

# Modeling Catchment Scale Nitrate Export using the StorAge Selection Functions

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➤ *Water age & solute dynamics at the catchment scale*

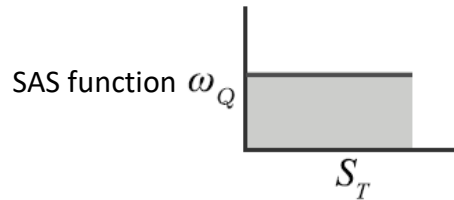
- Catchments store and release water of different ages.
- The age of a water parcel has big implications for understanding flow and transport mechanisms (Botter et al., 2011; Sprenger et al., 2019).
- The water-age based concept, the formulation of transport by transit time distributions (TTDs), has been emerging as a useful tool for understanding catchment-scale solute export (Sprenger et al., 2019).

➤ *Formulation of transport by transit time distributions*

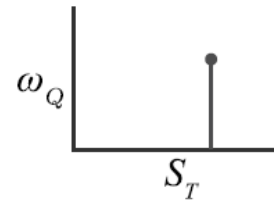
- TTD-based models have been used to explore solute export at the catchment scale, including nitrogen legacy (Ilampooranan et al., 2019; van Meter et al., 2018; 2017).
- These models assume that TTDs are time-invariant.
- Experimental data and numerical studies have indicated that TTDs (e.g., for discharge) are time-variant for many hydrological systems (Yang et al., 2018a; Kaandorp et al., 2018; Rodriguez et al., 2018; Kim et al., 2016; van der Velde et al., 2012).

➤ *Formulation of transport with SAS-based approach*

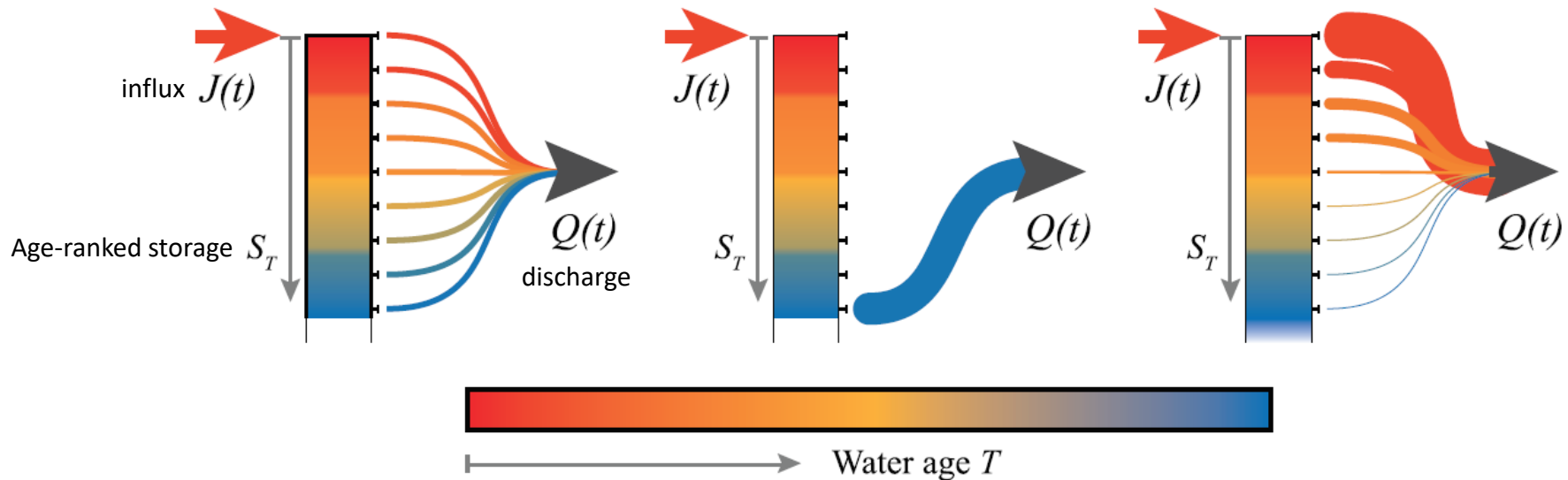
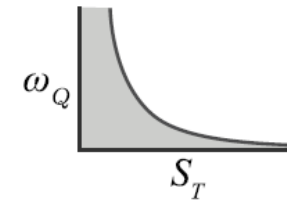
A - Uniform



B - Dirac delta



C - Gamma



Concept of the SAS-based approach (Harman et al., 2015)

➤ *Formulation of transport with SAS-based approach*

- StorAge Selection (SAS) function is a transformed TTD function.
- SAS functions have a clearer physical meaning and are more stable in time, easier for parameterization than TTDs (van der Velde et al., 2012)
- SAS functions could be combined with storage-discharge functions to provide a coherent framework for describing both velocity and celerity transport mechanisms (Harman et al., 2019; Hrachowitz et al., 2016)

*Spatial heterogeneity of catchment characteristics and large scale testing have not been addressed with the SAS-based model.*

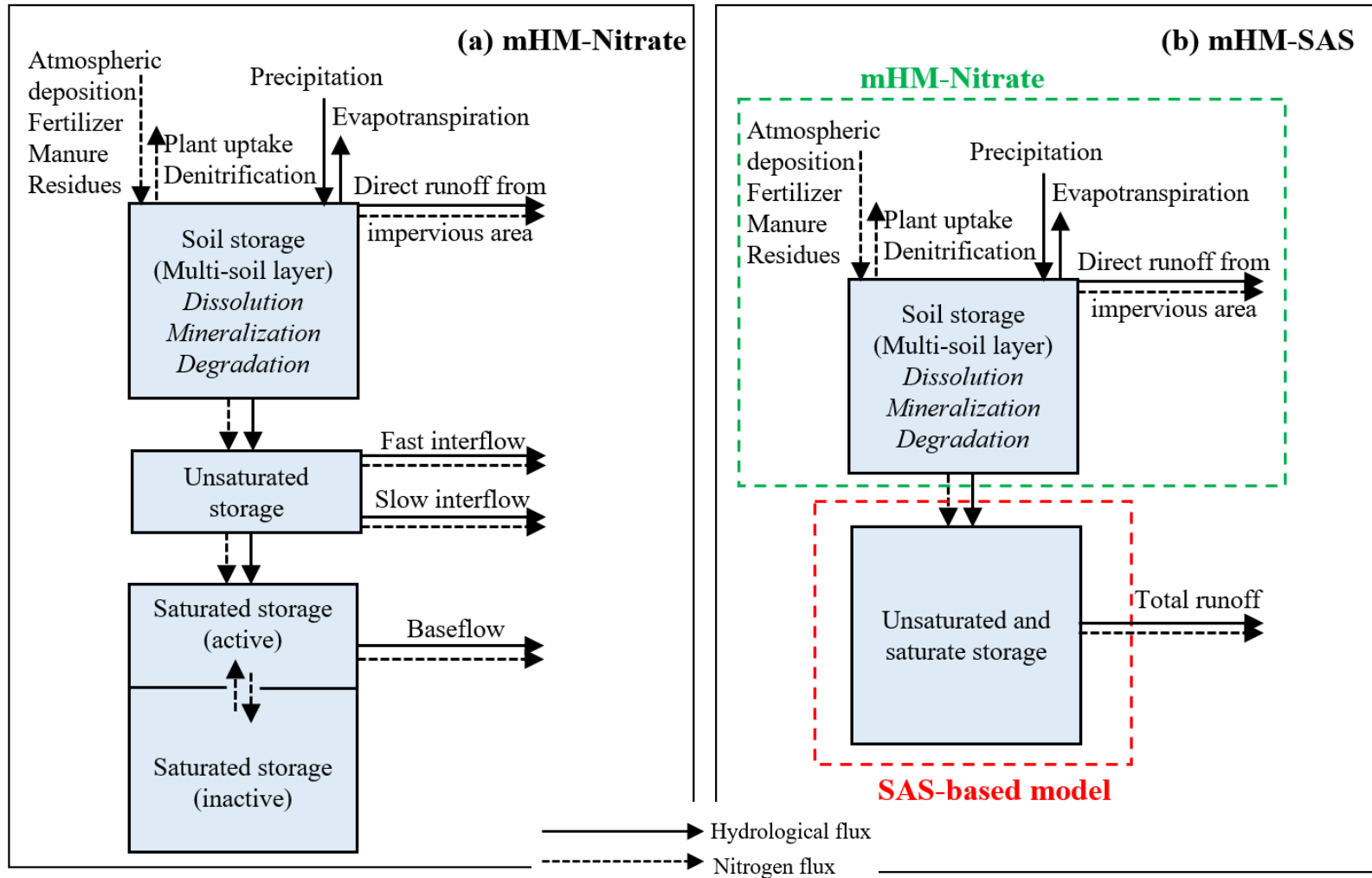
➤ *Research objectives*

- Introducing a new model, allowing a distributed representation of soil nitrogen dynamics and a spatially implicit representation of subsurface transport pathways based on the SAS-based approach.
- Validating the proposed model at a mesoscale catchment with heterogeneous characteristics.

➤ *mHM-Nitrate model*

- a grid-based water quality (nitrate) model (Samaniego et al., 2010; Kumar et al., 2013; Lindström et al., 2010; Yang et al., 2018b).
  - accounts for spatial heterogeneity in land use management practices (fertilizer/manure application, crop rotation).
  - has a simple subsurface nitrate transport module (no denitrification below the root zone, inadequate representation of celerity-driven transport).
- Replace the subsurface transport module with the SAS-based concept

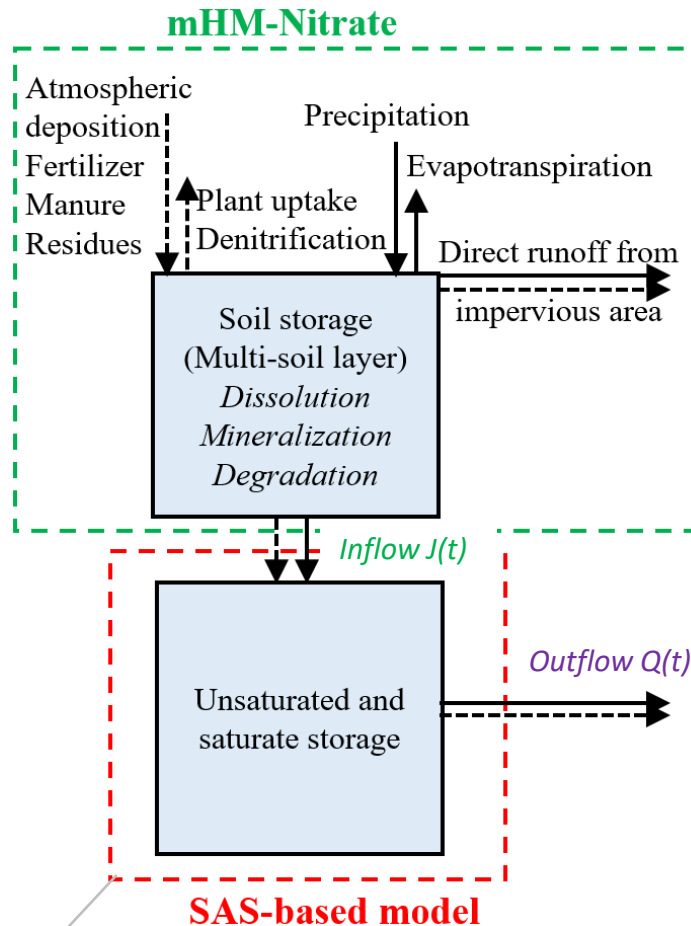
➤ *mHM-Nitrate model vs. proposed mHM-SAS model*



Conceptual model of (a) the mHM-Nitrate model and (b) the proposed mHM-SAS model at a grid cell level



## ➤ mHM-SAS model



Master equation for the SAS compartment

changes of the  
water volume  
in storage  
with age  $\leq T$

$$\frac{\partial S_T(T, t)}{\partial t} = \overset{\text{inflow}}{J(t)} - \overset{\text{outflow}}{Q(t)} \cdot \underset{\text{TTD of discharge}}{P_Q(T, t)} - \overset{\text{aging}}{\frac{\partial S_T(T, t)}{\partial T}}$$

Solute (nitrate) concentration at the outlet

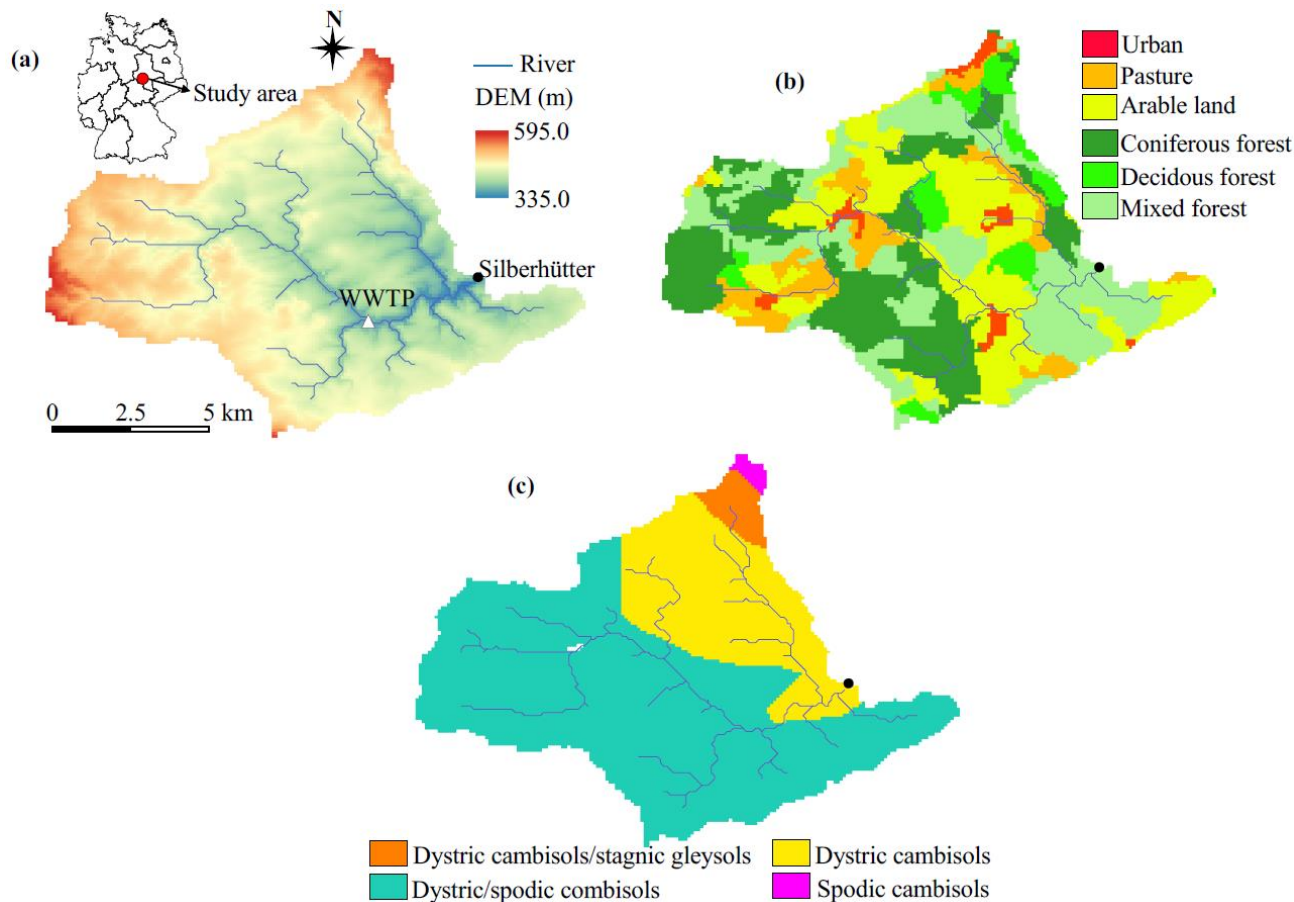
$$C_Q(t) = \int_0^\infty C_J(T, t) \cdot \underset{\text{TTD of discharge}}{p_Q(T, t)} \cdot \exp\left(-\frac{T}{\underset{\text{Half life of nitrate}}{t_{12}}}\right) \cdot dT$$

normalized age-ranked storage

$$P_Q(T, t) = \underset{\text{SAS function}}{\Omega_Q}(\overset{\text{normalized age-ranked storage}}{P_S(T, t)}, t)$$

SAS compartment: unsaturated and saturate zone below the root zone over the whole catchment

## ➤ Study area



Location of the upper Selke with (a) the digital elevation model (DEM), (b) land use/land cover map, and (c) soil map. The catchment outlet is indicated by a black dot.

➤ *Study area*

- Catchment area: 100 km<sup>2</sup> (61% forest, 36% agricultural)
- Main crops: winter wheat, triticale, winter barley, rye, rapeseed, corn.
- Fertilizer/manure application rate: 130 – 190 kg N/ha/yr
- Strong seasonality in runoff regime
- Chemodynamic C(nitrate)-Q relationship

➤ *Representation of the time-variant SAS functions*

- Two-parameter beta function  $\beta(P_S, a, b)$
- Two beta functions are used to characteristics of the time-variant SAS functions:  $\beta_{wet}(P_S, a_{wet}, b_{wet})$ , and  $\beta_{dry}(P_S, a_{dry}, b_{dry})$
- The wet and dry periods are defined based on the following factor:

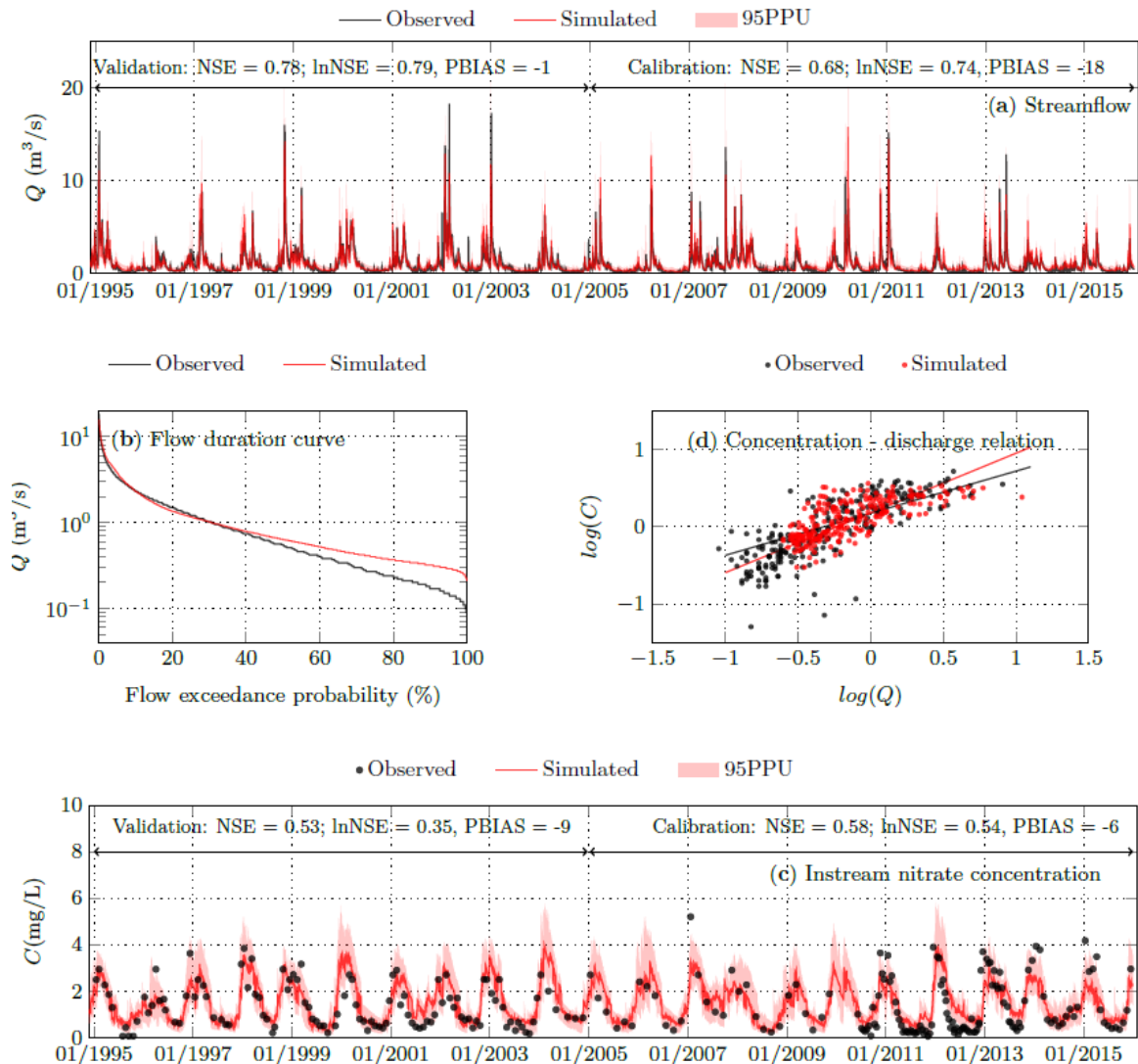
$$r_t = \frac{\sum_{i=t-n}^t J_i}{\sum_{i=t-n}^t Q_i}$$

← Inflow to the SAS compartment  
← Outflow  
← n: number of time steps

$r_t \geq 1 \rightarrow wet \rightarrow \beta_{wet}$  : Young water selection preference

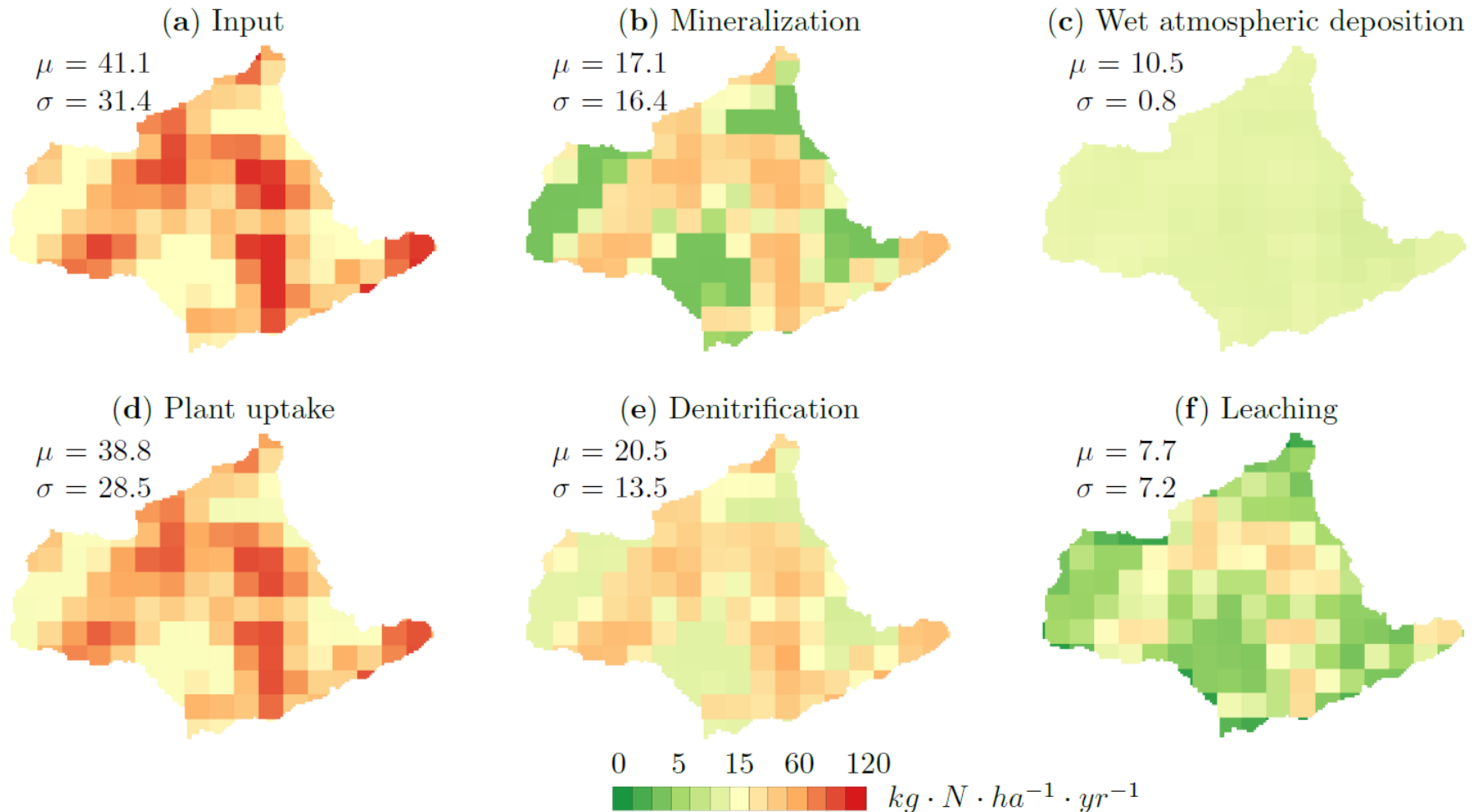
$r_t < 1 \rightarrow dry \rightarrow \beta_{dry}$  : Old (and young) water selection preference

## ➤ Simulated discharge and in-stream nitrate ( $N - NO_3$ ) concentration at Silberhütter

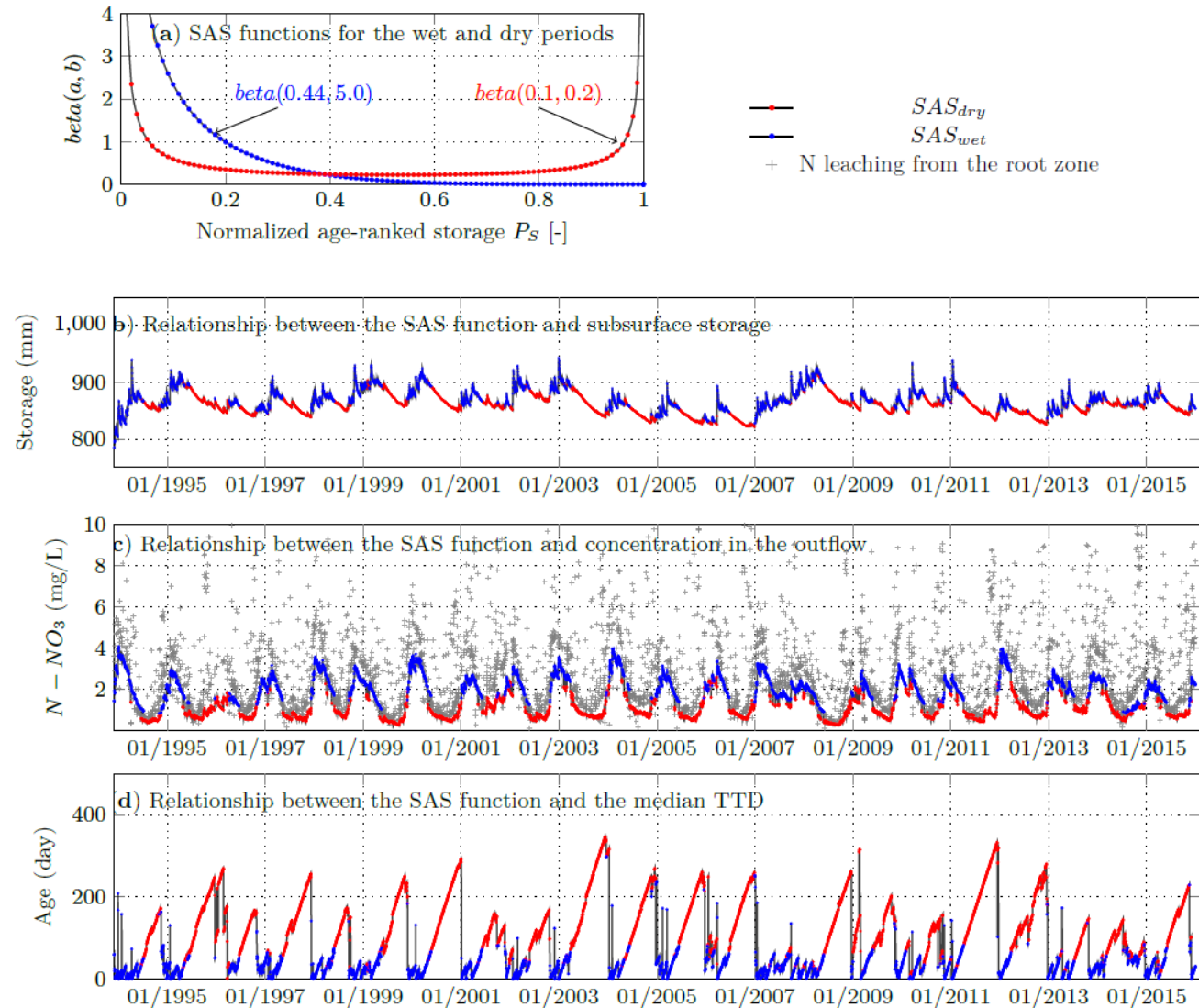


half life of nitrate = 134 days

➤ *Simulated spatial nitrogen dynamics within the root zone*



➤ *SAS functions – subsurface storage – nitrate concentration – median TTD of discharge*



- Denitrification below the root zone should be accounted for.
- Discharge and in-stream nitrate concentration dynamics at the catchment outlet could be well represented by the proposed model
- The mHM-SAS model could provide explicit spatial information about soil nitrogen
- The mHM-SAS model can represent the relation between the SAS function, storage, and median TTD of discharge in a qualitative and reasonable manner.



- Outlook
  - Quantitative verification of the simulated travel time and spatial nitrogen dynamic within the root zone
  - Testing of the model for catchments with nitrogen legacy (velocity-driven transport)

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Thank you for your attention ☺

Questions and Suggestions are welcome