

# Fractal reconstruction of the subgrid scales in turbulence models in applications to cloud microphysics



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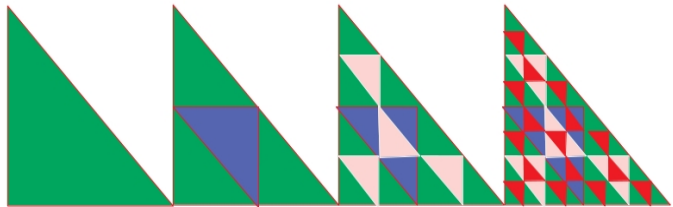
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## What is the fractal interpolation technique (FIT)?



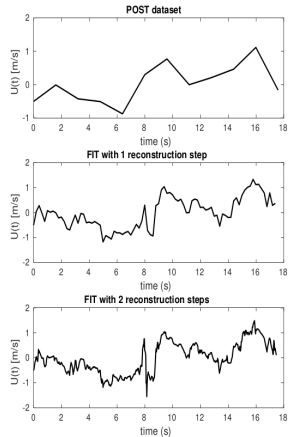
Fractal interpolation is an iterative mapping procedure to construct the synthetic (unknown) small-scale field from its known large-scale structure, assuming self-similarity of the investigated field.



# How the FIT can be applied in turbulence study?



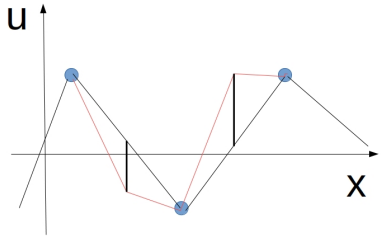
FIT was applied by Scotti & Meneveau [Phys. Rev. Lett. 78, 86, 1997] to synthetically generate subgrid eddies in Large Eddy Simulation and to model their effect on resolved scales.



## Stretching parameters.



A free parameter in the FIT method is the "stretching parameter"  $d$  which controls how the structures are rescaled into each other.



In Scotti & Meneveau (1997)

$$d = \pm 2^{-1/3}$$

# PDF of the stretching parameter in the inertial range is a universal function !

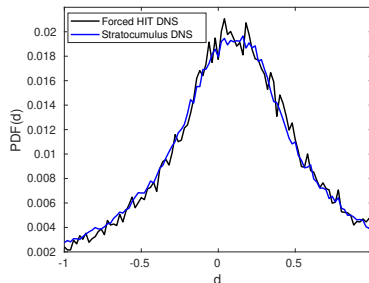


In Akinlabi et al.

[Flow, Turbulence and Combustion 103:293-322 (2019)]

values of stretching parameters were calculated directly from numerical and experimental data of stratocumulus cloud.

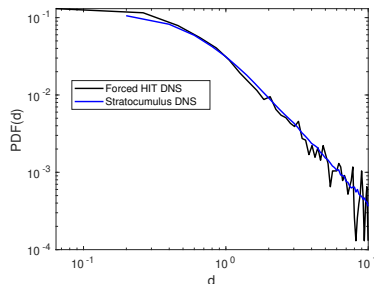
**New result:** comparison with Direct Numerical Simulation (DNS) of the forced isotropic turbulence and for wider range of  $d$  values.



# PDF of the stretching parameter in the inertial range is a universal function !

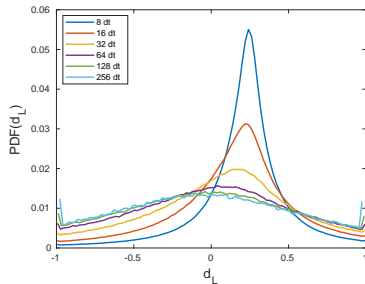
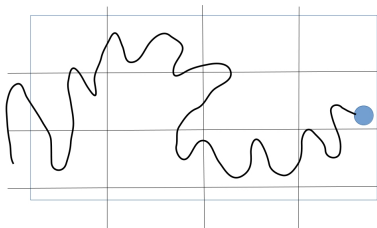
The PDF of the stretching parameter

- is universal and independent of  $Re$
- slightly skewed
- has non-Gaussian tails



# PDF of the stretching parameter along Lagrangian particle tracks.

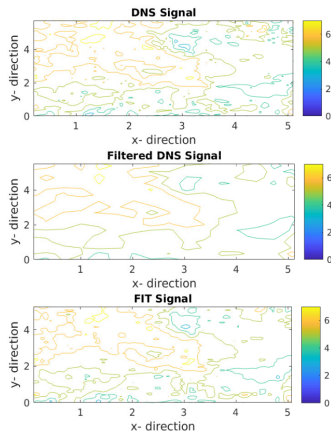
**New result:** Self-similarity of the PDF of the stretching parameter along Lagrangian particle paths in LES.



# Fractal reconstruction of velocity field in stratocumulus cloud

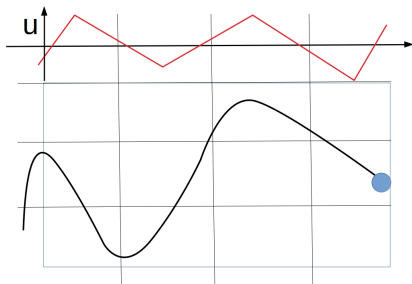


In the improved method the stretching parameters  $d$  are random numbers with prescribed PDF.

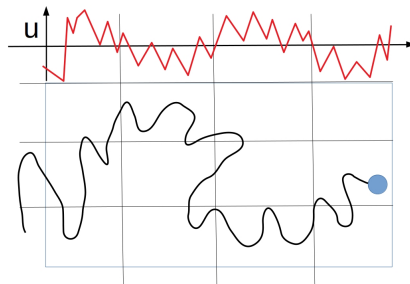




# Tracking of Lagrangian particles in the FIT reconstructed field.

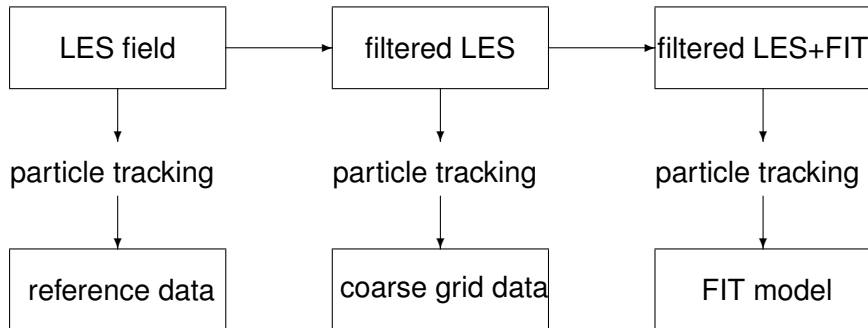


LES field



LES+FIT field

# Tracking of Lagrangian particles in the FIT reconstructed field (LES of stratocumulus cloud)



# Tracking of Lagrangian particles in the FIT reconstructed field (LES of stratocumulus cloud)

Particle equations:

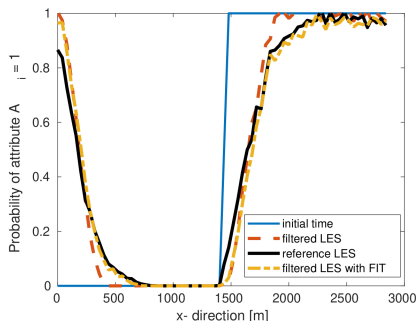
$$d\mathcal{X} = (\mathbf{u}_{LES} + \mathbf{u}'_{FIT}) dt$$

$$d\Theta = 0$$

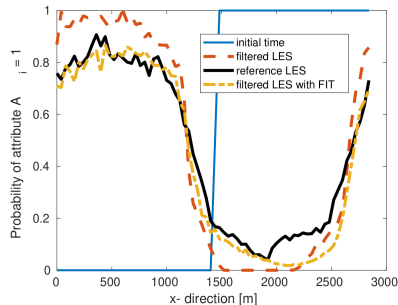
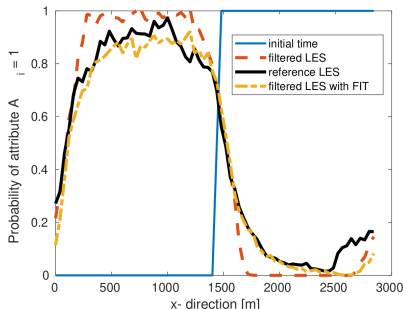
Initial conditions:

$$\Theta = 0 \text{ for } x < L/2$$

$$\Theta = 1 \text{ for } x > L/2$$



# Tracking of Lagrangian particles in the FIT reconstructed field (LES of stratocumulus cloud)



$\Theta$  properties averaged over the x- and y directions in the in-cloud region only at (a) t = 30 minutes (b) t = 60 (c) 90 minutes of simulation time.

## Perspectives



- Particle tracking in high-resolution LES of stratocumulus cloud with FIT
- Fractal reconstruction of the scalar fields (water vapor and potential temperature)
- Coupling with the super-droplet method of Shima et al. [Q. J. R. Meteorol. Soc., 135, 1307-1320, 2009]

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