

Ocean Modeling with Adaptive REsolution (OMARE)

– A New Multi-Scale Ocean Modeling Framework

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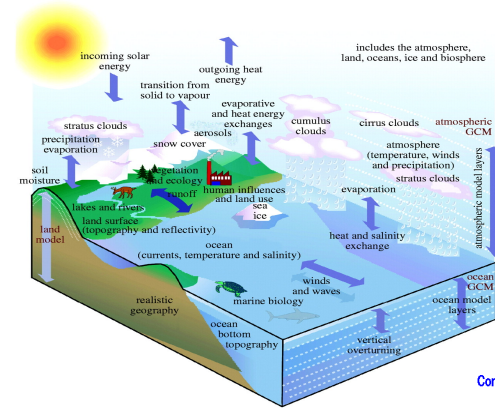
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Status Quo:

- High-res. models simulates turbulent & (arguably) more realistic ocean dynamics
- Ocean & climate research frontiers calls for multi-scale capable & flexible models:
 - Sub-mesoscale, energy cycle & cascading, key regions (ice shelf, coastal, etc.), multi-physics
- Challenges to multiple disciplines: parameterization (scale-awareness), computatbility, etc.

Key Points:

- Adaptive mesh refinement (AMR) to support long-term model devel. & key scientific problems/applications
- **OMARE**: refactor **NEMO** with software middleware of **JASMIN**, with support for: **AMR**, parallelization, I/O, etc.
- Laminar – eddy-rich – submesoscale-capable simulations w/ OMARE



Geofluid Dynamics

Mathematical Modeling & Numerics

Continuity:
$$\frac{\partial \rho}{\partial t} + \frac{\partial (\rho u)}{\partial x} + \frac{\partial (\rho v)}{\partial y} + \frac{\partial (\rho w)}{\partial z} = 0$$

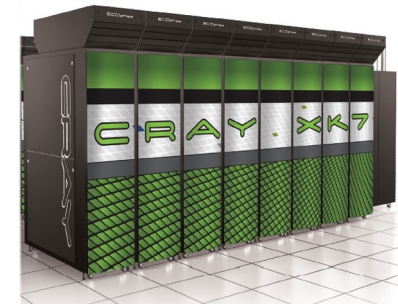
X - Momentum:
$$\frac{\partial (\rho u)}{\partial t} + \frac{\partial (\rho u^2)}{\partial x} + \frac{\partial (\rho uv)}{\partial y} + \frac{\partial (\rho wu)}{\partial z} = -\frac{\partial p}{\partial x} + \frac{1}{Re_r} \left[\frac{\partial \tau_{xx}}{\partial x} + \frac{\partial \tau_{xy}}{\partial y} + \frac{\partial \tau_{xz}}{\partial z} \right]$$

Y - Momentum:
$$\frac{\partial (\rho v)}{\partial t} + \frac{\partial (\rho uv)}{\partial x} + \frac{\partial (\rho v^2)}{\partial y} + \frac{\partial (\rho vw)}{\partial z} = -\frac{\partial p}{\partial y} + \frac{1}{Re_r} \left[\frac{\partial \tau_{xy}}{\partial x} + \frac{\partial \tau_{yy}}{\partial y} + \frac{\partial \tau_{yz}}{\partial z} \right]$$

Z - Momentum:
$$\frac{\partial (\rho w)}{\partial t} + \frac{\partial (\rho wu)}{\partial x} + \frac{\partial (\rho wv)}{\partial y} + \frac{\partial (\rho ww)}{\partial z} = -\frac{\partial p}{\partial z} + \frac{1}{Re_r} \left[\frac{\partial \tau_{xz}}{\partial x} + \frac{\partial \tau_{yz}}{\partial y} + \frac{\partial \tau_{zz}}{\partial z} \right]$$

Energy:
$$\frac{\partial (\rho E)}{\partial t} + \frac{\partial (\rho u E)}{\partial x} + \frac{\partial (\rho v E)}{\partial y} + \frac{\partial (\rho w E)}{\partial z} = -\frac{\partial (up)}{\partial x} - \frac{\partial (vp)}{\partial y} - \frac{\partial (wp)}{\partial z} + \frac{1}{Re_r Pr_r} \left[\frac{\partial q_x}{\partial x} + \frac{\partial q_y}{\partial y} + \frac{\partial q_z}{\partial z} \right] + \frac{1}{Re_r} \left[\frac{\partial}{\partial x} (u \tau_{xx} + v \tau_{xy} + w \tau_{xz}) + \frac{\partial}{\partial y} (u \tau_{xy} + v \tau_{yy} + w \tau_{yz}) + \frac{\partial}{\partial z} (u \tau_{xz} + v \tau_{yz} + w \tau_{zz}) \right]$$

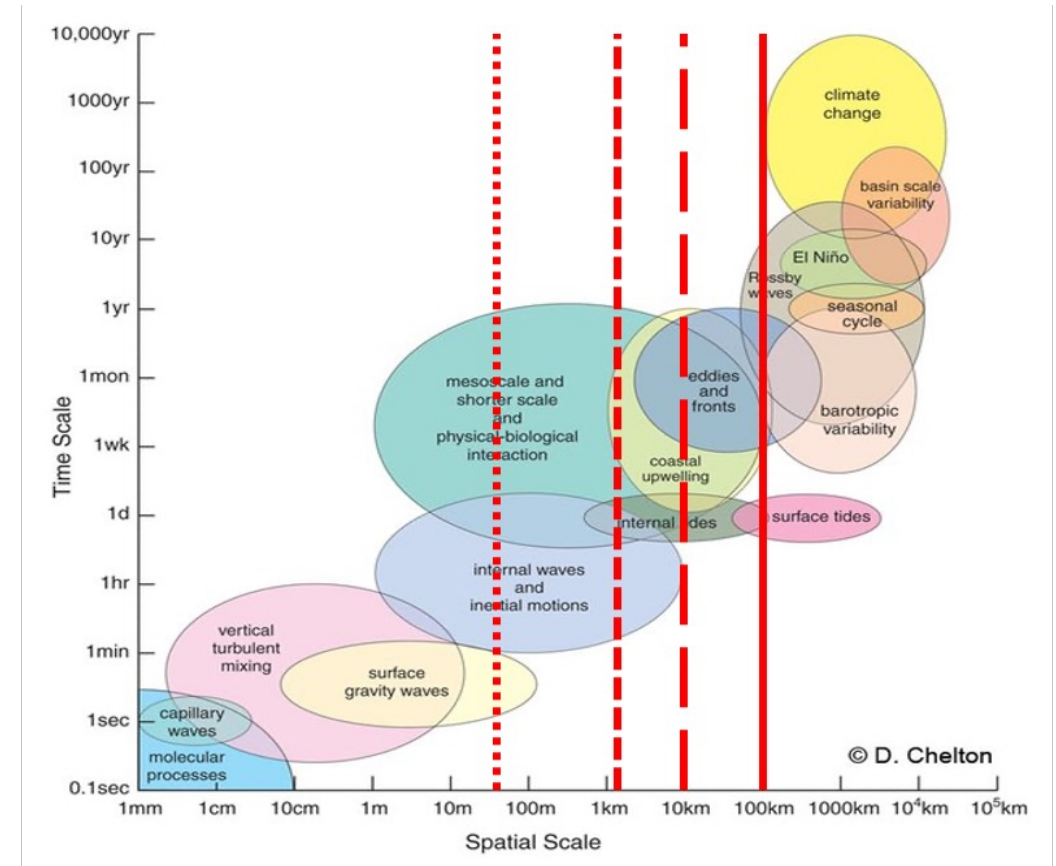
Code Implementation & HPC



Multi-Scale Ocean Dynamic Processes

Challenges to High-Res. Models:

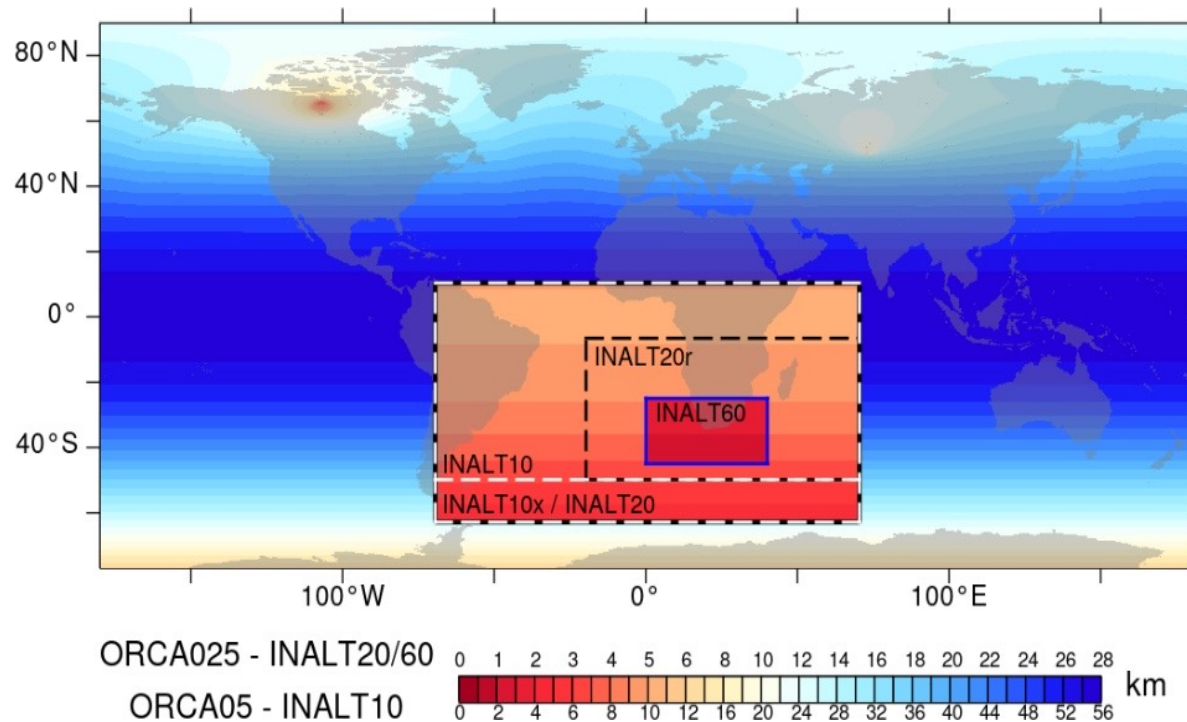
- Upscaling of small-scale processes, oceanic energy cycle & forward/backward cascading
- Scale-aware parameterization
- Looming future of multi-physics (non-hydrostatic, LES, etc.)
- High computational overhead, low time-to-solution



- 100km: climate models (i.e., CMIP)
- - - 10~25km: eddy-rich / global operational
- . - . 1~2km: submeso.-rich / state-of-the-art
- <100m: LES, DNS

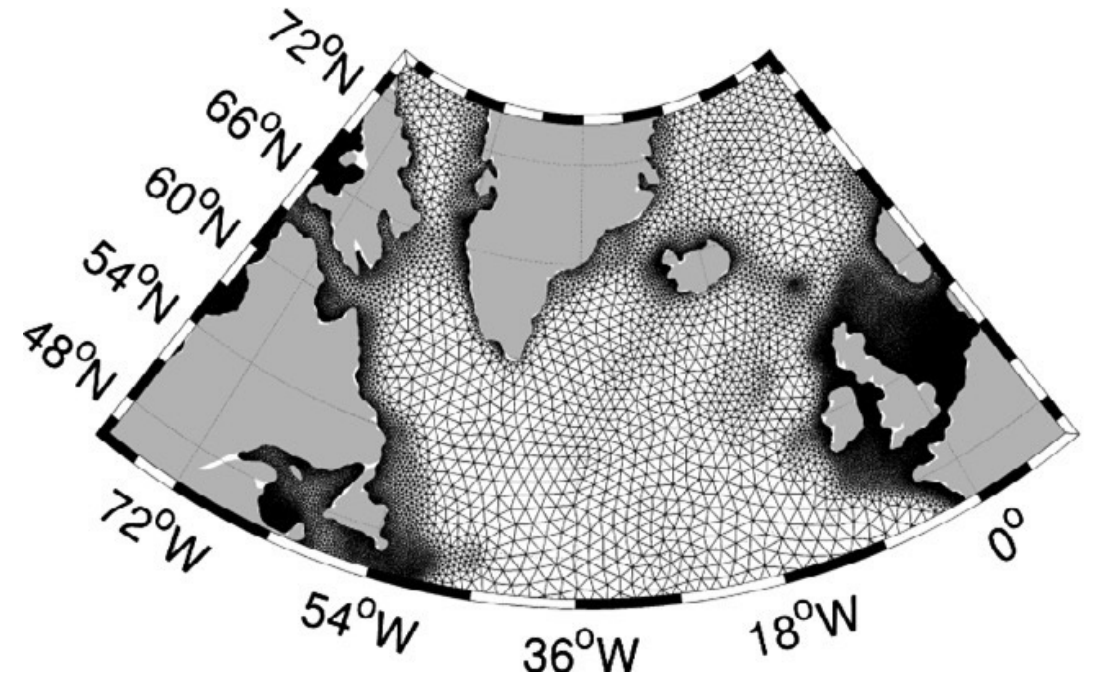
Two Typical Approaches to Multi-Res. Modeling

Nesting w/ Structured Grid
Traditional Finite-Difference, Finite-Volume



[Schwarzkopf et al., 2019]

Unstructured Grid
Finite-Element methods



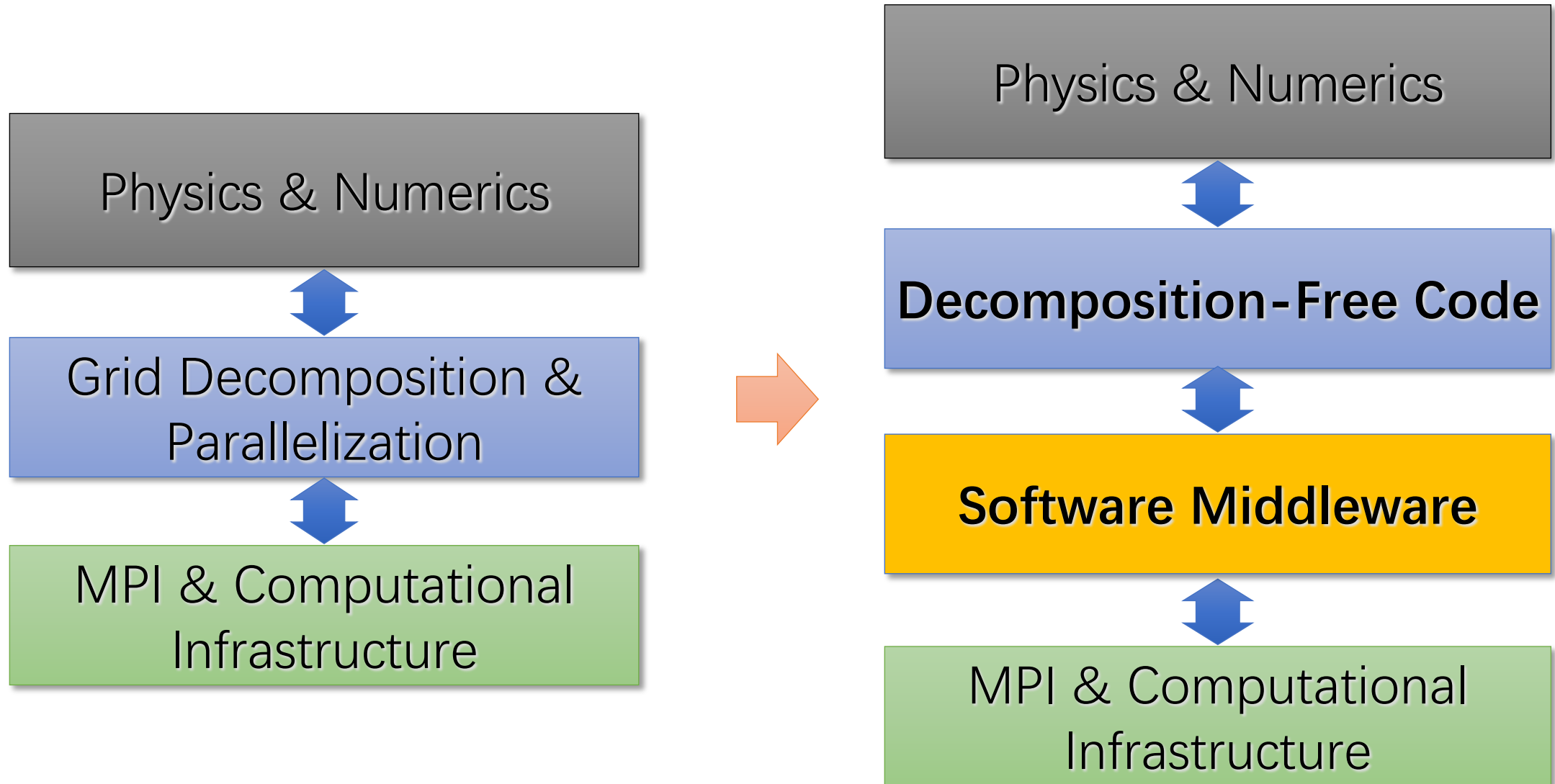
[Danilov, 2013]

Adaptive Mesh Refinement (AMR) as a Future-Proof Ocean Modeling Framework

Advantages:

1. Flexibility in resolving multi-scale processes: ***adding resolution only when & where it is `needed`***
 - Lateral boundaries, channels
 - Temporally changing features (i.e., ocean fronts, etc.)
2. Friendliness to existing parameterization (i.e., different parameterization on different refinement levels)
 - Also a platform for further improve parameterizations with upscaling
3. Good computability

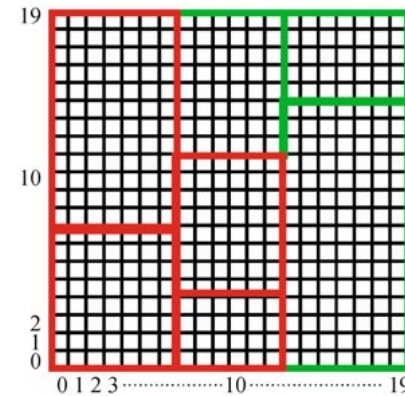
Model Grid As A Key Abstraction Layer



JASMIN – J parallel Adaptive Structured Mesh applications INfrastructure

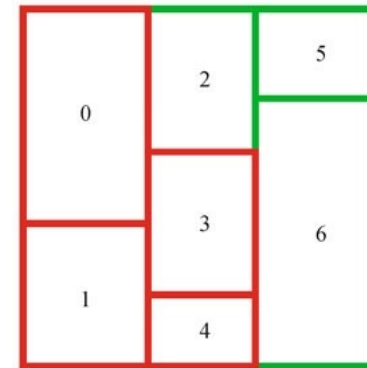
[Mo et al., 2010]

- JASMIN provides AMR supports:
 - Abstraction of structured grid (including staggered grids)
 - Management of domain decomposition & communications
 - Rule-based, automatic recursive grid refinement
 - Inter-level exchanges (boundary, interpolation, update, etc.)
 - Model restart
 - Parallel I/O
- JASMIN is based on C++



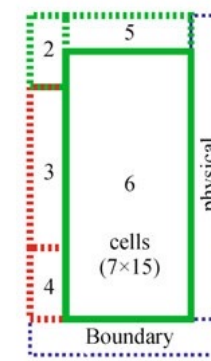
Mesh cells : 20×20
Cell indices : (i, j)

(a)



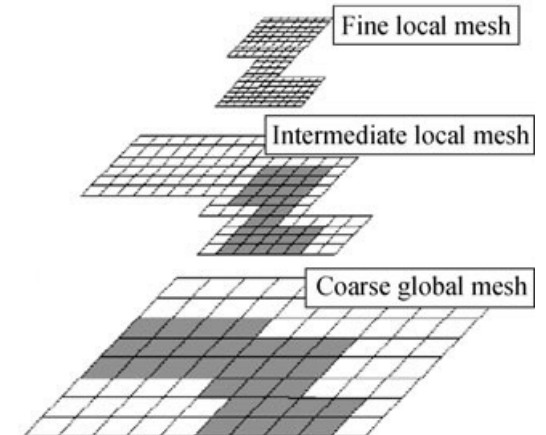
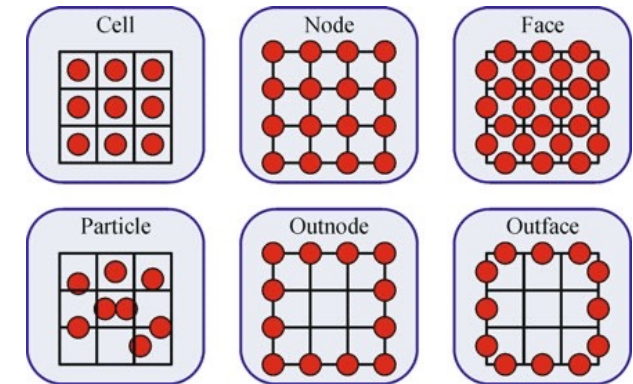
Mesh: 20×20 cells, 7 boxes
Load distribution: 2 proc.

(b)



Box, GhostBox
(width = 2)

(c)



OMARE – NEMO on JASMIN

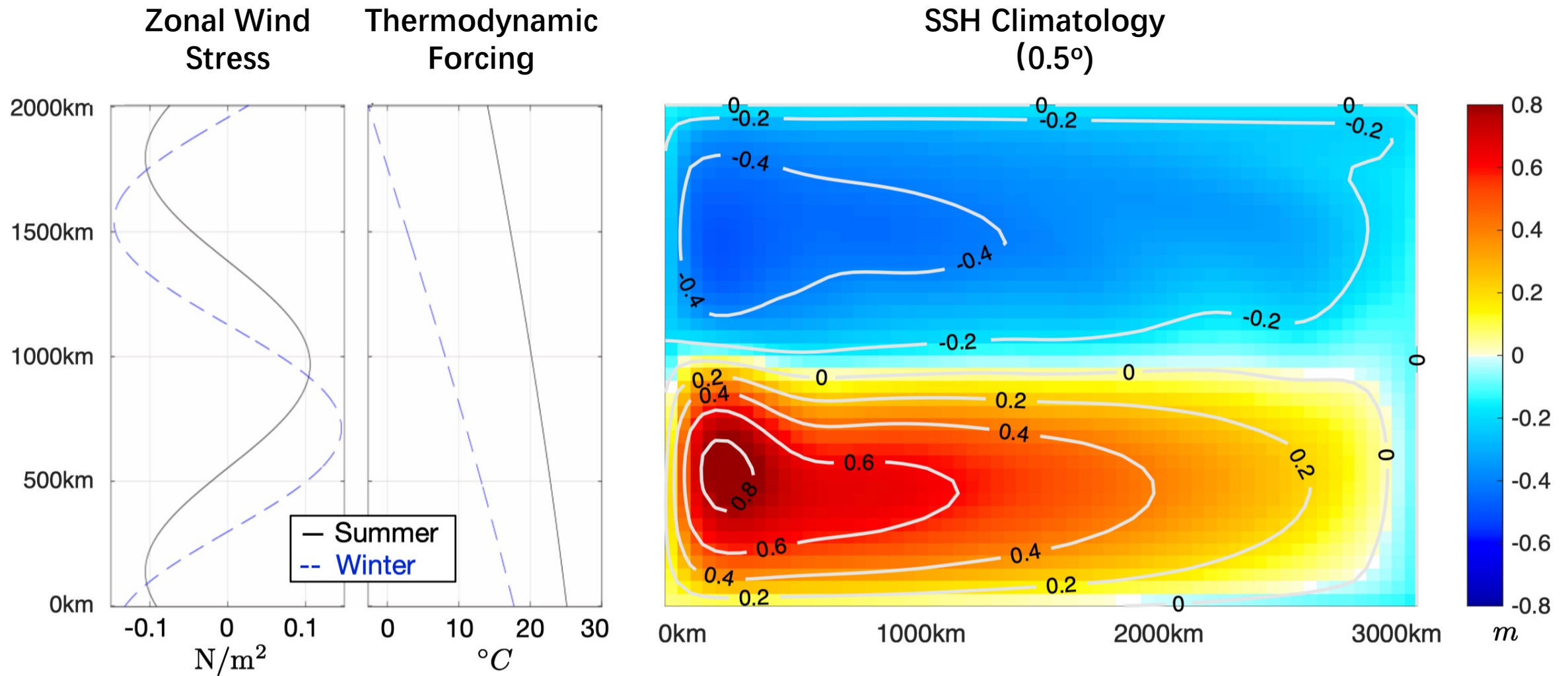
- Porting NEMO (decomposition-independent code) onto JASMIN
 - Including full 3-D dynamic core, key parameterizations, sea ice, etc.
- Re-write the whole time-integration procedure in JASMIN
 - Patch & inter-level communication carried out by JASMIN
- HDF5-based history & restart files (parallel I/O)
- **Result:** Ocean Modeling with Addaptive Refinement (**OMARE**)
- Codebase in FORTRAN & C++: ~127k lines (**27k new**) & **67k lines** respectively

Typical Resolutions of OMARE

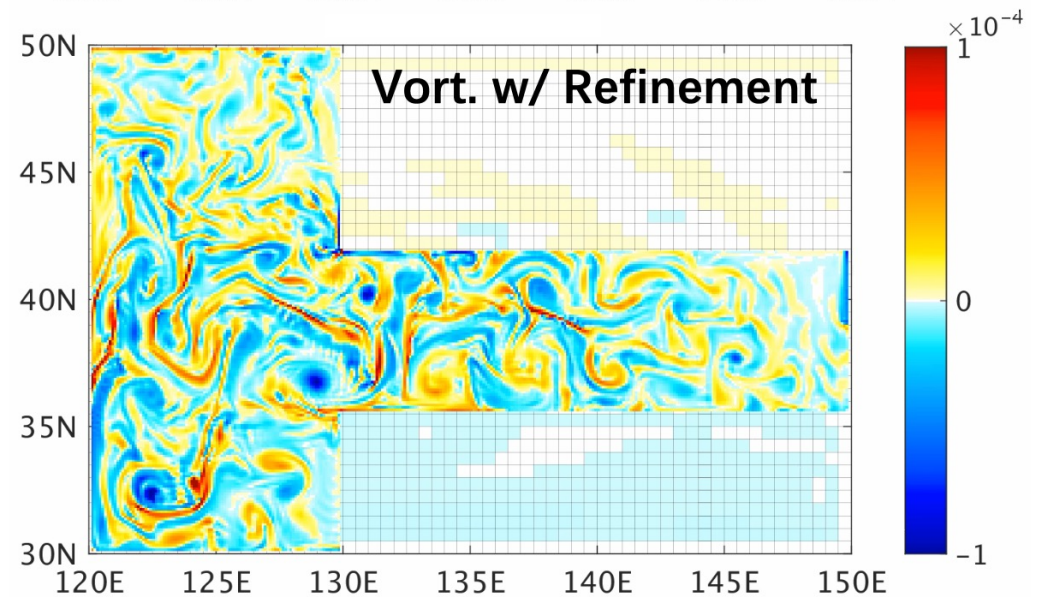
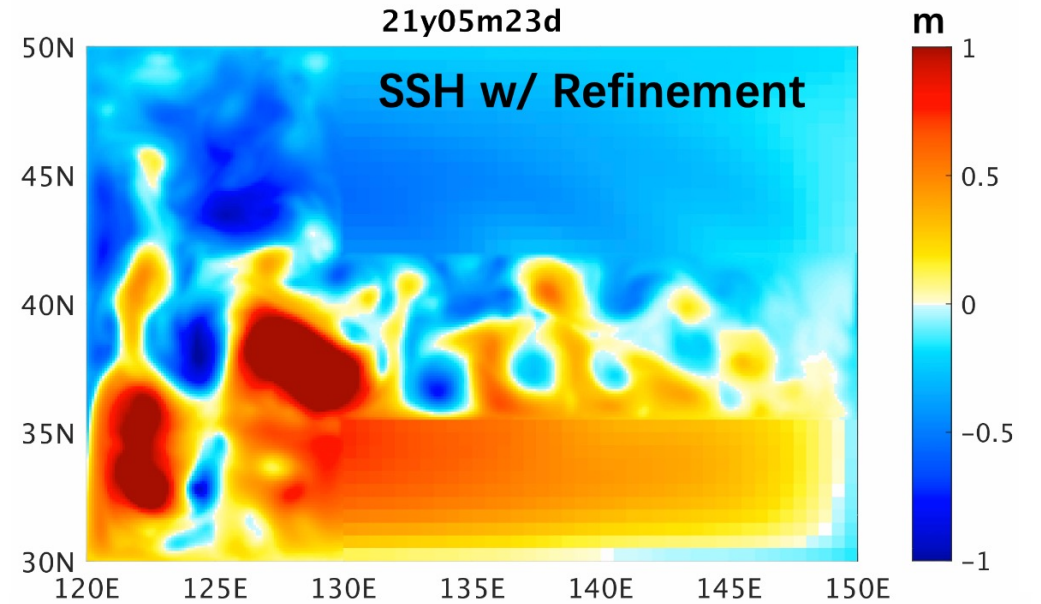
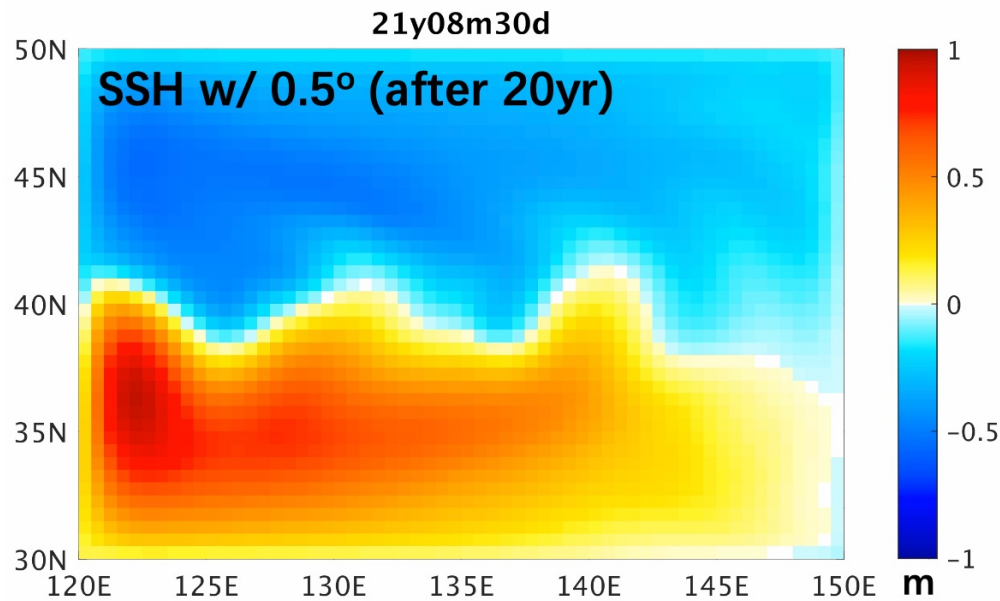
Level	Abbr.	Resolution	Time Step	Note
I	L aminar ocean (Low res.)	0.5-deg	1 h	Climate modeling
II	M esoscale- resolving	0.1-deg	10 m (x6)	Eddying, or mesoscale-rich
III	S ubmesoscale- capable	0.02-deg	2 m (x5)	Mesoscale resolving, w/ certain submesoscale features
IV	e X perimental	0.004-deg	24 s (x5)	Resolving large portion of submesoscale Computational performance study

- Resolution range span: climate modeling & fine-scale process study
- 2-D refinement w/ shared z-coordinate
- Future extension to include NH & LES (i.e., multi-physics)

Double-Gyre: Idealized Test Case of WBC

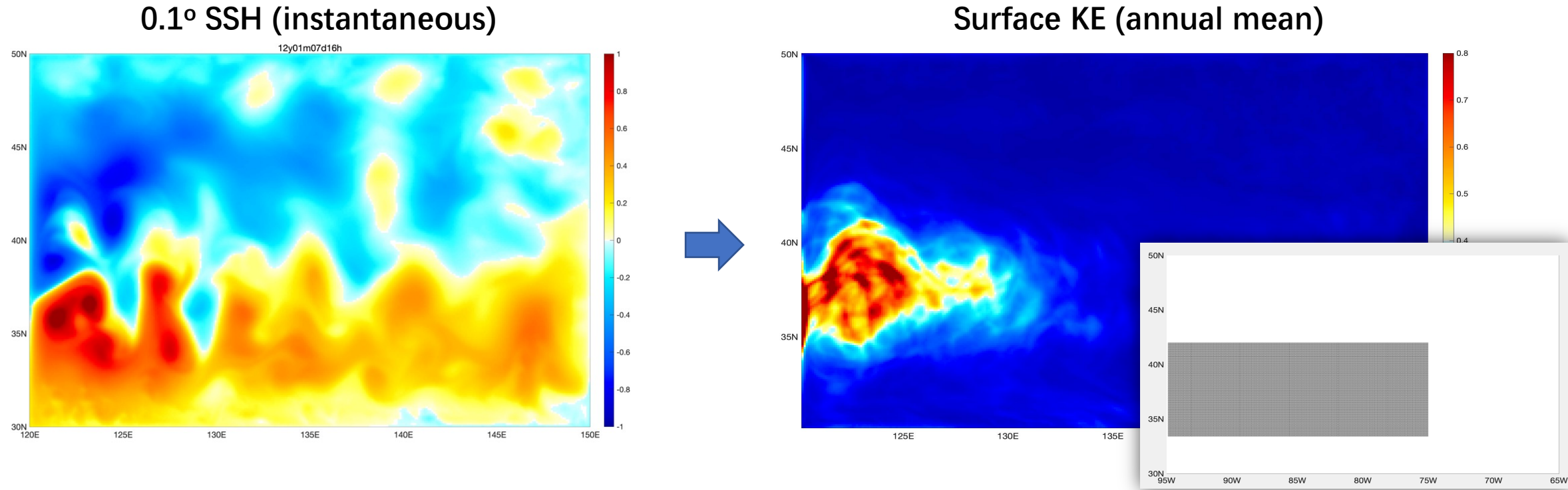


1) Laminar Ocean $\rightarrow$ Turbulent Ocean ($0.5^\circ \rightarrow 0.1^\circ$)



1. Spin-up w/ 0.5° (20-yr) $\rightarrow$
 2. T-shape refinement w/ 0.1°
 - Focus on western boundary & WBC
 - Shifting tail w/ seasonal cycle
- **Result:** saturated & rich mesoscale features w/ refinement

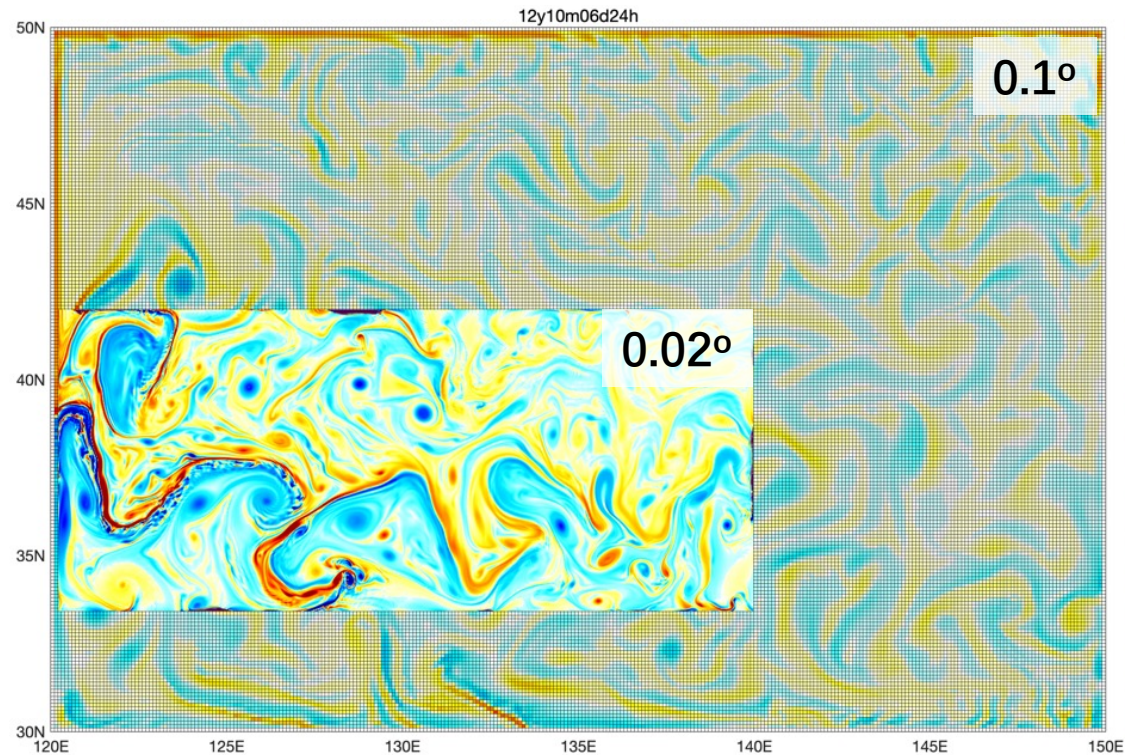
2.1) Mesoscale $\rightarrow$ Submesoscale ($0.1^\circ \rightarrow 0.02^\circ$): Static Refinement



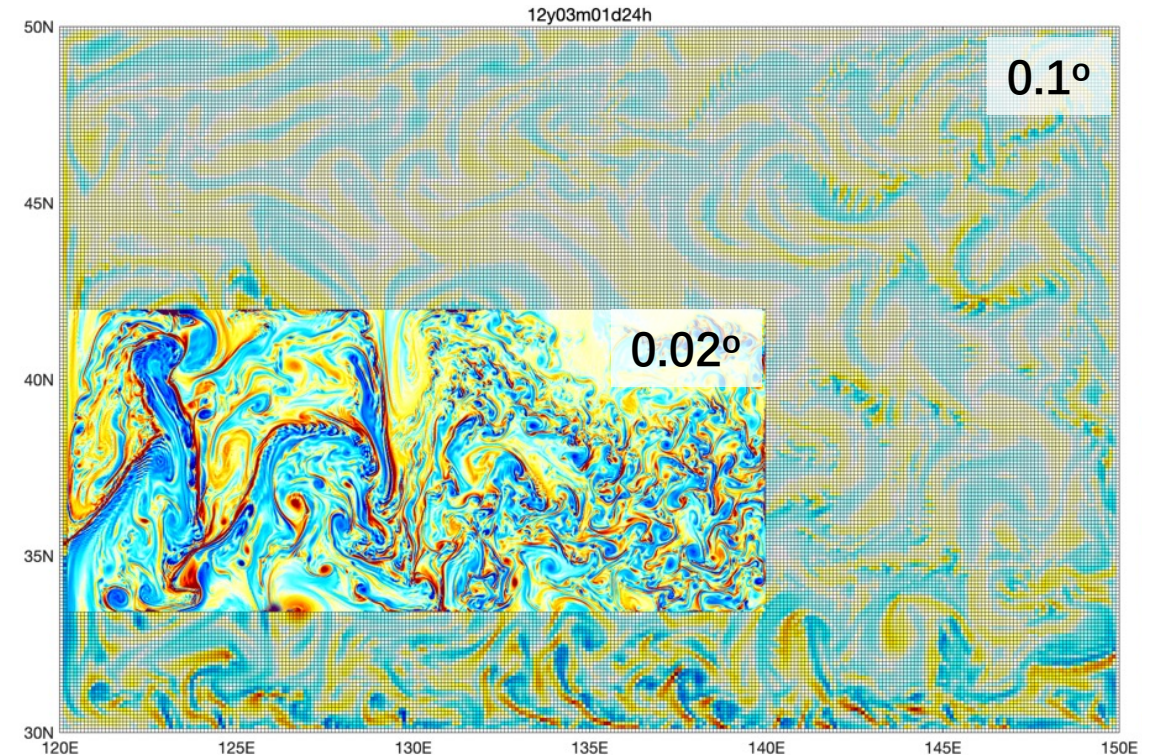
- **Refinement setting:** a regular (i.e., rectangular) refined region encapsulating the kinematically active region

2.1) Mesoscale $\rightarrow$ Submesoscale ($0.1^\circ \rightarrow 0.02^\circ$): Static Refinement

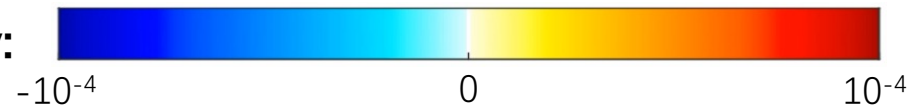
- Summer



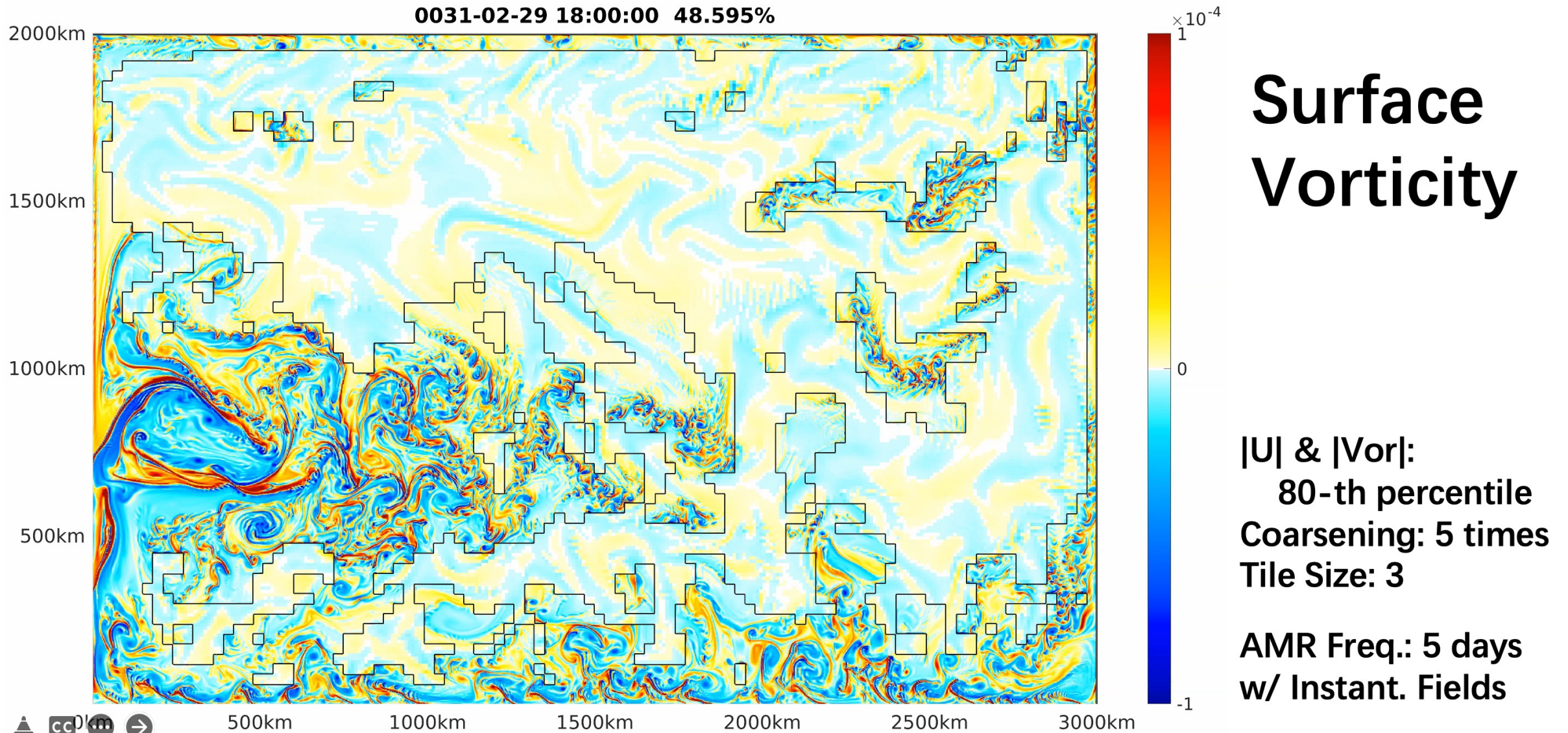
- Winter



Surface vorticity:

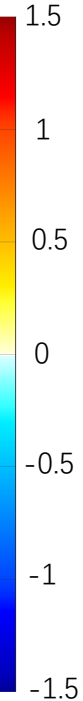
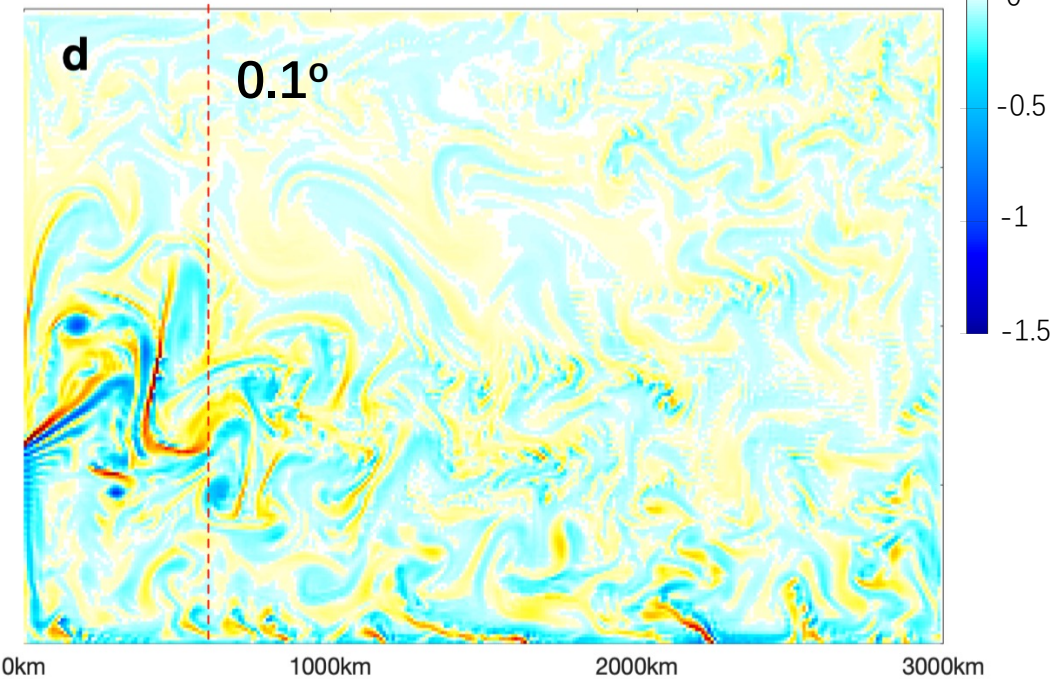
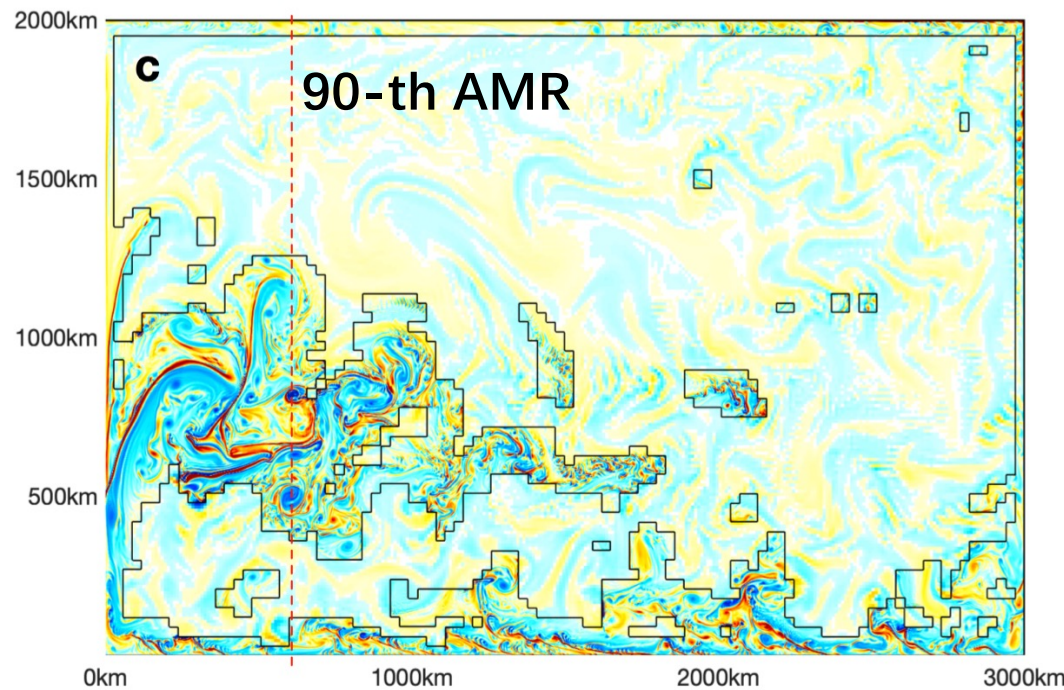
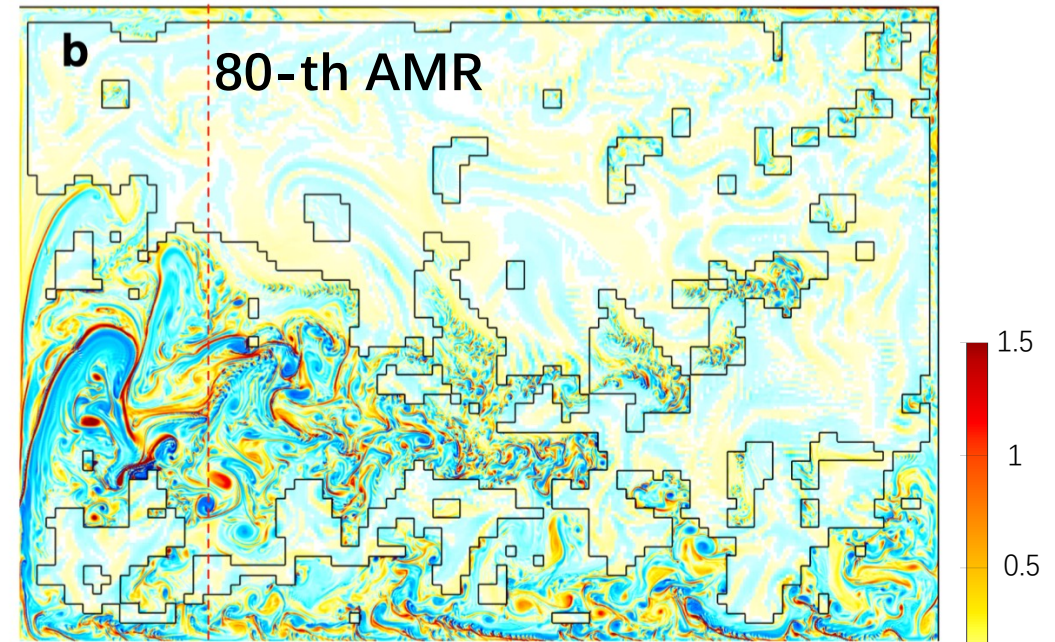
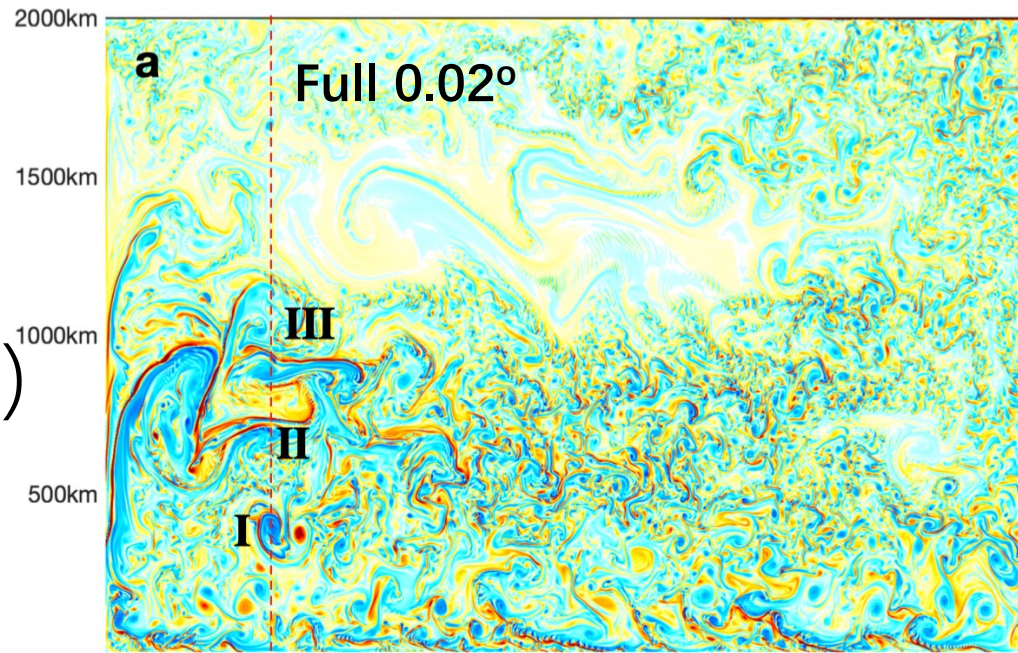


2.2) Mesoscale $\rightarrow$ Submesoscale ($0.1^\circ \rightarrow 0.02^\circ$): Adaptive Refinement (since Feb.-1st)



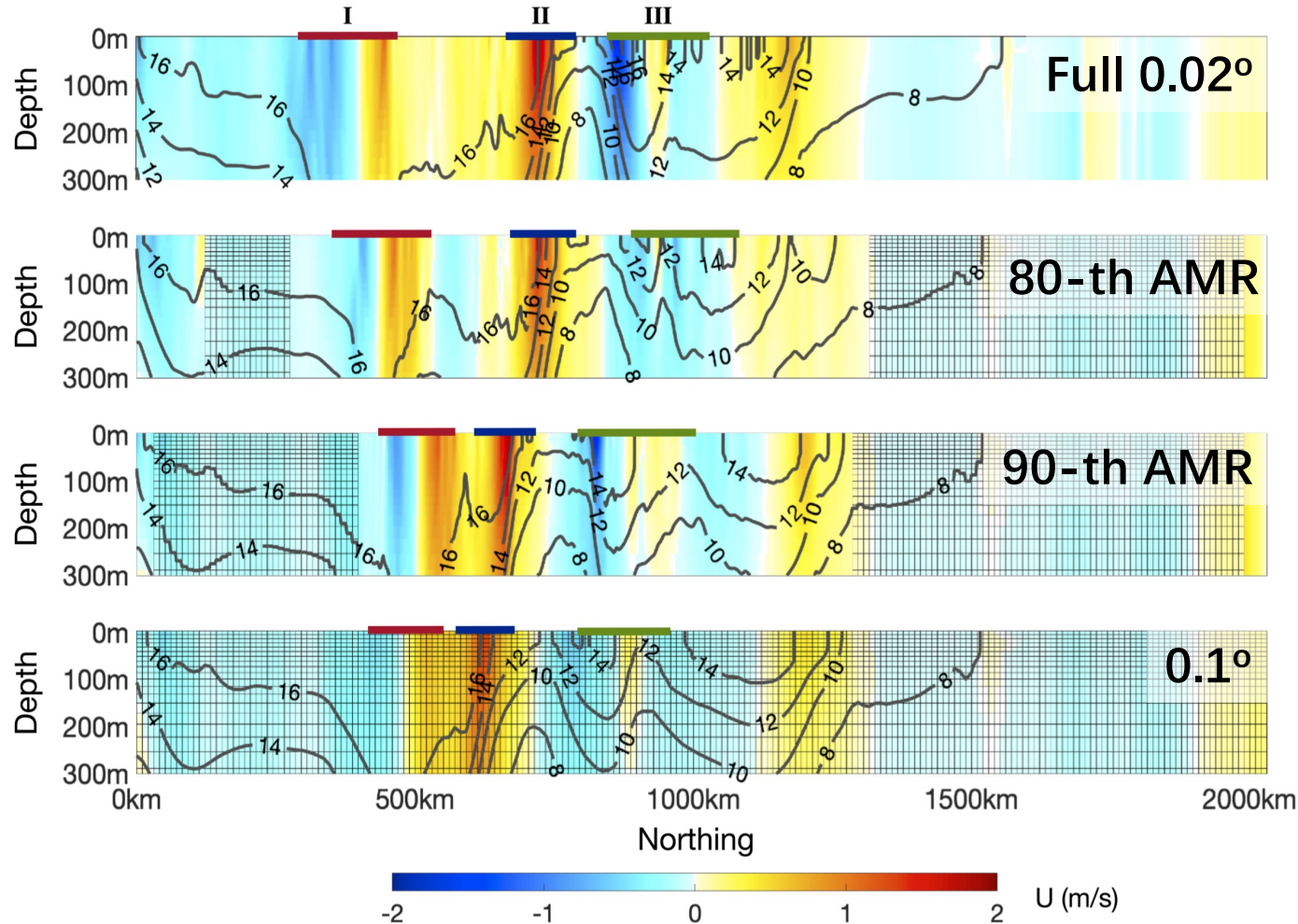
50 Days
after AMR
in Winter
(since Feb.)

Ro
(ζ/f)

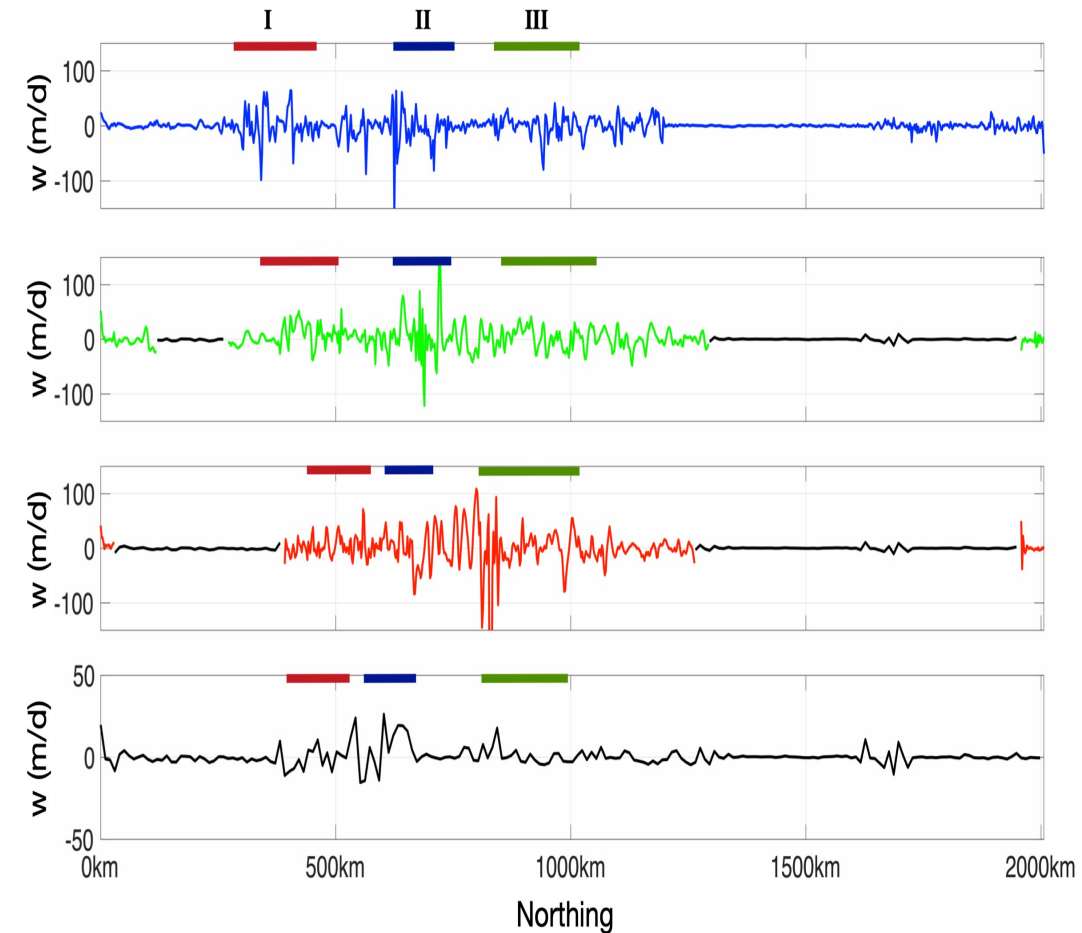


2.2) Mesoscale $\rightarrow$ Submesoscale ($0.1^\circ \rightarrow 0.02^\circ$): Vertical Transect in WBC

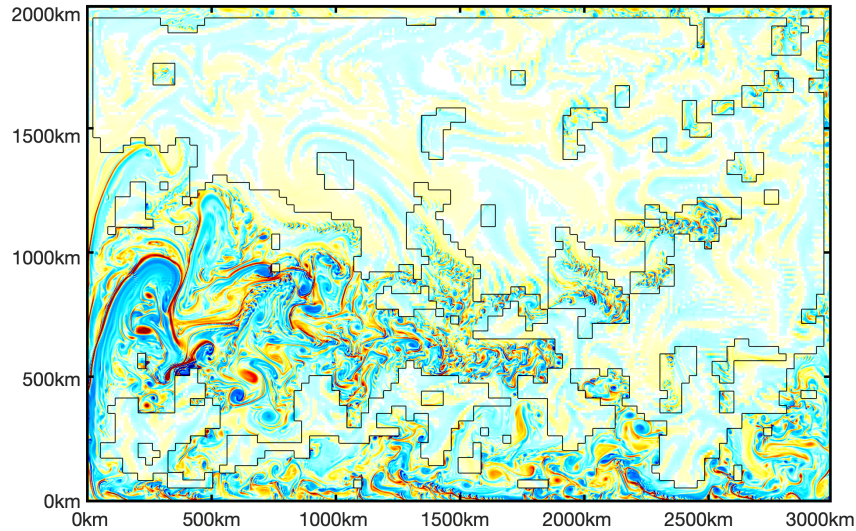
U (filled, m/s) & Temp ($^\circ\text{C}$)



W at 50m Depth (m/d)

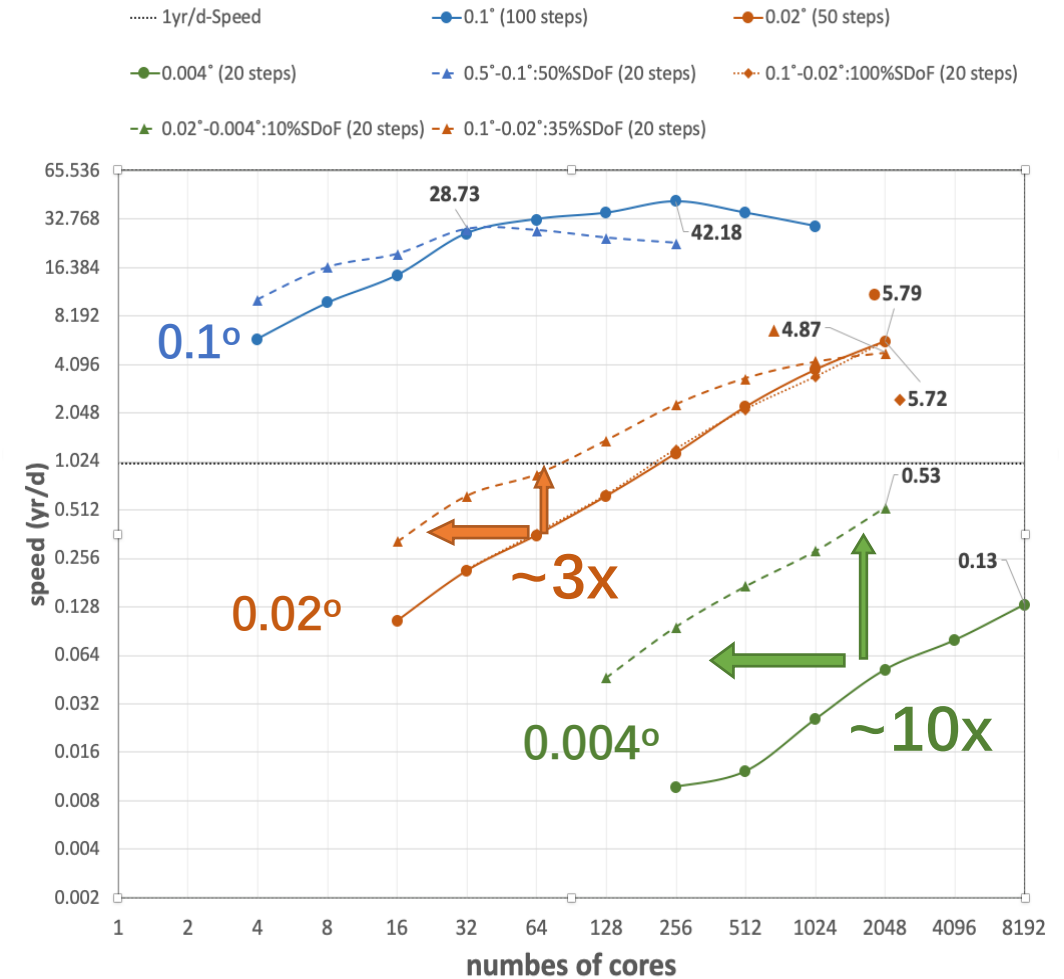
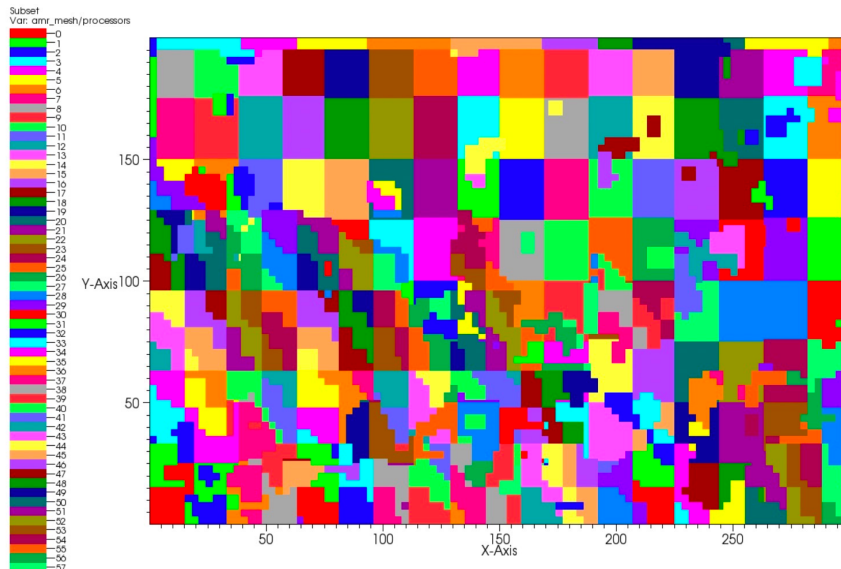


Computational Aspects



AMR Example:
 $0.01^\circ \sim 0.02^\circ$

Processor
Mapping
(128 proc.)



- Platform: Intel multi-core (28c/node) w/ IB interconnect
- Refinement ratio: $0.1^\circ - 0.02^\circ @ 35\%$, $0.02^\circ - 0.004^\circ @ 10\%$
- Ongoing analysis & optimization



Summary & Outlook

1. **OMARE**: a framework for flexible, multi-scale ocean modeling
2. ***Physics***: mesoscale & submesoscale w/ AMR in Double-Gyre
3. ***Computation***: reasonable speed
4. A basis model to study WBC & related issues
 - *Paper to be submitted to GMD journal*
 - Outlook:
 1. Realistic cases: bathymetry, atm. forcings, tide, sea ice, etc.
 2. Computational aspects: optimization for AMR & arch.-specific optimizations
 3. Focus region/process: polar & sub-polar regions, ocean & sea ice
 4. Upscaling of small-scale ocean processes