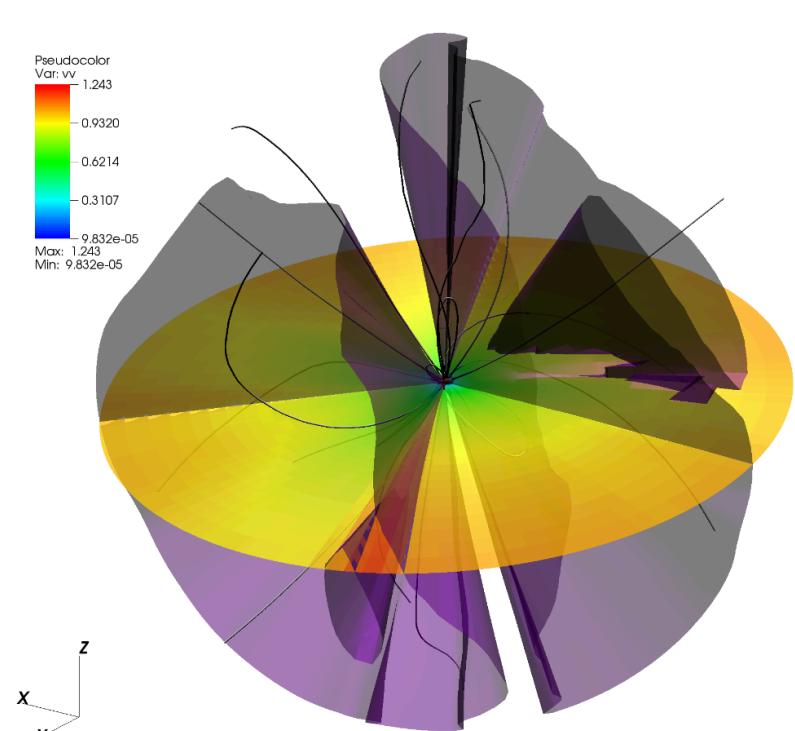
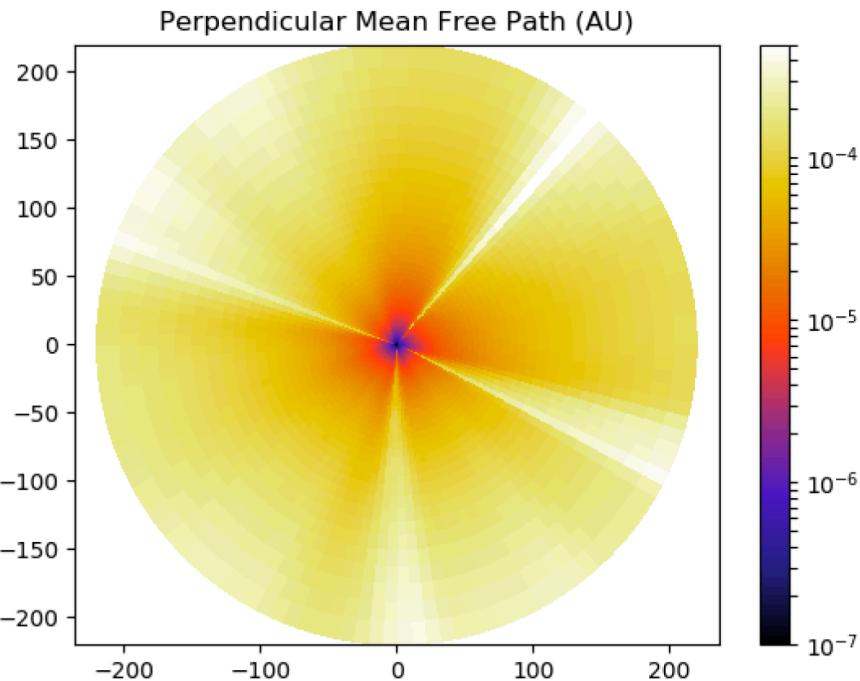


# Impact of solar magnetic field amplitude and geometry on SEPs and GCRs diffusion coefficients

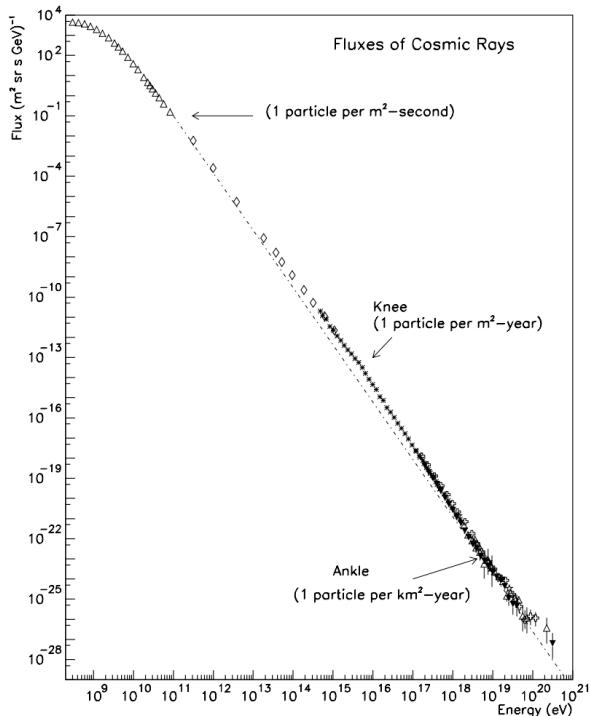
## Collaborators:

Dr. Allan Sacha **Brun** (AIM), Dr. Antoine **Strugarek** (AIM), Dr. Victor **Réville** (IRAP), Dr. **Éric Buchlin** (IAS)



# Cosmic rays and the solar cycle

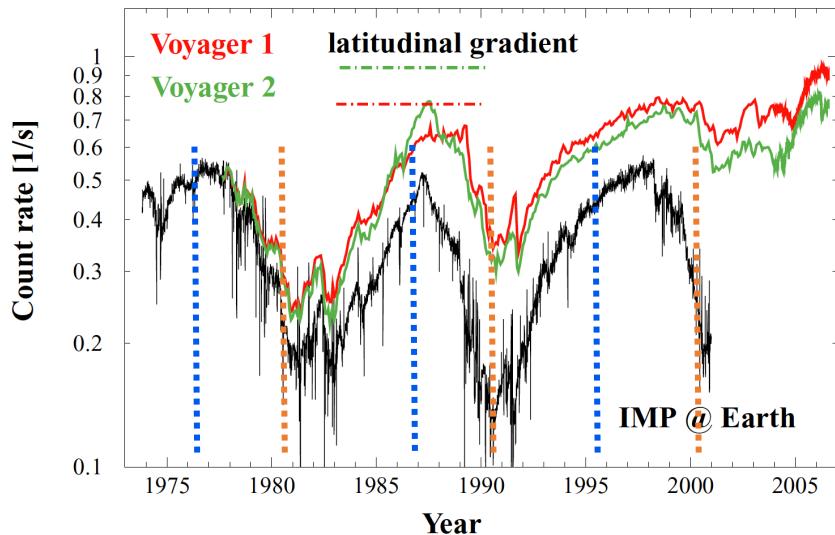
[Cronin+1997, Swordy 2001]



**Cosmic rays (CRs)** are energetic particles that reach the Earth

The lower part of the energy distribution is composed of **SEPs (Solar Energetic Particles)**, the higher part of **GCRs (Galactic Cosmic Rays)**

Minimum of activity      Maximum of activity



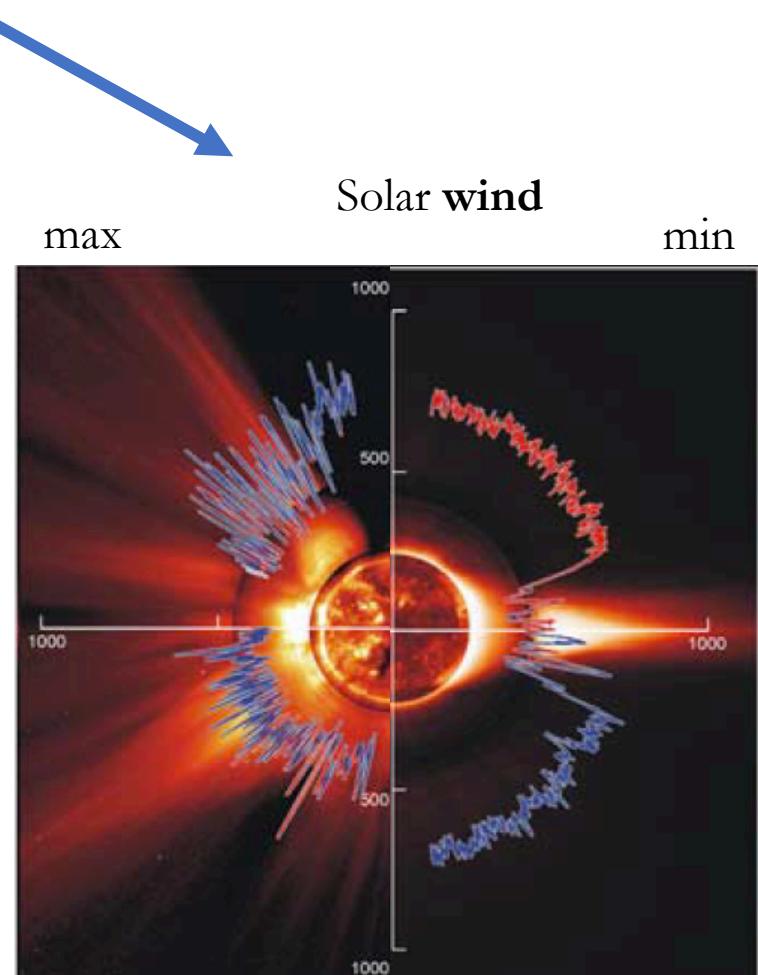
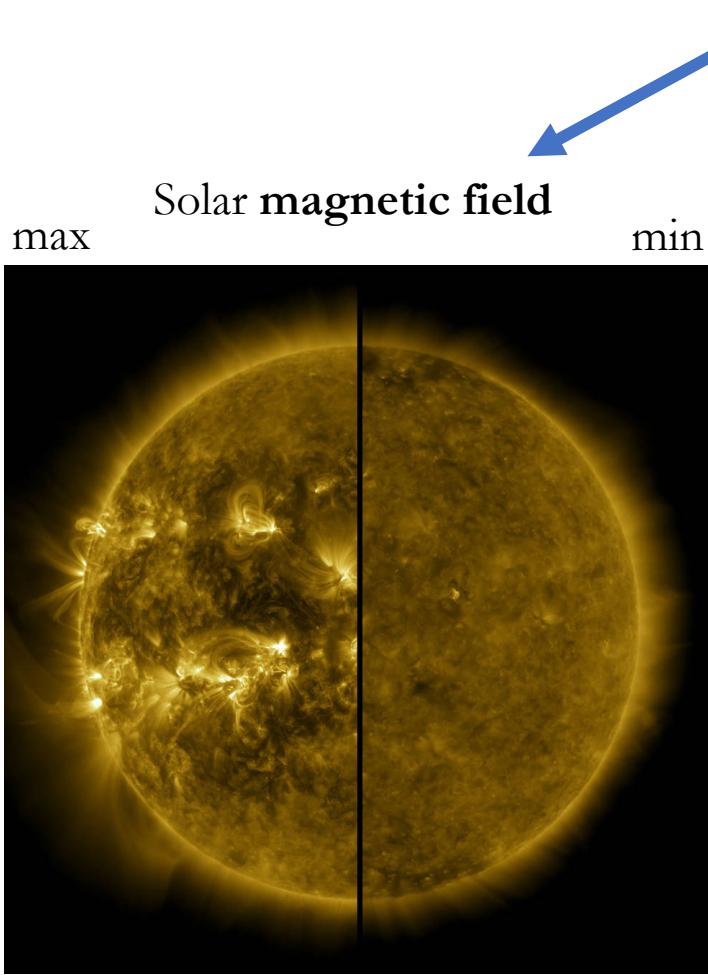
[Heber & Potgieter 2006]

**SEPs are correlated with the solar cycle**  
 → more particles produced at maximum of activity

**GCRs are anti-correlated with the solar cycle**  
 → the most energetic particles are driven away by the intense solar wind

# Cosmic rays and the solar cycle

SEPs and GCRs propagation will depend on their interaction with :



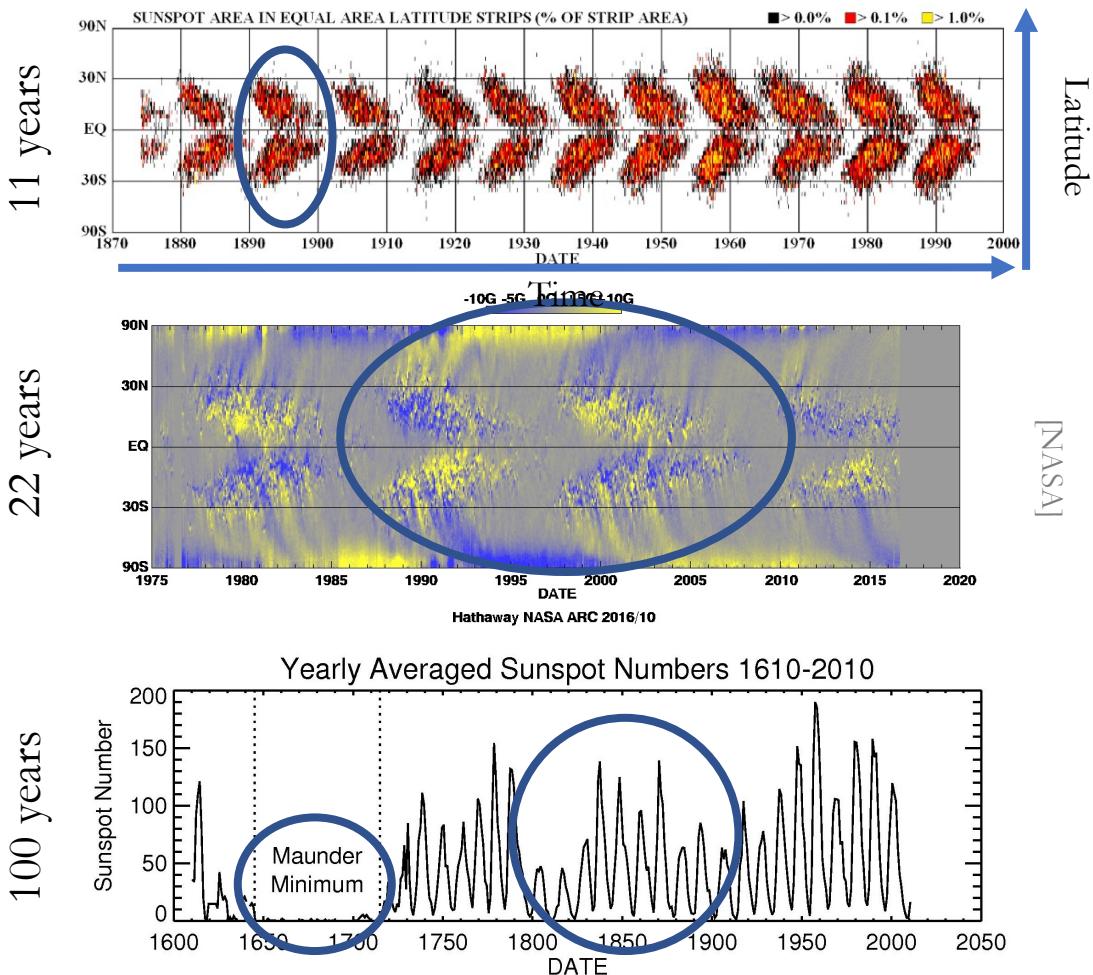
[NASA, SDO]

[McComas+2003]

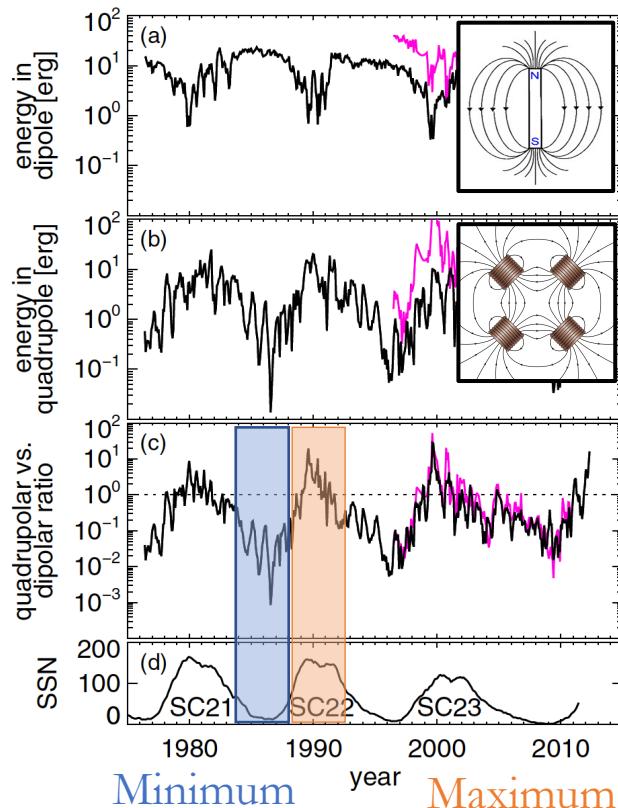
Both show a lot of **variability** over a dynamo cycle → difficult to prescribe analytically

# Observations of solar magnetism

The Sun has many characteristic periods



**Changes in geometry**  
More dipolar at minimum  
More quadrupolar at maximum

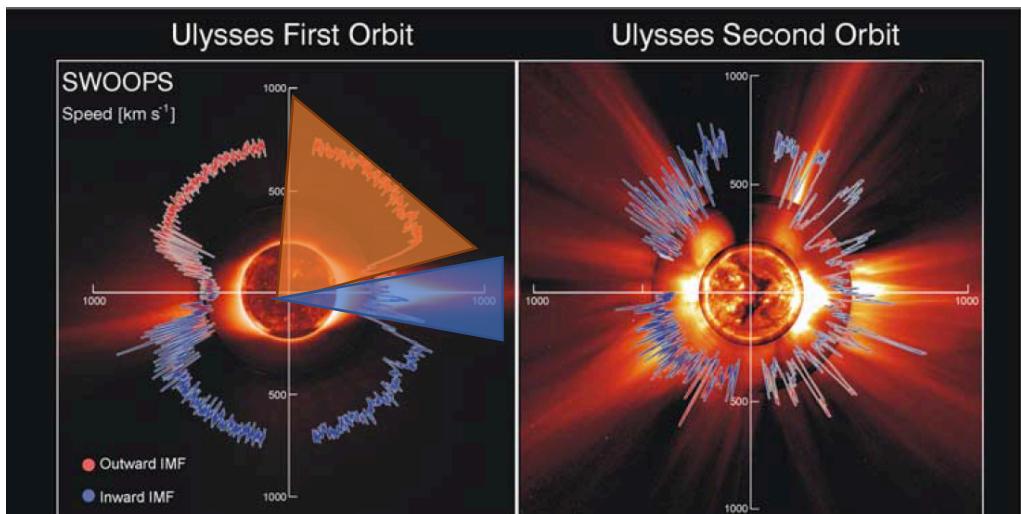


[DeRosa+2012]

# Observations of solar wind

Continuous flow of particles ejected by the Sun

→ Creates a connection between the Sun and the Earth



[McComas+2003]

## Slow solar wind

400 km/s

Cold (80 000 K)

Dense ( $6.6 \text{ cm}^{-3}$ )

From streamers and active regions

## Fast solar wind

800 km/s

Hot (680 000 K)

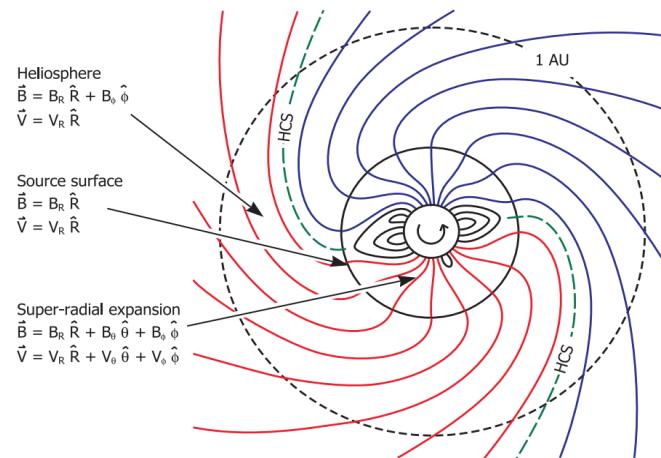
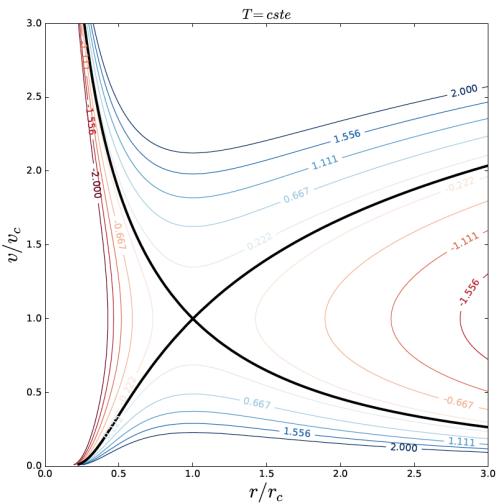
Less dense ( $3 \text{ cm}^{-3}$ )

From coronal holes

# State of the art

Usually, analytical prescriptions for the wind and the magnetic field → simplified

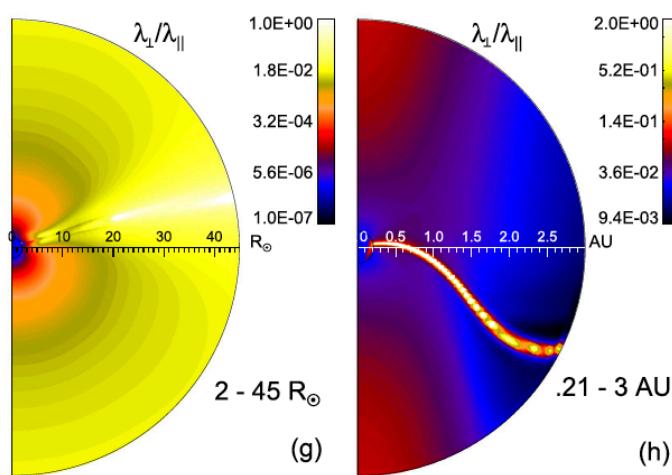
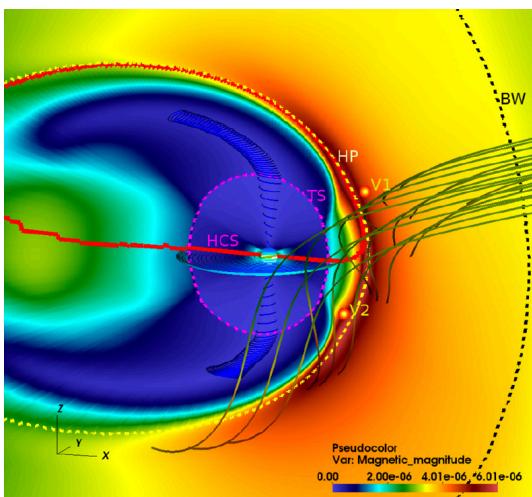
[Réville 2016]



[Owens & Forsyth 2013]

Use of numerical simulations instead, and combination with non-empirical diffusion

[Guo & Florinski 2014]

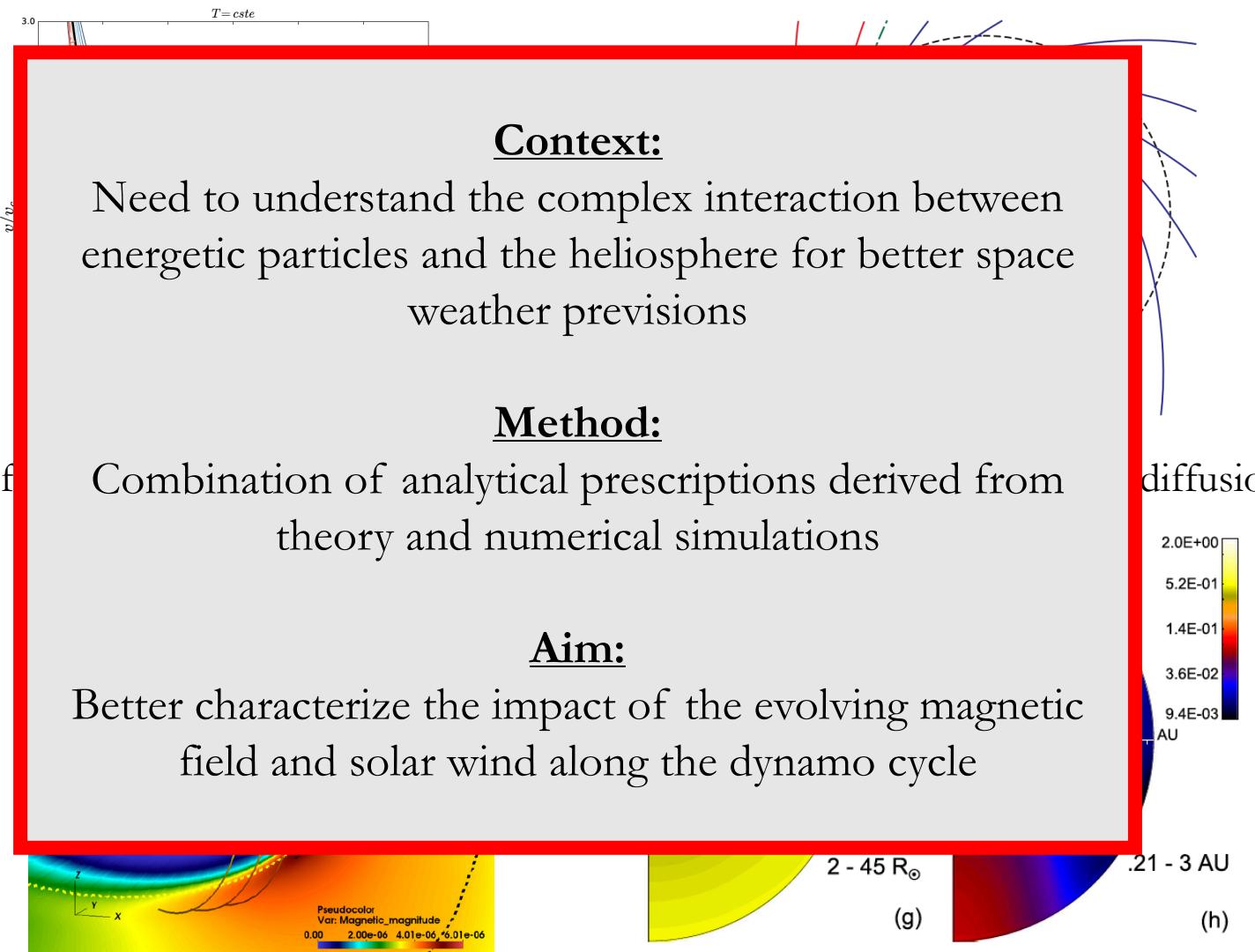


[Chhiber+ 2017]

# State of the art

Usually, analytical prescriptions for the wind and the magnetic field → simplified

[Réville 2016]



[Guo & Florinski 2014]

[Owens & Forsyth 2013]

[Chhiber+ 2017]

# Modeling cosmic rays

We start from the Fokker-Planck equation:

$$\frac{\partial U}{\partial t} = \nabla \kappa \nabla U - \nabla(vU) - v_D \nabla U + \frac{1}{3} \nabla \cdot \nabla \frac{\partial}{\partial T} (\alpha T U)$$

We focus on the diffusivity term:

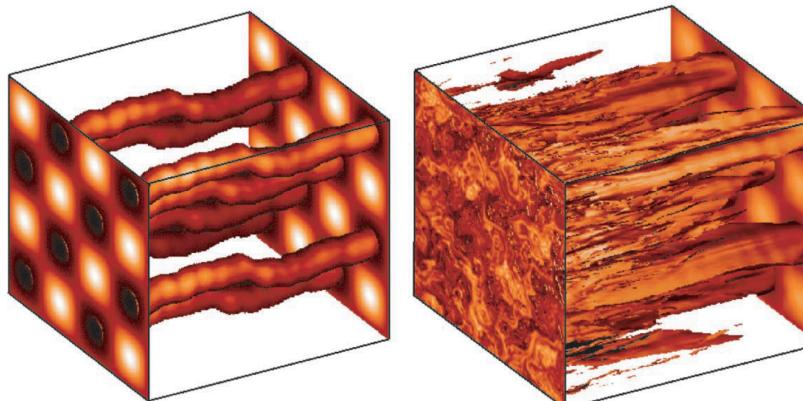
$$\kappa_{ij} = \kappa_{\perp} \delta_{ij} + \frac{B_i B_j}{B^2} (\kappa_{||} - \kappa_{\perp}) + \epsilon_{ijk} \kappa_A \frac{B_k}{B}$$

We treat the diffusion parallel and perpendicular to the magnetic field lines: [Zank+1998]

$$\lambda_{||} \propto \frac{B^{5/3}}{\langle b_s^2 \rangle} \lambda_s^{2/3} F(P, R_L, \lambda_s) \quad \kappa = \frac{1}{3} \lambda v \quad P = \frac{mv c}{Ze} \quad \lambda_{\perp} = \begin{cases} \frac{a^2}{2} \frac{\langle b_2^2 \rangle}{B^2} \lambda_{||} & \text{if } P < 10^2 MeV \\ \left( C \lambda_s \frac{\langle B'^2 \rangle}{B^2} \right)^{2/3} \lambda_{||}^{1/3} & \text{otherwise} \end{cases}$$

NB: Hypothesis of 80% 2D geometry and 20% slab geometry

[Matthaeus+1990, Bieber+1994]



[Matthaeus+2003]

# Modeling cosmic rays

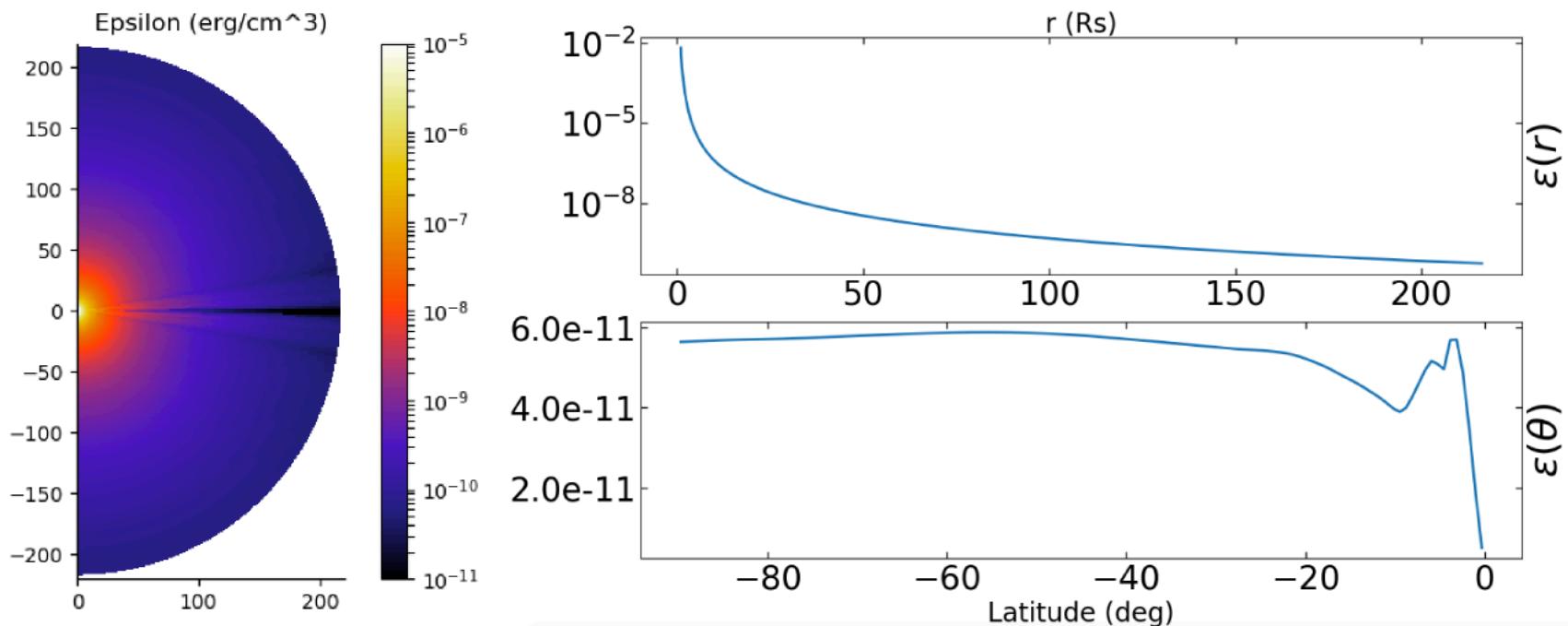
MHD models will provide directly the wind velocity and the magnetic field  
However, due to our polytropic model for the wind, we need to model the turbulence:

$$\lambda_s \propto 2B^{-1/2} \quad \langle b_s^2 \rangle = 4\langle b_2^2 \rangle = \frac{4}{5}\epsilon\pi \quad \epsilon \approx 0.0104B^{1.25}J^{0.166}v_P^{-0.123}$$

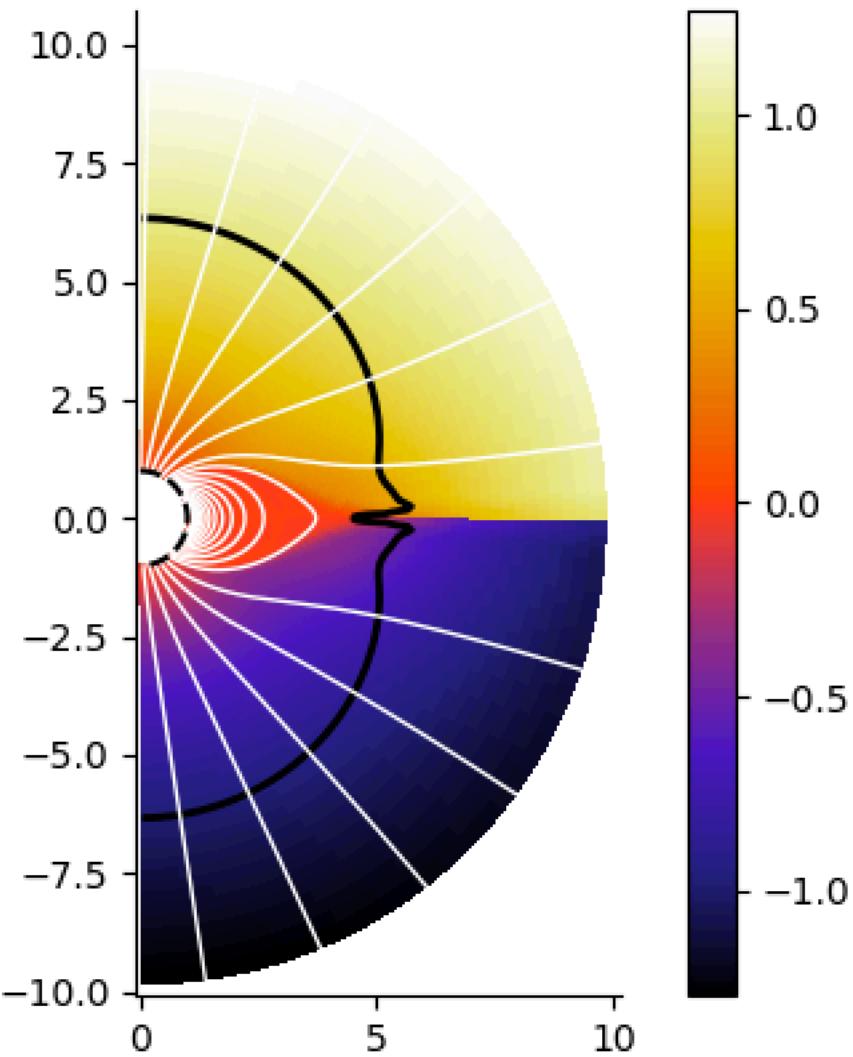
[Spruit 1981]

[Chhiber+2017]

[Réville+2020]



# Reference Case



We solve the ideal MHD equations up to 1 AU  
using the multi-physics code PLUTO with a  
polytropic wind model

[Mignone+2007, Réville+2015a, Perri+2018]

First we perform a 2.5D parameter study on  
reference cases

Wind reference case D1:

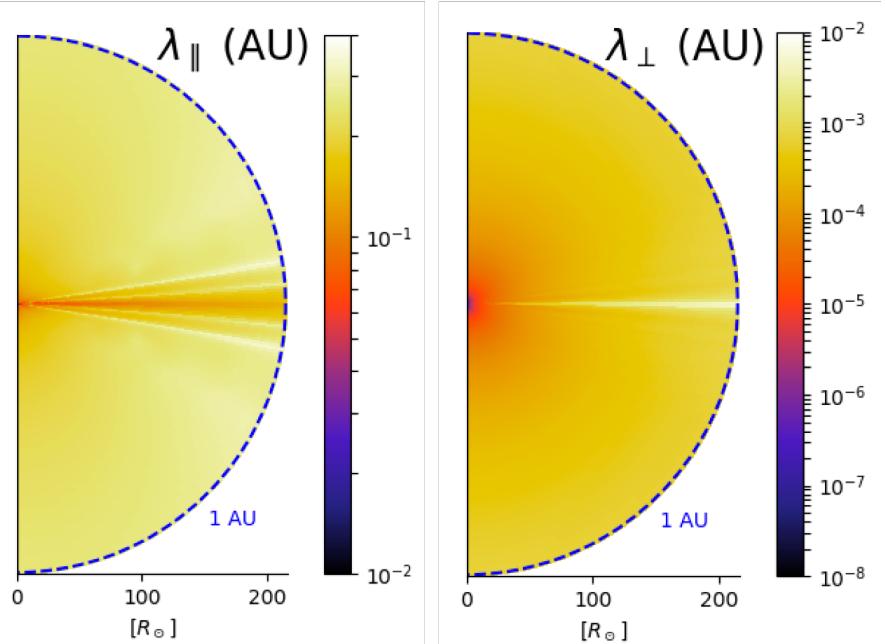
$$\rho_0 = 1.67 \times 10^{-16} g.cm^{-3} \Rightarrow n = 1.0 \times 10^8 cm^{-3}$$
$$\frac{v_{rot}}{v_{esc}} = 2.93 \times 10^{-3} \Rightarrow \Omega_0 = 2.6 \times 10^{-6} s^{-1}$$
$$\gamma = 1.05, \frac{c_s}{v_{esc}} = 0.243 \Rightarrow T = 1.5 \times 10^6 K$$
$$\frac{v_A}{v_{esc}} = 0.176 \Rightarrow B_0 = 0.5 G$$

→ D1 = Dipole with low amplitude

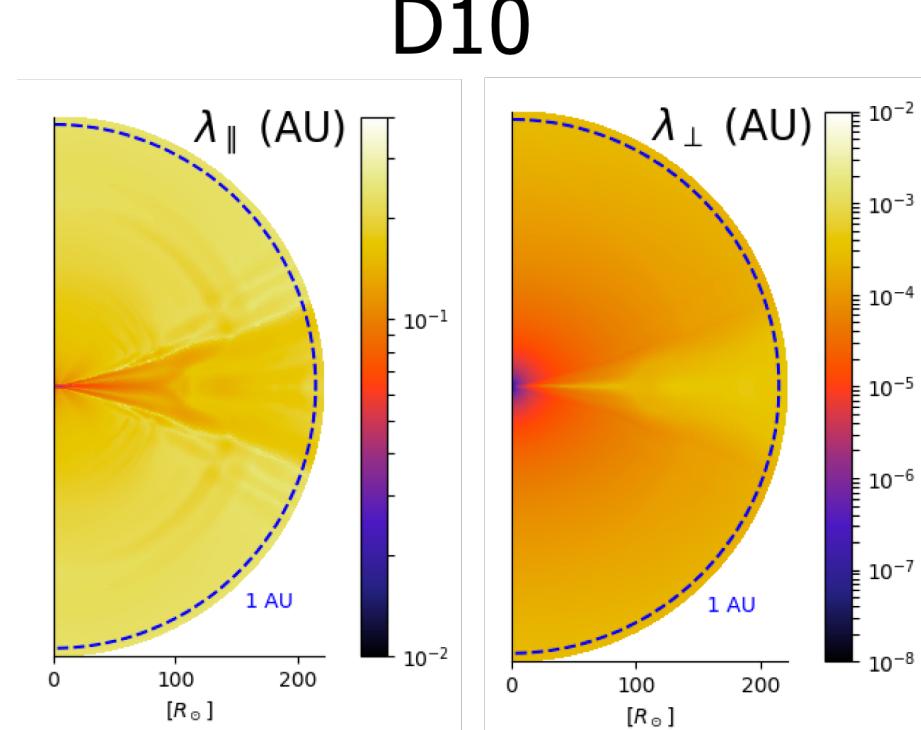
# Impact of amplitude

Two dipoles with different amplitudes:  $B_0 = 0.5G$  for D1 &  $B_0 = 5G$  for D10

D1



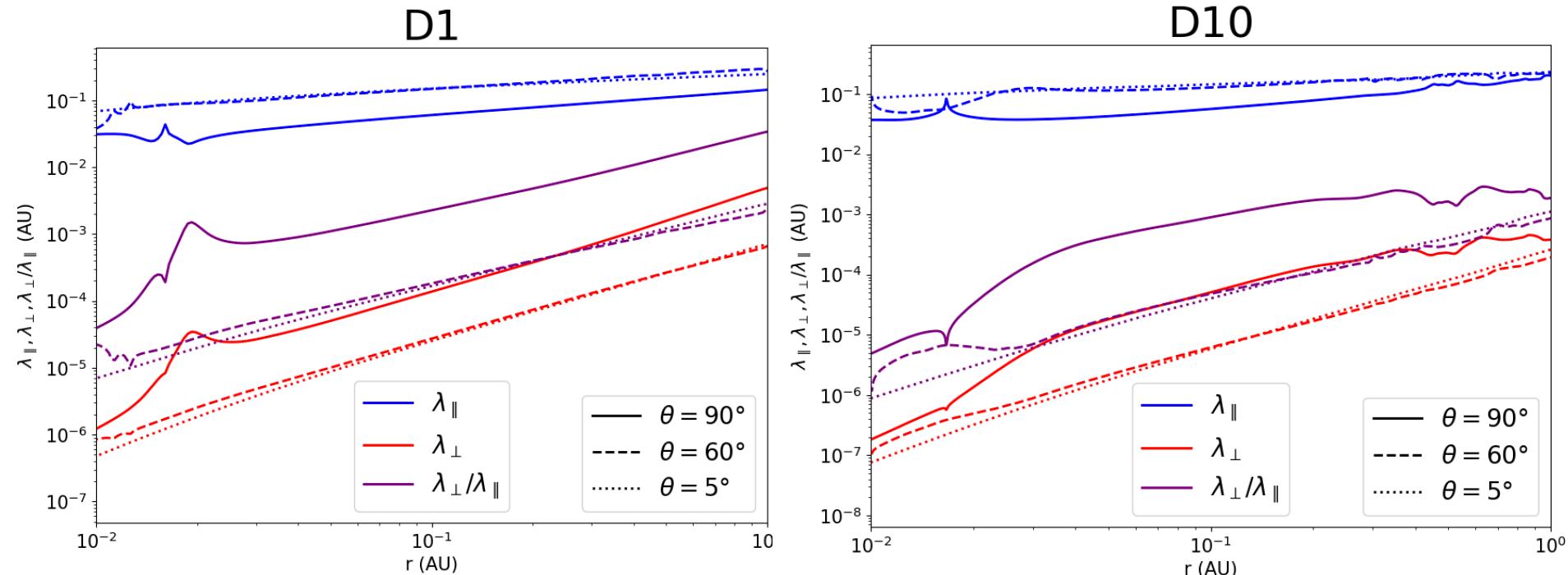
D10



→ Increase of the spread of the current sheet, so wider diffusion zone with stronger field

# Impact of amplitude

Two dipoles with different amplitudes:  $B_0 = 0.5G$  for D1 &  $B_0 = 5G$  for D10

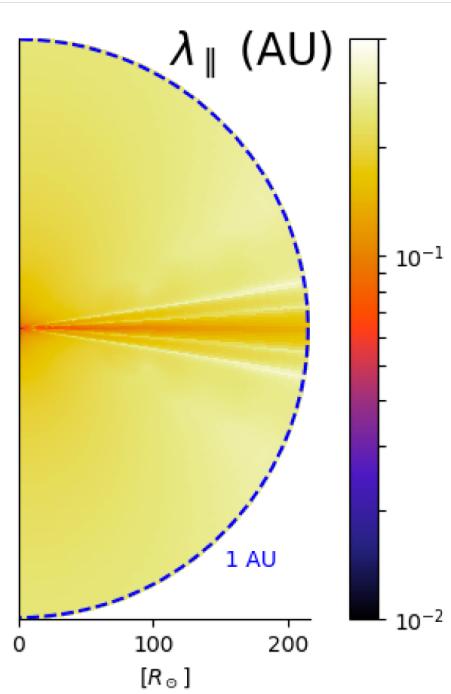


→ Higher parallel diffusion with higher amplitude  
→ Lower perpendicular diffusion

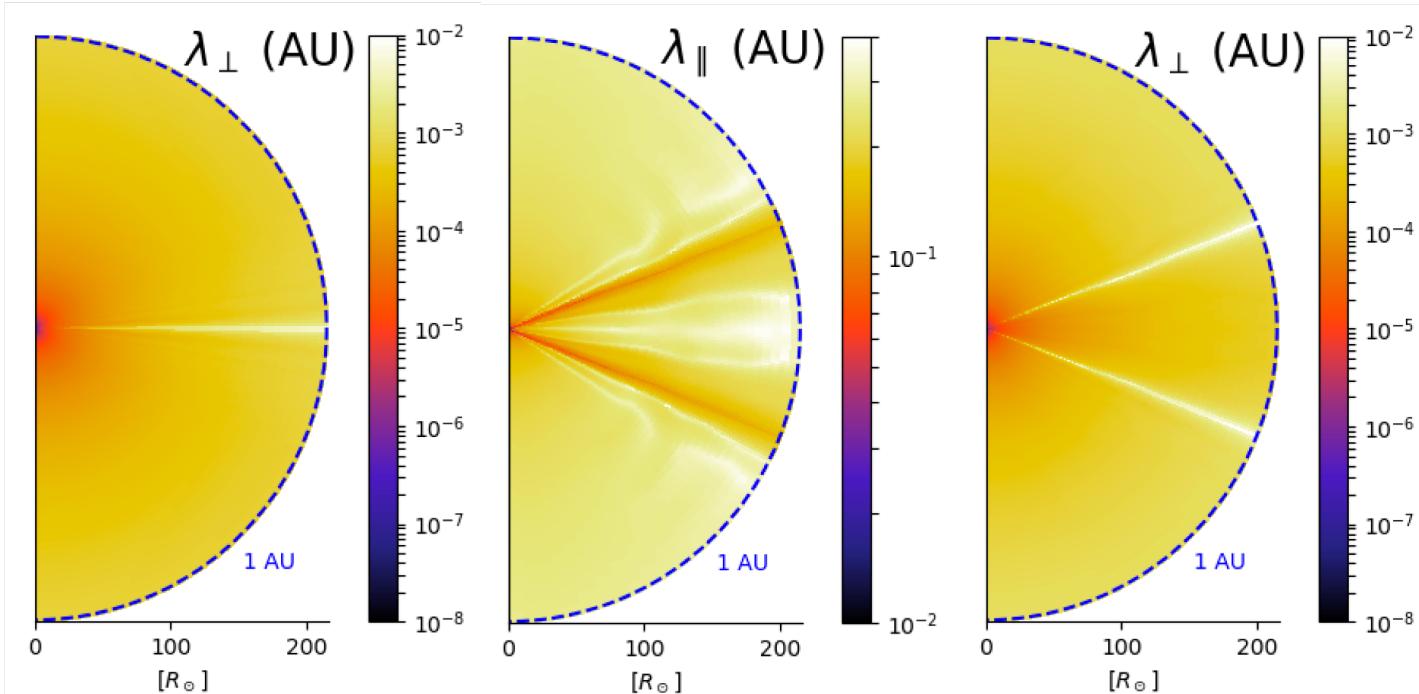
# Impact of topology

Dipole vs quadrupole for D1 and Q1, but same amplitude

D1



Q1

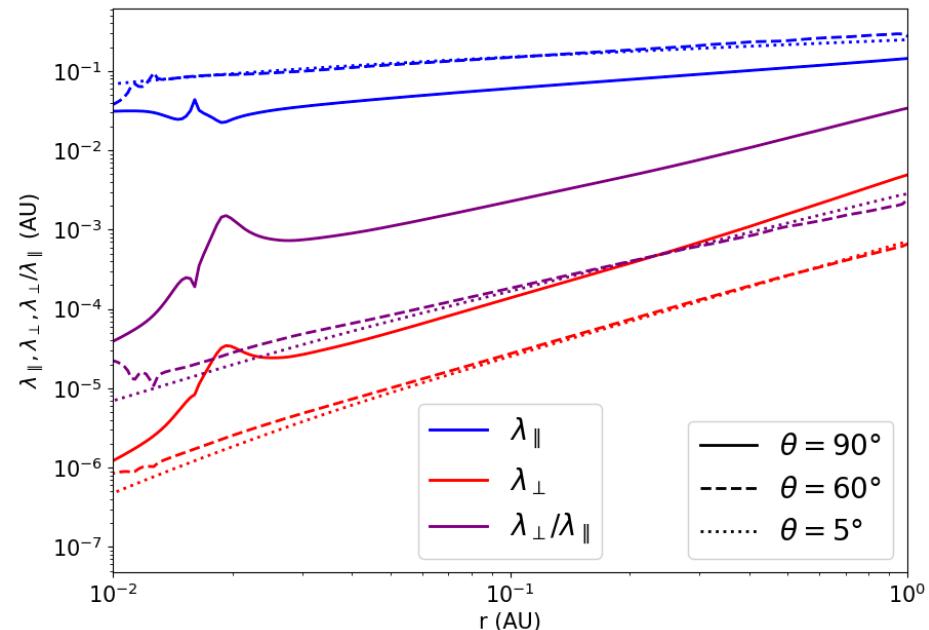


→ Different positions of the current sheets, so different latitudinal distribution

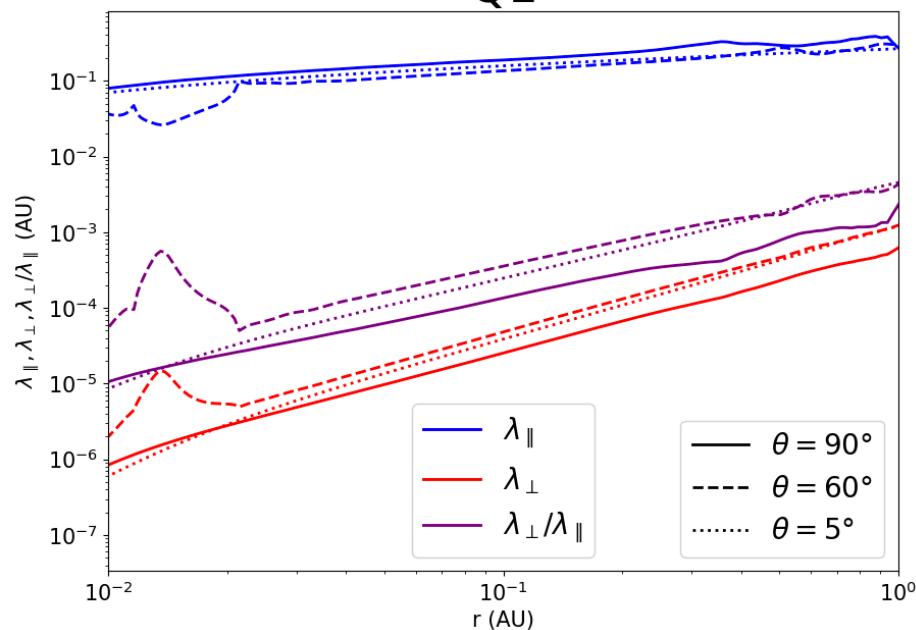
# Impact of topology

Dipole vs quadrupole for D1 and Q1, but same amplitude

D1



Q1

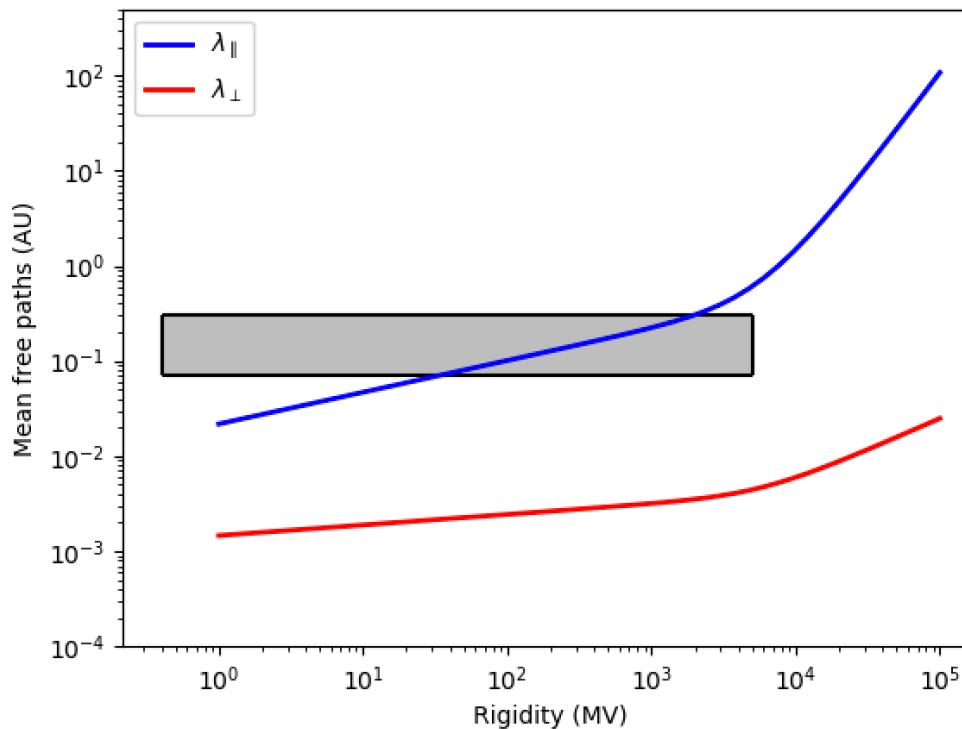


→ The amplitude is not affected

# Impact of energy

Diffusion depending on the energy of the particle → difference between SEPs and GCRs

D1

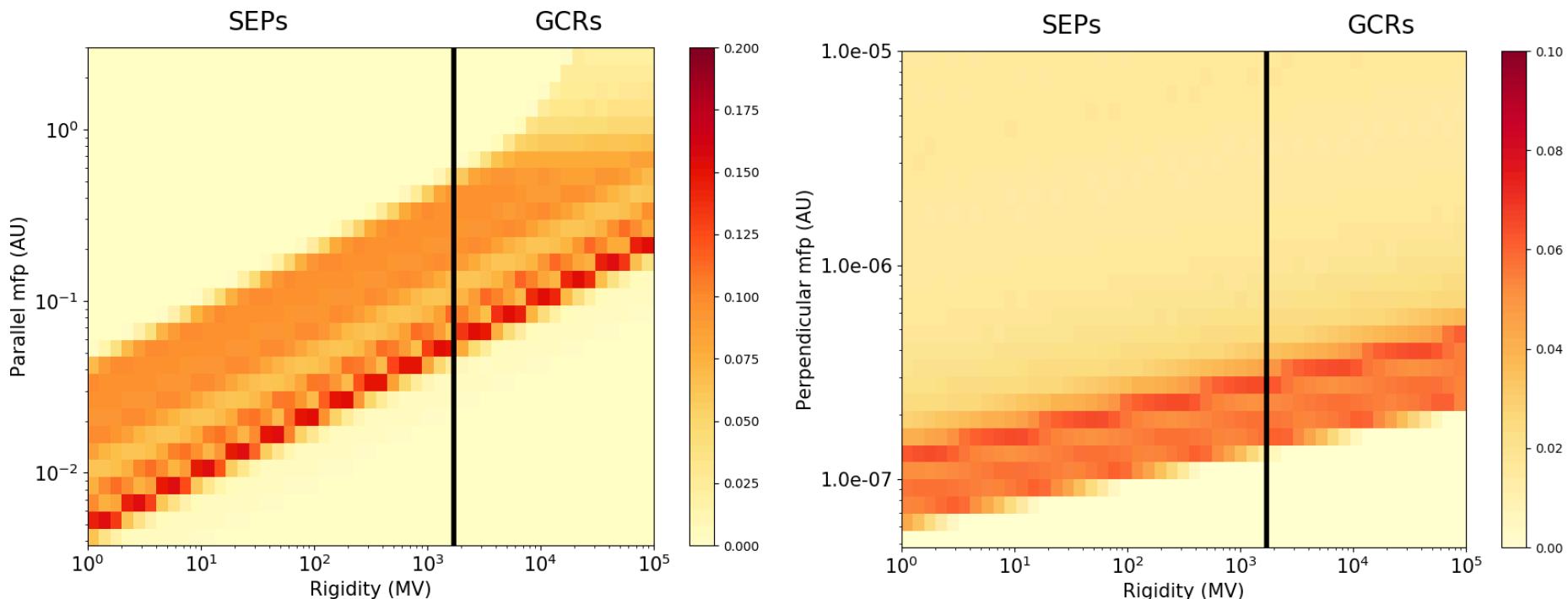


[Palmer 1982]

→ 1D cuts show that we are in agreement with observations, especially the Palmer consensus

# Impact of energy

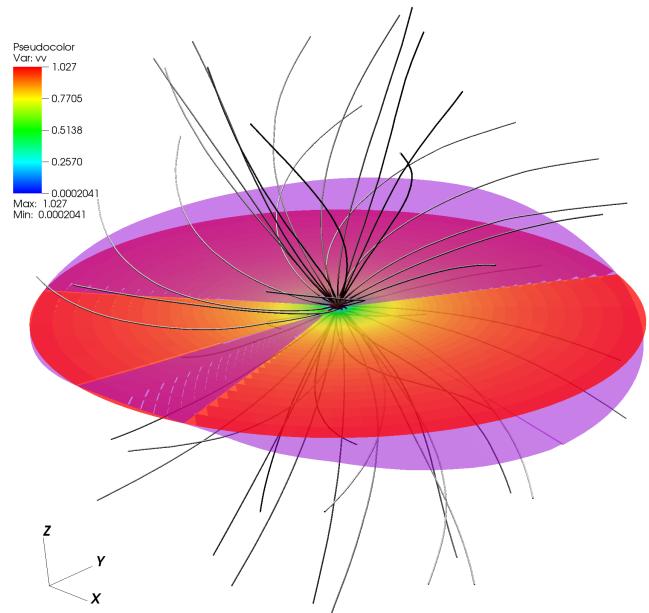
Diffusion depending on the energy of the particle → difference between SEPs and GCRs



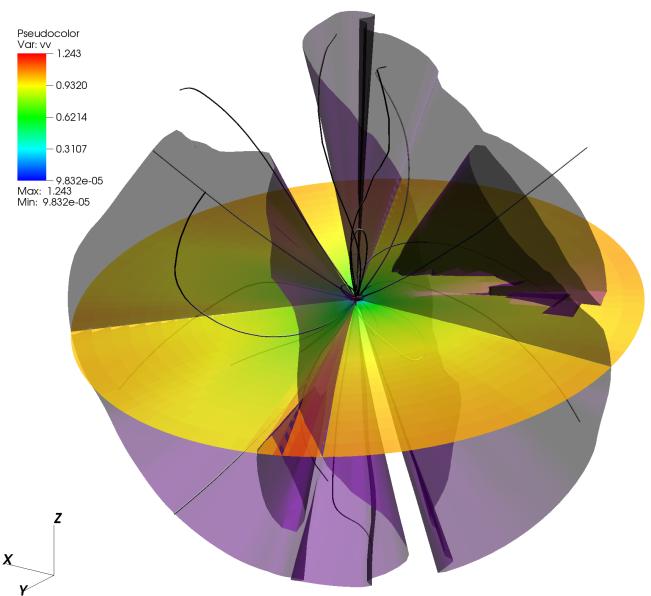
→ Compilations of 1D histograms per energy show a drift of the peak value, and we see that we have a bigger spread in diffusion for SEPs

# Realistic solar configurations

Minimum



Maximum

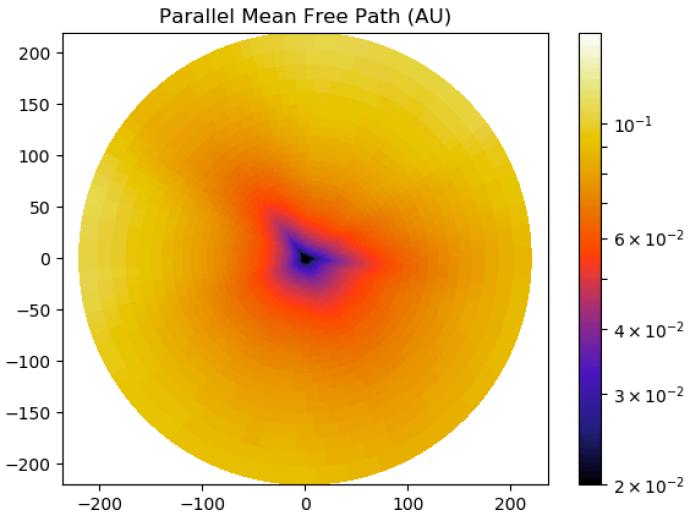


[Réville & Brun 2017]

Minimum and maximum  
of activity in 3D  
→ Mix of dipole and  
quadrupole at various  
amplitudes

# Realistic solar configurations

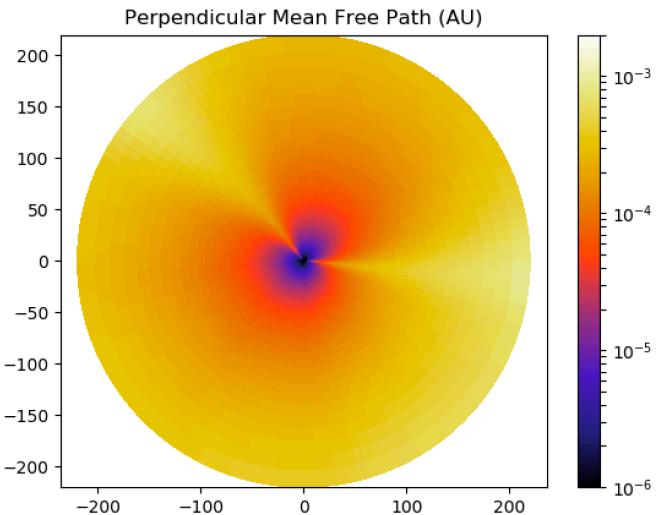
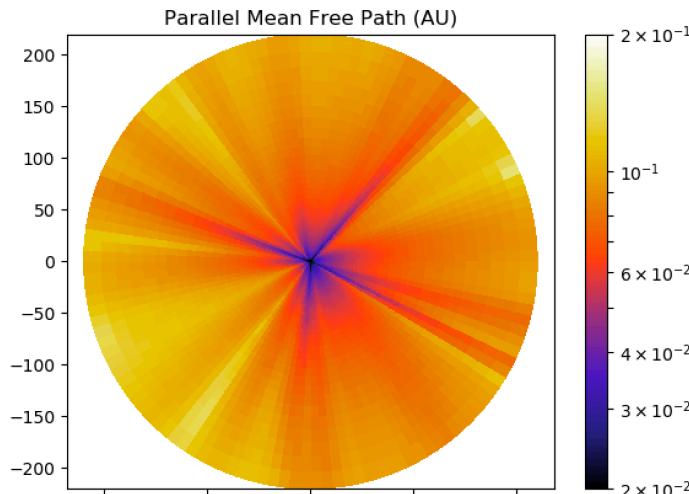
Minimum



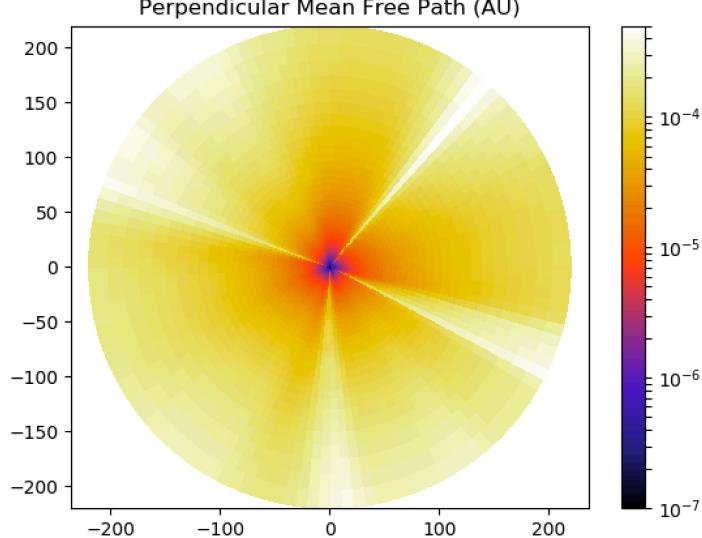
[Réville & Brun 2017]

Minimum and maximum  
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→ Mix of dipole and  
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Maximum

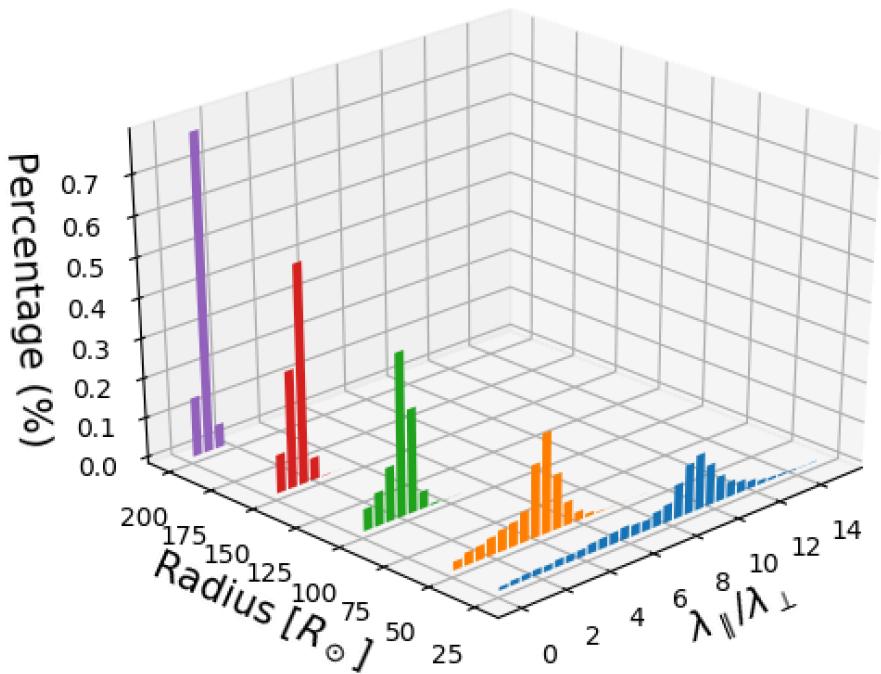


→ 3D maps of parallel  
diffusion coefficient  
from 3D wind  
simulations

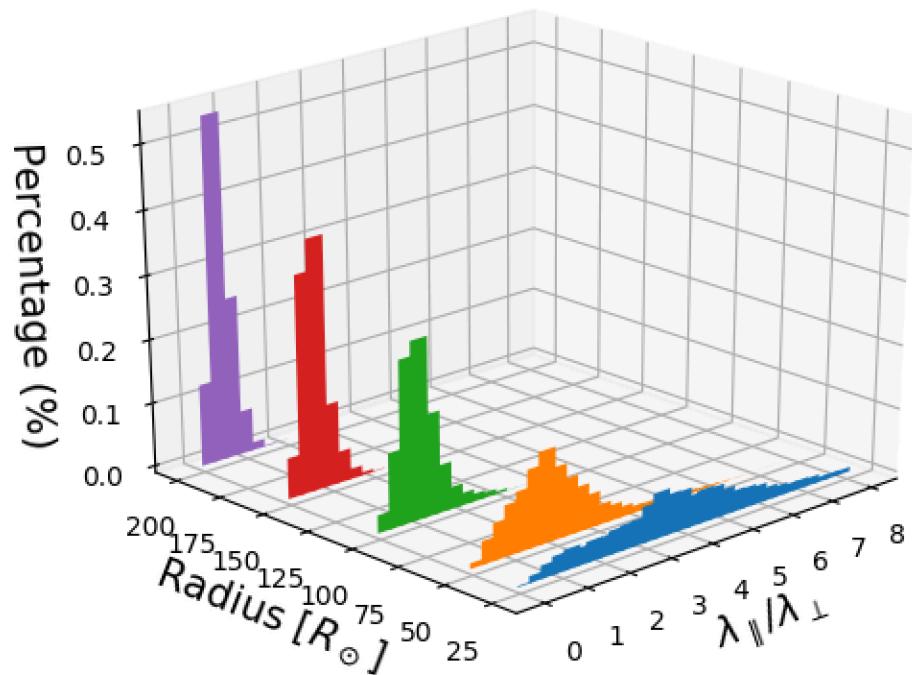


# Realistic solar configurations

Minimum



Maximum



→ Histograms show different behaviors with the distance to the Sun, especially at minimum of activity

# Conclusions and Perspectives

## Conclusions:

- Implementation of the parallel and perpendicular diffusion in post-process of polytropic wind simulations
- Study of the impact of amplitude, topology and energy
- Application to real configurations in 3D
  - Impact of amplitude on radial gradients, topology on latitudinal gradients
  - GCRs have more spread distribution in diffusion than SEPs
  - More difference in diffusion with the distance to the Sun in minimum of activity

## Perspectives:

- Addition of the drift coefficient in diffusion
- Alfvén-wave driven wind model
- Solver for the full Fokker-Planck equation

## To read more:

- Article published in the topical issue of JSWSC “Space climate: The past and future of solar activity”: <https://doi.org/10.1051/swsc/2020057>
- Results of the simulations available for visualization on the MEDOC facility :  
[https://idoc.ias.u-psud.fr/wind\\_predict\\_cr/](https://idoc.ias.u-psud.fr/wind_predict_cr/)