

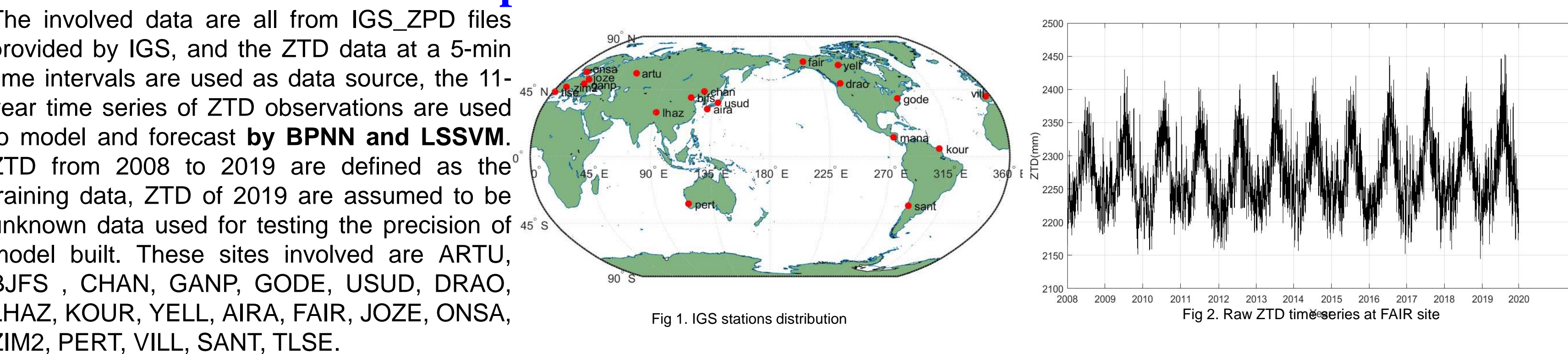
# Zenith Troposphere Delay Prediction based on BP Neural Network and Least Squares Support Vector Machine

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## Abstract

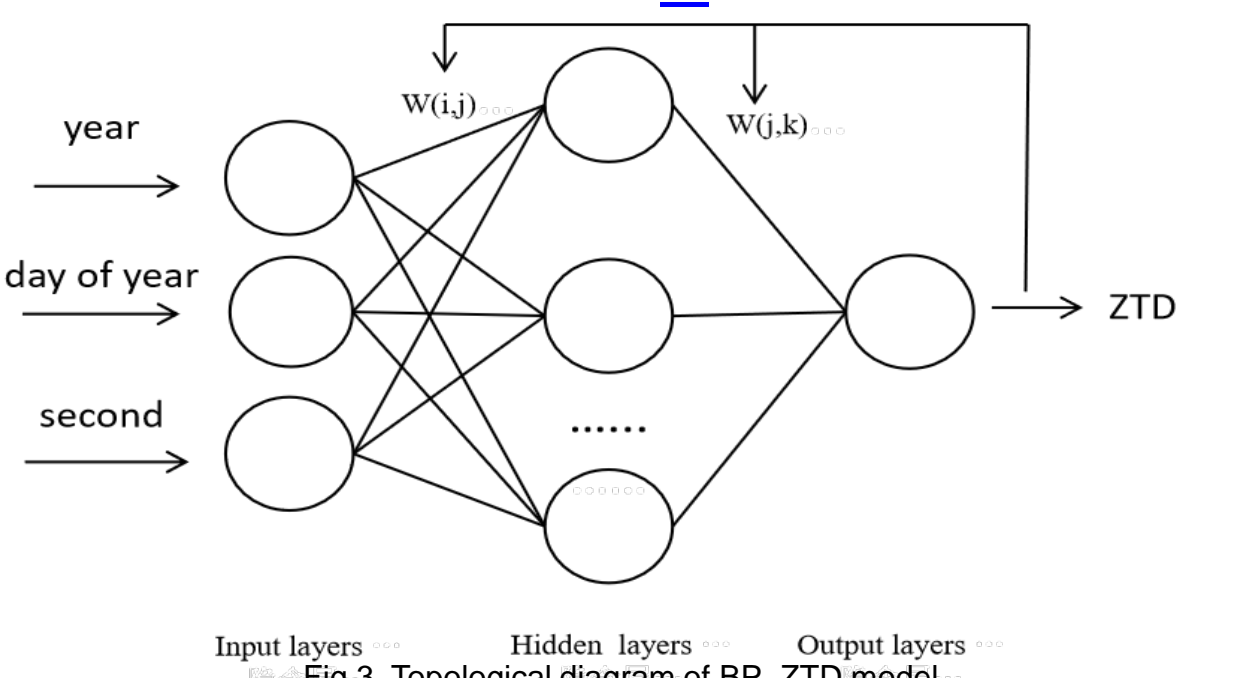
With the rapid development of artificial intelligence, machine learning has become an high-efficient tool applied in the fields of GNSS data analysis and processing, such as troposphere, ionosphere or satellite clock modeling and prediction. In this paper, zenith troposphere delay (ZTD) prediction algorithms based on BP neural network (BPNN) and least squares support vector machine (LSSVM) are proposed in the time and space domain. The main trend terms in ZTD time series are deducted by polynomial fitting, and the remaining residuals are reconstructed and modeled by BPNN and LSSVM algorithm respectively. The test results show that the performance of LSSVM is better than that of BPNN in term of prediction stability and accuracy by using ZTD products of International GNSS Service (IGS) of 20 stations in time domain. In order to further improve LSSVM prediction accuracy, a new strategy of training samples selection based on correlation analysis is proposed. The results show that using the proposed strategy, about 80% to 90% of the 1-hour prediction deviation of LSSVM can reach millimeter level depending on the season, and the percentage of the prediction deviation value less than 5 mm is about 60% to 70%, which is 5% to 20% higher than that of the classical random selection in different month. The mean values of RMSE in all 20 stations using the new strategy are 1-3mm smaller than those of the classical one. Then different prediction span from 1 to 12 hours is conducted to show the performance of the proposed method. Finally, the ZTD predictions based on BPNN and LSSVM in space domain are also verified and compared using GNSS CORS network data of Hong Kong, China.

## Introduction of data and experimental results



- (1) The accuracy of ZTD provided by IGS can reach 4-5mm, with higher precision and large data volume.
- (2) The ZTD time series has obvious annual and semiannual periods, and there are also complicated high-frequency signal that is hard illustrated by special formulas.
- (3) Results of experiments at stations with data integrity over 90% are chosen for analysis, which reflect the relationship between ZTD and time parameters more comprehensively.
- (4) Predictions of FAIR station with the highest data integrity are taken as an example to visualize the experimental results of model.

## Classic model BP\_ZTD



parameter name	Value
Input_train	year, day of year, second (2008-2019)
Output_train	ZTD (2008-2019)
Input_test	year, day of year, second (2019-2020)
Output_test	ZTD (2019-2020)
hiddenum	7
net.divideFcn	'dividerand'
net.layers(1).transferFcn	'tansig'
net.layers(2).transferFcn	'purelin'
net.trainParam.epochs	100
net.trainParam.lr	0.1
net.trainParam.goal	0.001
net.trainParam.max_fail	8

- (1) The classic model BP\_ZTD can well predict ZTD annual period rather than high-frequency signals. It is failed to predict high-frequency signals of the ZTD time series.
- (2) There are lower accuracy of BP\_ZTD model, most of bias range from -50 to 50mm, and the maximum value of bias is more than 100 mm, the average RMSE of eleven sites is around 40mm, the maximum value of RMSE reaches 69 mm, the minimum value closes to 17mm, ZTD can be predicted with the centimeter accuracy by the BP\_ZTD model and about 10 percent of ZTD predictions are viewed as the available..

## References

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## New model LSSVM\_ZTD

The core idea of new model is that historical ZTD are viewed as inputs to make informed estimates that are predictive in determining the direction of future trends, and ZTD of 24 hours before the starting moment of forecasting are considered as historical data, ZTD of few hours after starting moment need to be predicted. There are two sets of simulation experiments to determine two independent variables affecting precision of new model, **strategy for selecting training samples and the time span of prediction.**

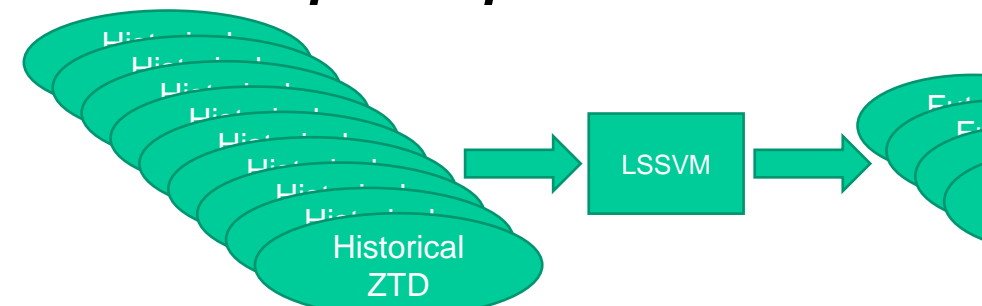


Fig 8. Topological diagram of the LSSVM\_ZTD model

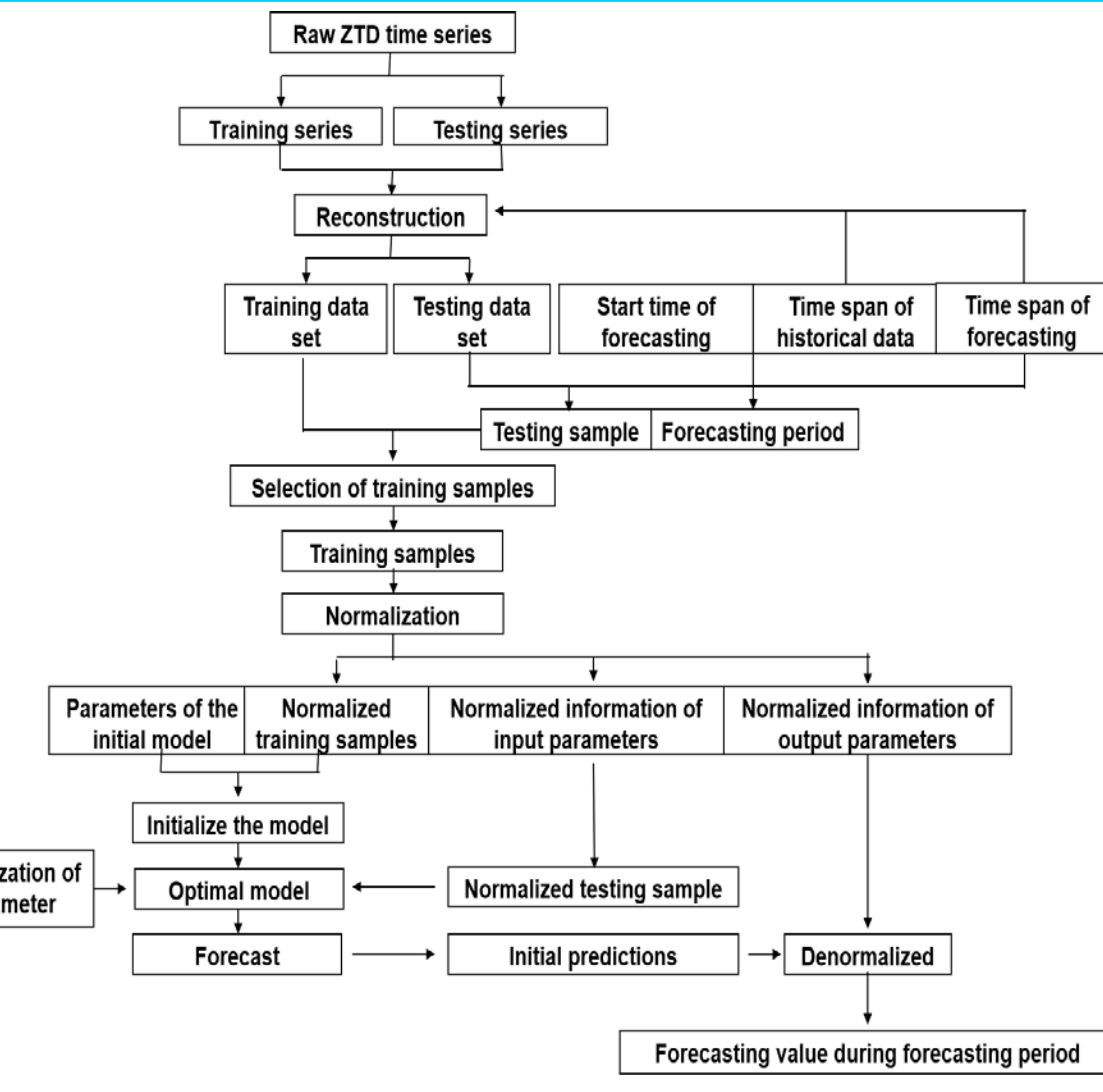


Fig 7. Flow chart of LSSVM\_ZTD model

## New model LSSVM\_ZTD (time span)

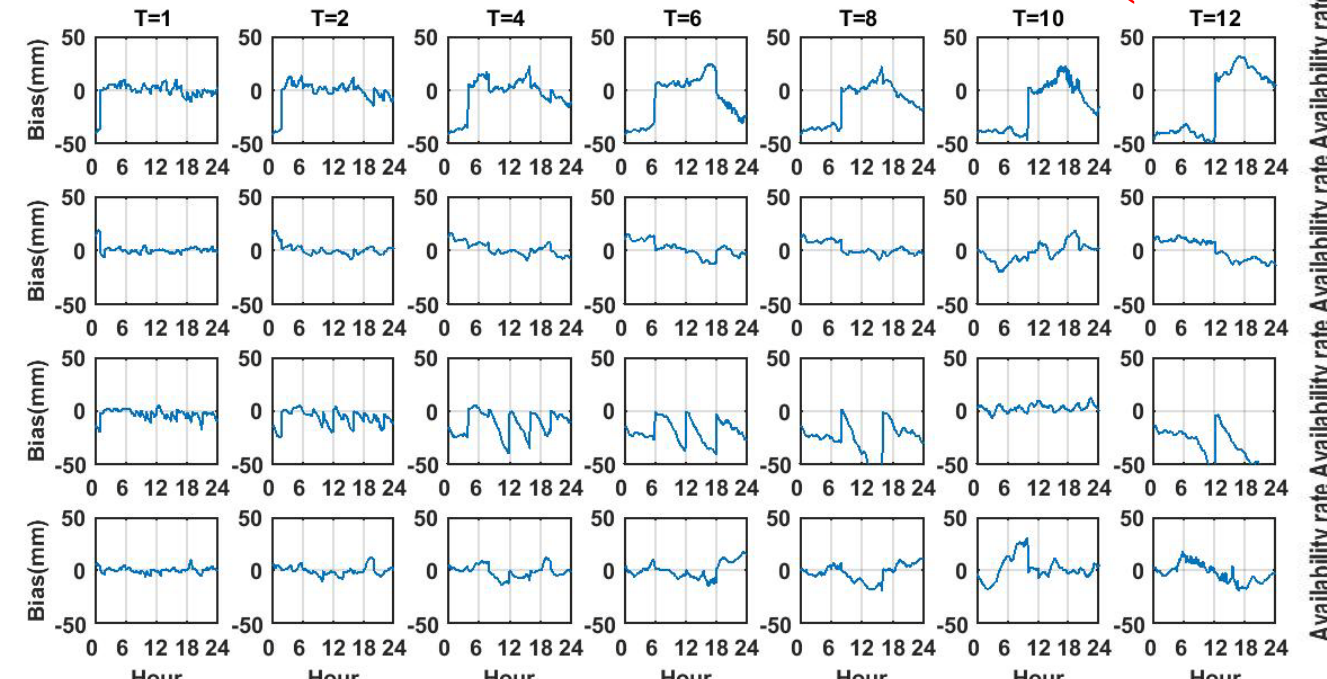


Fig 10. Bias with different span at FAIR station

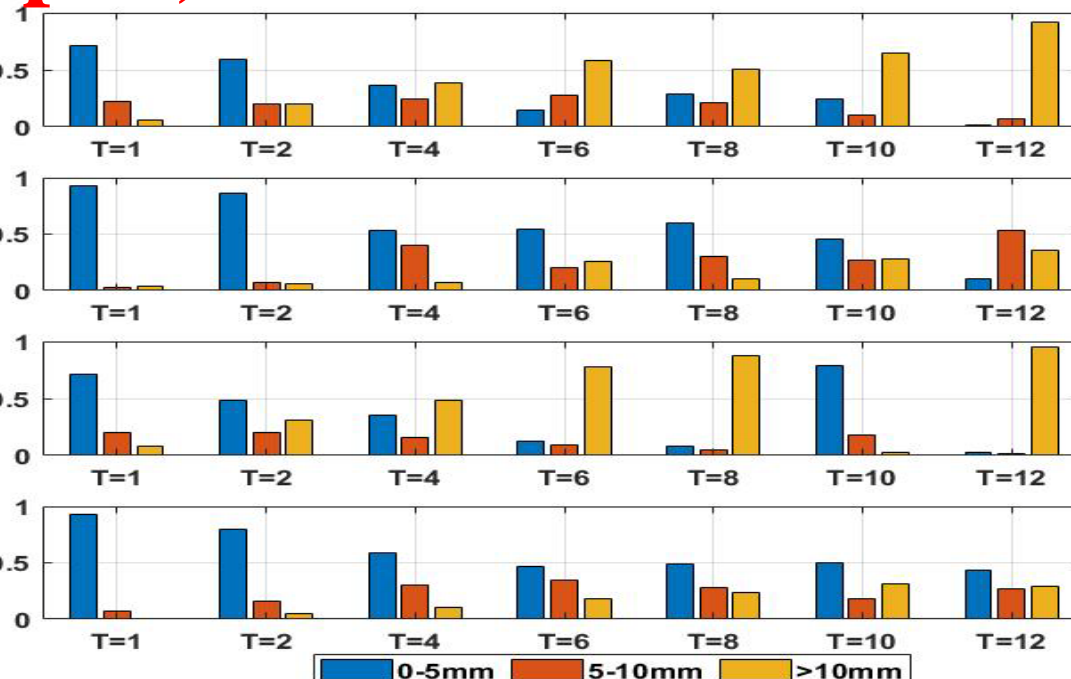


Fig 11. Availability with different span at FAIR station

Month	T=1	T=2	T=4	T=6	T=8	T=10	T=12
12-02	5.35 [0.73,38.96]	8.11 [2.11,39.17]	12.61 [1.61,37.60]	19.35 [5.20,36.36]	17.94 [6.70,36.36]	21.76 [9.75,39.79]	30.03 [18.72,41.34]
03-05	2.40 [0.23,16.13]	3.72 [1.47,13.77]	5.42 [2.43,11.02]	6.51 [2.90,11.17]	5.18 [2.80,9.38]	7.25 [3.01,5.60]	9.31 [30.12,42.03]
06-08	4.43 [0.93,16.35]	8.56 [1.69,21.00]	14.66 [3.48,23.95]	21.18 [16.66,26.40]	28.49 [18.90,41.97]	4.35 [3.80,16.26]	36.07 [6.79,10.31]
09-11	2.21 [0.60,6.32]	3.62 [1.42,9.11]	5.38 [2.28,9.11]	6.72 [3.65,11.15]	8.32 [3.67,11.92]	8.02 [3.80,16.26]	8.55 [6.79,10.31]
mean	3.60	6.00	9.52	13.44	14.73	10.34	20.99

## New model LSSVM\_ZTD (comparison of different models)

Based on the conclusions of the above two simulation studies, the new model LSSVM\_ZTD with training samples having high correlation with testing samples for modeling (strategy 2) and two-hour time span of forecasting are built, by which we can predict ZTD of any sites at any consecutive two hours (in unit of whole hour) as long as we know the 24-hour historical ZTD immediately before the beginning moment of forecasting and the ZTD data of this station for the past few years. 30-day result are obtained through loop constructing many LSSVM\_ZTD models for different testing samples.

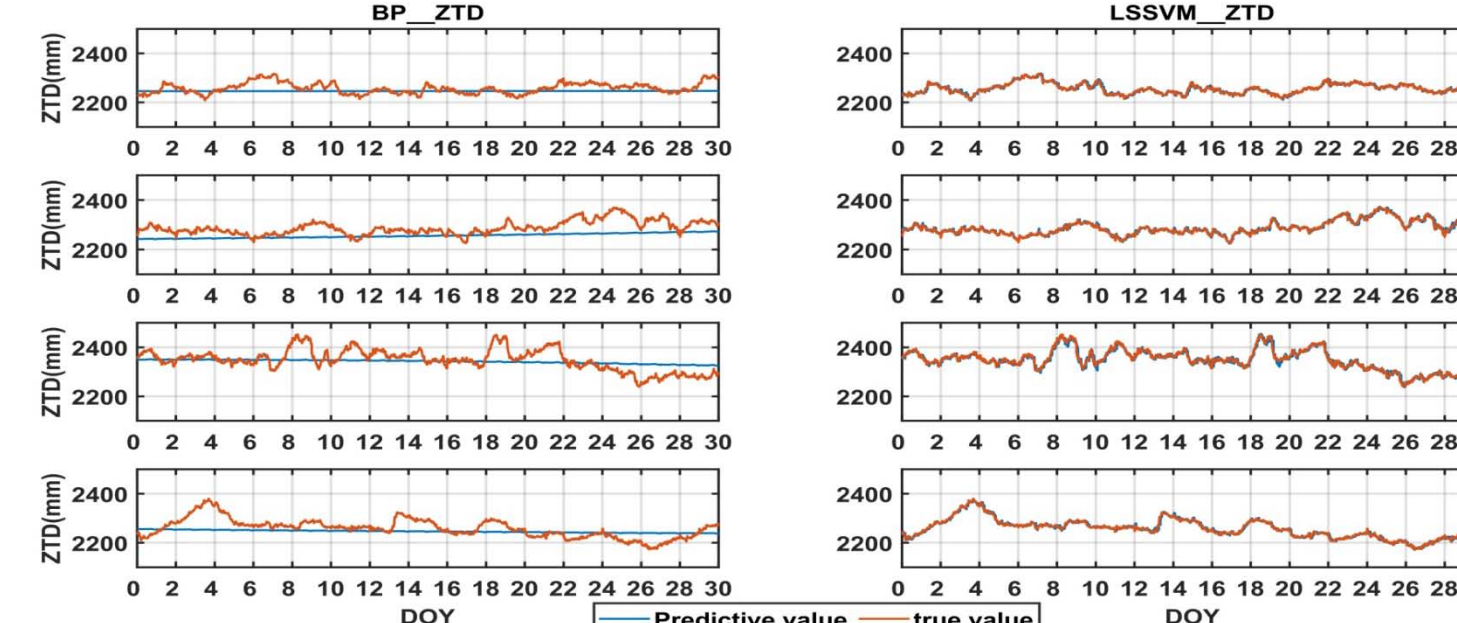


Fig 12. Forecast results of BP\_ZTD and LSSVM\_ZTD at FAIR station

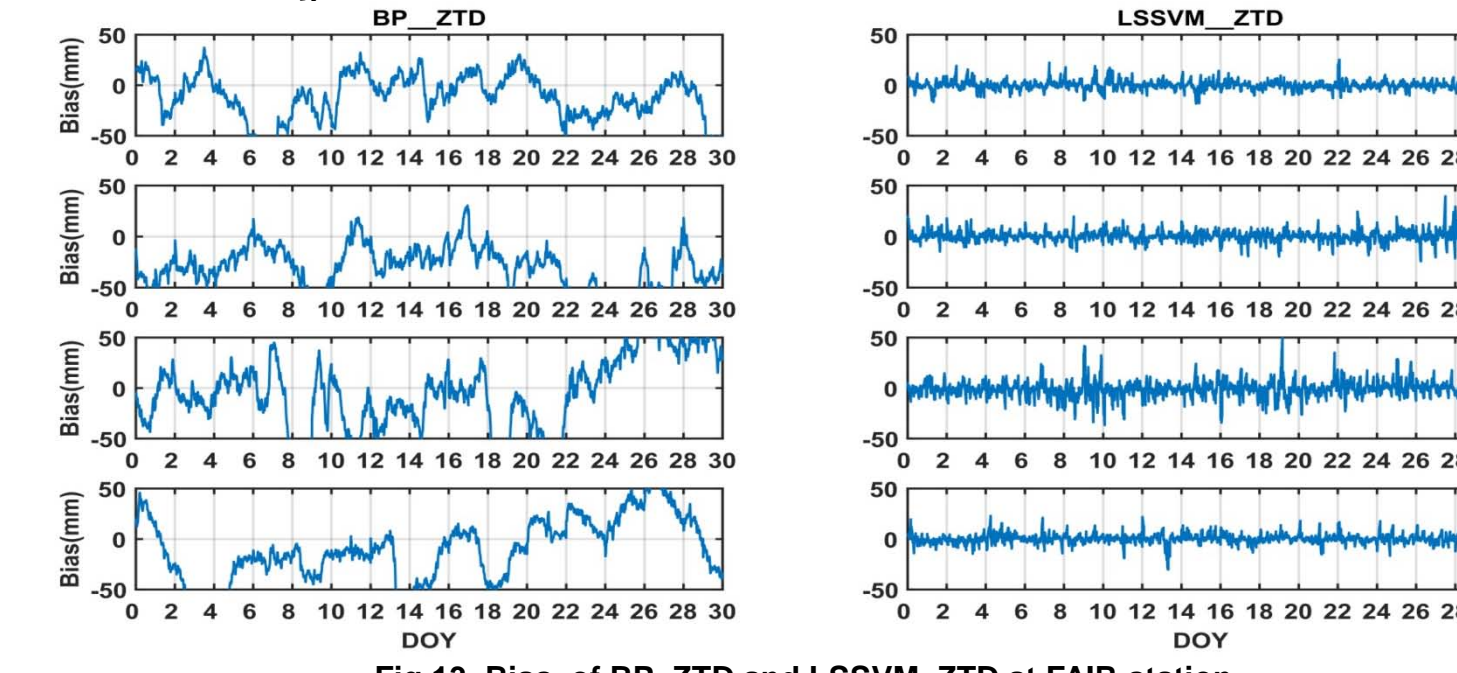


Fig 13. Bias of BP\_ZTD and LSSVM\_ZTD at FAIR station

## Conclusions

- (1) The prediction accuracy of classic model BP\_ZTD is at the centimeter level.
- (2) The prediction accuracy of the new model LSSVM\_ZTD is an order of magnitude higher than that of the classic model BP\_ZTD.
- (3) LSSVM\_ZTD with selecting the training samples by correlation analysis can further improve the prediction accuracy.

## Acknowledgements

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## New model LSSVM\_ZTD (strategy)

**Strategy 1:** randomly select ZTD in consecutive periods to form set  $\{x_{train,i}, y_{train,i}\}$ . **Strategy 2:** choose training samples that are more relevant to the testing sample, which means that  $x_{train,i}$  with smaller euclidean distance from the testing sample  $x_{test,i}$ . Take consideration of the fact that the further out the forecast, the higher the chance that the estimate will be inaccurate, the time span  $T$  are fixed as **one hour** When determining strategies.

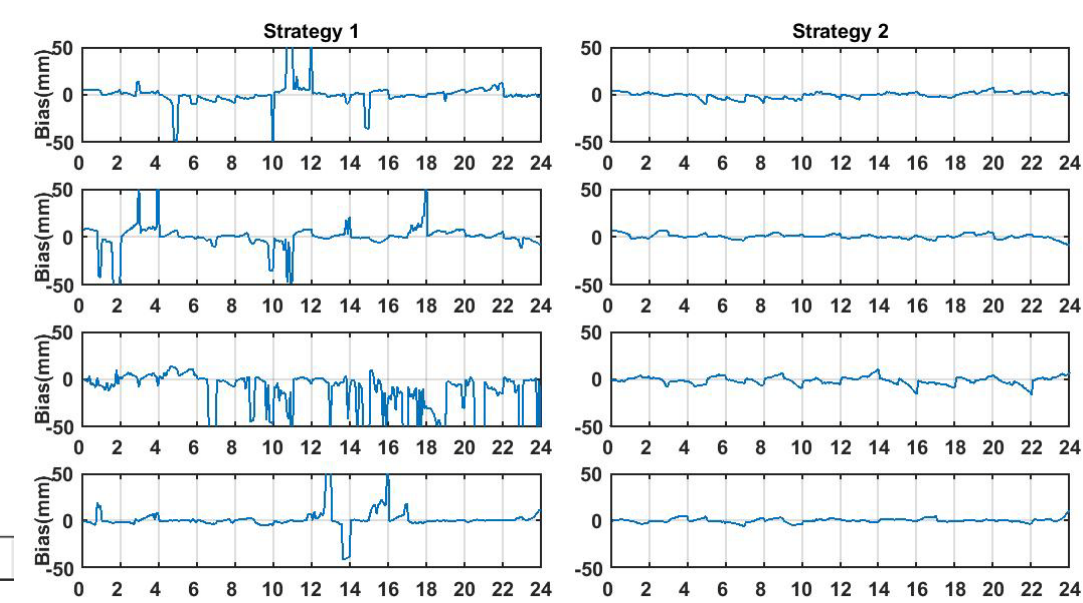


Fig 9. Bias of different strategies at FAIR station

Station	strategy 1		strategy 2	
	Availability rate	RMSE (mm)	Availability rate	RMSE (mm)
GODE	29.17%	46.81	57.29%	4.23
USUD	58.33%	29.83	76.04%	4.74
DRAO	78.13%	7.72	88.54%	2.56
LHAZ	59.03%	15.91	92.01%	2.45
YELL	80.90%	9.41	93.40%	3.28
AIRA	68.75%	25.56	77.08%	4.06
FAIR	83.68%	13.11	97.22%	2.59
JOZE	67.01%	15.64	76.04%	4.23
MANA	65.63%	18.40	69.44%	3.83
ONSA	47.92%	22.50	63.89%	3.85
VILL	56.25%	16.80	78.47%	4.07
mean	63.16%	20.15	79.04%	3.63

Table 4. RMSE with different strategies at different stations

Table 3. RMSE with different strategies at FAIR station			
month	strategy 1	strategy 2	
12-02	7.85 [1.41,37.91]	2.63 [0.52,6.47]	
03-05	9.48 [0.51,37.51]	2.10 [0.31,6.05]	
06-08	26.62 [1.90,113.59]	3.84 [0.87,9.59]	
09-11	6.49 [0.39,45.79]	1.79 [0.38,4.93]	
mean	13.11	2.59	

- (1) The accuracy of model built with strategy 2 is higher than that of model with strategy 1, among them, the average availability rate of eleven IGS stations increased by 15.88%, and the average RMSE decreased by 16.52mm.

Station	Table 6. Availability and RMSE with different duration of different stations (mm)											
	T=1	T=2	T=4	T=6	T=8	T=10	T=12	T=1	T=2	T=4	T=6	T=8
GODE	3.87	79.70%	7.07	60.40%	12.65	34.90%	18.77	38.80%	23.34	23.60%	15.20	27.00%
USUD	5.23	70.20%	9.50	52.00%	11.58	46.40%	15.99	39.30%	17.03	35.70%	16.99	22.40%
DRAO	3.76	77.50%	6.20	60.80%	8.71	43.50%	8.62	47.10%	10.33	37.90%	8.77	47.70%
LHAZ	2.77	88.40%	4.56	70.60%	6.57	55.00%	7.09	60.60%	8.97	44.50%	9.85	51.90%
YELL	3.45	81.80%	5.83	60.90%	8.66	48.20%	10.86	38.80%	11.36	40.10%	19.88	21.50%
AIRA	8.53	61.70%	14.67	36.30%	23.64	25.60%	30.20	17.10%	34.15	16.60%	13.93	33.20%
FAIR	3.60	82.30%	6.00	68.50%	9.52	46.00%	13.44	32.10%	14.73	36.40%	10.34	49.90%
JOZE	4.25	73.80%	6.55	63.50%	7.96	55.90%	12.80	53.90%	18.42	43.00%	13.98	37.80%
MANA	4.21	74.70%	6.41	57.00%	10.04	44.10%	11.62	39.70%	17.58	30.30%	18.08	29.30%
ONSA	2.86	87.00%	4.84	71.80%	8.11	49.80%	10.69	47.80%	14.61	37.60%	13.41	26.40%
VILL	3.74	78.50%	6.47	61.10%	8.52	48.70%	15.20	20.90%	13.41	36.00%	10.71	33.20%
mean	4.20	77.80%	7.10	60.30%	10.54	45.30%	14.12	39.60%	16.72	34.70%	13.74	34.60%

- according to the last experiment, the training samples more relevant to the testing sample are selected (strategy 1).
- (1) The forecasting accuracy of model decreases with the increase of forecasting span, when span is two hours, the average RMSE of eleven stations closes to 7mm, and the average availability rate is above 60%.

Table 7. RMSE with different models at FAIR station (mm)				Table 8. Result with different models at different stations				Table 9. Efficiency with different models at different stations			
Month	BP_ZTD	LSSVM_ZTD		Station	BP_ZTD	LSSVM_ZTD		Station	BP_ZTD	LSSVM_ZTD	
12-02	24.59	3.66 [0.62, 22.40]	GODE	7.55%	57.4	55.67%	7.81	GODE	73.48	105.71	
03-05	39.50	4.38 [0.45, 26.69]	USUD	8.42%	35.88	57.40%	7.14	USUD	73.69	106.05	
06-08	39.54	6.35 [0.92, 37.93]	DRAO	14.20%	29.52	71.08%	4.75	DRAO	35.81	108.54	
09-11	37.36	3.78 [0.59, 24.39]	LHAZ	20.65%	17.82	74.11%	4.33	LHAZ	54.41	106.67	
mean	35.25	4.54	YELL	18.02%	22.62	76.57%	4.20	YELL	73.99	106.02	
			AIRA	4.50%	61.45	50.46%	8.24	AIRA	72.18	103.11	
			FAIR	10.49%	35.25	73.22%	4.54	FAIR	74.22	104.76	
			JOZE	9.69%	34.81	59.75%	6.29	JOZE	71.02	110.37	
			MANA	8.65%	37.91	53.22%	7.72	MANA	69.89	108.13	
			ONSA	14.99%	35.79	67.38%	5.54	ONSA	73.90	107.05	
			VILL	10.29%	34.30	64.37%	5.86	VILL	73.83	105.15	
			mean	11.59%	36.61	63.93%	6.04	mean	67.66	106.51	

Fig 15. RMSE of different LSSVM\_ZTD models at FAIR station

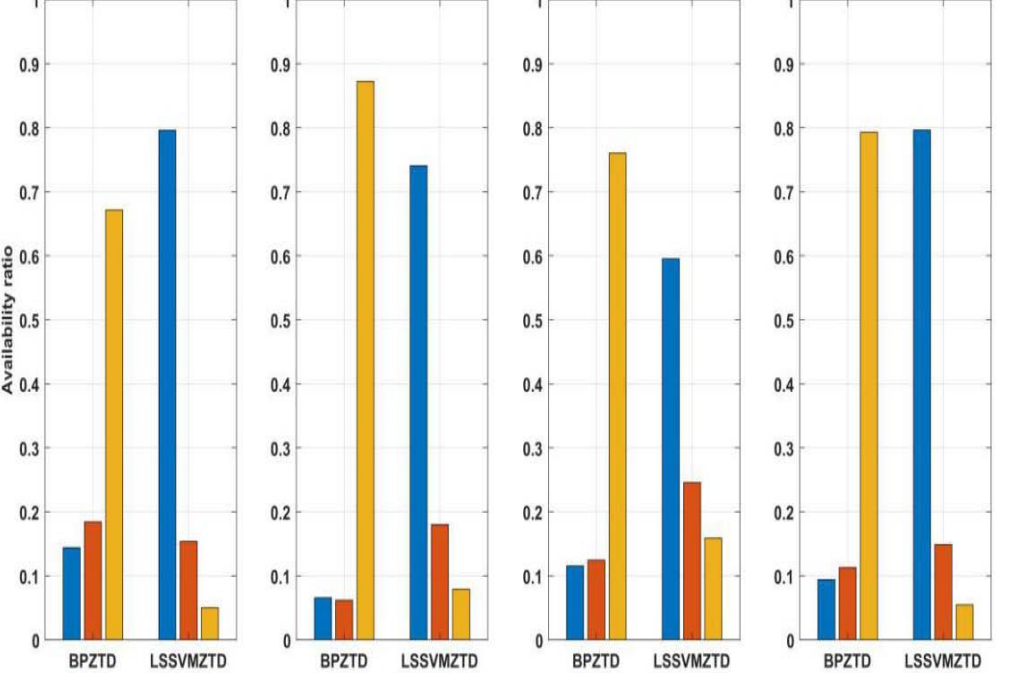


Fig 14. Availability of BP\_ZTD and LSSVM\_ZTD at FAIR station