

Space oddity: estimating Earth biodiversity from a satellite

Duccio Rocchini

Alma Mater Studiorum University of Bologna, Italy
Czech University of Life Sciences Prague, Czech Republic



Aim

Showing the most powerful approaches to measure the diversity of life from space.





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Outline

- 1 Information theory
- 2 Solving non-dimensionality
- 3 Solving point description

Information Theory

Reprinted with corrections from *The Bell System Technical Journal*,
Vol. 27, pp. 379–423, 623–656, July, October, 1948.

A Mathematical Theory of Communication

By C. E. SHANNON

INTRODUCTION

THE recent development of various methods of modulation such as PCM and PPM which exchange bandwidth for signal-to-noise ratio has intensified the interest in a general theory of communication. A basis for such a theory is contained in the important papers of Nyquist¹ and Hartley² on this subject. In the present paper we will extend the theory to include a number of new factors, in particular the effect of noise

$$H' = - \sum p_i \times \ln(p_i) \quad (1)$$

Issues

Main issues related to the use of Shannon's H' in remote sensing:

- **Non-dimensionality:** H' is only based on relative abundance and not on numbers, i.e. pixel values
- **Point description:** H' , as many other indices, represents only a part of the whole diversity spectrum

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Distance matrices and relative abundance: the Rao's Q diversity

$$H' = - \sum p_i \times \ln(p_i) \quad (2)$$

Distance matrices and relative abundance: the Rao's Q diversity

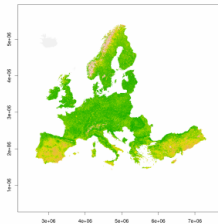
$$H' = - \sum p_i \times \ln(p_i) \quad (2)$$

$$Q = \sum \sum d_{ij} \times p_i \times p_j \quad (3)$$

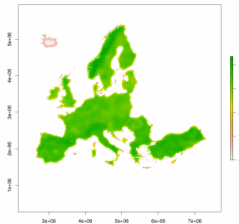
$$\begin{pmatrix} d_{1,1} & d_{1,2} & \cdots & d_{1,n} \\ d_{2,1} & d_{2,2} & \cdots & d_{2,n} \\ \vdots & \vdots & \ddots & \vdots \\ d_{n,1} & d_{n,2} & \cdots & d_{n,n} \end{pmatrix}$$

Rao's Q diversity

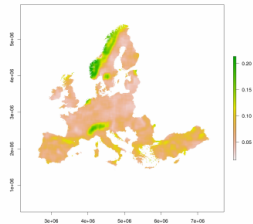
MODIS NDVI image



Shannon's H'



Univariate Rao's Q



Rocchini et al. (Ecol. Indic, 2017)

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Solving point description: the Rényi Generalised Entropy

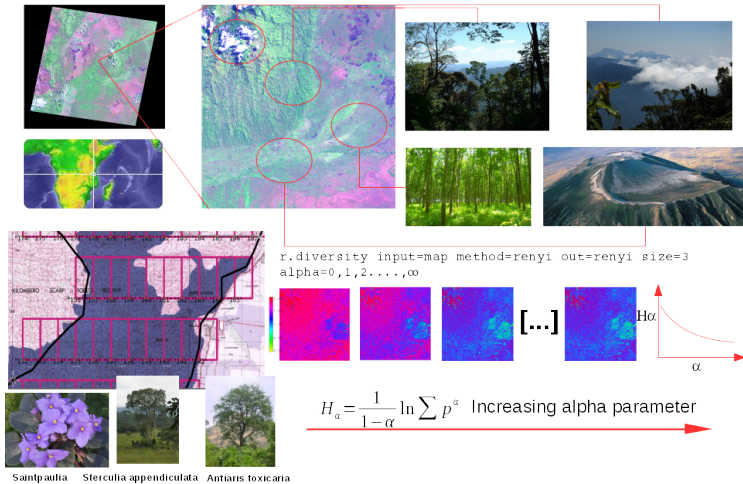
Rényi (1970) generalised entropy:

$$H_{\alpha} = \frac{1}{1-\alpha} \ln \sum p^{\alpha} \quad (4)$$

where p =relative abundance of each spectral reflectance value (DN).
Such measure is extremely flexible and powerful since many popular diversity indices are simply special cases of H_{α} .

$$H_{\alpha} = \begin{cases} \alpha = 0, H_0 = \ln(N) \\ \alpha \rightarrow 1, H_1 = -\sum p \times \ln(p) \\ \alpha = 2, H_2 = \ln(1/D) \end{cases} \quad (5)$$

Solving point description: the Rényi Generalised Entropy



R package: rasterdiv



Package 'rasterdiv'

February 25, 2020

Title rasterdiv Package Version 0.0

Authors Duccio Rocchini, Martina Iannacito, Elisa Thouverai, Giovanni Bacaro, Manuele Bazzichetto, Alessandra Bernardi, Daniele Da Re, Giles M. Foody, Jonathan Lenoir, Marco Malavasi, Matteo Marcantonio, Alessandro Montagni, Vítězslav Moudrý, Carlo Ricotta, Petra Šímová, Clara Tattoni, Enrico Tordoni, Michele Torresani, Saverio Vicario, Martin Wegmann

...

Maintainer Duccio Rocchini<duccio.rocchini@unitn.it>

Many thanks!



ALMA MATER STUDIORUM
UNIVERSITÀ DI BOLOGNA

Contact:

Duccio Rocchini, PhD - Full Professor @:
Alma Mater Studiorum University of Bologna, Italy
duccio.rocchini@unibo.it



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