

ESTIMATING ADDITIONAL ROOT COHESION BY EXPLOITING A ROOT TOPOLOGICAL MODEL BASED ON LEONARDO'S RULE

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Motivations

- Slope stabilization by plants is mainly controlled by the **biotechnical characteristics** of the root system and the roots-soil interaction
- Root structure can be represented through **root topological models**, i.e. schematic representations based on a defined topology graph theory

Biotechnical characteristics

- Root length
- Root density/area
- Root diameter profile
- Total number of roots
- Tensile strength



From Preti e Giadrossich (2009)



Landslide and vegetation in Rio Mameyes Basin (Puerto Rico)

Motivations

- Describing adequately the root architecture maybe helpful to answer to the following **questions**:
 - ❖ Which root architecture does guarantee a certain additional root reinforcement?
 - ❖ Which is the most suitable plant species to be adopted in certain soil or water availability conditions?



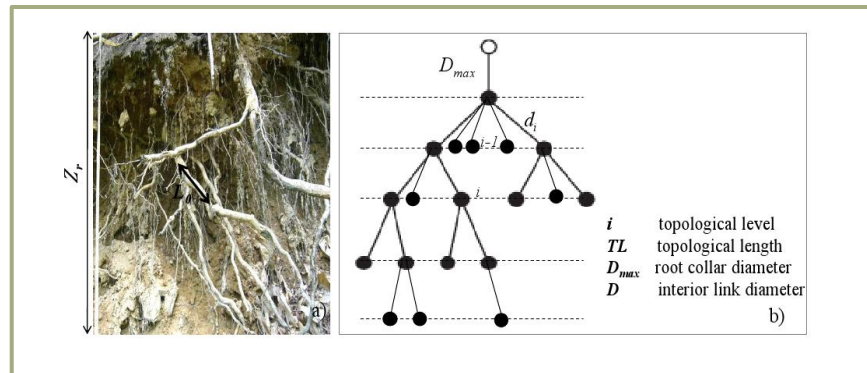
Objectives

- Exploiting a modeling framework for estimating the additional root cohesion in different configuration of root architectures, assumed as representative of different static plant-growth conditions
- Assessing the ultimate effects on **slope stability** of a synthetic slope

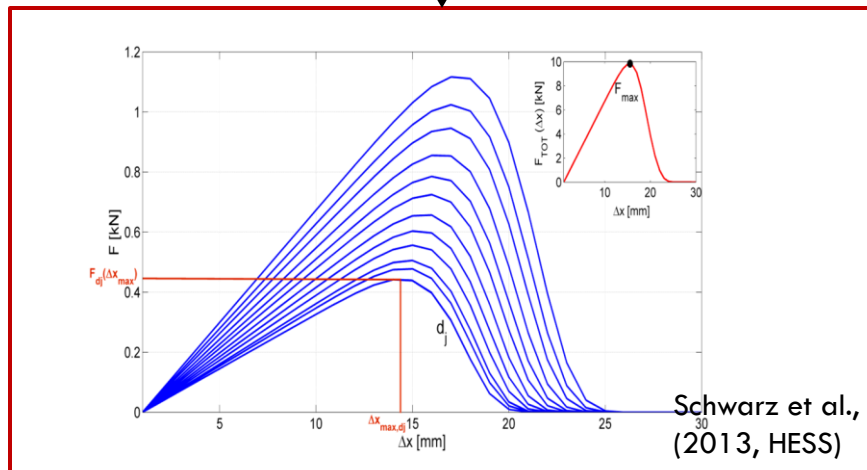
Modeling framework

Arnone et al., 2016 (WRR)

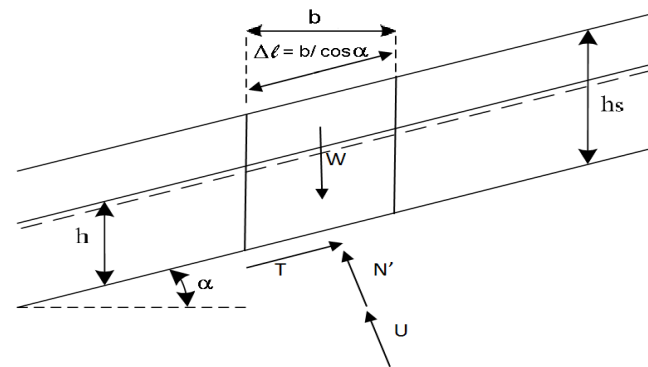
Topological Model



Root Bundle Model



Stability model: Infinite slope



Root Cohesion Term

$$FS_{tot} = \Delta FS_r + FS_s = \frac{c_r}{\gamma_t(\theta) z_n \sin \omega} + FS_s$$



Additional FS due to root reinforcement

Topological model

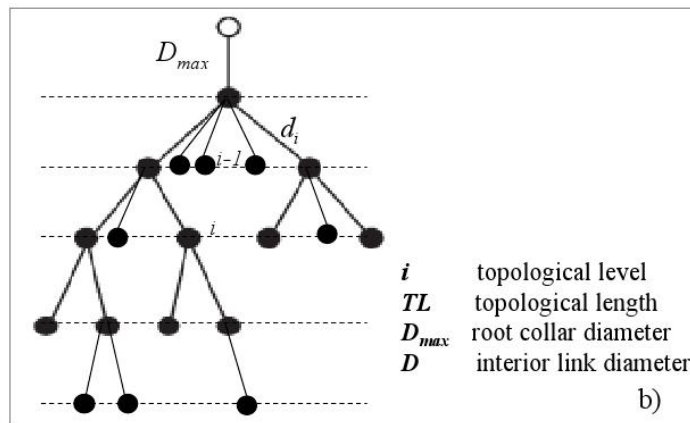
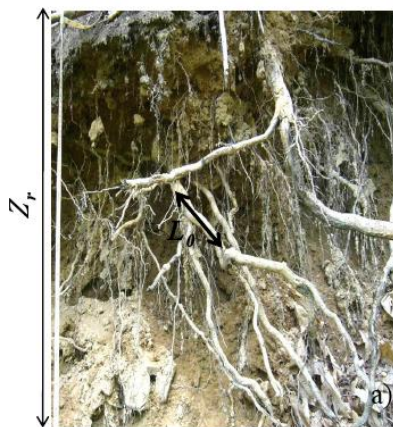
LEONARDO'S RULE: The cross-sectional area of a branch of a tree is equal to the sum of the cross-sectional areas of the branches at any higher level (Oppelt et al., 2001)

$$\alpha_d \cdot N_i \cdot d_i^2 = N_{i-1} \cdot d_{i-1}^2$$

$$d_i = d_{i-1} \sqrt{\frac{1}{\alpha_d} \cdot \frac{N_{i-1}}{N_i}}$$

$$AR_i = \frac{\pi}{4} \cdot \frac{d_{i-1}}{\alpha_d} N_{i-1}$$

$$N_i = f(i|r, p) \cdot N_{tot}$$



α_d and D_{max} are the calibration parameters (by means of measured data of AR)

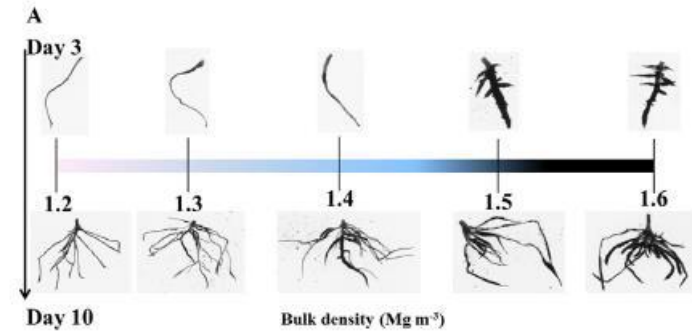
TL , total root length (RL) and N_{tot} are the required input parameters

Root system development

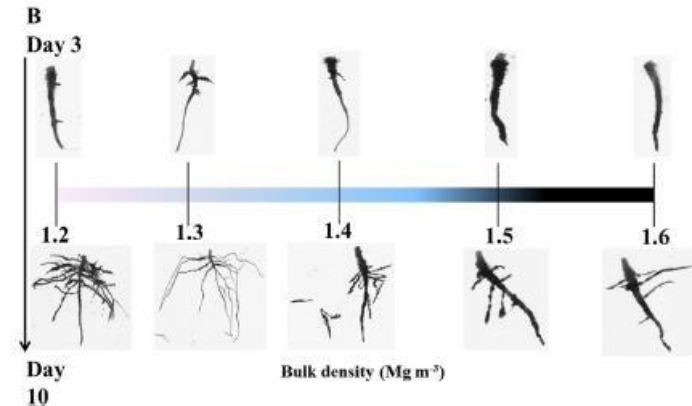
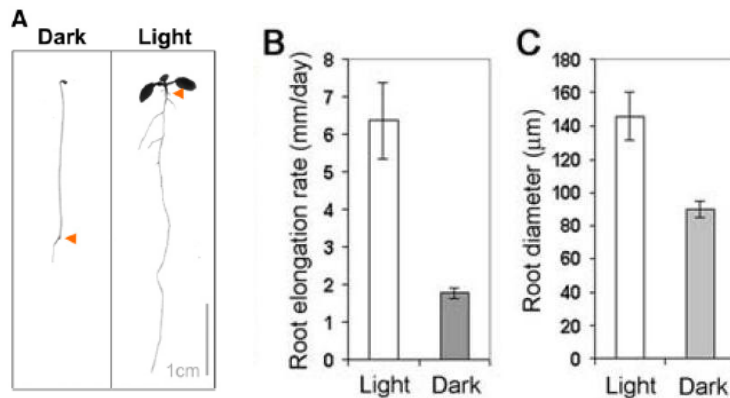
Controlling factors

- Exposure to light
- Water availability
- Nutrient availability
- Soil effects (i.e., compaction, mechanical stress, topography, ...)

Tracy et al., 2013



Laxmi et al. 2008



Case study: reference data

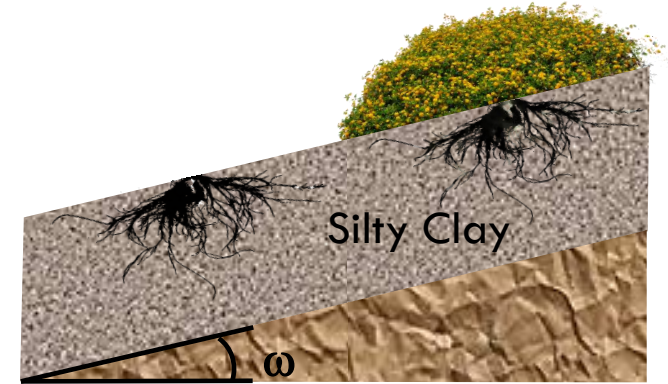
Arnone et al., 2016 (WRR)

Reference Scheme

In Situ DATA		
Depth	N_{roots}	A_r obs
m	-	cm ²
0.00	1	2.8
0.05	16	
0.10	25	1.8
0.15	21	1.4
0.20	12	1.55
0.25	12	1.2
0.30	8	1.3
0.35	6	0.5
0.40	5	0.45
0.45	3	0.4
0.50	3	0.47
0.55	2	0.2
0.60	2	
0.65	1	
0.70	0	



Spartium Junceum (Spanish broom).
From Preti e Giadrossich, 2009



Biotechnical properties ^a					
α	β	A_0	E_0	RL	N_{tot}
[-]	[-]	[MPa/mm]	[MPa/mm]	[cm]	[-]
-0.306	-0.826	37.605	649	70	117
Soil Parameters					
ϕ'	c'	γ	γ_w	ω	
[°]	[kPa]	[kN/m ³]	[kN/m ³]	[°]	
20	0	20	9.81	26.5	

^a Parameters α - A_0 and β - E_0 are respectively exponents and coefficients of the power laws that describe tensile strength and Young's modulus of the roots, and RL is the root length. From [14,15]

Case study: model configurations

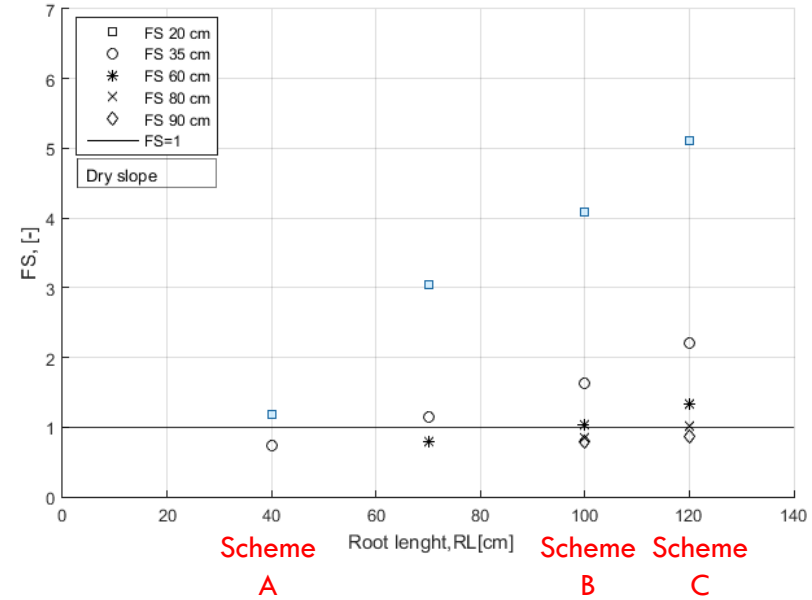
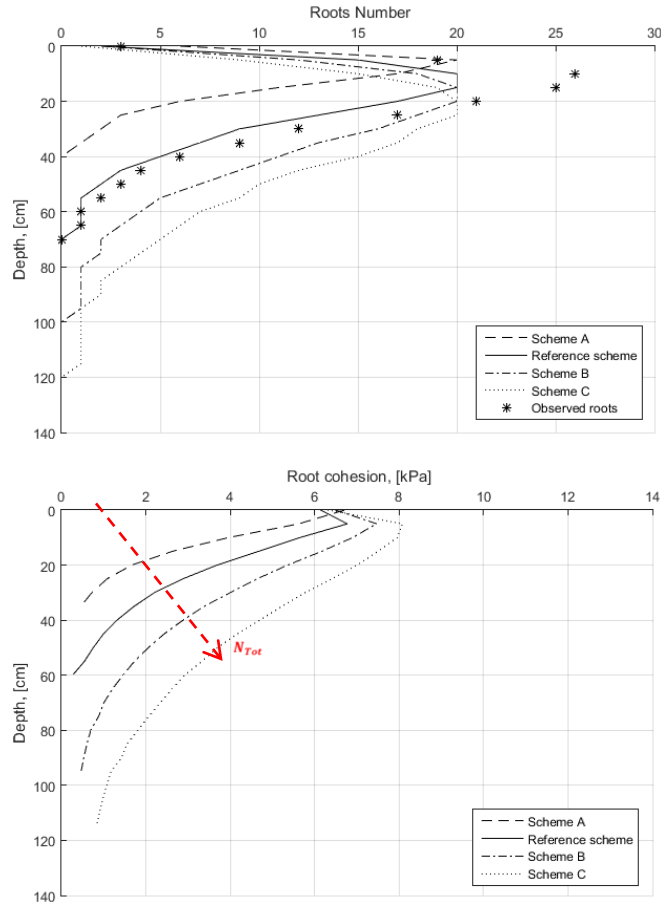
	Exposure to light	Soil Compaction	Water availability	Nutrient availability
Reference Scheme	normal	normal	normal	normal
Scheme A	normal	HIGH	normal	normal
Scheme B	HIGH	normale	HIGH	normale
Scheme C	HIGH	normale	HIGH	HIGH



	Root Length (RL) [cm]	N _{tot}
Reference Scheme	70	117
Scheme A	40	67
Scheme B	100	167
Scheme C	120	200

$$\frac{RL}{N_{tot}} = cost$$

Case study: results



Concluding remarks

- ❑ The ultimate effects of additional root reinforcement on slope stability depend on the slope conditions and the location of the hypothetical failure plane
- ❑ The effective utility of the plant reinforcement depends on its root length, compared with the position of the depth of failure. A root length simply greater than the failure depth might be not sufficient to improve the stability of the slope
- ❑ Results are useful for identifying the depth of the failure surface, beyond which the root reinforcement is not sufficient to avoid shallow landslide
- ❑ The use of the presented coupled modeling framework can be helpful in planning phase, for assessing whether the plant-growth conditions would be favorable for the stabilizing scopes

Main References

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