

Pacific CO₂ fluxes pattern analysis through SST clustering

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Jerry TJIPUTRA



Outline

1 Context

2 Data & Methods

3 Results

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CONSTRAINT the GCM uncertainties to obtain a better estimate of future climate change projections :

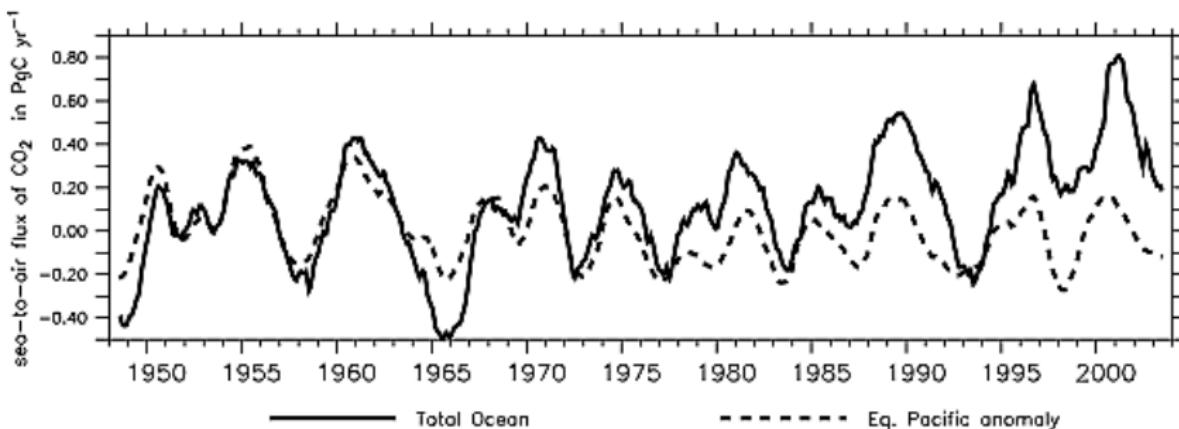
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CONSTRAINT the GCM uncertainties to obtain a better estimate of future climate change projections : future CMIP6 models spread of **CARBON UPTAKE**.

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[WETZEL *et al.*, 2005]



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Constraint the **VARIABILITY** of CMIP6 models carbon uptake by using its the relationship with ENSO [FEELY *et al.*, 2006].

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One way to study spatial pattern thanks to **STATISTICAL CLUSTERING**.

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**Aim : analyse carbon uptake pattern
thanks SST clustering.**

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Monthly **OBSERVATIONS** over pacific basin

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**Clustering (regrouping) applied to
SST-based NINO3, NINO4 and PDO.**

Gaussian mixture model

Approximate the distribution of a datafield x as a weighted sum of K (the number of cluster or groups) Gaussian distribution f_k [PEARSON, 1894; McLACHLAN & PEEL, 2000] :

$$f(x) = \sum_{k=1}^K \pi_k f_k(x; \alpha_k)$$

where π_k is the mixture ratio.

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Each monthly field is assigned to one cluster C_k (represented by f_k) by applying the principle of *posterior* maximum :

$$C_k = \{\mathbf{x}; \pi_k f_k(\mathbf{x}, \alpha_k) \geq \pi_j f_j(\mathbf{x}, \alpha_j), \forall j = 1, \dots, K\}.$$

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The **BIC** to be minimised to determine K : $BIC = -2 \log(L) + p \log(n)$, with p the number of free parameters, n the sample's size, L the likelihood.

Expectation-Maximization (EM) algorithm [DEMPSTER *et al.*, 1977]

Successive iterations (i) of the E and M steps :

EXPECTATION (E) step : for each C_k $k \in [1, \dots, K]$, and month $j \in [1, \dots, n]$:

$$\tau_k^i(x_j) = \frac{\pi_k^i f_k(x_j | \alpha_j^i)}{\sum_{k=1}^K \pi_k^i f_k(x_j | \alpha_j^i)};$$

where $\tau_k^i(x_j)$ is the posterior probability that x_j belongs to C_k at iteration i .

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MAXIMIZATION (M) step : for each C_k $k \in [1, \dots, K]$:

$$\pi_k^{i+1} = \frac{1}{n} \sum_{j=1}^n \tau_k^i(x_j);$$

which is the Maximum likelihood of the ratios.

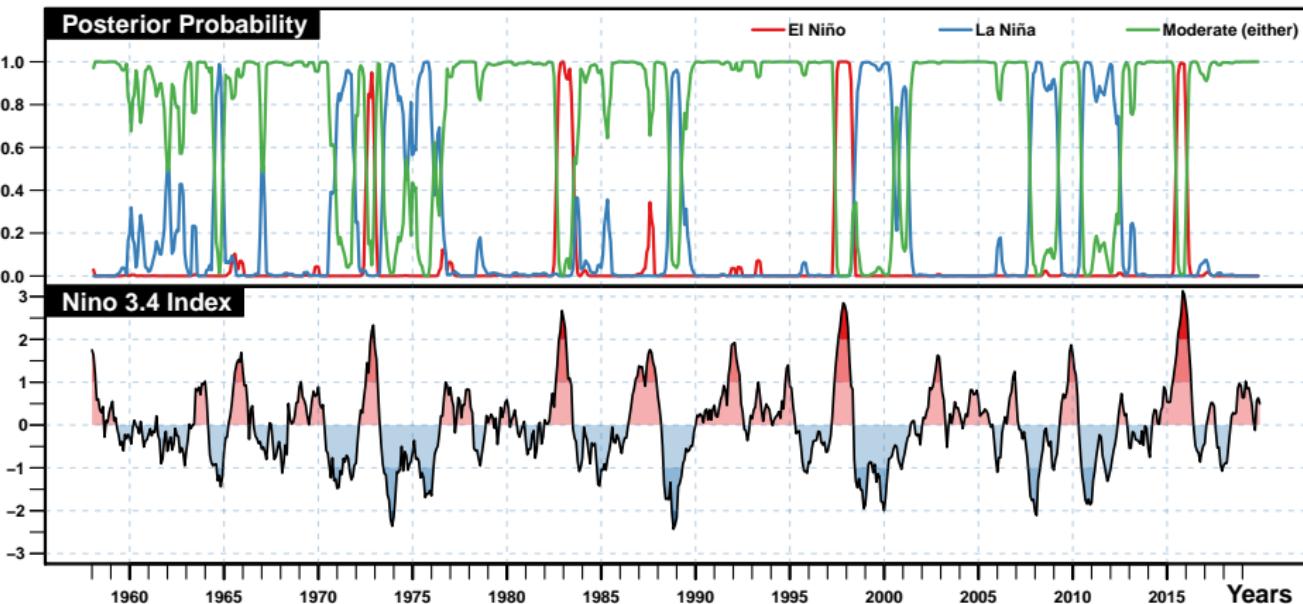
Outline

1 Context

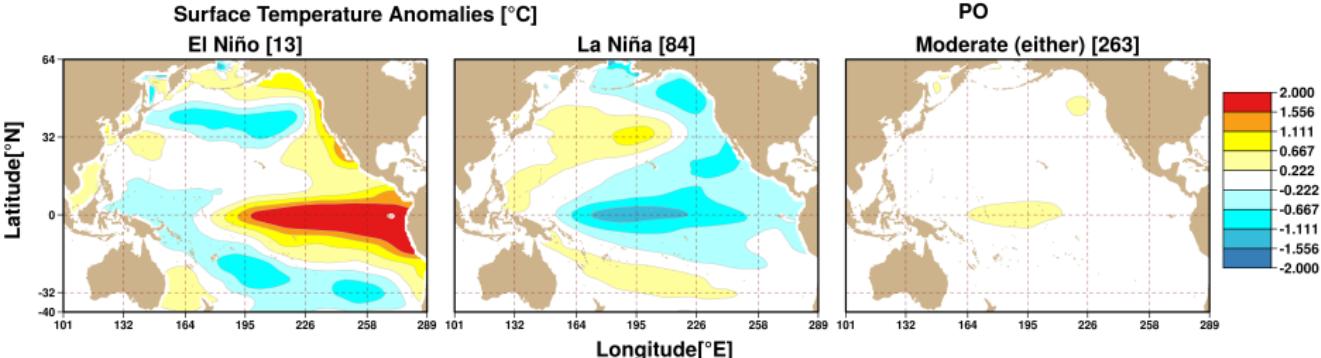
2 Data & Methods

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Clustering results



Observed patterns (1985-2014)

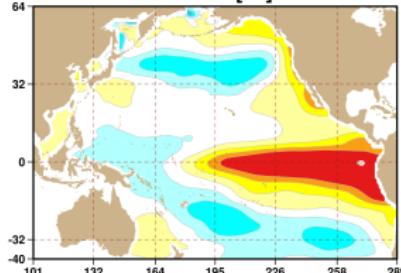


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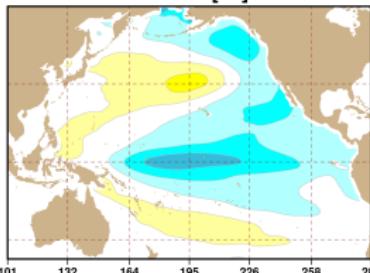
Surface Temperature Anomalies [°C]

El Niño [13]

Latitude [°N]

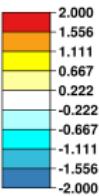
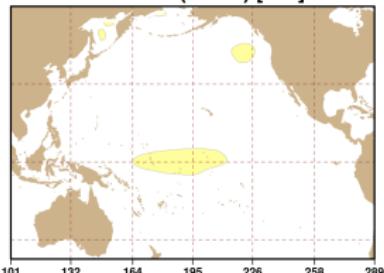


La Niña [84]



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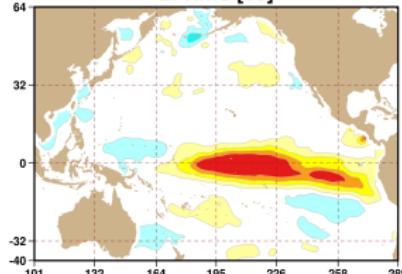
Moderate (either) [263]



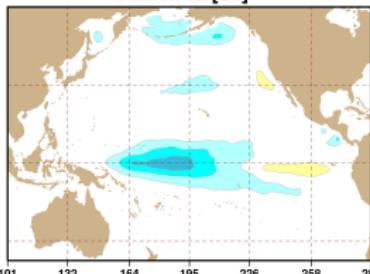
Carbone Uptake Flux fgCO_2 Anomalies [TgC.yr^{-1}]

El Niño [13]

Latitude [°N]

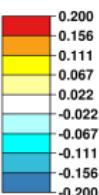
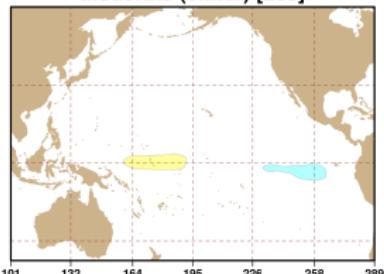


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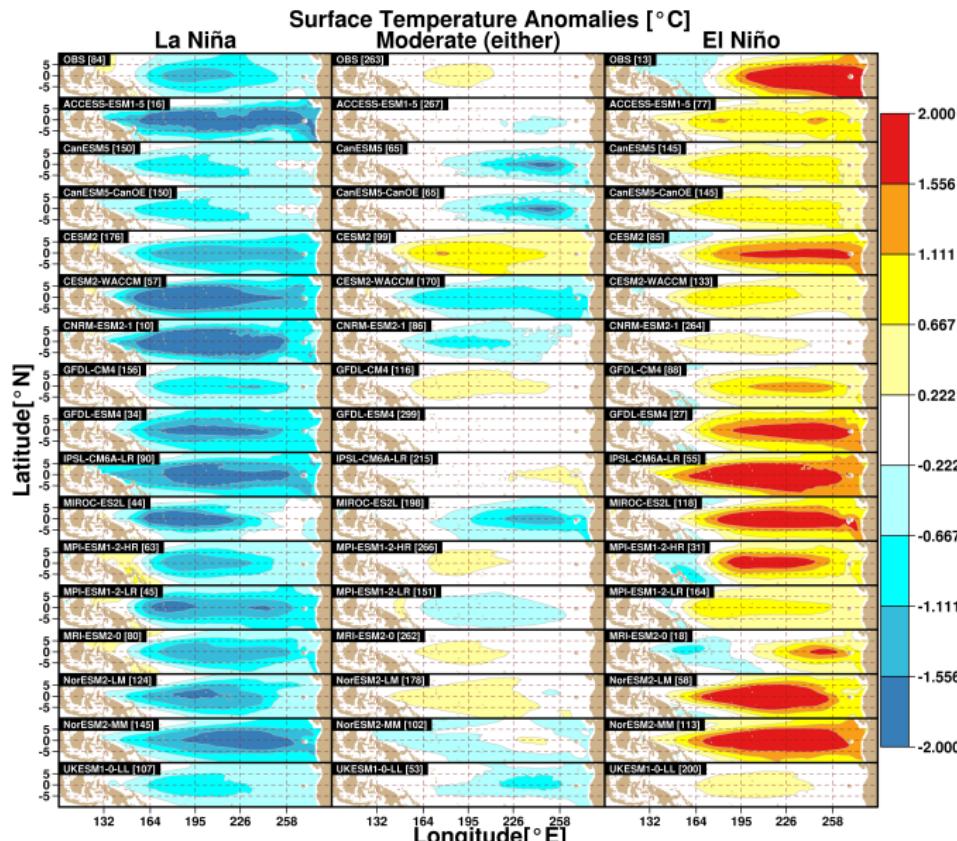


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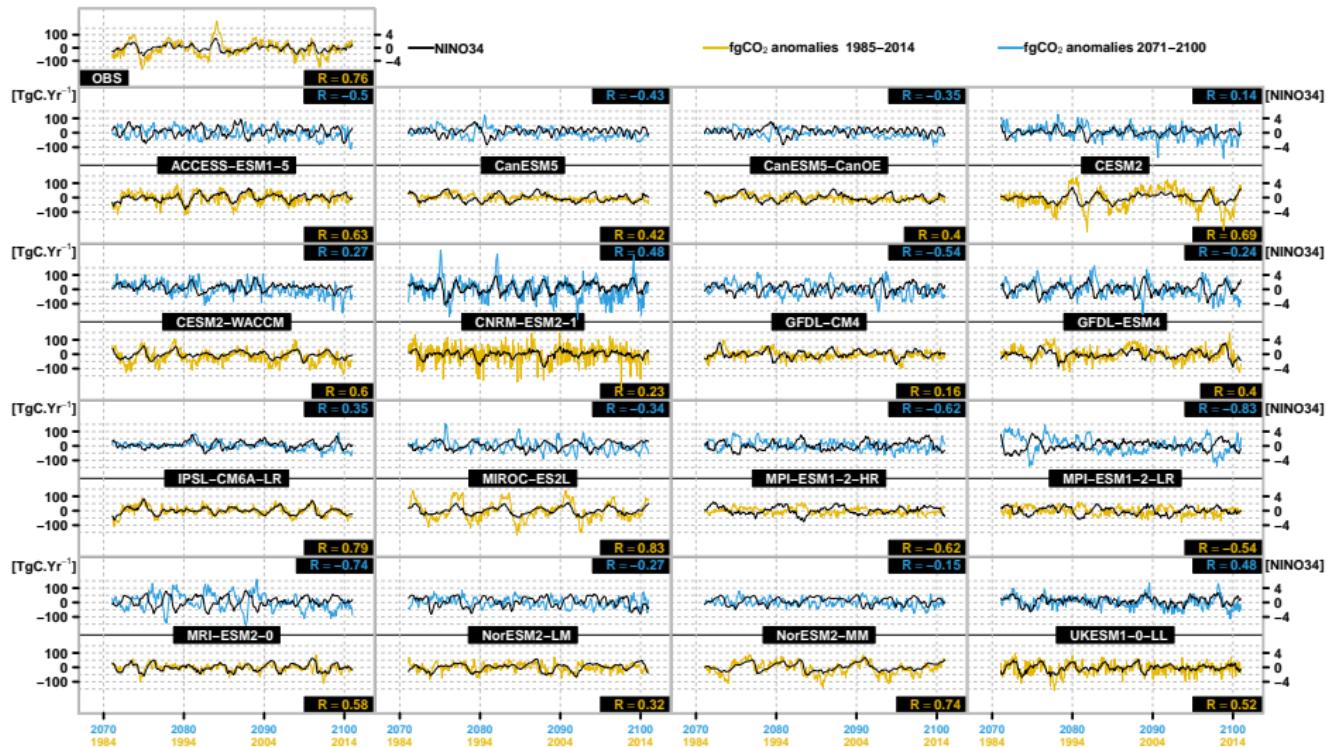
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CMIP6 patterns (1985-2014)



Results for CMIP6 : NINO34 vs. fgCO₂ anomalies



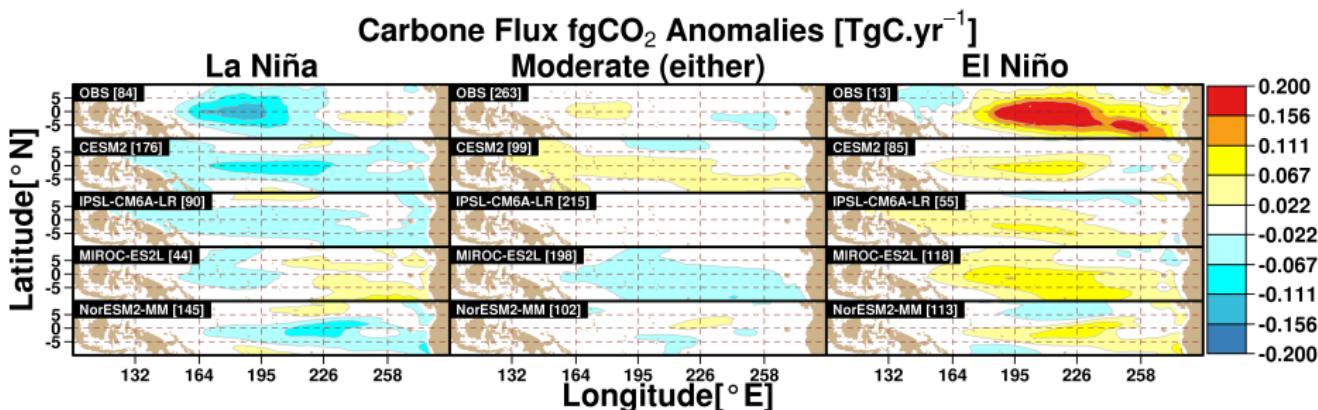
CMIP6 NINO34 vs. fgCO₂ anomalies

	Correlation fgCO ₂ vs. NINO3.4	
	1985-2014	2071-2100
OBS	.76	-
ACCESS-ESM1-5	.63	-.5
CanESM5-CanOE	.42	-.43
CanESM5	.40	-.35
CESM2	.69	.14
CESM2-WACCM	.60	.27
CNRM-ESM2-1	.23	.48
GFDL-CM4	.16	-.54
GFDL-ESM4	.40	-.24
IPSL-CM6A-LR	.79	.35
MIROC-ES2L	.83	-.34
MPI-ESM1-2-HR	-.62	-.62
MPI-ESM1-2-LR	-.54	-.83
MRI-ESM2-0	.58	-.74
NorESM2-LM	.32	-.27
NorESM2-MM	.74	-.15
UKESM1-0-LL	.52	.48

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CMIP6



CMIP6 fgCO_2 anomalies vs. NINO3.4/ $P_{\text{CO}_2}^{\text{nt}}$ anomalies

NON-THERMAL $P_{\text{CO}_2}^{\text{nt}} = P_{\text{CO}_2} \exp(\gamma_T(<\text{SST}> - \text{SST}))$,

γ_T : CO₂ temperature sensitivity ($4.23\% \cdot {}^\circ\text{C}^{-1}$), $<\text{SST}>$: long-term mean SST
[LANDSCHÜTZER *et al.*, 2018].

CMIP6 fgCO₂ anomalies vs. NINO3.4/P^{nt}_{CO₂} anomalies

	Correlation fgCO ₂ vs.			
	NINO3.4		Non-thermal P ^{nt} _{CO₂}	
	1985-2014	2071-2100	1985-2014	2071-2100
OBS	.76		-.85	
ACCESS-ESM1-5	.63	-.5	-.38	.37
CanESM5-CanOE	.42	-.43	-.33	.18
CanESM5	.40	-.35	-.34	.14
CESM2	.69	.14	-.3	-.28
CESM2-WACCM	.60	.27	-.28	-.29
CNRM-ESM2-1	.23	.48	-.01	-.60
GFDL-CM4	.16	-.54	-.02	.38
GFDL-ESM4	.40	-.24	-.16	-.04
IPSL-CM6A-LR	.79	.35	-.24	-.28
MIROC-ES2L	.83	-.34	-.36	.31
MPI-ESM1-2-HR	-.62	-.62	.20	.17
MPI-ESM1-2-LR	-.54	-.83	.09	.31
MRI-ESM2-0	.58	-.74	-.54	.31
NorESM2-LM	.32	-.27	-.09	.02
NorESM2-MM	.74	-.15	-.27	.05
UKESM1-0-LL	.52	.48	-.32	-.29

**Thank you for your
attention !!**

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