

Quantifying the probability distribution function of the transient climate response to cumulative CO₂ emissions

Emission pathways, carbon budgets, and climate-carbon response: governing mechanisms, limitations, and implications for policymakers

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Near Linear Δ Temperature with Total Emitted CO_2

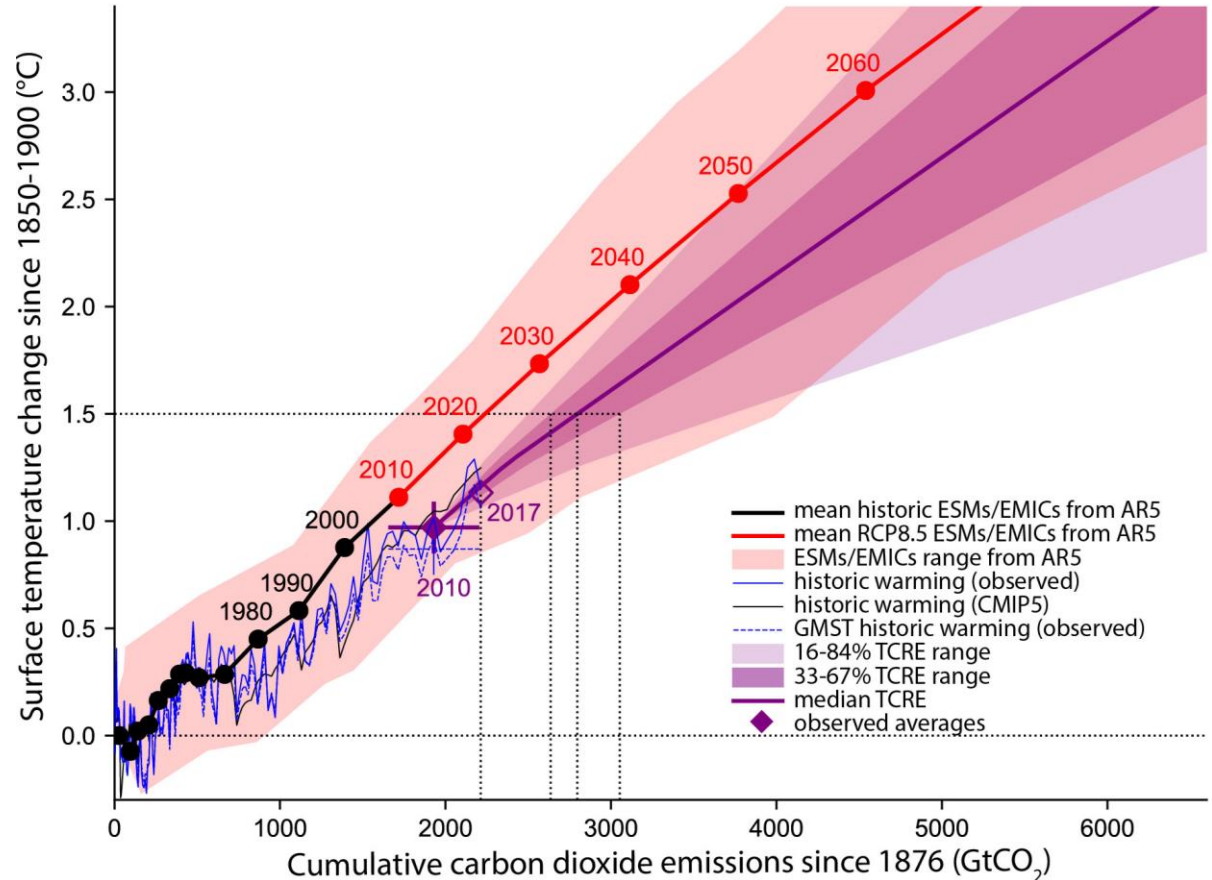
Saturation in
radiative
forcing per
unit CO_2
emission



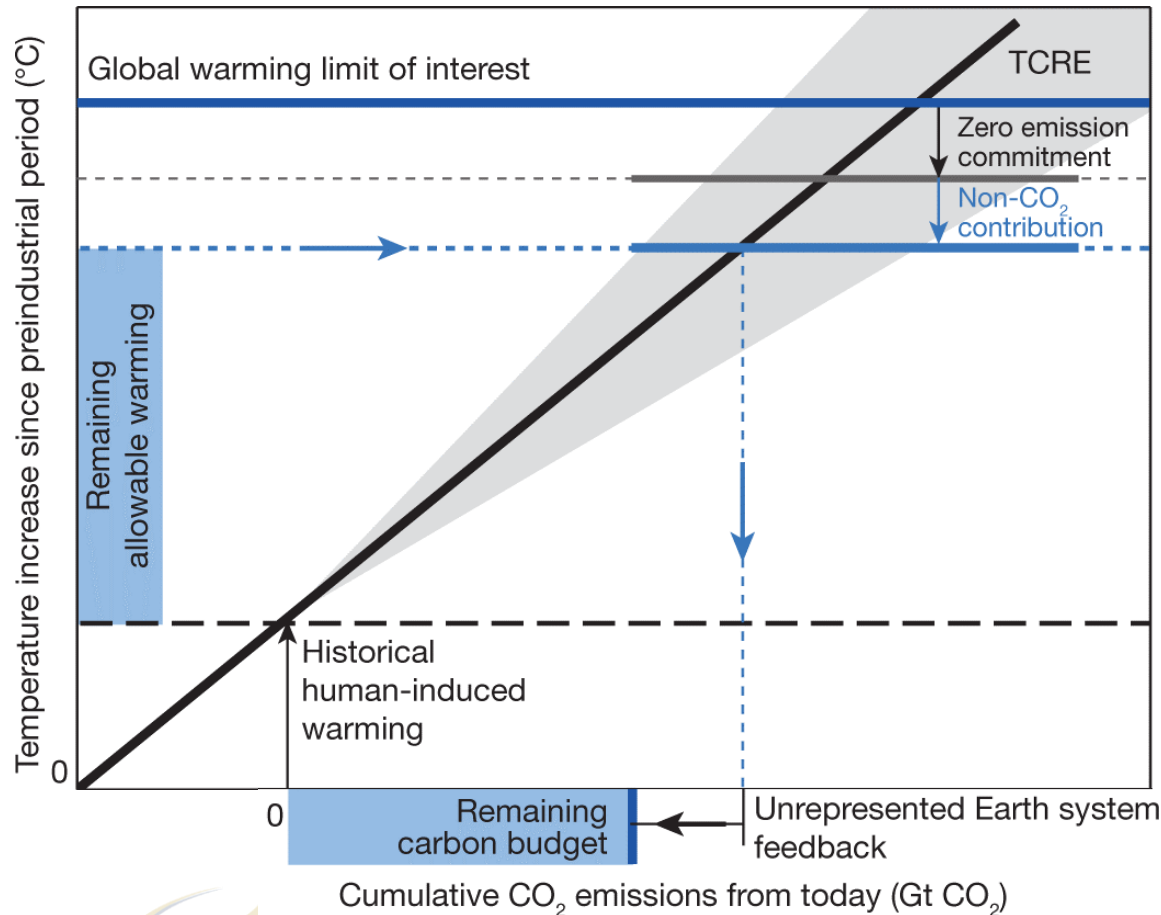
Reduced heat
and carbon
uptake
efficiency with
more CO_2
emissions



Transient **C**limate **R**esponse
to Cumulative CO_2 **E**missions
(TCRE)



Implications of the TCRE



- Fixed quantity of total CO₂ emissions consistent with not exceeding a threshold in global warming (ie. 2°C or 1.5°C) :
 $\text{carbon budget} = \text{warming goal} \div \text{TCRE}$
- Pathway independence - for typical emission scenarios, the TCRE holds, so mitigation policies can follow a carbon budget rather than emissions pathway
- Ultimately need to reach net-zero emissions to limit global warming

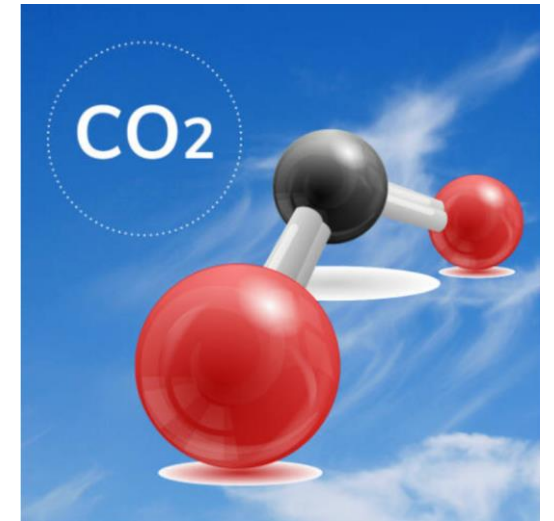
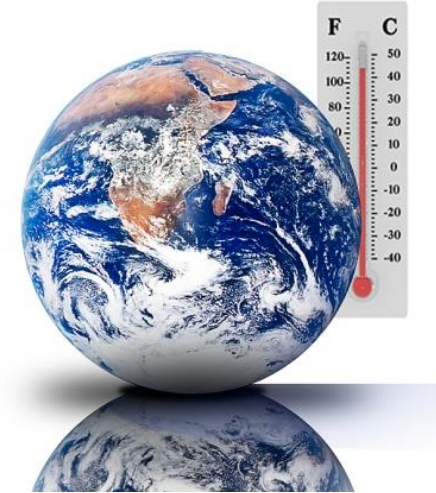
Limitations for carbon budgets from the TCRE:

- Non-CO₂ radiative forcing
- Zero emission commitment
- Earth system feedbacks
- Constant, declining, zero, or negative CO₂ emissions

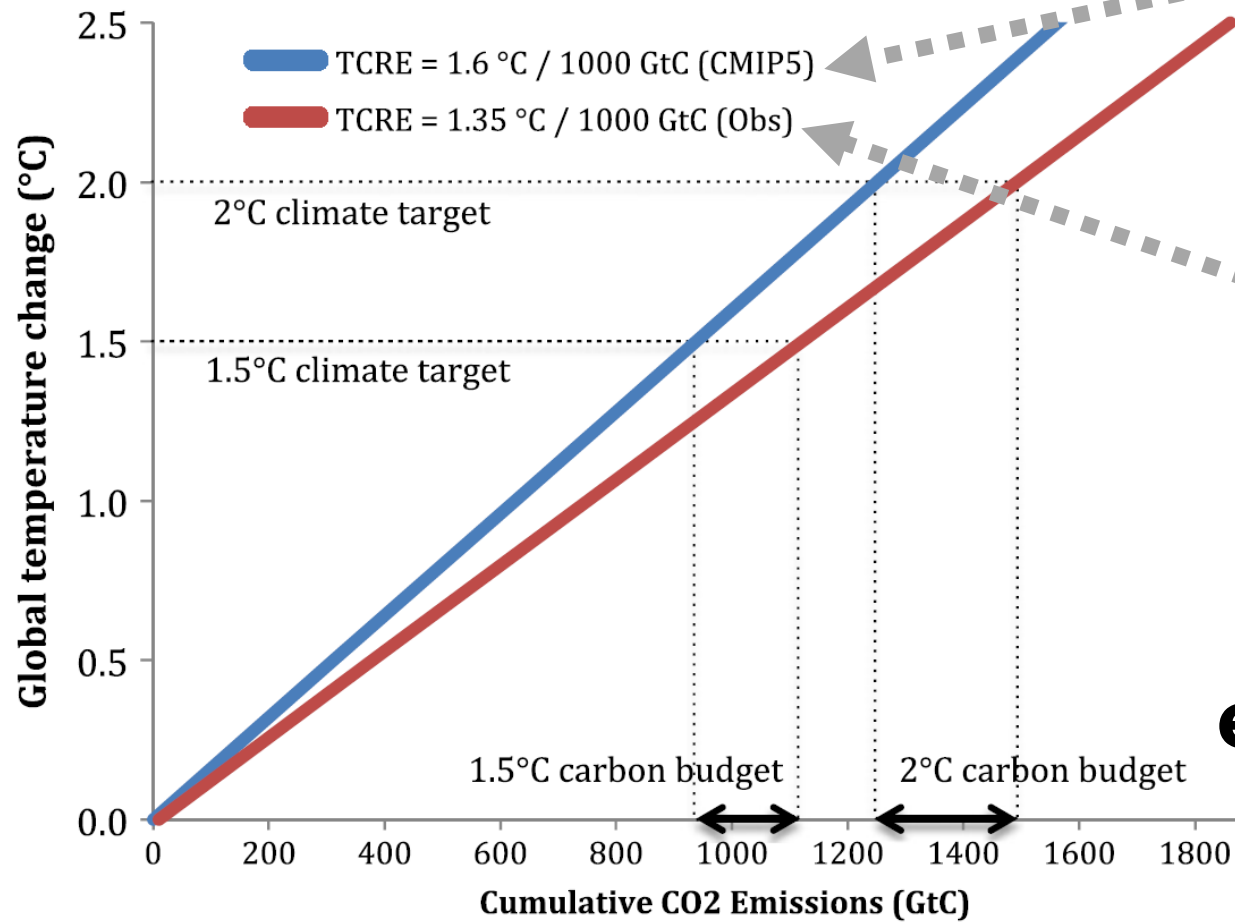
TCRE Components

1. Climate sensitivity to atmospheric CO₂ concentration

2. Carbon cycle response to cumulative CO₂ emissions



TCRE uncertainty

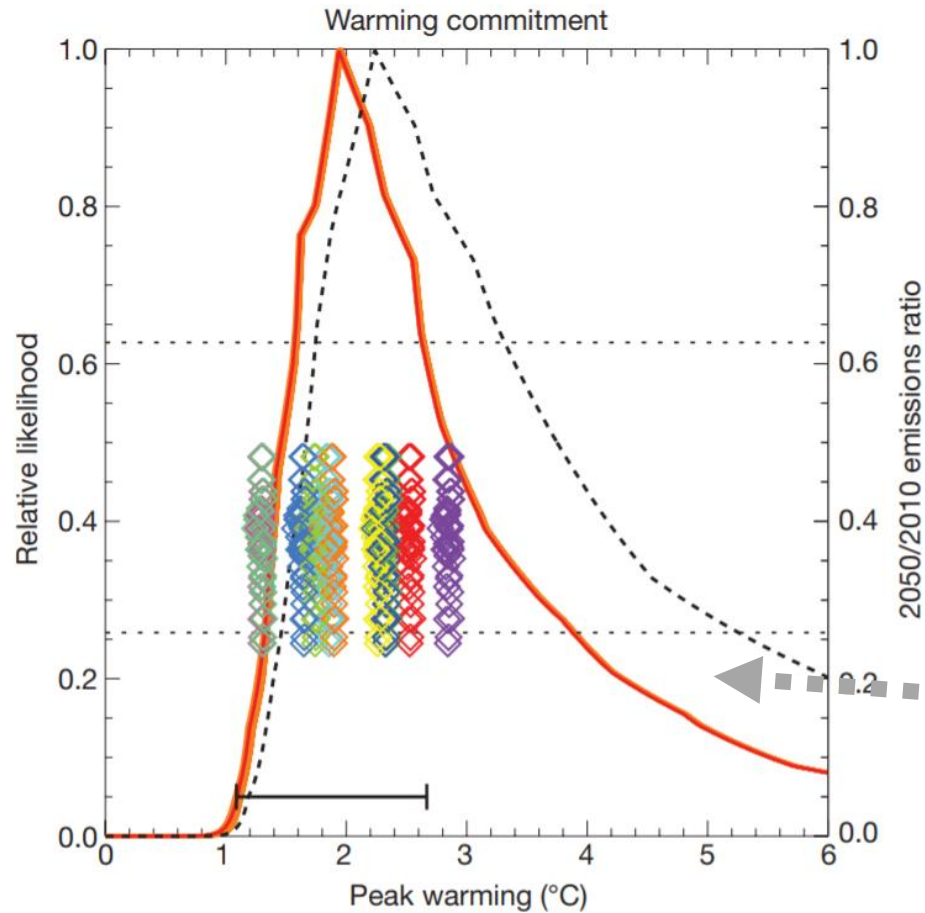


Modelling studies often report a higher mean and greater spread of TCRE values (ie. Gillett et al. (2013) - CMIP5: median: 1.6°C/EgC, 5-95% confidence: 0.8-2.4°C/EgC)

Observational studies often report a lower mean and reduced spread of TCRE values (ie. Gillett et al. (2013) : \bar{x} : 1.35°C/EgC, 5-95% confidence: 0.7-2.0°C/EgC)

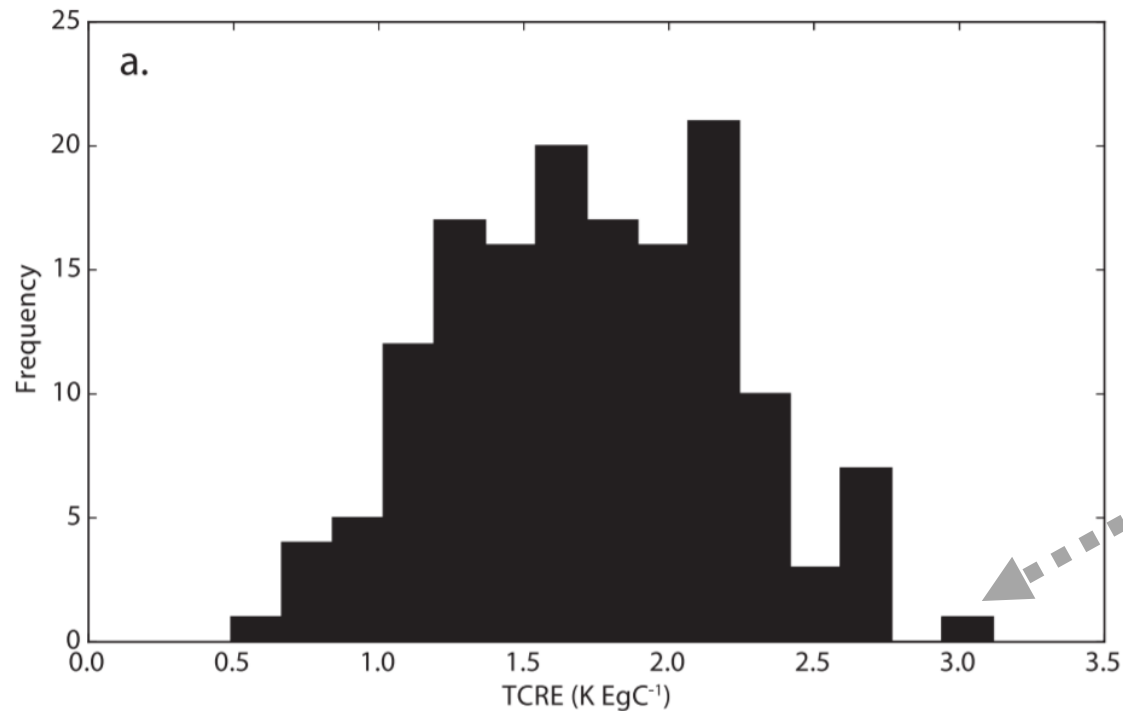
No study to date has explicitly addressed whether the TCRE is normally or non-normally distributed

TCRE Probability Distribution Function (PDF)?



In a study of the Cumulative Warming Commitment (CWC) (equivalent to the TCRE assuming a negligible zero emissions commitment), Allen et al. (2009) reports asymmetry in the distribution of the CWC

TCRE Probability Distribution Function (PDF)?



In a study of the TCRE using a perturbed physics approach, MacDougall et al. (2017) show the TCRE PDF may be well described by a normal distribution, though there is a slight positive skew suggested to be due to climate sensitivity

The IPCC SR1.5 report shows this uncertainty in whether or not the TCRE is normally distributed has a considerable influence upon remaining carbon budget calculations, though did not advocate for one distribution over the other

Table 2.2 from IPCC SR1.5: The assessed remaining carbon budget and its uncertainties.


Additional Warming since 2006–2015 [°C] ^{*(1)}	Approximate Warming since 1850–1900 [°C] ^{*(1)}	Remaining Carbon Budget (Excluding Additional Earth System Feedbacks ^{*(5)}) [GtCO ₂ from 1.1.2018] ^{*(2)}			Key Uncertainties and Variations ^{*(4)}					
		Percentiles of TCRE ^{*(3)}			Earth System Feedbacks ^{*(5)}	Non-CO ₂ scenario variation ^{*(6)}	Non-CO ₂ forcing and response uncertainty	TCRE distribution uncertainty ^{*(7)}	Historical temperature uncertainty ^{*(1)}	Recent emissions uncertainty ^{*(8)}
		33rd	50th	67th						
					[GtCO ₂]	[GtCO ₂]	[GtCO ₂]	[GtCO ₂]	[GtCO ₂]	[GtCO ₂]
0.3		290	160	80	Budgets on the left are reduced by about –100 on centennial time scales	±250	–400 to +200	+100 to +200	±250	±20
0.4		530	350	230						
0.5		770	530	380						
0.53	~1.5°C	840	580	420						
0.6		1010	710	530						
0.63		1080	770	570						

Objectives

1. Calculate the TCRE based upon current understandings of the interactions between climate and carbon processes.
2. Examine the probability distribution function of the TCRE using a Monte-Carlo error propagation.
3. Explore the sensitivity of the TCRE to various Earth system parameters.
4. Compute the CO₂-only carbon budget consistent with 2°C warming.

Methods: ZD²OM - Zero Dimensional **D**iffusive **O**cean Heat and Carbon Uptake **M**odel

$$\Lambda = \frac{R(1-l)}{\lambda} \left(\frac{\ln\left(\frac{C_A}{C_{AO}}\right)}{1 + \frac{f_o \rho C_p \tau \epsilon \sqrt{\beta}}{\sqrt{\mu \lambda^2 \ln\left(\frac{C_A}{C_{AO}}\right)}}} \right) \times \left(\frac{1}{C_A - C_{AO} + \frac{2B_o \Gamma \ln\left(\frac{C_A}{C_{AO}}\right)^{\frac{3}{2}}}{3\sqrt{\mu \beta}}} \right)$$


↑

TCRE

**Monte-Carlo simulation with 10 million ZD²OM iterations
drawing randomly from 5 Earth System parameter PDFs**

Methods: ZD²OM

$$\Lambda = \frac{R(1-l)}{\lambda} \left(\frac{\ln\left(\frac{C_A}{C_{AO}}\right)}{1 + \frac{f_o \rho C_p \tau \epsilon \sqrt{\beta}}{\sqrt{\mu \lambda^2 \ln\left(\frac{C_A}{C_{AO}}\right)}}} \right) \times \left(\frac{1}{C_A - C_{AO} + \frac{2B_o \Gamma \ln\left(\frac{C_A}{C_{AO}}\right)^{\frac{3}{2}}}{3\sqrt{\mu\beta}}} \right)$$

Radiative forcing from an e-fold increase in atmospheric CO₂


Methods: ZD²OM

$$\Lambda = \frac{R(1 - l)}{\lambda} \left(\frac{\ln\left(\frac{C_A}{C_{AO}}\right)}{1 + \frac{f_o \rho C_p \tau \epsilon \sqrt{\beta}}{\sqrt{\mu \lambda^2 \ln\left(\frac{C_A}{C_{AO}}\right)}}} \right) \times \left(\frac{1}{C_A - C_{AO} + \frac{2B_o \Gamma \ln\left(\frac{C_A}{C_{AO}}\right)^{\frac{3}{2}}}{3\sqrt{\mu \beta}}} \right)$$

Land-borne fraction of carbon

Methods: ZD²OM

$$\Lambda = \frac{R(1 - l)}{\lambda} \left(\frac{\ln\left(\frac{C_A}{C_{AO}}\right)}{1 + \frac{f_o \rho C_p \tau \epsilon \sqrt{\beta}}{\sqrt{\mu \lambda^2 \ln\left(\frac{C_A}{C_{AO}}\right)}}} \right) \times \left(\frac{1}{C_A - C_{AO} + \frac{2B_o \Gamma \ln\left(\frac{C_A}{C_{AO}}\right)^{\frac{3}{2}}}{3\sqrt{\mu\beta}}} \right)$$



Climate feedback

Methods: ZD²OM

$$\Lambda = \frac{R(1 - l)}{\lambda} \left(\frac{\ln\left(\frac{C_A}{C_{AO}}\right)}{1 + \frac{f_o \rho C_p \tau \epsilon \sqrt{\beta}}{\sqrt{\mu \lambda^2 \ln\left(\frac{C_A}{C_{AO}}\right)}}} \right) \times \left(\frac{1}{C_A - C_{AO} + \frac{2B_o \Gamma \ln\left(\frac{C_A}{C_{AO}}\right)^{\frac{3}{2}}}{3\sqrt{\mu\beta}}} \right)$$

↑ Effective ocean diffusivity
 ↑

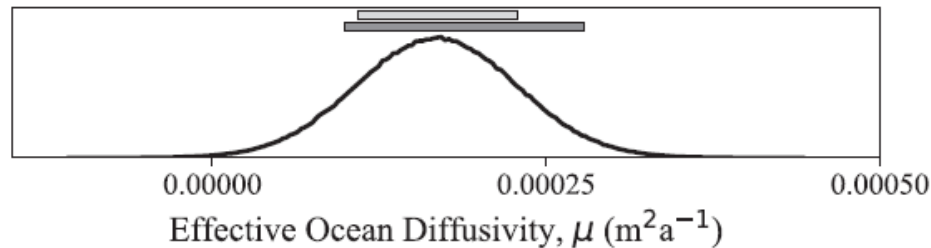
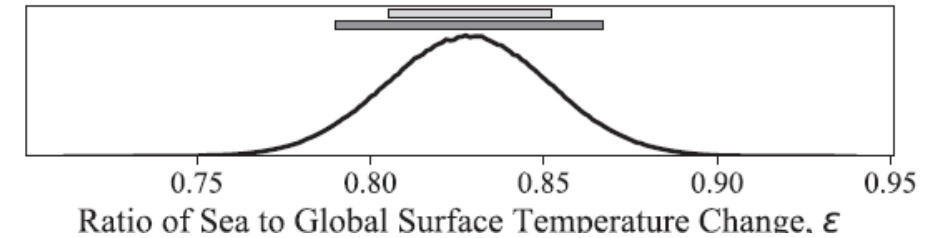
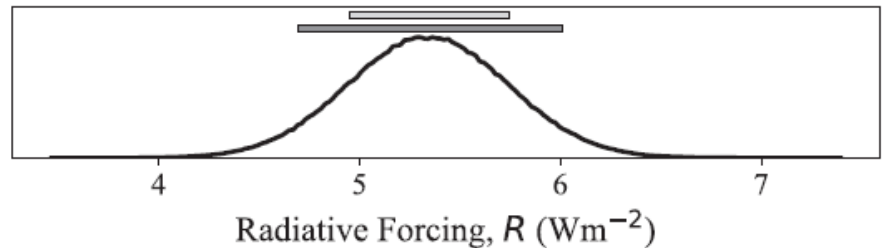
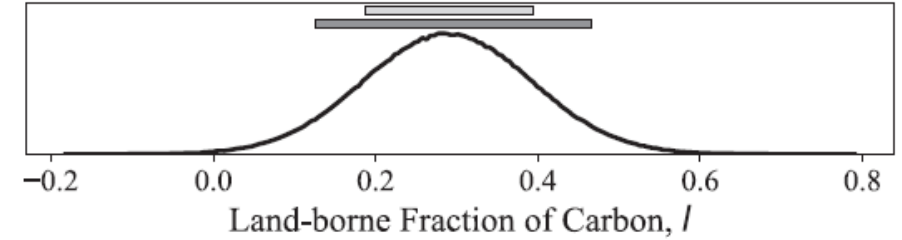
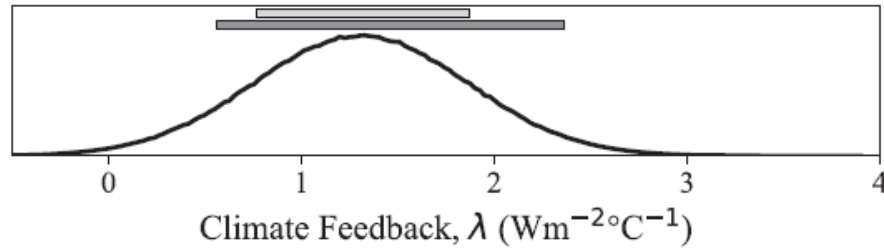
Methods: ZD²OM

$$\Lambda = \frac{R(1 - l)}{\lambda} \left(\frac{\ln\left(\frac{C_A}{C_{AO}}\right)}{1 + \frac{f_o \rho C_p \tau \epsilon \sqrt{\beta}}{\sqrt{\mu \lambda^2 \ln\left(\frac{C_A}{C_{AO}}\right)}}} \right) \times \left(\frac{1}{C_A - C_{AO} + \frac{2B_o \Gamma \ln\left(\frac{C_A}{C_{AO}}\right)^{\frac{3}{2}}}{3\sqrt{\mu\beta}}} \right)$$

Ratio of sea surface temperature change to global temperature change

Methods: Source Parameter PDFs

Density

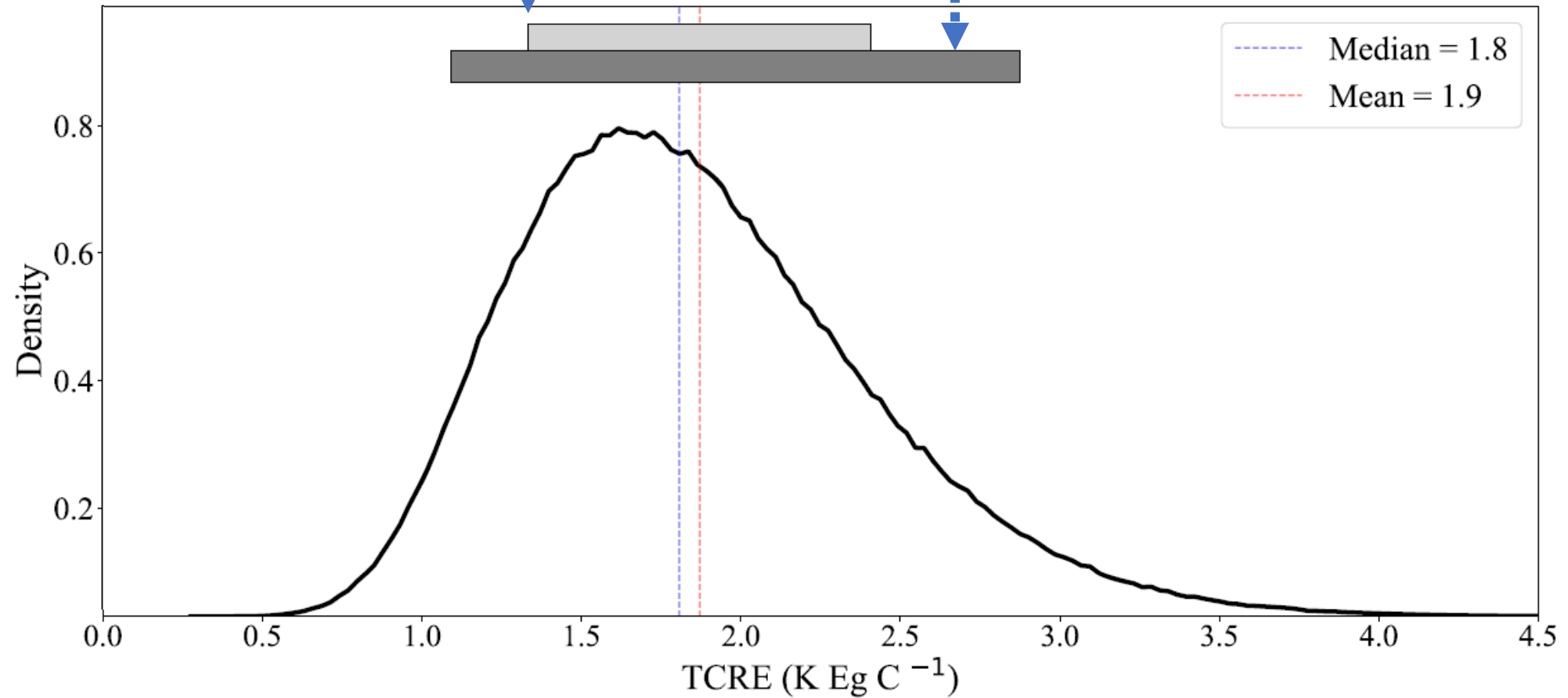


Each Earth System parameter distribution had 10 million values

I also performed sensitivity tests with normal and uniform priors

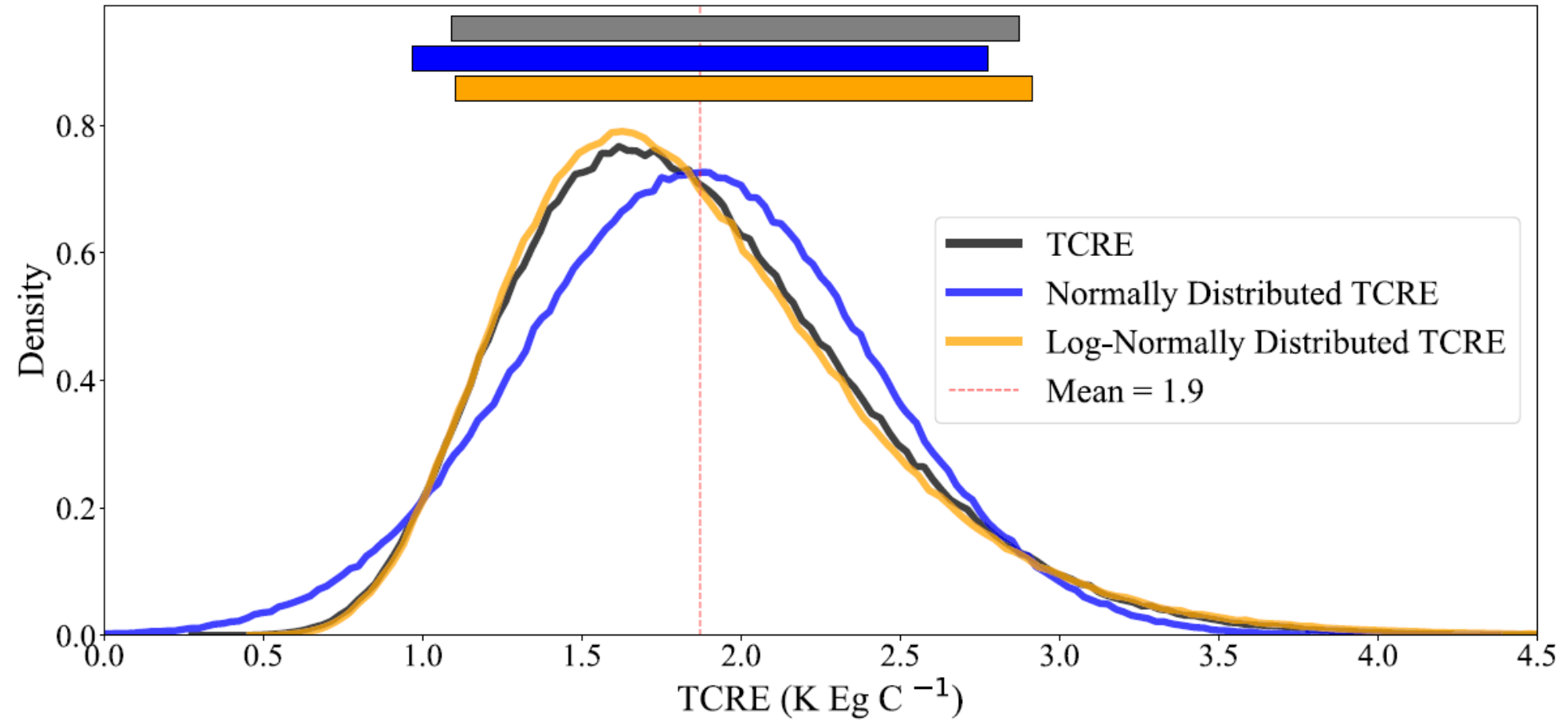
Results

16 – 84% confidence interval: 1.3 to 2.4 °C/EgC
5 – 95% confidence interval: 1.1 to 2.9 °C/EgC

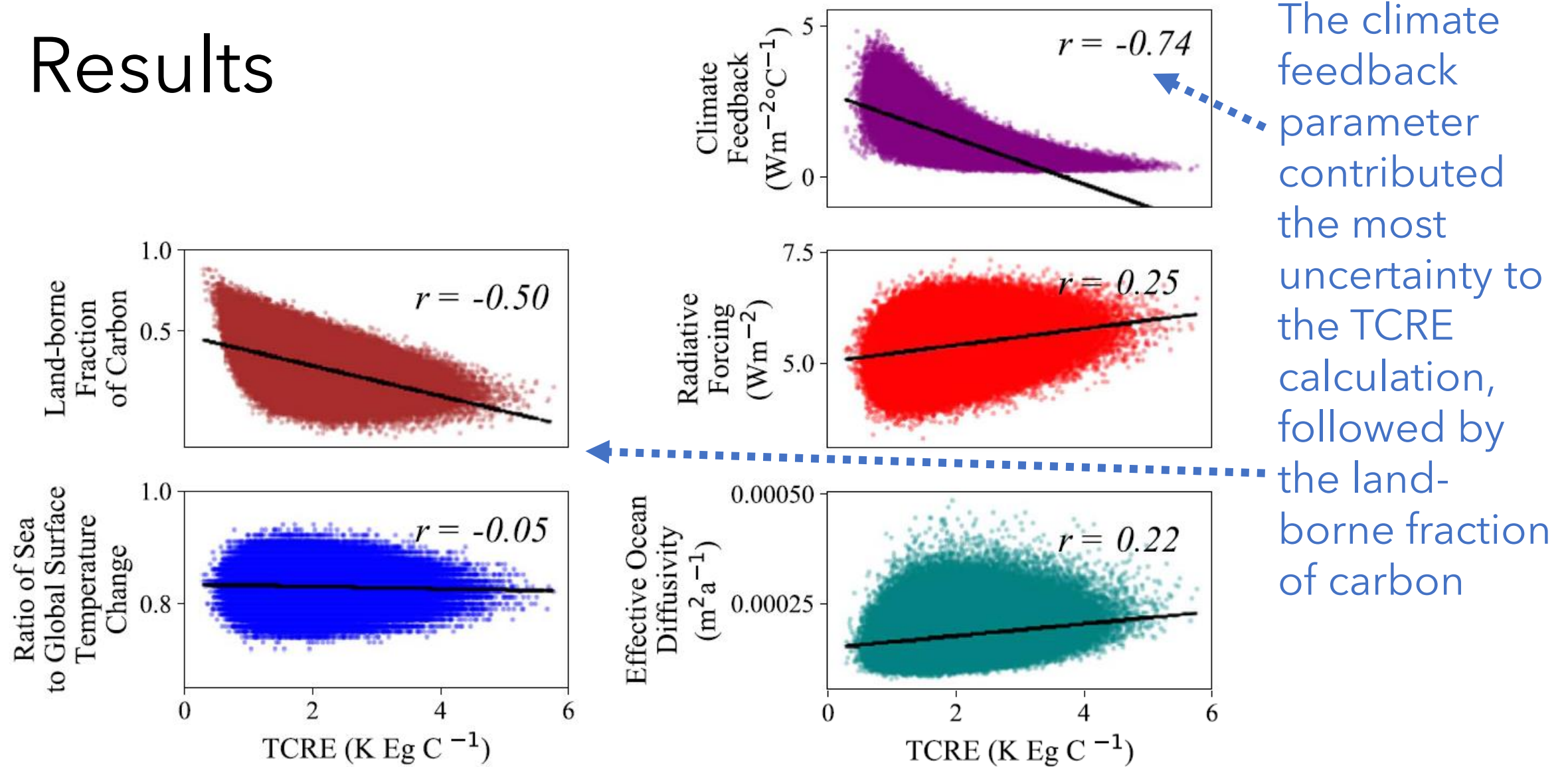


Results

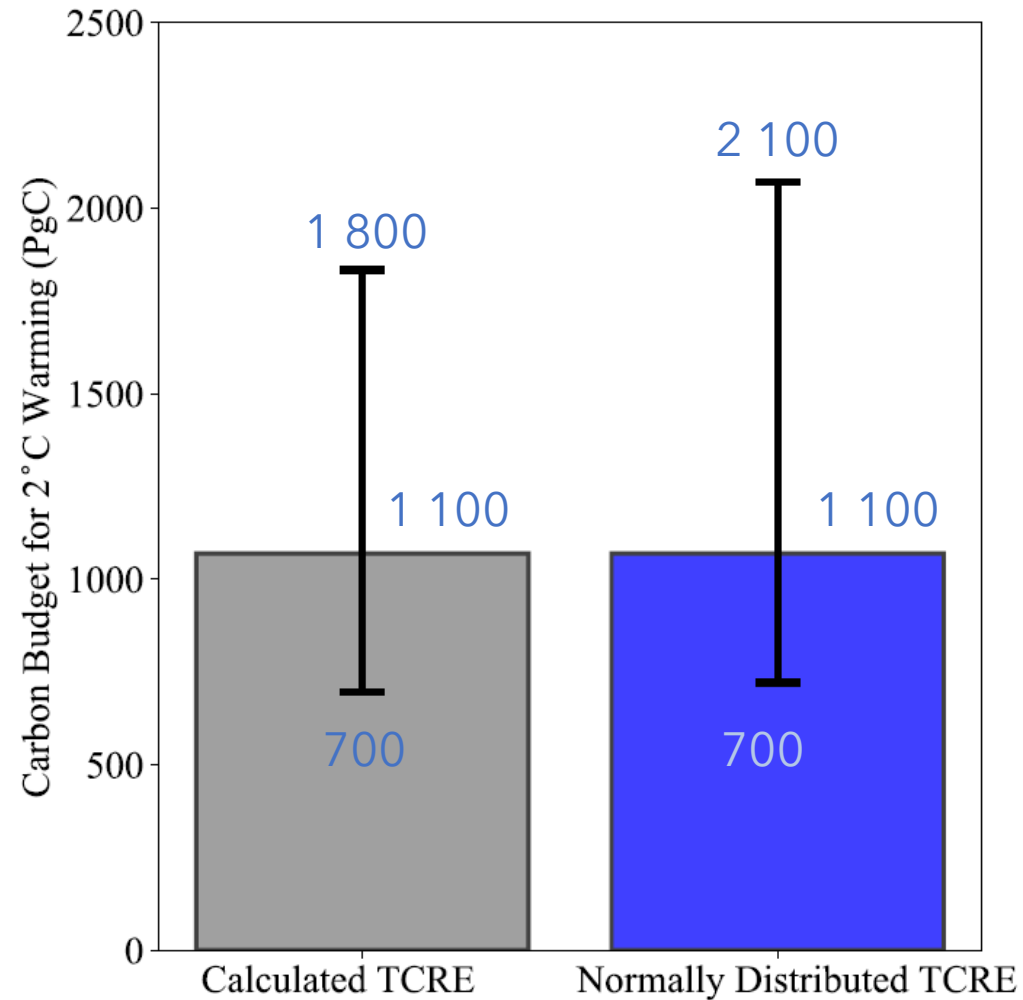
The distribution of TCRE values I calculated is well described by a log-normal distribution, which was robust to the distribution of the priors



Results



Results



- From the TCRE I calculated, the CO₂-only total carbon budget (including past, present, and future CO₂ emissions) for 2°C warming is 1 100 billion tonnes of carbon (or petagrams - PgC), ranging from 700 - 1 800 PgC at 5-95% confidence
- Assuming a normally-distributed TCRE results in a 700 - 2 100 PgC budget estimate at 5-95% confidence
- While the true TCRE is likely close to the centre of the PDF, assuming a normally distributed TCRE overestimates the upper limit of the carbon budget estimate by ~300 PgC, or ~27 years of emissions at a rate of 11 Pg C yr⁻¹

Conclusions


1. The TCRE is well described by a log-normal distribution.
2. The TCRE we calculated ranges from 1.1 to 2.9 K EgC⁻¹ (5-95% confidence), with a mean of 1.9 K EgC⁻¹ and median of 1.8 K EgC⁻¹.
3. Climate sensitivity (feedback) is most influential, followed by land-borne fraction of carbon, radiative forcing from an e-fold rise in CO₂, ocean diffusivity, and the ratio of sea to global warming.
4. The CO₂-only carbon budget for 2°C warming is 1100 PgC (700-1800, 5-95% confidence), while assuming a normal TCRE PDF suggests a 2°C budget of 1100 PgC (700-2100, 5-95% confidence).

Conclusions

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Thank You!



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