

On the droplet spectral broadening numerics

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- ▶ super-droplet vs. bin μ -physics
- ▶ spectral broadening numerics:
 - ▶ bin (Eulerian-in-size):
 - numerical diffusion
 - no activation-related attr.
 - ▶ SD (Lagrangian-in-size):
 - spectral sampling issues
 - stiff equations (activation)
 - ▶ general:
 - incorporation of fluctuations

background

- ▶ super-droplet vs. bin μ -physics
- ▶ spectral broadening numerics:
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 - ▶ general:
 - incorporation of fluctuations
- ▶ trigger and focus for today:
Morrison et al. 2018 (bin condensation using MPDATA vs. Lagrangian numerics)

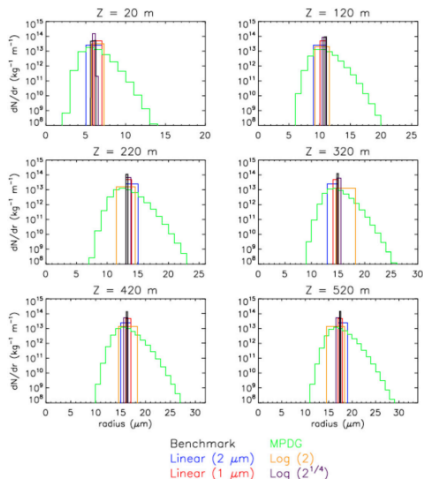


FIG. 7. Drop size distributions at various heights z : from the Lagrangian microphysical benchmark (black) and the bin model simulations (colored lines) for the parcel test with a bulk drop number mixing ratio of 50 mg^{-1} . Different colored lines illustrate results using different bin mass grid configurations and growth methods, as listed in Table 1.

MPDATA & MPyDATA

<https://github.com/atmos-cloud-sim-uj/MPyDATA>

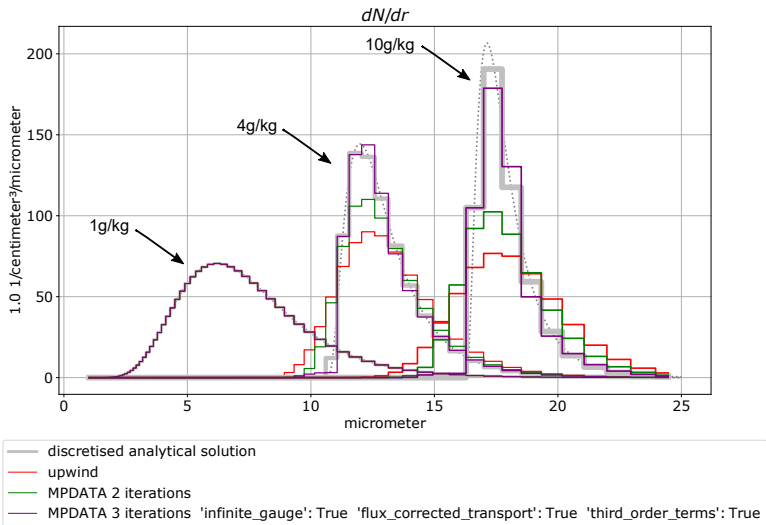
README.md

build passing coverage 70%

MPyDATA

MPyDATA is a high-performance Numba-accelerated Pythonic implementation of the MPDATA algorithm of Smolarkiewicz et al. for numerically solving generalised transport equations - partial differential equations used to model conservation/balance laws, scalar-transport problems, convection-diffusion phenomena (in geophysical fluid dynamics and beyond). As of the current (early) version, MPyDATA supports homogeneous transport in 1D and 2D using structured meshes, optionally generalised by employment of a Jacobian of coordinate transformation. MPyDATA includes implementation of a set of MPDATA **variants** including flux-corrected transport (FCT), infinite-gauge, divergent-flow and third-order-terms options. It also features support for integration of Fickian-terms in advection-diffusion problems using the pseudo-transport velocity approach. No domain-decomposition parallelism supported yet.

$$\partial_t(Gn_p) + \partial_x(\dot{x}Gn_p) = 0, \quad G(r) \equiv \det(Dp(r)/Dx(r)) = \frac{dp}{dx}$$



mass doubling grid: $p = \log_2(r^3)$, and surface-proportional coordinate: $x = r^2$

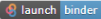
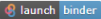
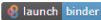


Lessons learned and prospects

- ▶ three-pass infinite gauge variant of MPDATA is a game-changer here
- ▶ proper handling of spectrum coordinate and grid layout matters
- ▶ next steps:
 - convergence analysis with different error measures
 - Lagrangian test case: ripening & fluctuations (PySDM)

Thank you for your attention!

To reproduce above plot (in the cloud) click in the link:
<https://github.com/atmos-cloud-sim-uj/MPyDATA>

MPyDATA ships with several demos that reproduce results from the literature, including:

- [Smolarkiewicz 2006](#) Figs 3,4,10,11 & 12 
(1D homogeneous cases depicting infinite-gauge and flux-corrected transport cases)
- [Arabas & Farhat 2020](#) Figs 1-3 & Tab. 1 
(1D advection-diffusion example based on Black-Scholes equation)
- [Olesik, Bartman et al. 2020](#) (in preparation)  
(1D particle population condensational growth problem with coordinate transformations)
- Molenkamp test (as in [Jaruga et al. 2015](#), Fig. 12) 
(2D solid-body rotation test)