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Additional information

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Hydro-mechanical fault model

- Quasi-static equilibrium

$$\tau(x, t) = \tau^o - \frac{E_p}{4\pi} \int_{a_-(t)}^{a_+(t)} \frac{\partial \delta(\zeta, t)/\partial \zeta}{\zeta - x} d\zeta$$

- Constitutive law for frictional slip

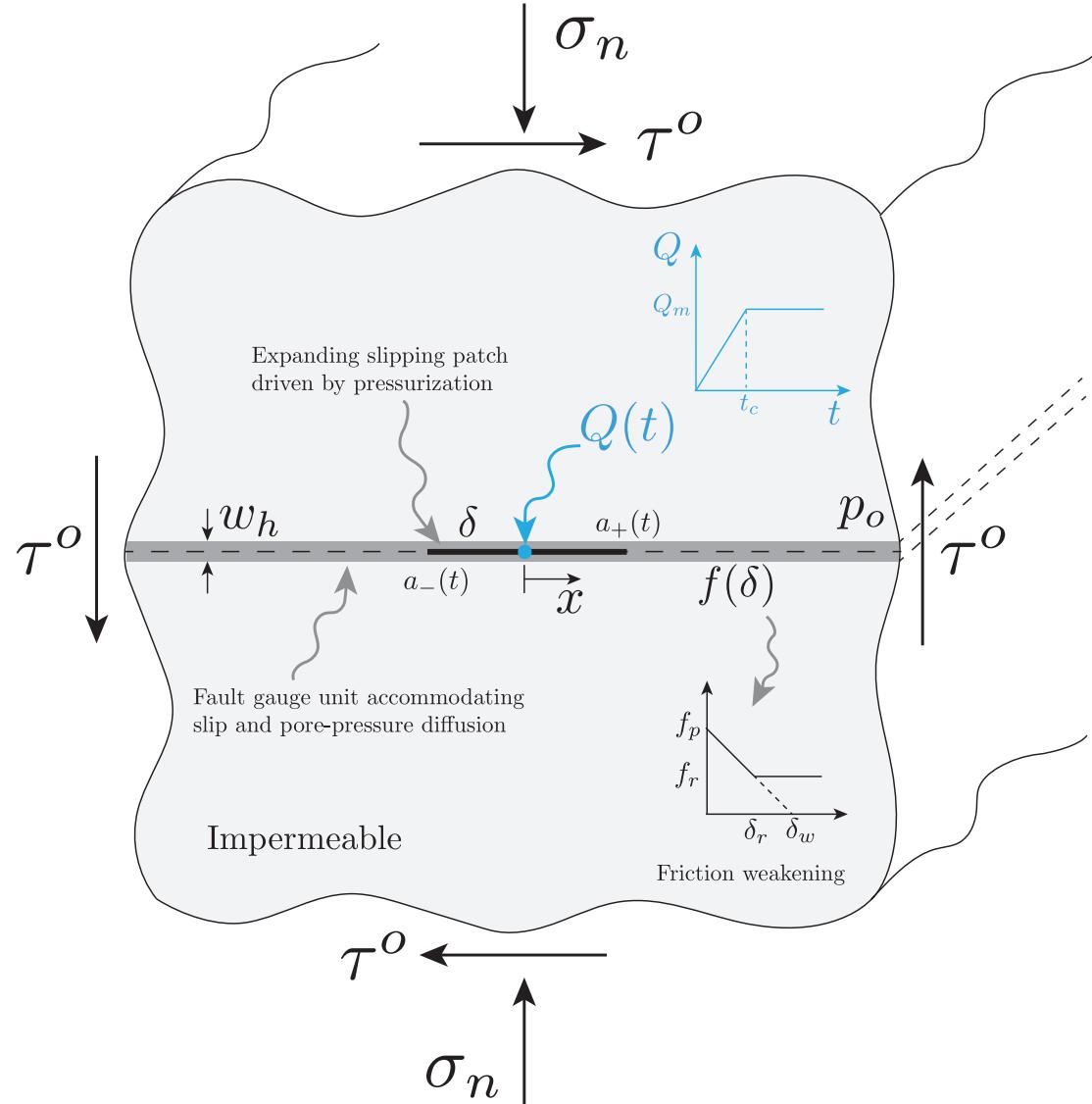
$$\tau(x, t) = f(\delta) (\sigma_n - p(x, t)), \quad |x| \leq a(t)$$

- Along-fault pore-pressure diffusion

$$w_h c_f \frac{\partial \bar{p}}{\partial x} + \frac{\partial w_h v}{\partial x} = 0, \quad v = -\frac{k_f}{\mu} \frac{\partial \bar{p}}{\partial x}$$

$$w_h v = \pm \frac{Q(t)}{2}, \quad \text{at } x = 0^\pm$$

$$Q(t) = \begin{cases} \frac{Q_m}{t_c} \cdot t & t \leq t_c \\ Q_m & t > t_c \end{cases}$$





Dimensionless governing parameters

Upon introduction of the following characteristic scales in the governing equations

$$\tau(x, t) = \underbrace{f_p \sigma'_o}_{\tau_p} \cdot \mathcal{T}(x, t) \quad \delta(x, t) = \delta_w \cdot \Delta(x, t) \quad \bar{p}(x, t) = \sigma'_o \cdot \Pi(x, t)$$

$x = a_w \cdot \mathcal{X}$ $t = t_w T$

Slipping patch length-scale ↪ ↤ Diffusion time-scale

$$a_w = \frac{E_p}{2\tau_p} \delta_w \quad t_w = \frac{a_w^2}{4\alpha}$$

$$(\mathcal{T}(\mathcal{X}, \mathcal{T}), \Delta(\mathcal{X}, \mathcal{T}), \Pi(\mathcal{X}, \mathcal{T})) = \mathcal{F}\left(\frac{\tau^o}{\tau_p}, \frac{f_r}{f_p}, \frac{Q_m}{Q^*}, \frac{t_c}{t_w}\right)$$

$$Q^* = \frac{2\sigma'_o w_h k_f}{a_w \mu}$$

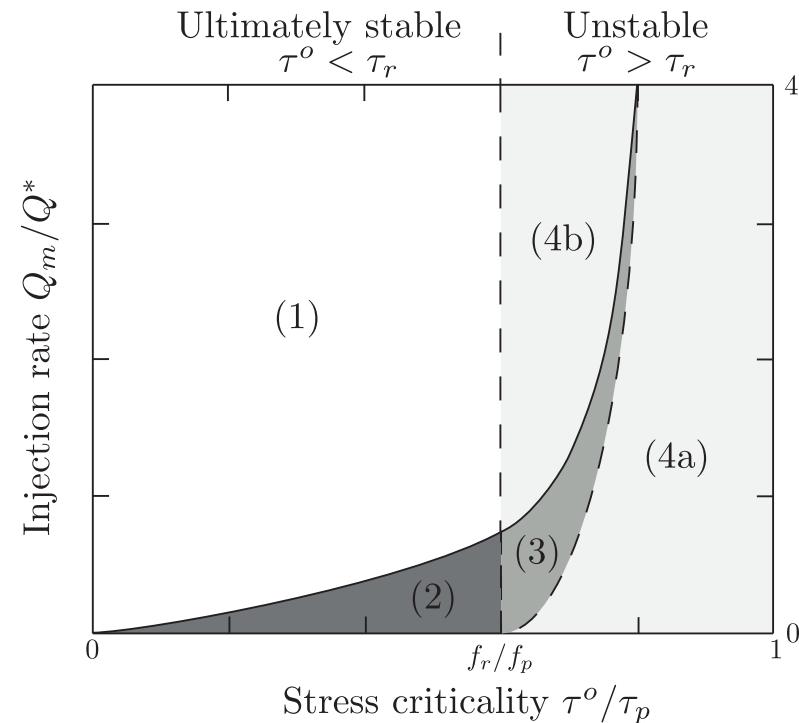
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Ultimately Stable fault ($\tau^o < \tau_r$) - $\frac{t_c}{t_w} \ll 1$

$t_c \ll t_w \ll t_n$ Hydro-mechanical response is governed by constant injection rate
 → Recover [Garagash & Germanovich, *JGR*, 2012] solution

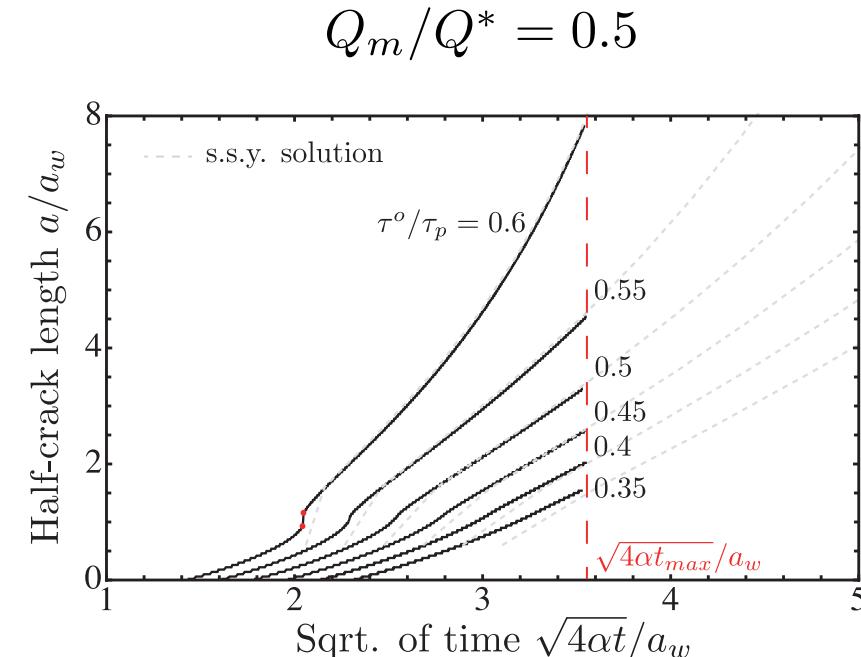
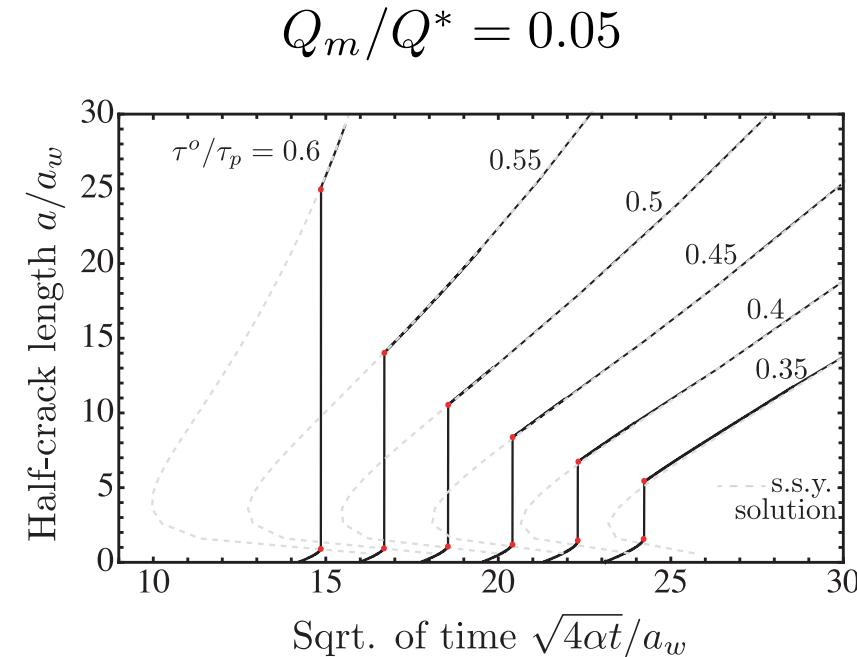
- (1) Aseismic slip only
- (2) Nucleation and arrest of a dynamic event
- (3) Nucleation, arrest and re-nucleation of unabated event
- (4a) Unabated dynamic event not affected by f_r
- (4b) Unabated dynamic event affected by f_r



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Ultimately Stable fault ($\tau^o < \tau_r$) - $\frac{t_c}{t_w} \ll 1$ (cont'd)



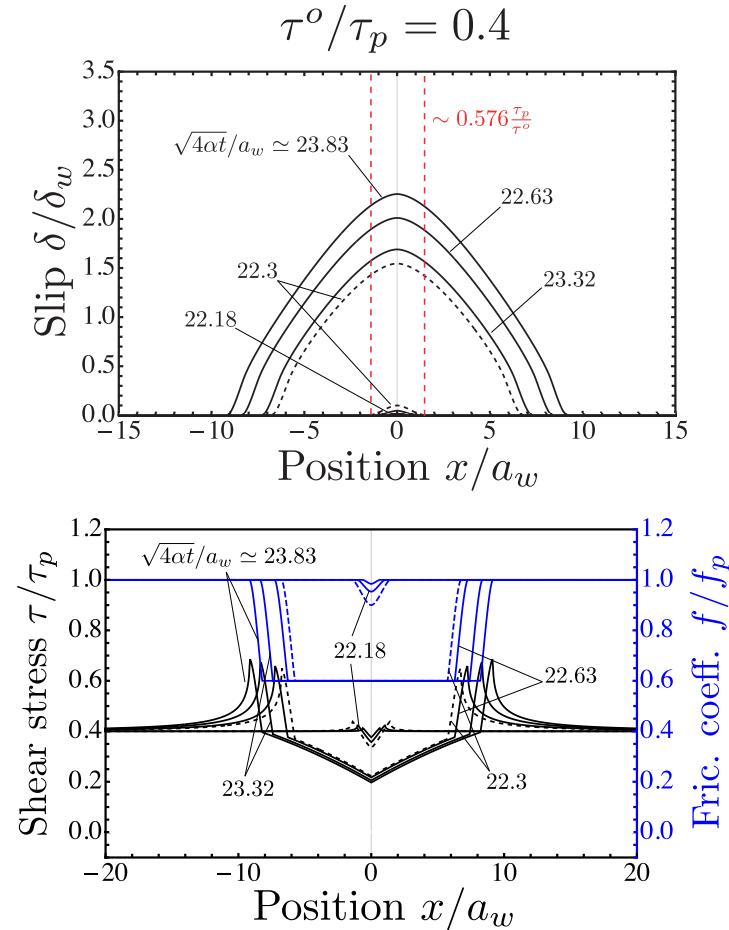
$$f_r/f_p = 0.6 \quad t_c/t_w = 0.01$$

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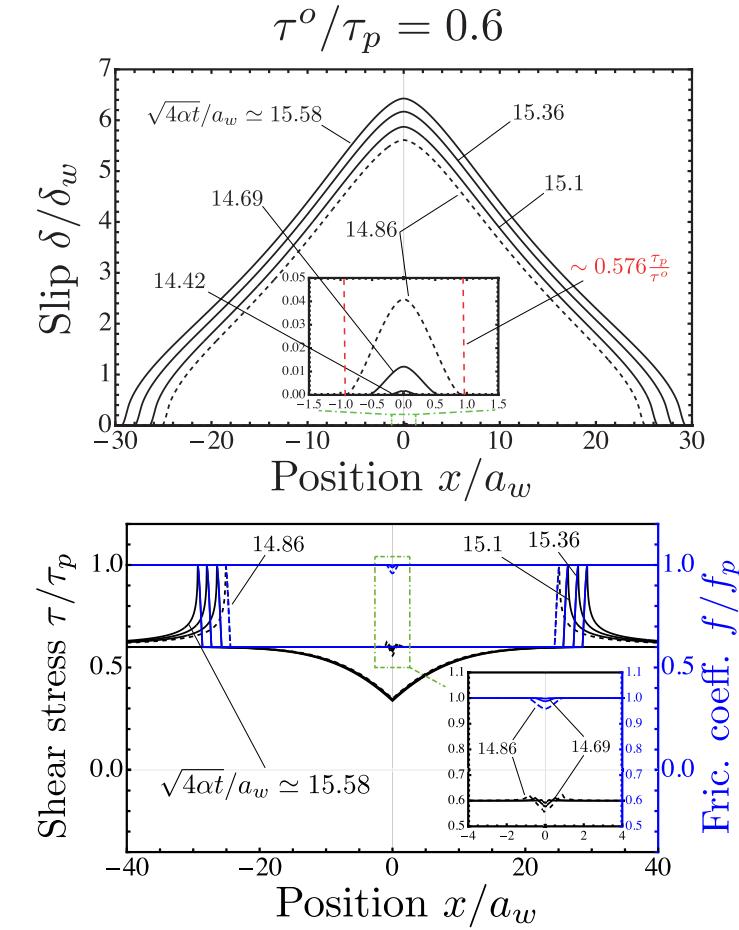
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Ultimately Stable fault ($\tau^o < \tau_r$) - $\frac{t_c}{t_w} \ll 1$

$$\frac{Q_m}{Q^*} = 0.05$$



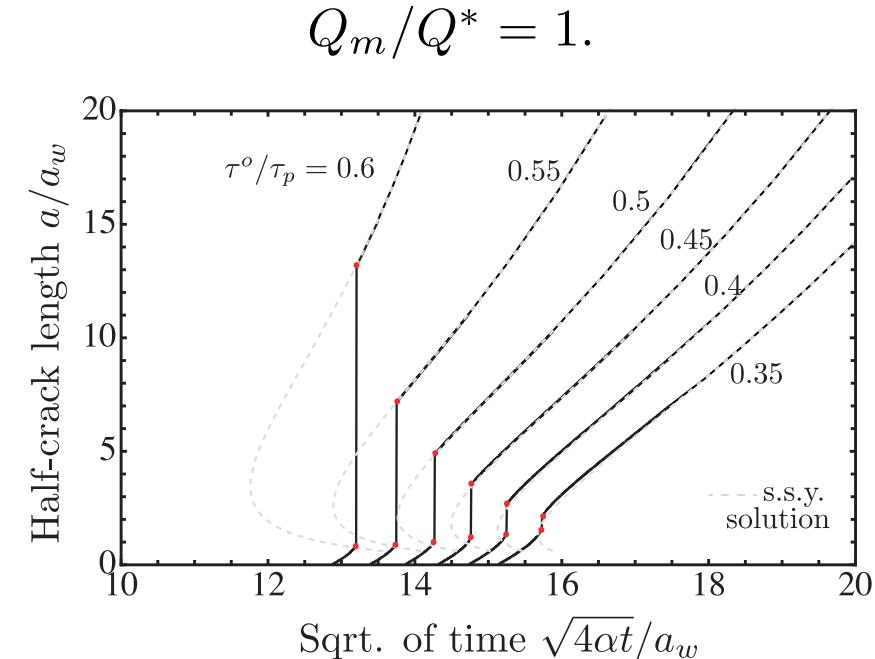
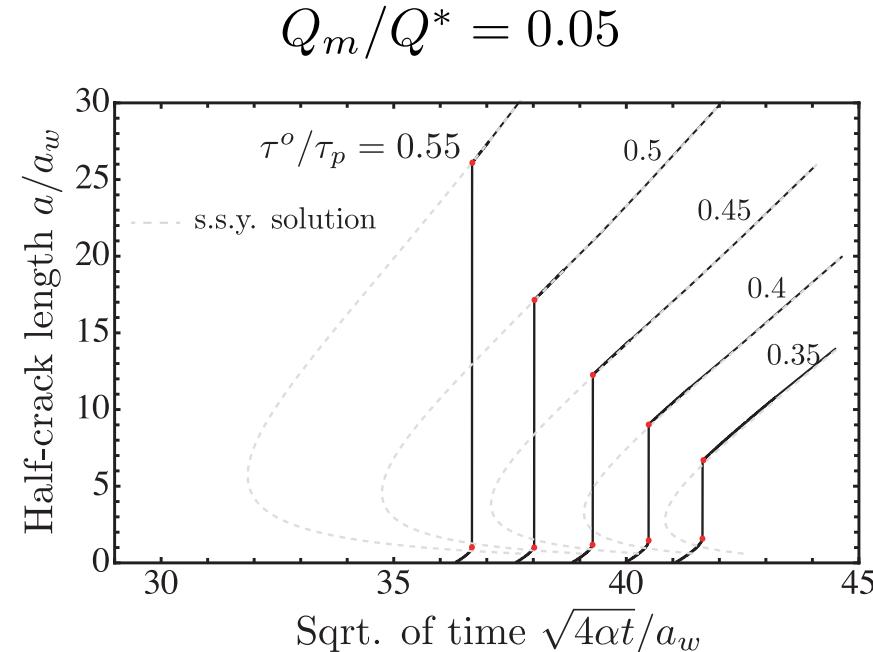
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Ultimately Stable fault ($\tau^o < \tau_r$) - $\frac{t_c}{t_w} \gg 1$

$$t_n \sim t_c \gg t_w$$



$$f_r/f_p = 0.6$$

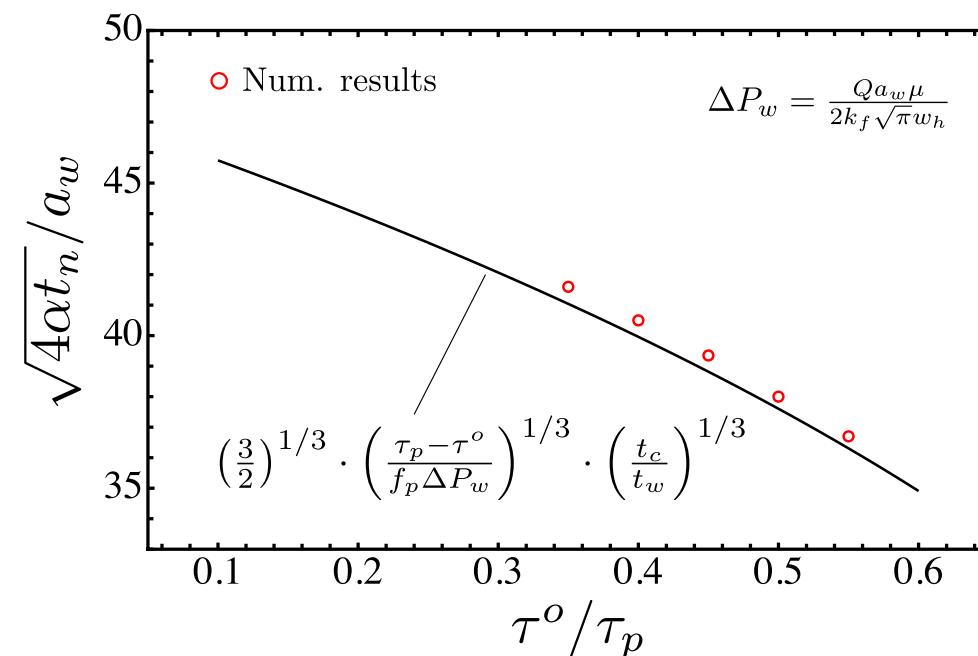
$$t_c/t_w = 2000.$$

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Ultimately Stable fault ($\tau^o < \tau_p$) - $\frac{t_c}{t_w} \gg 1$ (cont'd)

Asymptotic solution: $\frac{\sqrt{4\alpha t_n}}{a_w} \sim \left(\frac{3}{2}\right)^{1/3} \cdot \left(\frac{\tau_p - \tau^o}{f_p \Delta P_w}\right)^{1/3} \cdot \left(\frac{t_c}{t_w}\right)^{1/3} \iff \frac{Q_m}{Q^*} \ll \sqrt{\pi} \left(1 - \frac{\tau^o}{\tau_p}\right)$

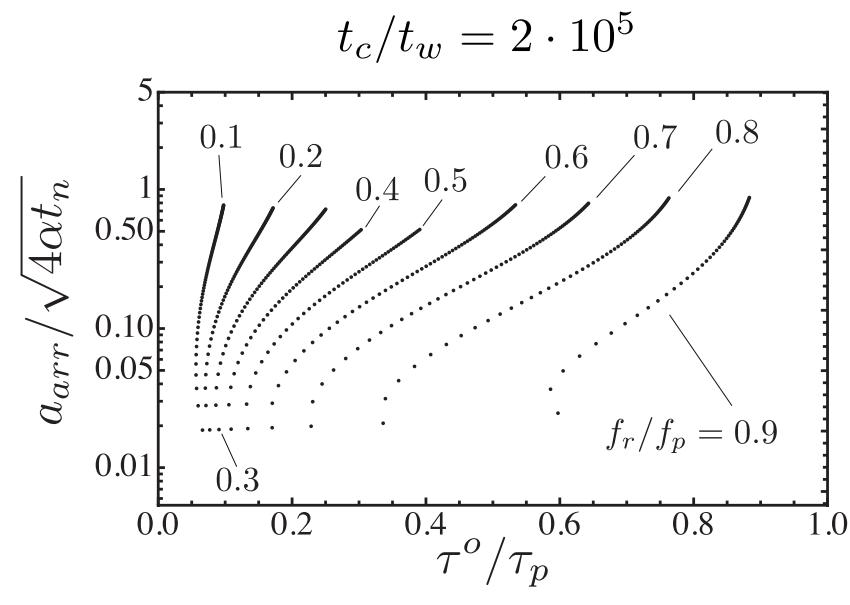
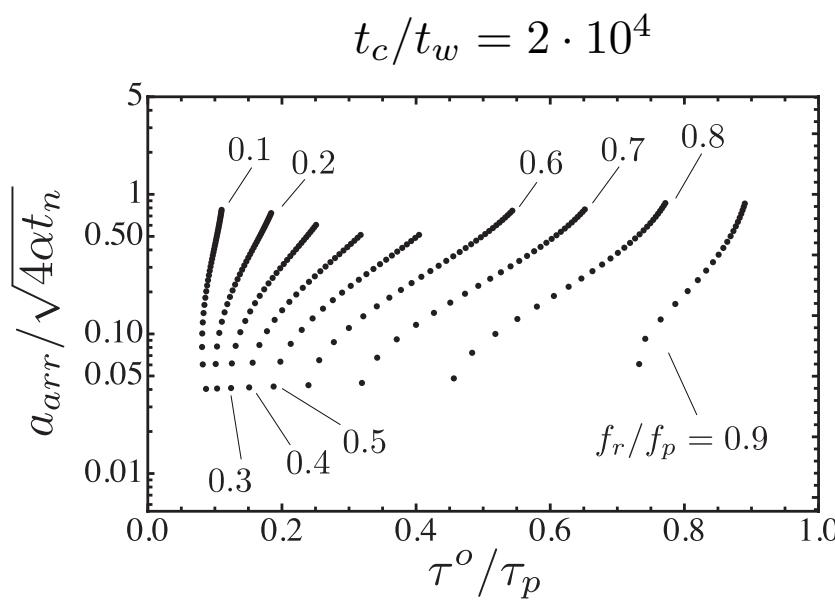
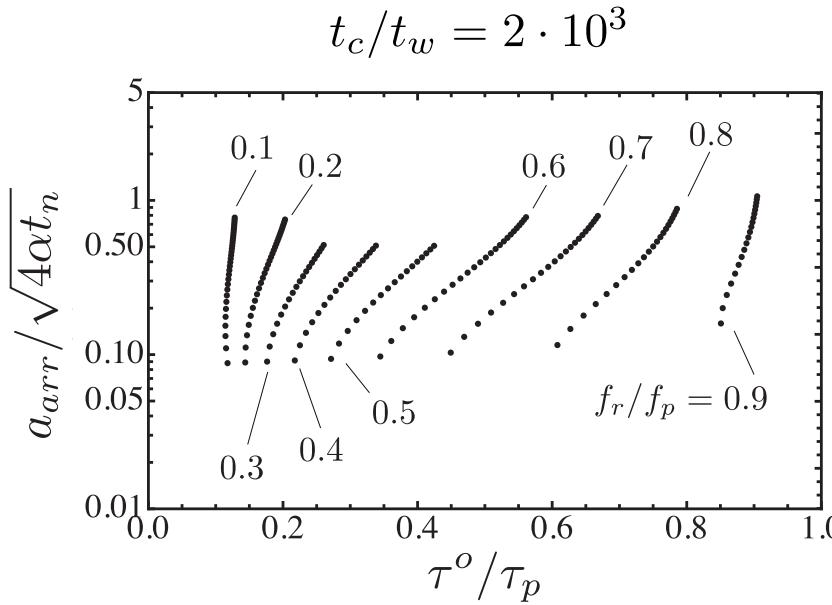


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Ultimately Stable fault ($\tau^o < \tau_r$) - $\frac{t_c}{t_w} \gg 1$ (cont'd)

$$Q_m/Q^* = 0.05$$

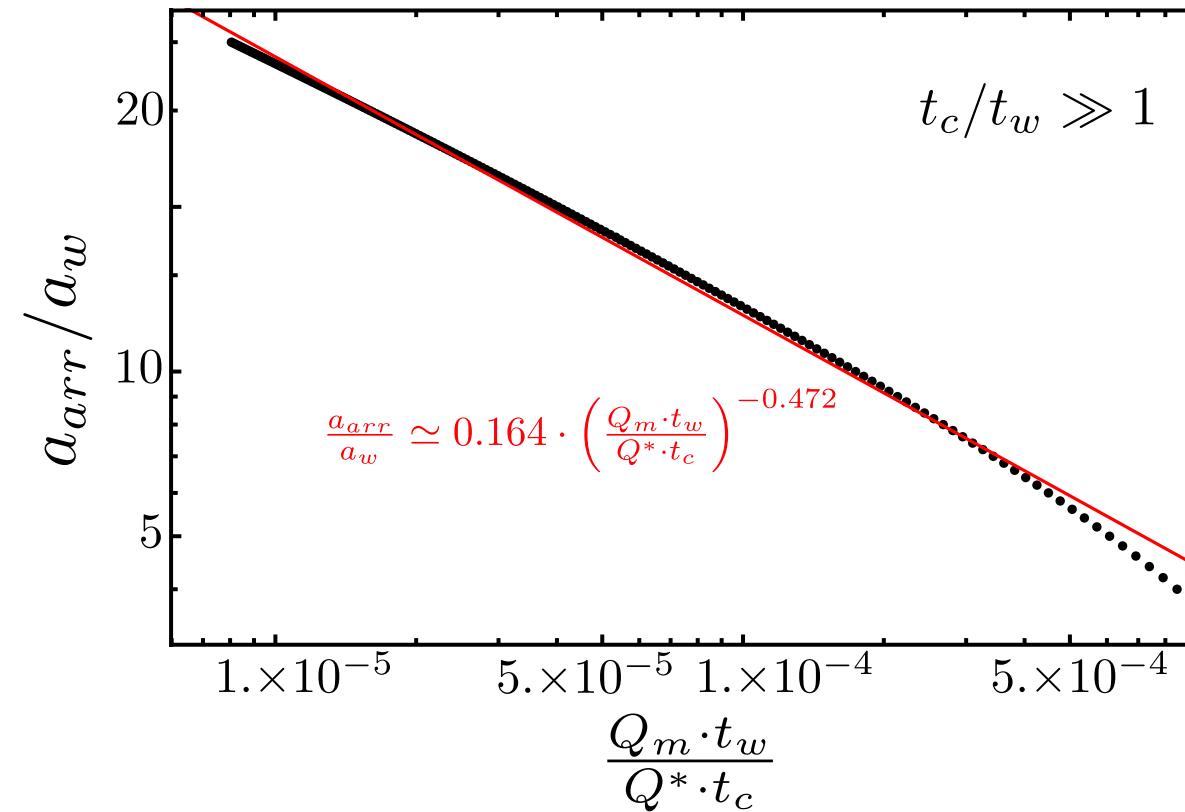


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Ultimately Stable fault ($\tau^o < \tau_r$) - $\frac{t_c}{t_w} \gg 1$ (cont'd)

$$f_r/f_p = 0.6, \quad \tau_o/\tau_p = 0.55$$



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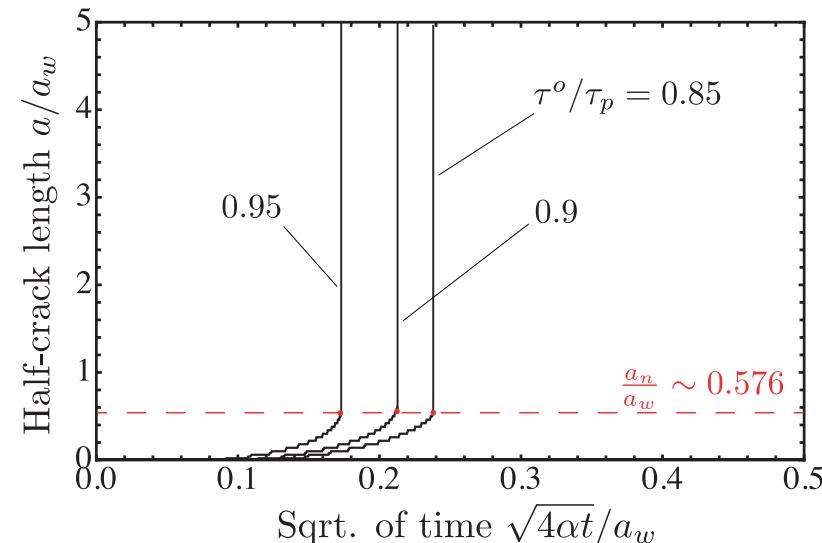
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Unstable fault ($\tau^o > \tau_p$)

$$t_n \ll t_w$$

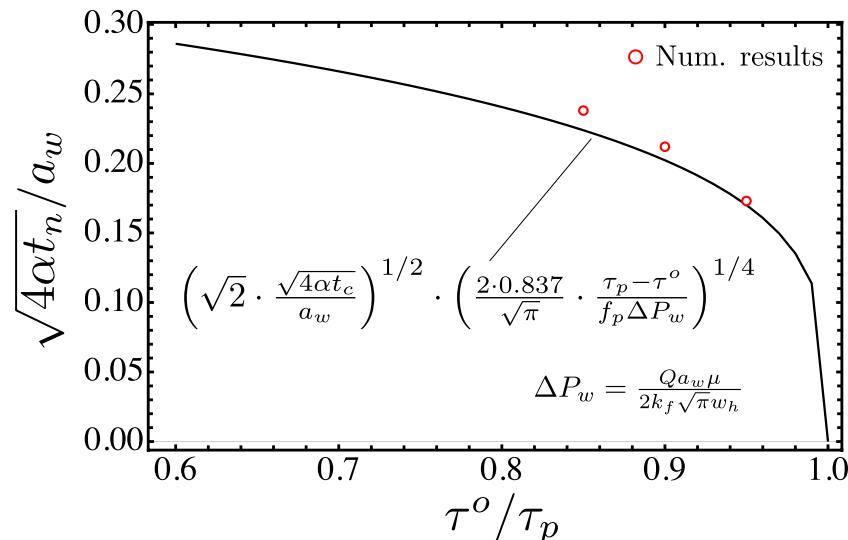
$$\text{Asymptotic solution: } \frac{\sqrt{4\alpha t_n}}{a_w} \sim \left(\sqrt{2} \cdot \frac{\sqrt{4\alpha t_c}}{a_w} \right)^{1/2} \cdot \left(\frac{2 \cdot 0.837}{\sqrt{\pi}} \cdot \frac{\tau_p - \tau^o}{f_p \Delta P_w} \right)^{1/4} \iff \frac{a}{a_w} \gg \frac{\sqrt{4\alpha t}}{a_w}, \quad \forall t$$

$$Q_m/Q^* = 100.$$



$$f_r/f_p = 0.6$$

$$t_c/t_w = 0.5$$



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Bibliography

1. Garagash, D. I., and L. N. Germanovich (2012), Nucleation and arrest of dynamic slip on a pressurized fault, *J. Geophys. Res.*, 117, B10310, doi:10.1029/2012JB009209
2. Ciardo, F., Lecampion, B., Fayard, F., & Chaillat, S. (2020). A fast boundary element based solver for localized inelastic deformations. *Int. J. Numer. Meth. Engng.*, 1-23.