



Development of a global geoid model 2020 (GGM2020)

WenBin Shen^{1,2}, Youchao Xie¹,
Jiancheng Han, Jiancheng Li¹

1. Dept. of Geophysics, School of Geodesy and Geomatics / Key Lab. of Geospace Environment and Geodesy, Wuhan University, China
2. State Key Lab. of Information Engineering in Surveying, Mapping and Remote Sensing, Wuhan University, China

1 Methodology

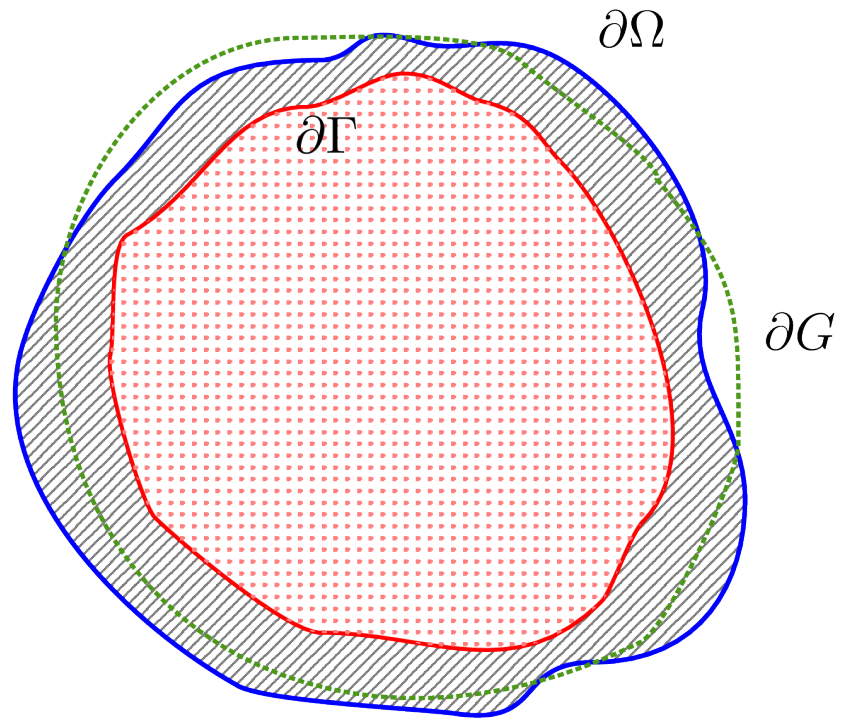


Fig 1 Definition of the shallow layer

Method (Shen 2006)

$$W(P) = V(P) + Q(P)$$

● Earth surface $\partial\Omega$

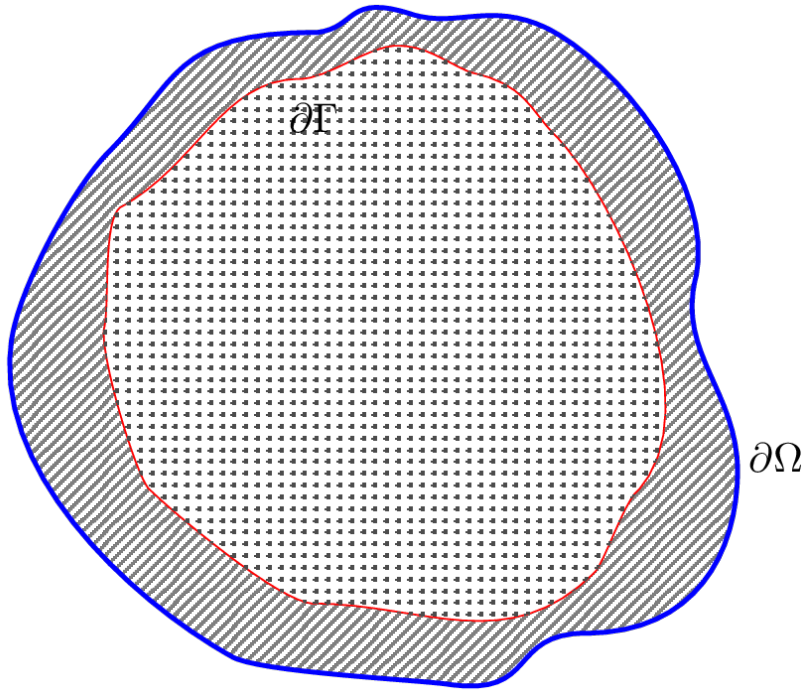
● Geoid ∂G

● Inner surface $\partial\Gamma$

Shallow-layer: the layer
bounded by $\partial\Gamma$ and $\partial\Omega$

1 Methodology

Gravitational potential $V(P)$: defined outside the Earth's surface $\partial\Omega$



$$M \rightarrow V(P)$$

$$M_0 \rightarrow V_0(P)$$

$$M_1 \rightarrow V_1(P)$$

$$V(P) = V_0(P) + V_1(P)$$

Fig 2 Two parts separated from the earth

1 Methodology

Calculation process

- i. Gravitational potential of shallow layer

$$V_1(P) = G \int_{\bar{\Gamma}-\bar{\Omega}} \frac{\rho_1}{l} d\tau, \quad P \in \bar{\Gamma}$$

- ii. Gravitational potential of the mass bounded by surface $\partial\Gamma$

$$V_0(P) = V(P) - V_1(P), \quad P \in \bar{\Omega}$$

- iii. Gravity field recovery, $V_0^*(P)$

Fictitious compress recovery approach (Shen, 2004)

Spherical harmonic analysis (SHA)

1 Methodology

iv. Gravitational potential produced by Earth in the region outside the surface $\partial\Gamma$

$$V^*(P) = V_0^*(P) + V_1(P)$$

v. Gravity potential of the Earth

$$W^*(P) = V^*(P) + Q(P)$$

vi. Solve geoid equation to determine point P , which defines the geoid (W_0 is the geopotential on the geoid)

$$W^*(P) = V^*(P) + Q(P) = W_0$$

2 Data & modeling

Construct 3D shallow-layer model

(1) upper surface

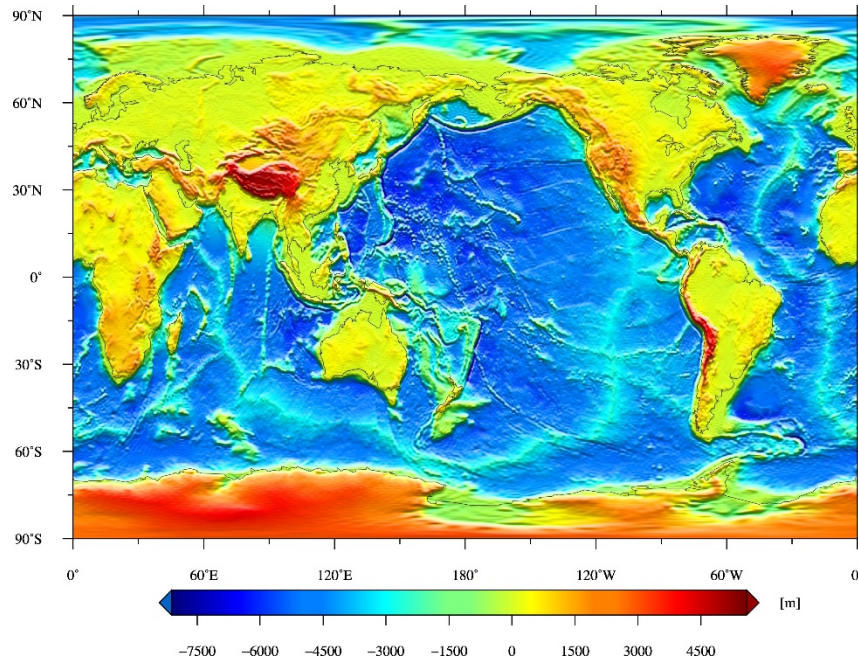


Fig 3 . land: DTM2006.0

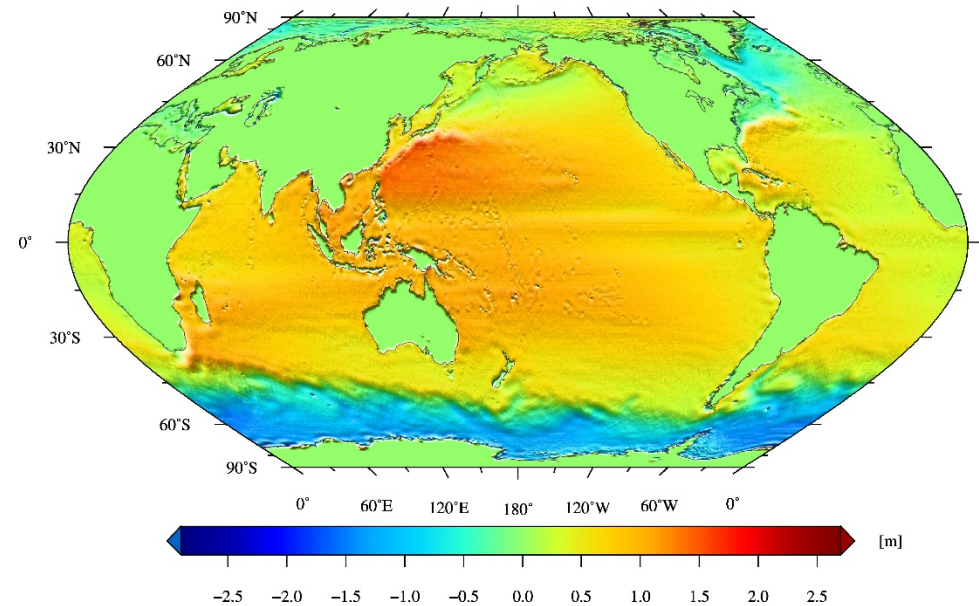


Fig 4 . Ocean: DNSC08

(2) Lower surface: extending from the EGM2008 geoid downward to a depth of 15 m

2 Data & modeling

3D shallow-layer body density: (3) CRUST2.0/1.0 model

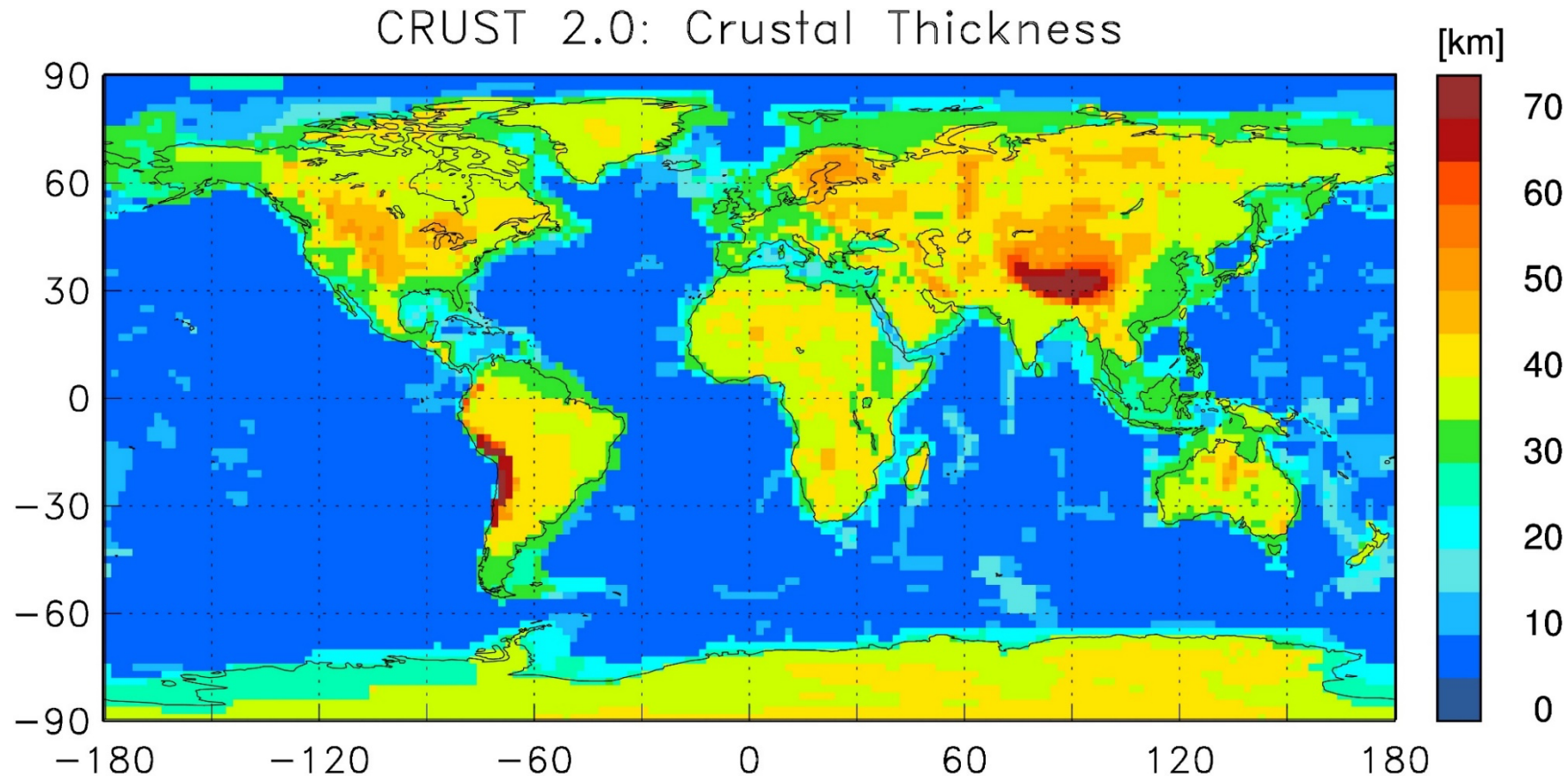
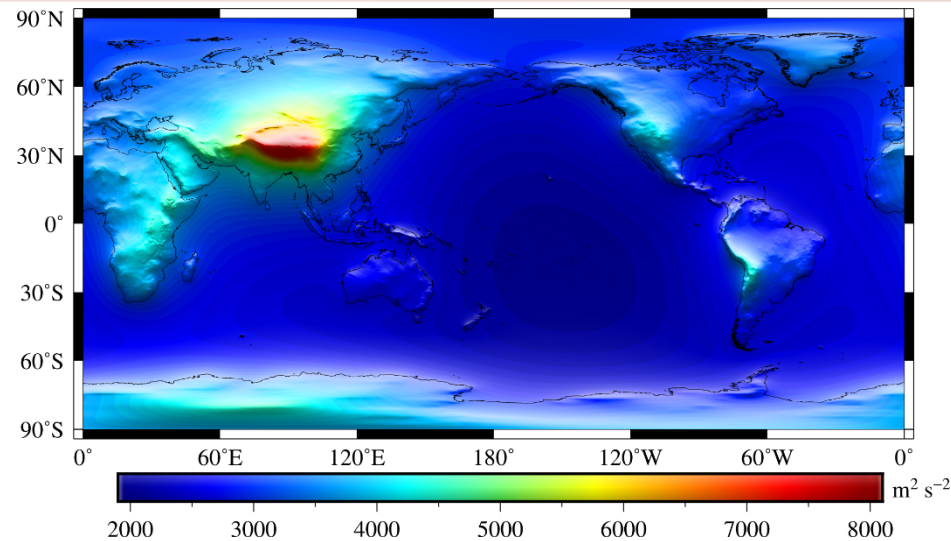
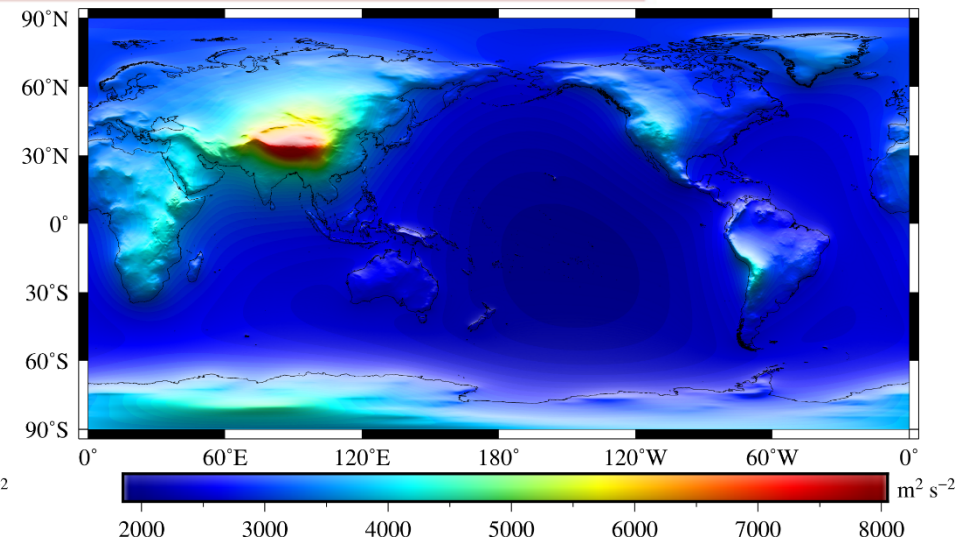


Fig 5 . Global crustal thickness from CRUST2.0

2 Results & validations



(a)



(b)

Fig 6 Gravitational potential of shallow-layer $V_1(P)$ ($R=6386$ km), $V_1(P)$ is based on (a) Crust 1.0 , or (b) Crust 2.0 , unit: **meters**

	Max	Min	Mean	STD
$V_1(P)$ (crust1.0)	8027.96	1908.8	2870.5	740.79
$V_1(P)$ (crust2.0)	7851.07	1866.29	2820.28	729.34

2 Results & validations

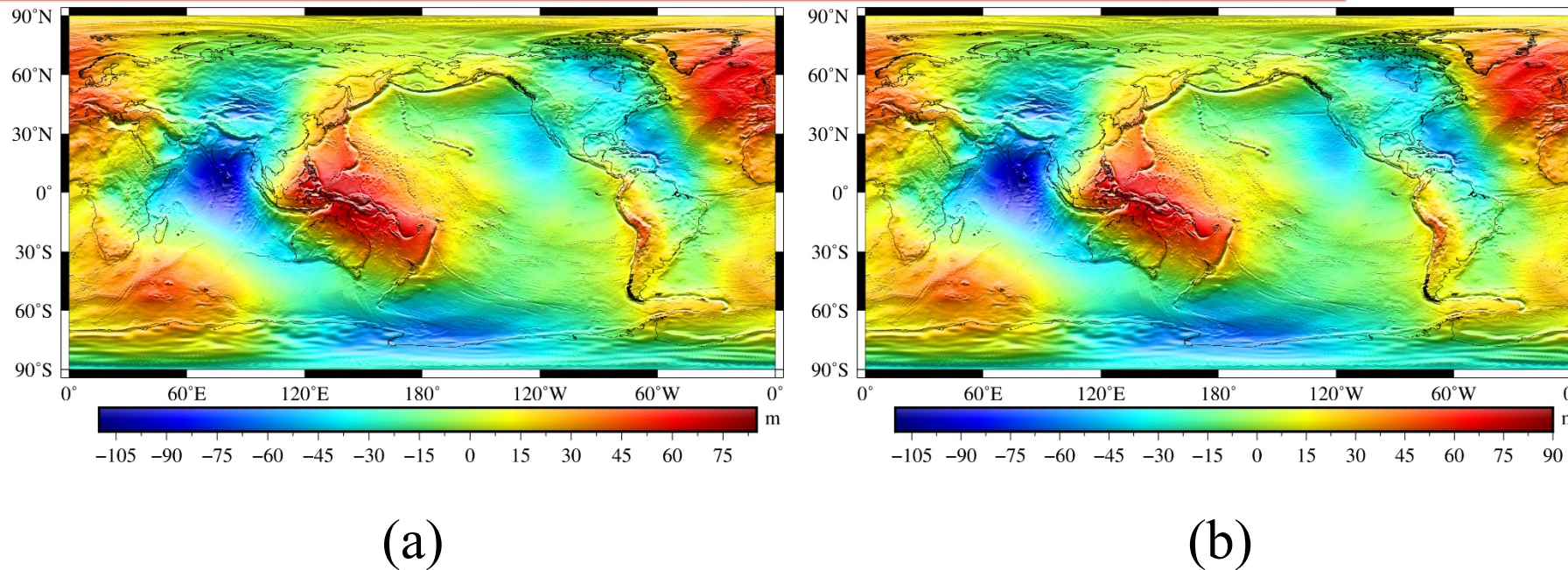
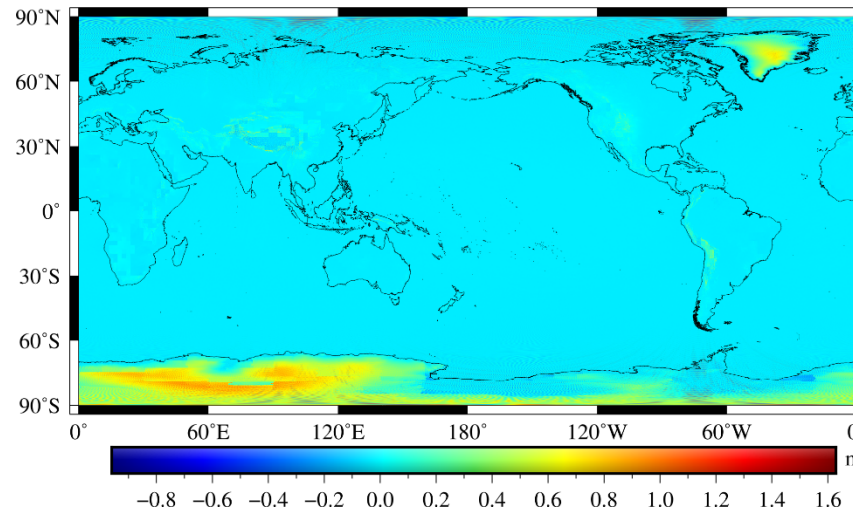


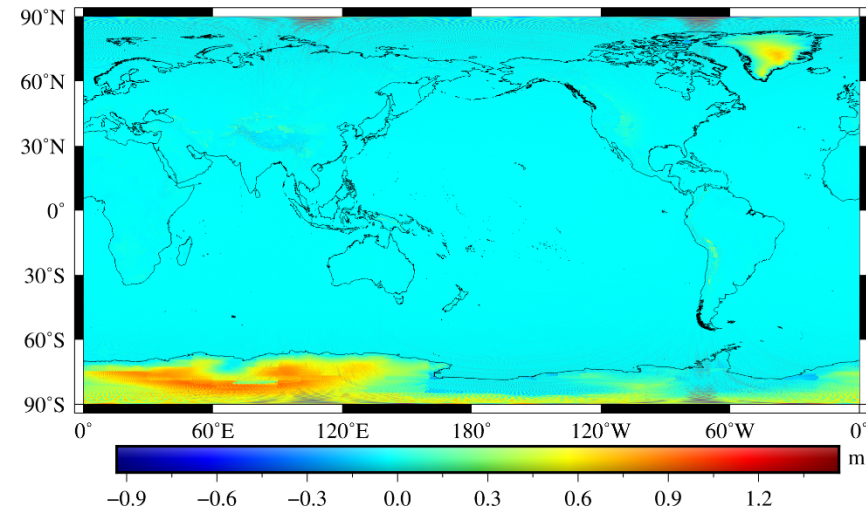
Fig 7 The calculated 5' × 5' global geoid (GGM2020), based on (a) Crust 1.0 , or (b) Crust 2.0 , unit: meters

	Max	Min	Mean	STD
<i>GGM2020</i> (crust1.0)	86.082	-106.93	-1.311	29.131
<i>GGM2020</i> (crust2.0)	86.186	-106.93	-1.310	29.130

2 Results & validations



(a)



(b)

Fig 8 Differences between GGM2020 and EGM2008 geoid. GGM2020 is based on (a) Crust 1.0 , or (b) Crust 2.0, unit: meters

	Max	Min	Mean	STD	RMS
GGM2020 (crust1.0)-EGM2008	1.467	-0.935	0.0058	0.1531	0.1532
GGM2020 (crust2.0)-EGM2008	1.630	-0.960	0.0063	0.150	0.1510

2 Results & validations

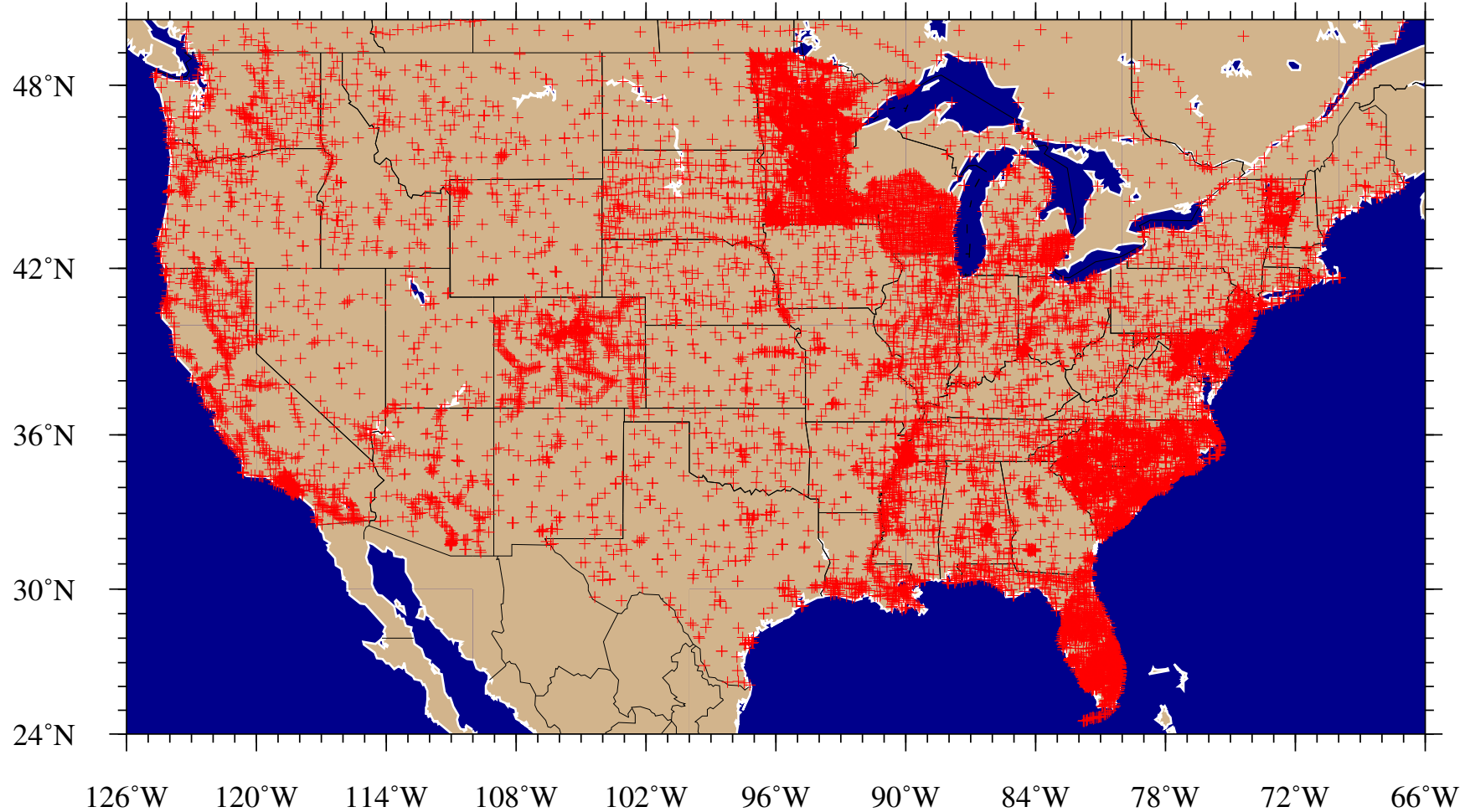


Fig 9 GPS leveling benchmarks in the USA (18972 points)

2 Results & validations

Statistics of differences between selected geoid models and GPSBM (GBM) in the US for all points, All units are in **meters**

USA (all)	Max	Min	Mean	STD	RMS
GPS leveling – E08GG	0.184	-1.321	-0.5144	0.3072	0.599
GPS leveling – GGM2020 (CRUST 1.0)	0.216	-1.307	-0.482	0.3071	0.571
GPS leveling – GGM2020 (CRUST 2.0)	0.216	-1.311	-0.485	0.3092	0.575

2 Results & validations

USA(low-lying , <300 m)	Max	Min	Mean	STD	RMS
GPS leveling – E08GG	0.183	-1.299	-0.359	0.272	0.451
GPS leveling – GGM2020 (CRUST 1.0)	0.216	-1.290	-0.326	0.271	0.424
GPS leveling – GGM2020 (CRUST 2.0)	0.216	-1.284	-0.326	0.271	0.425
USA(mountainous , 300- 3700 m)	Max	Min	Mean	STD	RMS
GPS leveling – E08GG	-0.144	-1.299	-0.709	0.239	0.748
GPS leveling – GGM2019 (CRUST 1.0)	-0.104	-1.307	-0.686	0.238	0.726
GPS leveling – GGM2019 (CRUST 2.0)	-0.116	-1.312	-0.706	0.235	0.744

3 Conclusions

- A $5' \times 5'$ global geoid, GGM2020, has been established based on the shallow-layer method (Shen 2006)
- Validations show that GGM2020 fits the GPSBMs better than the EGM2008 geoid in the US



Thanks