

ESTÜ, 2 Eylül Kampüsü

Real-Time Reservoir Operation by Tree-Based Model Predictive Control Including Forecast Uncertainty

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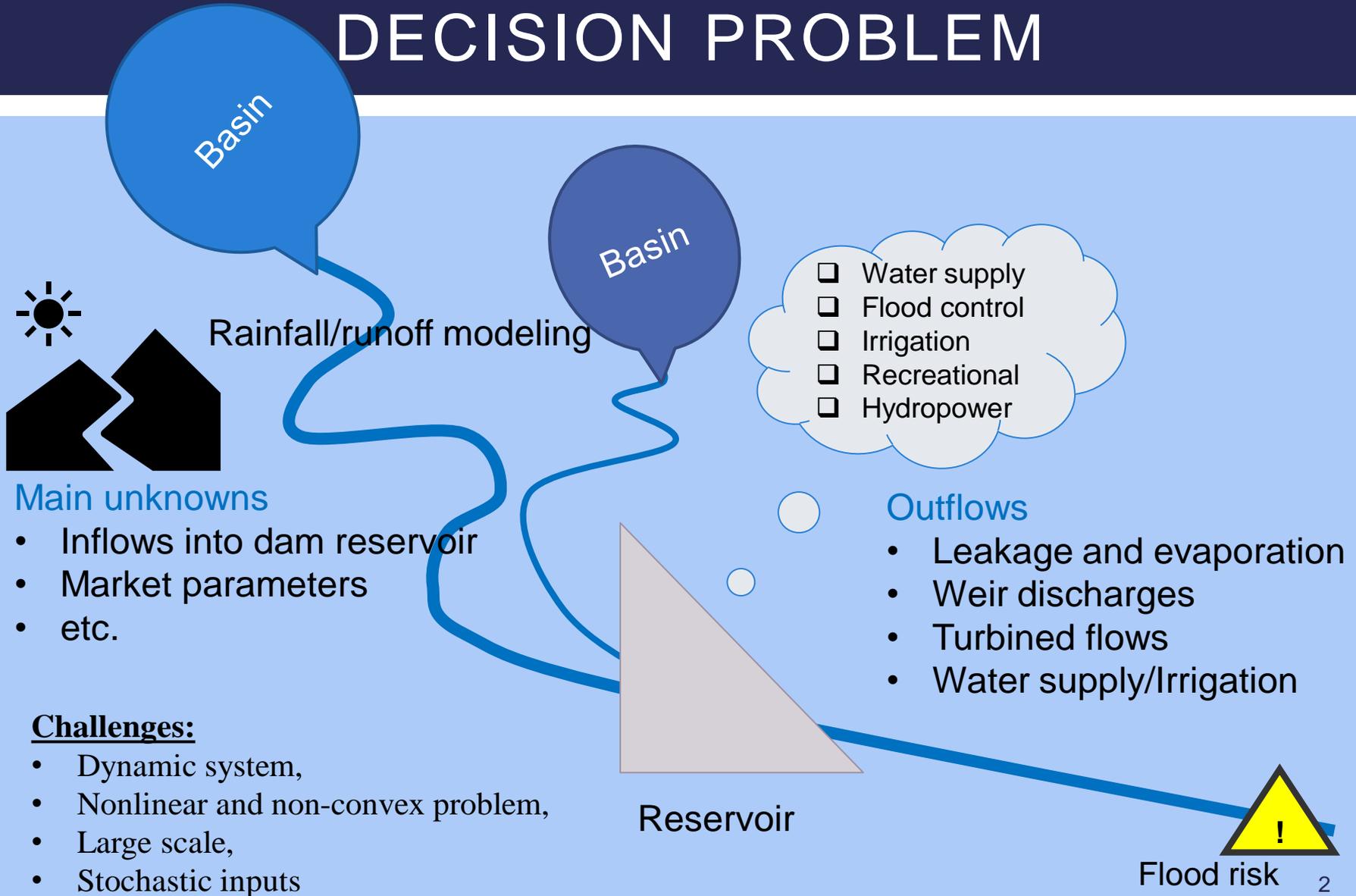
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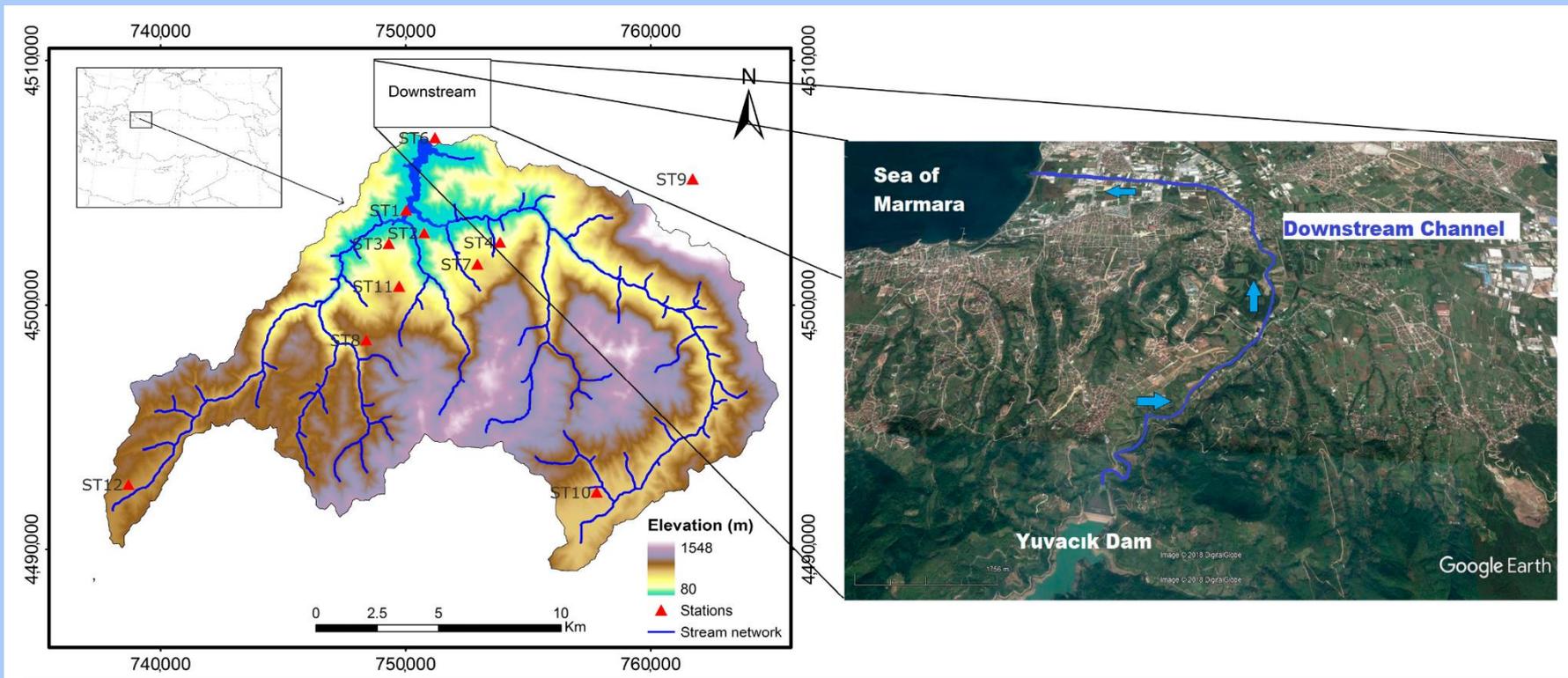


REAL-TIME RESERVOIR SYSTEM DECISION PROBLEM



STUDY AREA: YUVACIK DAM & BASIN

Uncertainty becomes much larger when managing small basins and small rivers.



- 11 Rain gauges
- 6 Temp. sensors
- 5 Snow depth sensors

Main Tasks: Water supply (1.5 m populated Kocaeli) +
Flood control (City)

DANGER OF FLOODING

- Excess amount of water during March through May months due to relatively small capacity is being spilled to a 12 km long manmade downstream channel and flowed into Marmara Sea.
- This channel passes through a rural and an industrial district and therefore, spillway discharges are getting important.
- These two photos are taken on 2010 year. Although spillway gates were not operated, a flood was observed in downstream channel area.



THE BACKGROUND OF THE CURRENT STUDY CAN BE FOUND AT...

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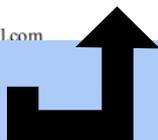
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Abstract Reservoir operations require enhanced operating procedures for water systems under stress attributed to growing water demand and consequences of changing hydro-climatic conditions. This study focuses on the management of the Yuvacik Dam Reservoir for water supply and flood mitigation in the Marmara Region of Turkey. We present an improved operating technique for fulfilling the conflicting water supply and flood mitigation objectives. This is accomplished by incorporating the long term water supply objectives into a Guide Curve (GC) whereas the extreme floods are attenuated by means of short-term optimization based on Model Predictive Control (MPC). The reference case implements operating rules with a constant GC at maximum forebay elevation targeting the fulfillment of the water supply objective. We compare the reference with a new time-dependent GC, derived using an Implicit Stochastic Optimization (ISO) approach. This new curve shows nearly the same performance regarding the water supply objectives, but significantly reduces the flooding risk downstream of the dam. Possible flood events observed at the end of the wet season, when the reservoir is at the maximum level to enable water supply for the dry season, can be eliminated by the application of an additional short-term optimization by MPC. The robustness of the approach is demonstrated via hindcasting experiments.

Keywords Reservoir operation · Optimization · Simulation · Water supply · Flood mitigation · Model Predictive Control

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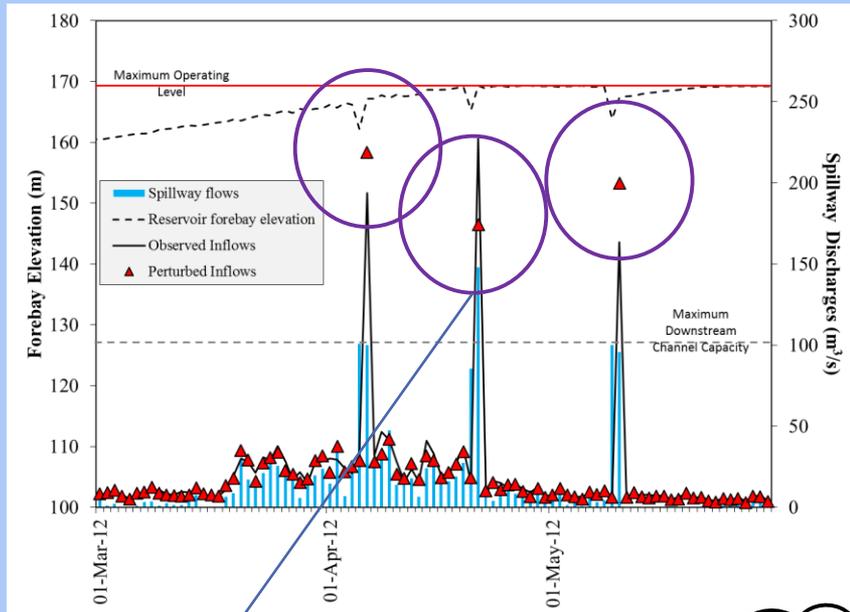
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- **Uysal et al. (2018a)** aims to derive operating Guide Curve (GC) based on Model Predictive Control (MPC) application.
- Also, the closed-loop simulation (hindcasts) shows the advantages of using MPC.

Uysal et al. (2018a)

THE MAIN CONCEPT WAS...



Uysal et al. (2018a)

✓ Proactive operation!

BUT



- While (daily) variable GC is useful for long term strategies in decision making, the model is not robust against forecast uncertainty.

AIM & CONTENT OF THIS STUDY

- This study practices (hourly) ensemble streamflows as input of the recurrent reservoir operation problem which can incorporate:



- (i) forecast uncertainty,
- (ii) forecasts with a higher lead-time and
- (iii) a higher stability

Thus, the aim of this study is to set a TB-MPC based real-time reservoir operation via hindcasting experiments.

FOR MORE INFORMATION...



Article

Real-Time Flood Control by Tree-Based Model Predictive Control Including Forecast Uncertainty: A Case Study Reservoir in Turkey

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Abstract: Optimal control of reservoirs is a challenging task due to conflicting objectives, complex system structure, and uncertainties in the system. Real time control decisions suffer from streamflow forecast uncertainty. This study aims to use Probabilistic Streamflow Forecasts (PSFs) having a lead-time up to 48 h as input for the recurrent reservoir operation problem. A related technique for decision making is multi-stage stochastic optimization using scenario trees, referred to as Tree-based Model Predictive Control (TB-MPC). Deterministic Streamflow Forecasts (DSFs) are provided by applying random perturbations on perfect data. PSFs are synthetically generated from DSFs by a new approach which explicitly presents dynamic uncertainty evolution. We assessed different variables in the generation of stochasticity and compared the results using different scenarios. The developed



HINDCAST EXPERIMENTS



- **Hindcasting experiments*** are the representation of a real-time system by an iterative process.
- We apply closed-loop hindcasting experiments by the following three modes:
 1. **Perfect Hindcast Experiments**: Best! (No Uncertainty)
 2. **Deterministic Hindcast Experiments**: No uncertainty (Only one single forecast member)
 3. **Probabilistic Hindcast Experiments**: Multiple forecast members!
This represents the skill of ensemble PSF evaluation by multi-stage stochastic TB-MPC.

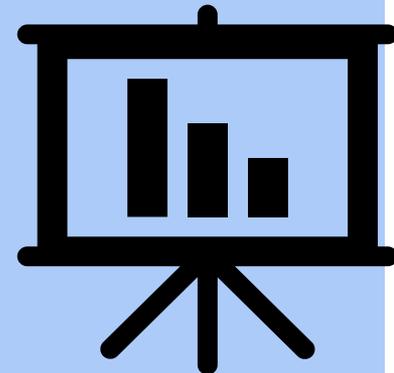
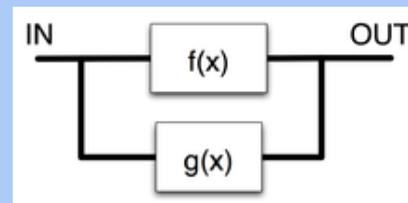
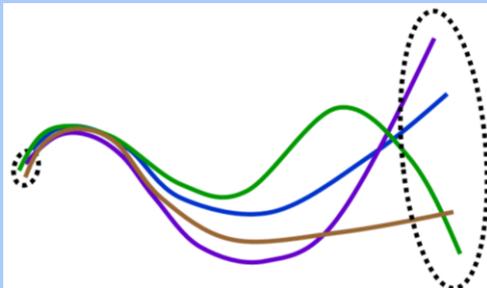
METHODOLOGY

... is comprised of ...

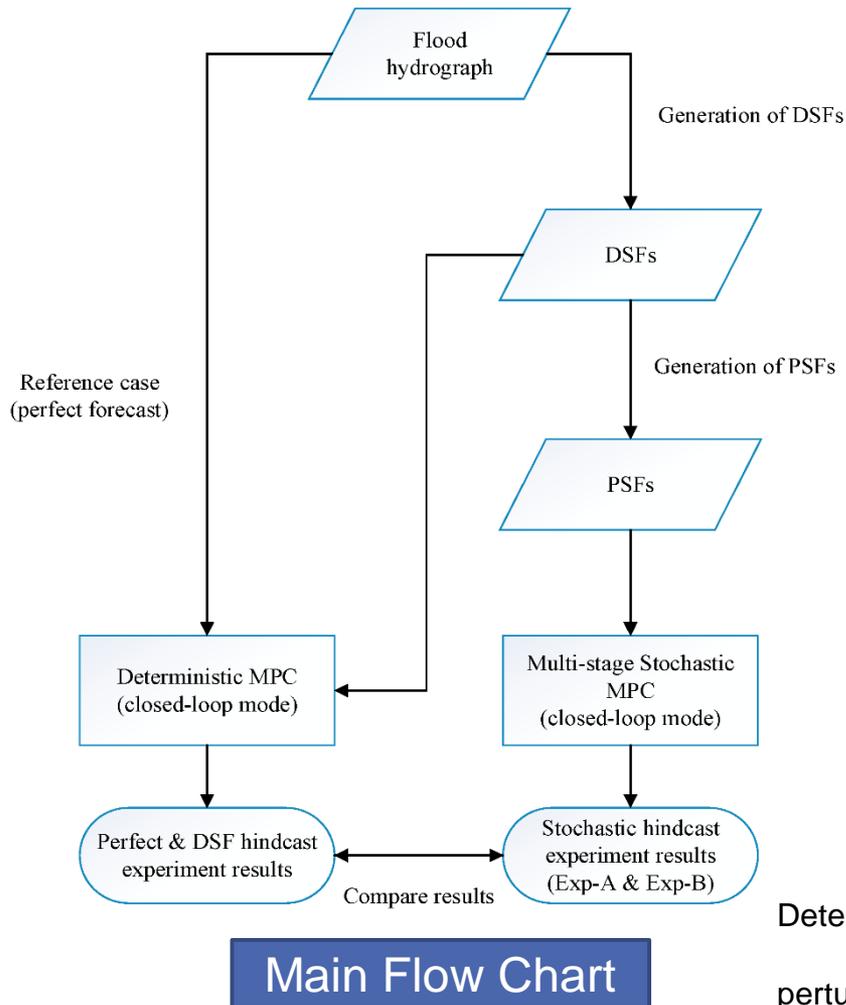
1. Reservoir Controls
2. Optimization
3. Uncertainties in flow forecasting
4. Stochastic Optimization + Control = ?



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This study complements deterministic methods by PSF integrated TB-MPC including forecast uncertainty.



Main Flow Chart

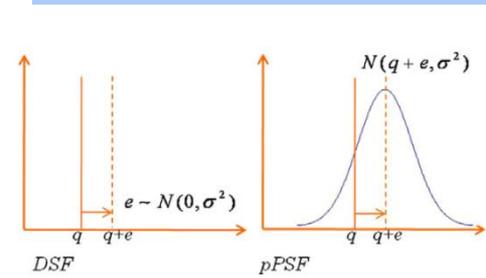
■ Mainly three scenarios are conducted in MPC

1. Perfect MPC (using observed data, Q_{100} flood hydrograph)
2. Deterministic MPC (using DSFs)
3. Multi-stage MPC (using PSFs)

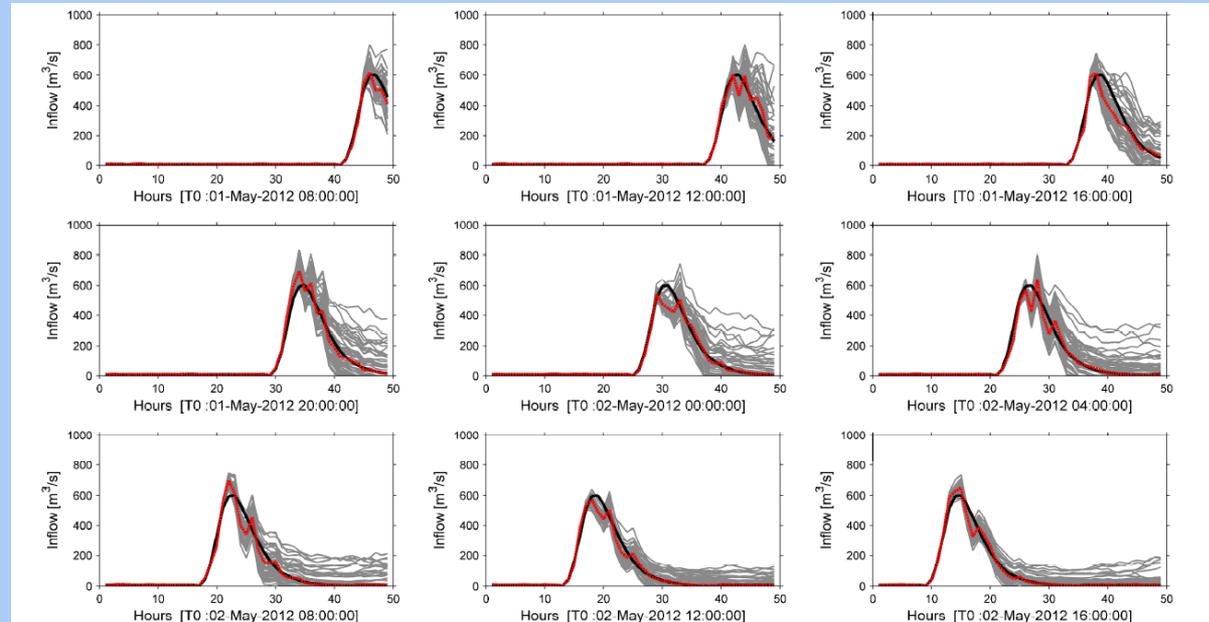
Deterministic Streamflow Forecasts (DSFs) are provided by applying random perturbations on perfect data.

FORECAST GENERATION (PERFECT, DSF & PSF)

Condition 1:
Normal distribution

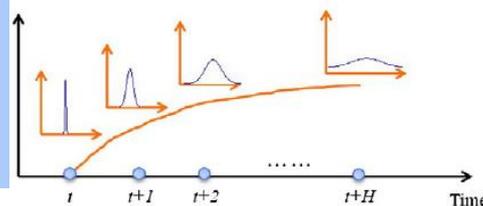


Condition 2:
Correlation
between
forecasts



Forecast uncertainty

Condition 3:
Increasing uncertainty



Condition 4:
Updating the inflows
(depending on
condition)

MODEL PREDICTIVE CONTROL (MPC)

Simultaneous MPC

$$x^k = f(x^{k-1}, x^k, u^k, d^k)$$

$$y^k = g(x^k, u^k, d^k)$$

where x , y , u , d are respectively **the state**, **dependent variable**, **control** and **disturbance vectors**, and $f()$, $g()$ are functions representing an arbitrary linear or nonlinear water resources model.

Cost function:

$$\min_{u, x \in \{0, \dots, T\}} \sum_{k=1}^{N-1} J(x^k, u^k, d^k) + E(x^N, u^N, d^N)$$

Subject to:

$$h(x^k, y^k, u^k, d^k) \leq 0, k = 1, \dots, N$$

$$x^k - f(x^{k-1}, x^k, u^k, d^k) = 0$$

the related model (herein, reservoir simulation equations) becomes an equality constraint of the optimization problem in the last equation.

...enabling the use of state-of-the-art Nonlinear Programming such as the open source optimizer IPOPT (**Wächter and Biegler 2006**). The model itself is implemented in RTC-Tools (Schwanenberg et al. 2014).

MULTI-STAGE STOCHASTIC SET-UP

The problem is extended through multi-stage stochastic set-up by changing d^k with d_j^k where j denotes the ensemble index ($j = 1, \dots, M$) and k denotes the time instant ($k = 1, \dots, N$).

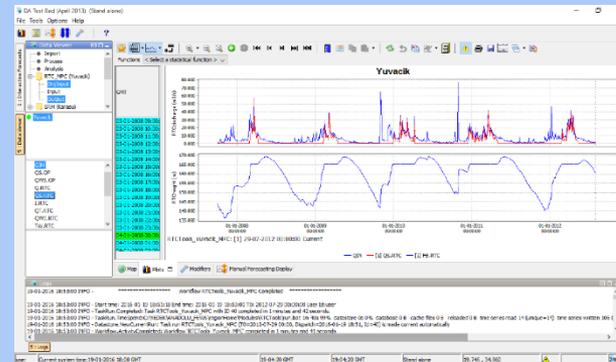
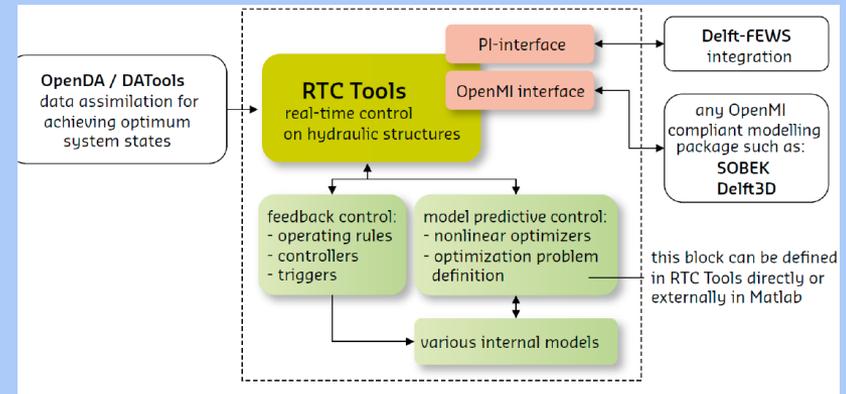
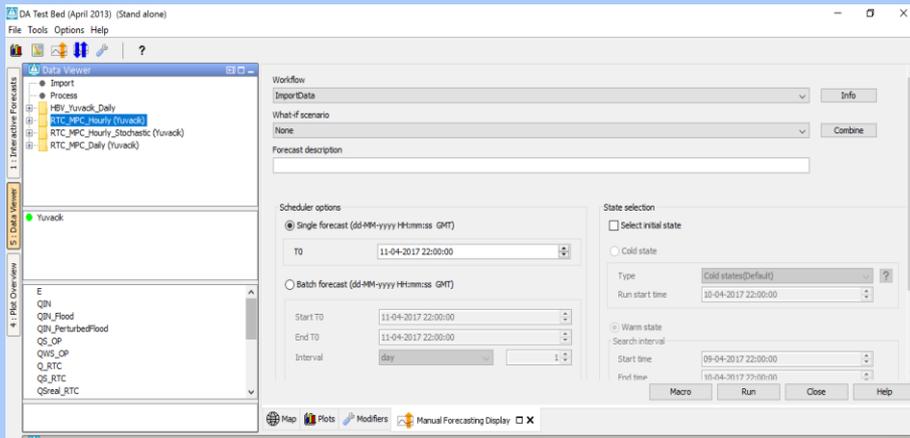
$$\min_{u, x \in \{0, \dots, T\}} \sum_{j=1}^M p_j \sum_{k=1}^{N-1} J(x_j^k, u_j^k, d_j^k) + E(x_j^N, u_j^N, d_j^N) \quad (6)$$

where p_j stands for the probability of the ensemble member, M stands for the number of the ensembles.

Definition of control variable u_j^k identifies the approach for stochastic MPC set-up. At this point, multi-stage stochastic optimization (so called Tree-based MPC, TB-MPC) is dedicated way which uses scenario trees for disturbance, states and control trajectories [4].

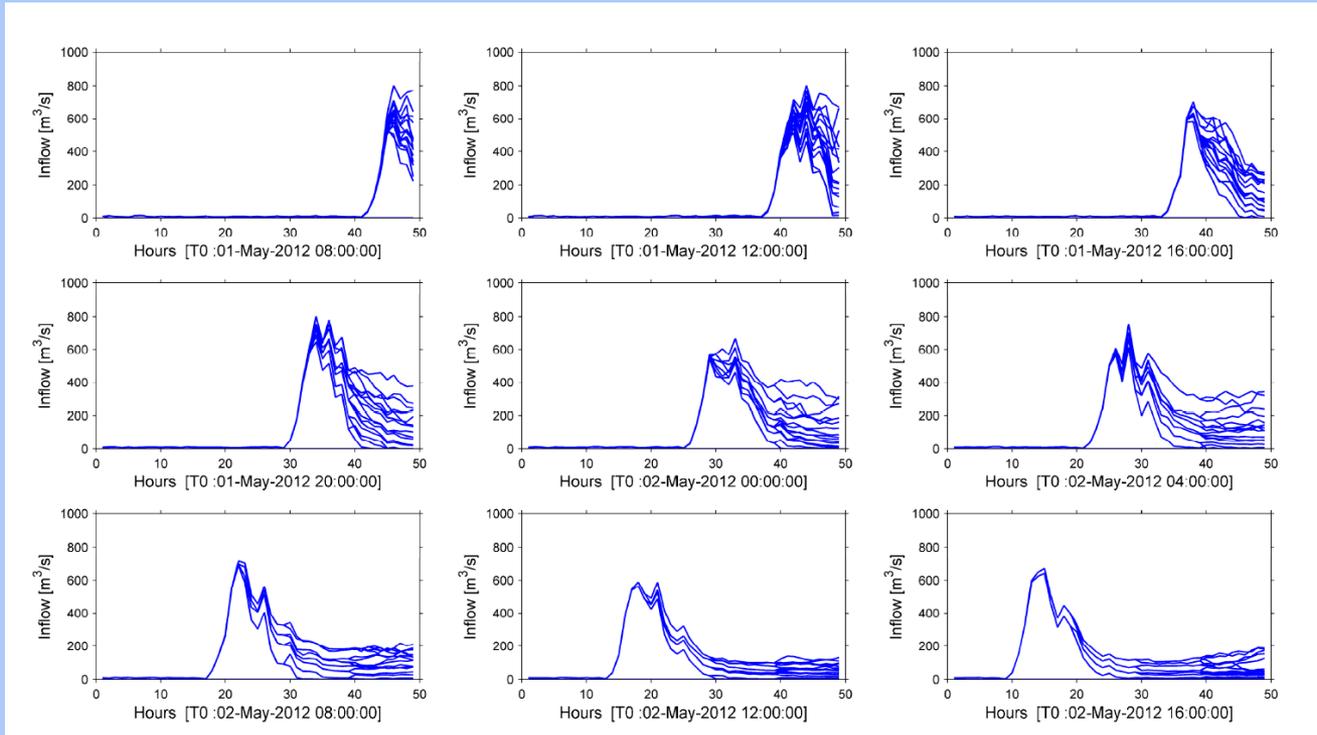
CONTROL INTERFACE AND MODELING SOFTWARE

- Deltares-Flood Early Warning System (FEWS) (Werner vd., 2013)
- Real Time Control (RTC)-Tools (Schwanenberg ve Becker, 2009)



TREE REDUCTION METHOD

- Tree-based reduction method is applied to ensemble members Fan et al. (2016)



PSF ensemble members (50) transformed into
optimization trees (16 branches)

MODEL SET-UP

Storage equation

$$s^k = s^{k-1} + \Delta t (Q_I^k - Q_S^k - Q_{WS}^k)$$

piecewise-linear level-storage relation

$$fb^k = f_{ls}(s^k)$$

$$r^k = s^k - s^{k-1} - \Delta t (Q_I^k - Q_S^k - Q_{WS}^k) = 0$$

mass balance definition

$$fb_{min} \leq fb^k \leq fb_{max}$$

The system's physical limits

$$Q_{S_{min}} \leq Q_S^k \leq Q_{S_{max}}^k$$

$$Q_{S_{max}}^k = f_{sdc}(fb^k)$$

A reservoir having a limited capacity should include the terms below for hourly management:

$$J1(fb) = w_1 \sum_{k=1}^N (f_{max} - fb^k)$$

$$J2(Q_S) = w_2 \sum_{k=1}^N (Q_S^k)$$

$$J3(Q_S) = w_3 \sum_{k=1}^N \max(Q_S^k - Q_{set}, 0)^2$$

$$J4(fb) = w_4 \sum_{k=1}^N \max(fb^k - fb_{set}, 0)^2$$

$$J5(Q_S) = w_5 \sum_{k=1}^N (Q_S^{k+1} - Q_S^k)^2$$

GC issue →

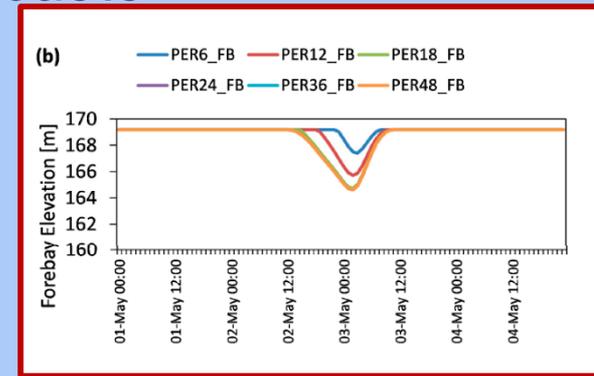
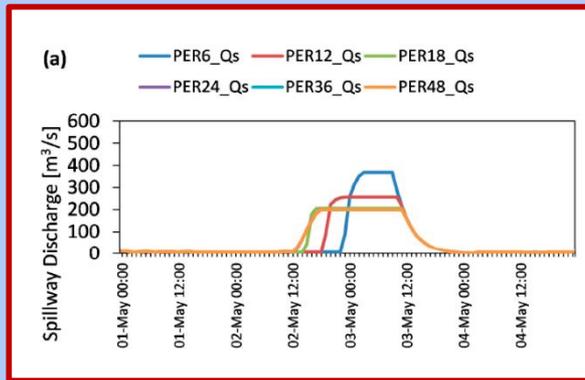
Objective Function

$$\min J(fb, Q_S) = J1 + J2 + J3 + J4 + J5$$

$$k \in \{0, \dots, T\}$$

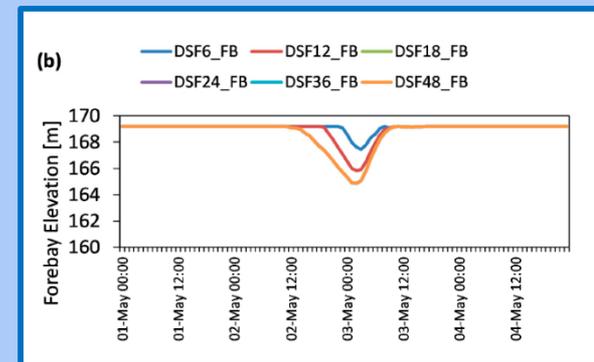
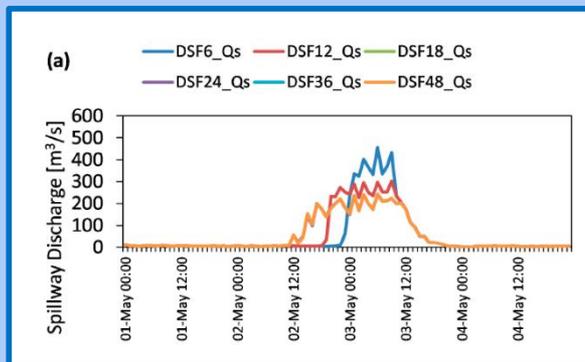
RESULTS (PERFECT AND DETERMINISTIC HINDCASTS)

- If there is no uncertainty in forecasts



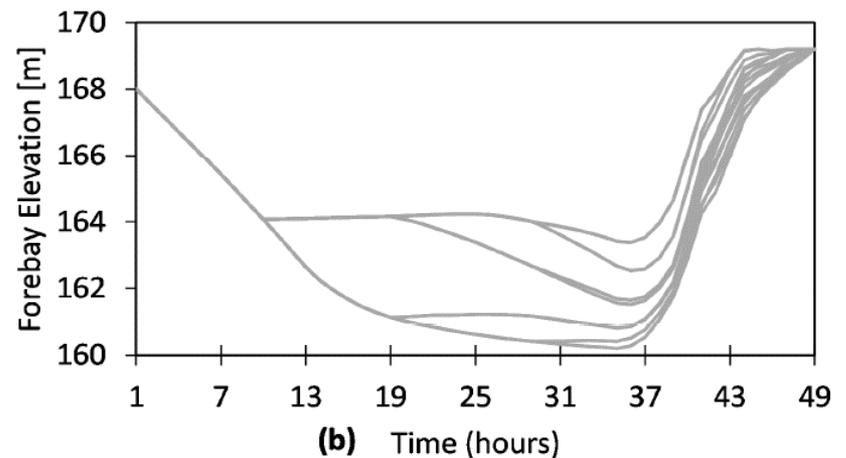
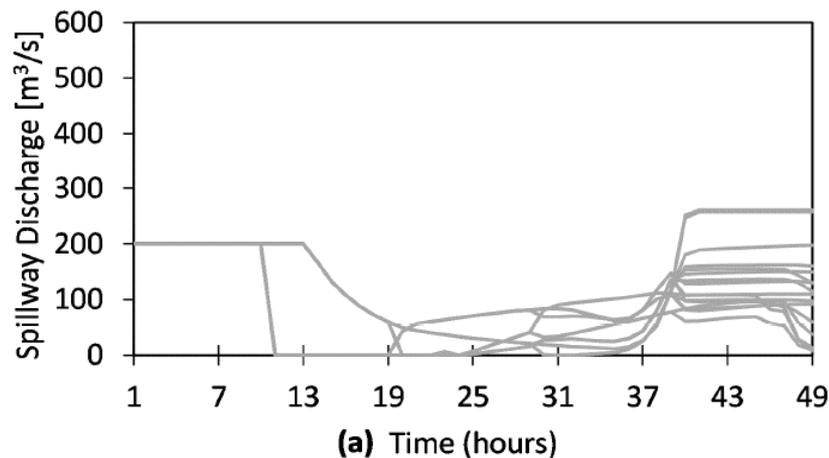
Forecast horizon should be at least 18 hr

- However, forecasts are biased and single forecast based results does not satisfy targets (>200 cms = flooding!)



AN OPEN-LOOP EXAMPLE RESULT FOR STOCHASTIC OPTIMIZATION

- Open-loop optimization results of multi-stage stochastic optimization (from Sce-Q100a) for 48 hr ahead



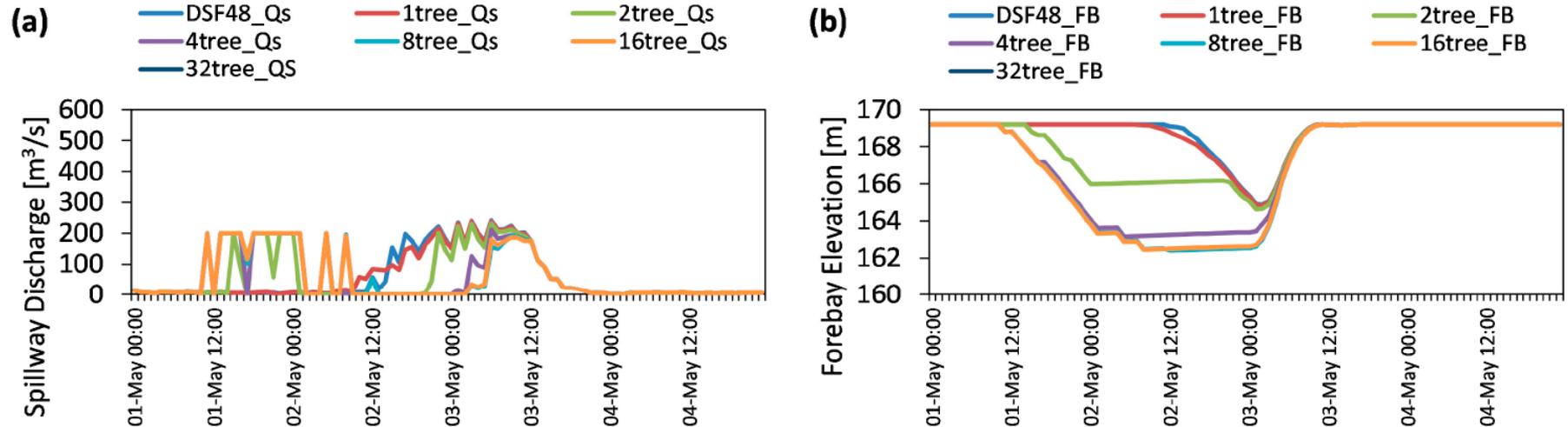
(a) Spillway discharge trees (m^3/s);
(b) (b) forebay elevation trees (m).

RESULTS (DIFFERENT BRANCHES)

What is should be the optimum branch number (due to reduction method)?

- Optimum results are received after 16 tree branches

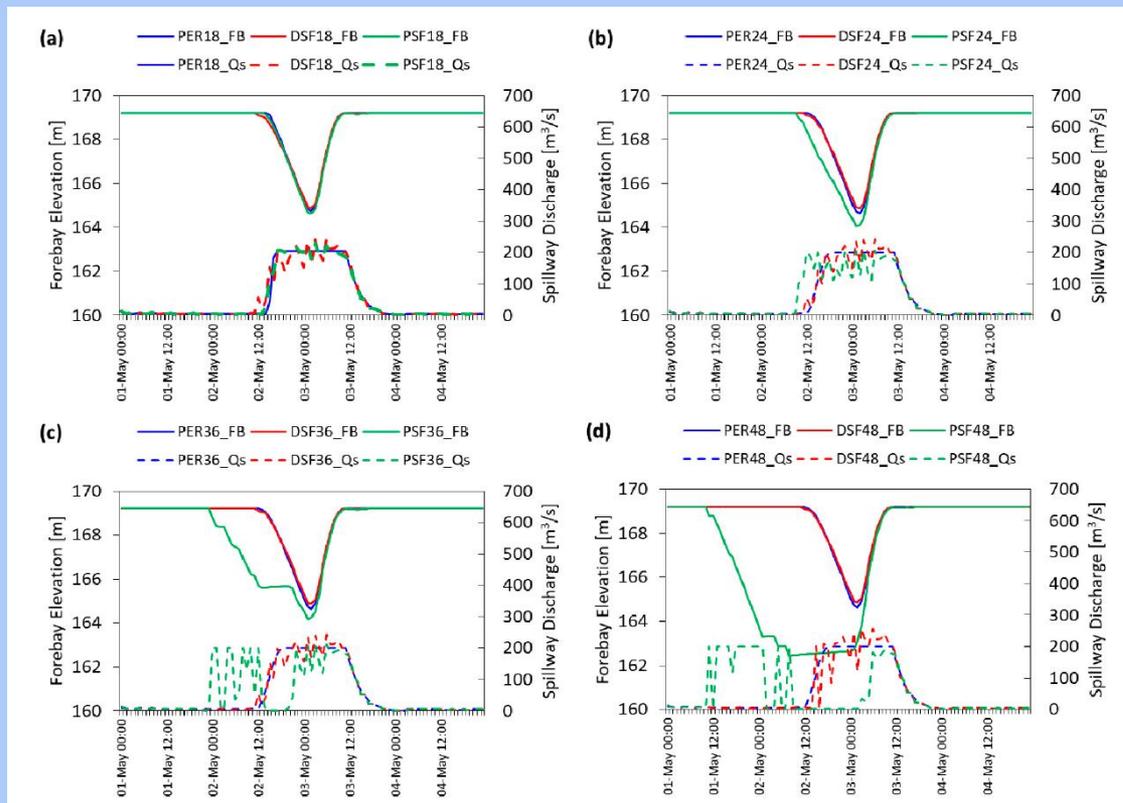
Note: 1 tree stochastic MPC = Deterministic MPC (almost)



Comparison of closed-loop MPC with different tree reduction branches for 48 h forecast horizon (Sce-Q100a): (a) Spillway discharge (m³/s); (b) forebay elevation (m).

RESULTS (FOREBAY ELEVATION & SPILLWAY DISCHARGE)

Comparison of deterministic (perfect and DSF) and stochastic (PSF) **closed-loop MPC results** with different forecast horizons (Sce-Q100a): (a) 18 h; (b) 24 h; (c) 36 h;



COMPARISON WITH DIFFERENT METRICS (1)

Peakflow assessment of deterministic and stochastic **closed-loop MPC results** for different inflow conditions with forecast horizons of 48 h.

Flood Hydrograph	Scenarios	Peakflow at Yuvacik Outlet (m ³ /s)	
		Deterministic MPC	Stochastic MPC
Q ₂₅	Sce-Q25a	243	231
	Sce-Q25b	255	243
	Sce-Q25c	248	243
Q ₅₀	Sce-Q50a	241	211
	Sce-Q50b	245	200
	Sce-Q50c	246	200
Q ₁₀₀	Sce-Q100a	242	200
	Sce-Q100b	269	235
	Sce-Q100c	278	233

Flood volume assessment of deterministic and stochastic **closed-loop MPC results** for different inflow conditions with forecast horizon of 48 h.

Flood Condition	Scenarios	Total Flood Volume (1 × 10 ⁶ m ³)	
		Deterministic MPC	Stochastic MPC
Q ₂₅	Sce-Q25a	0.507	0.302
	Sce-Q25b	0.549	0.254
	Sce-Q25c	0.438	0.271
Q ₅₀	Sce-Q50a	0.666	0.062
	Sce-Q50b	0.471	0.004
	Sce-Q50c	0.331	0.004
Q ₁₀₀	Sce-Q100a	0.690	0.004
	Sce-Q100b	1.256	0.184
	Sce-Q100c	1.018	0.127

COMPARISON WITH DIFFERENT METRICS (2)

FSI value assessment of deterministic and stochastic closed-loop MPC according to Flood Control Levels (FCLs) for different inflow conditions with forecast horizon of 48 h.

Flood Condition	Scenarios	Flood Storage Index (FSI)	
		Deterministic MPC	Stochastic MPC
Q ₂₅	Sce-Q25a	0.652	0.800
	Sce-Q25b	0.659	0.990
	Sce-Q25c	0.659	0.796
Q ₅₀	Sce-Q50a	0.566	0.723
	Sce-Q50b	0.598	0.770
	Sce-Q50c	0.606	0.758
Q ₁₀₀	Sce-Q100a	0.457	0.650
	Sce-Q100b	0.463	0.645
	Sce-Q100c	0.456	0.645

$$FSI = \frac{\sum_{k=1}^N v_f^k}{\sum_{k=1}^N v_{FCL}^k}$$

v_f^k → effective flood storage
 v_{FCL}^k → actual volume of the flood control pool
 $v_f^k = \begin{cases} v_{act}^k & \text{if } v^k \leq v_{FCL}^k \\ v_{FCL}^k & \text{if } v^k > v_{FCL}^k \end{cases}$ for $k = 1, 2, \dots, N$
 v^k → current storage
 k → time instant

Uysal et al. (2018b)
 storage corresponds to flood control level

CONCLUSIONS

- **Assessment of forecast uncertainty** is still lack in real time operation of water resources optimization.
- **The operation of multi-purpose dam reservoir** having water supply, flood control targets is tested in a real-time operation against a major flood scenario.
- MPC models are developed to mimic a real-time control via hindcast experiments.
- **Synthetic deterministic and probabilistic hourly streamflows** with 48 hours lead-time are employed in deterministic and stochastic MPC models, respectively.
- Tree-based MPC is selected ***because of including forecast uncertainty consideration*** in the decision system.
- **The preliminary results of TB-MPC are promising** in terms of downstream region safety compared to deterministic MPC without harming water supply targets.
- In the future studies, the developed framework can be tested with numerical weather prediction based forecasts.

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