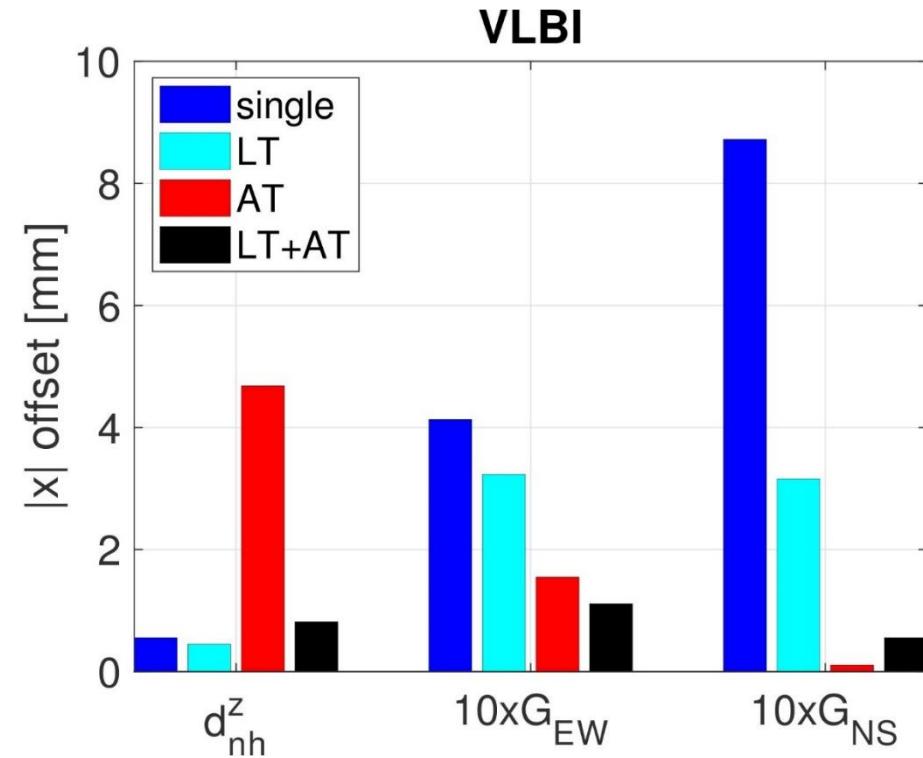
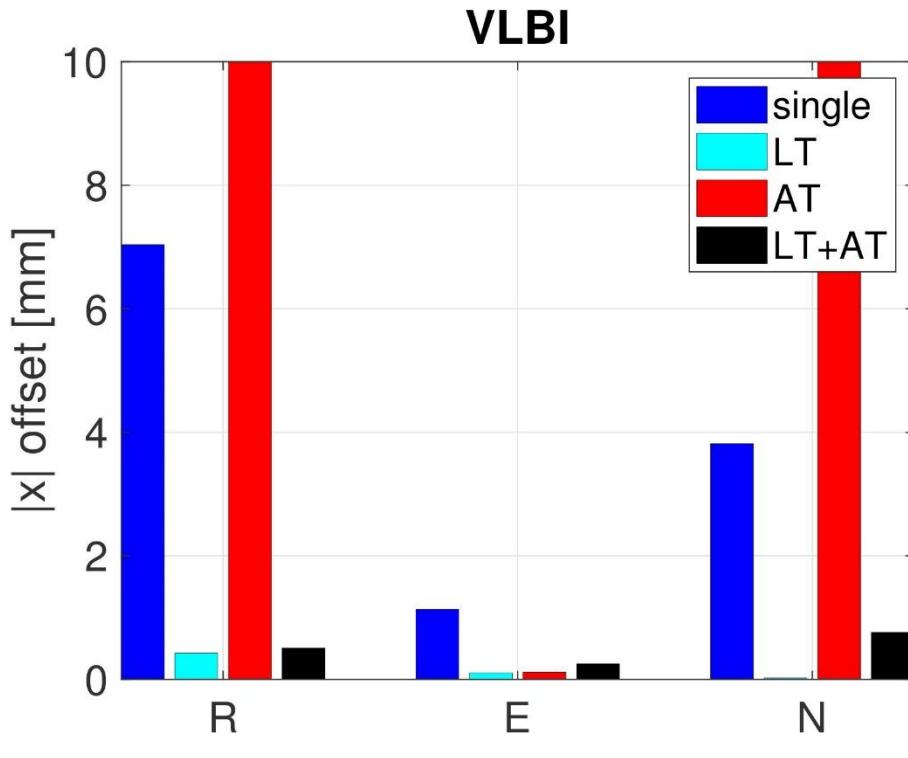
# ... Introducing 1cm Bias in VLBI Height

- Detr. for coordinates/troposphere → offset increase



# . . . Introducing 1cm Bias in VLBI $d_{nh}^z$

- Detr. for coordinates/troposphere → offset increase



# Recapitulation

- ❑ Frequency: optical gradients smoother spatially and temporally than microwave
- ❑ Position: symmetric/asymmetric delays decrease with increasing altitude
- ❑ System:  $mf^L < mf_{h,nh}^R < mf_{h,nh}^P < mf_{h,nh}^D$
- ❑ Based on simulations (PRLD combination with atmospheric and local ties):
  - ❑ ATs improve coordinate and troposphere estimation
  - ❑ ATs slightly mitigate the “damage” induced by biased LTs
  - ❑ ATs useful to detect biased LTs

# Thank you!

*contact*

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IGS

INTERNATIONAL  
GNSS SERVICE



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# Some references

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