

MAKE OUR
PLANET
GREAT
AGAIN



History Matching for the tuning of climate models: Lessons from the L96 model

Redouane Lguensat
Research Engineer IPSL
Paris, France





MOPGA project: HRMES

Using machine learning to help tuning climate models



Modeling groups tune by hand models to make them match observations

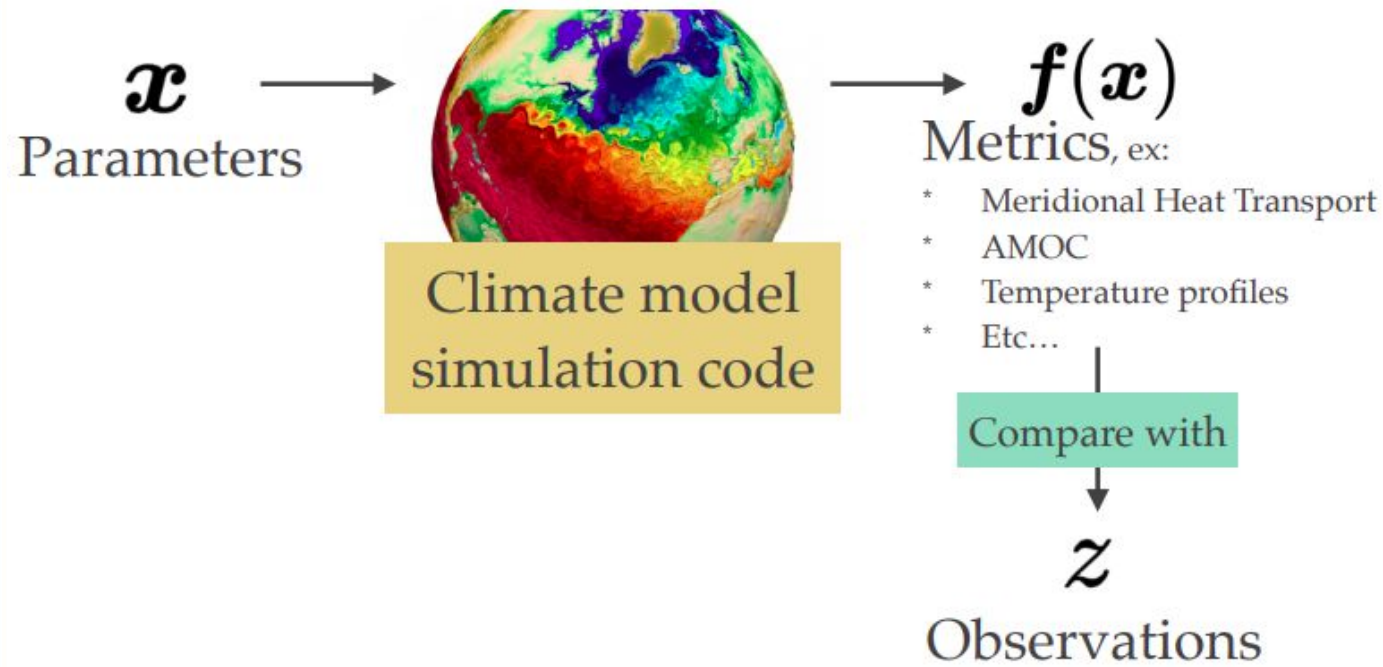
Very expensive, for example it took **5 years** to find an acceptable tuning of IPSL model

Our goal:

- Use ML-based emulators to replace the expensive climate model
 - find one or many good tunings
 - run the expensive model with these “good” tunings

MAKE OUR
PLANET
GREAT
AGAIN





$$\mathbf{x}^* = \arg \min_{\mathbf{x}} \|\mathbf{z} - \mathbf{f}(\mathbf{x})\|_f$$

But ! tuning to a handful of metrics may risk achieving improved performance in those metrics at the expense of unphysical behavior in metrics or processes that were not used in tuning
 —> **Overtuning**

« Overtuning is a real concern and the raison d'être for Bayesian UQ methods » Hourdin et al. 2017

History Matching:

- * Established technique used in particle physics, molecular dynamics, population genetics, neuroscience, epidemiology, ecology, astrophysics and recently **climate science**
- * Has always benefited from ML advances

Instead of looking for THE best set of parameters that solves an optimization problem. History Matching uses observed data to rule-out any parameter settings which are **“implausible”**.



History Matching and ML

Ideally we would individually check every possible parameter setting for the input:

Impossible (climate models are **expensive** to run)



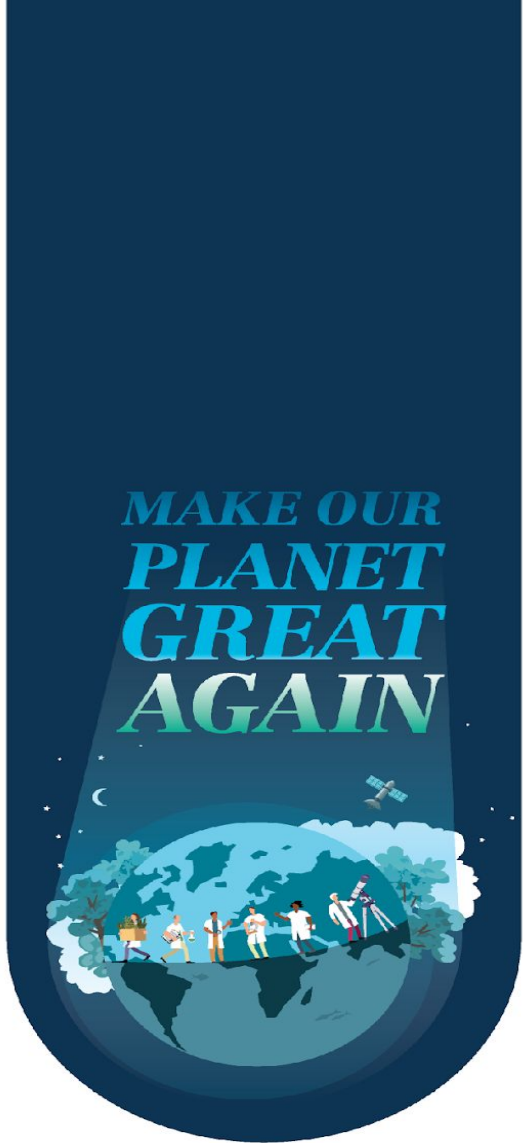
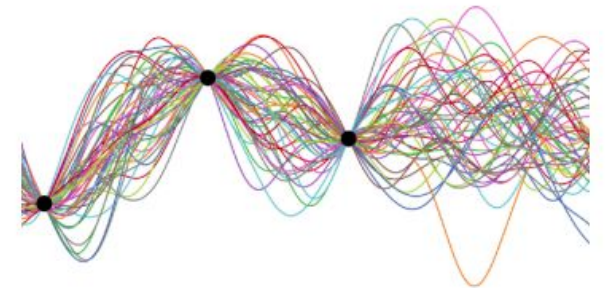
Need for **space-filling designs** to cover the space of parameter search

Need for replacing the expensive simulator with a rapid and cheap **emulator**

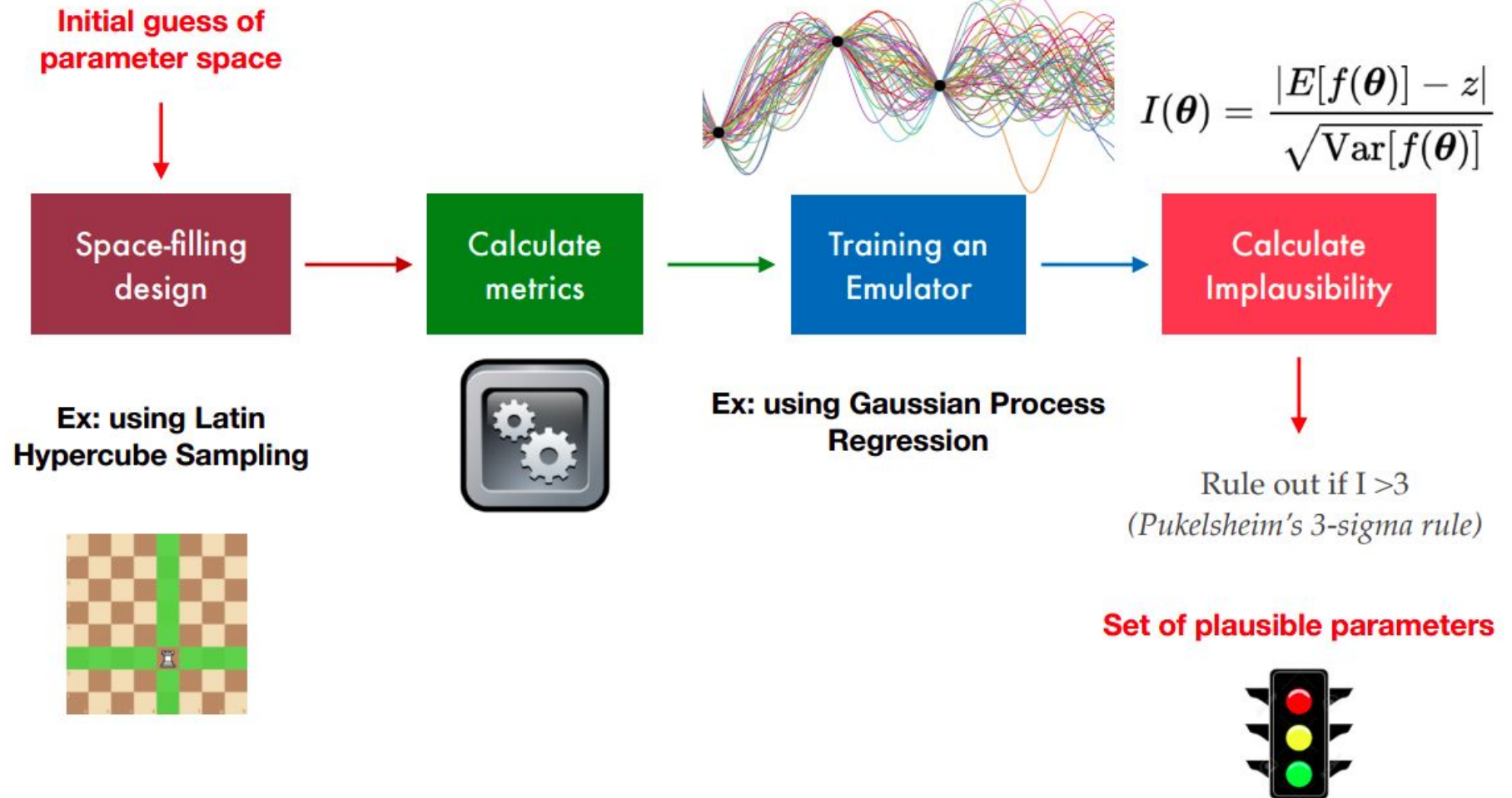
Ex: using Latin Hypercube Sampling



Surrogate modeling



History Matching pipeline



HM is an iterative process: done in *waves*

MAKE OUR
PLANET
GREAT
AGAIN



HM for climate model tuning

Tuning atmospheric models:

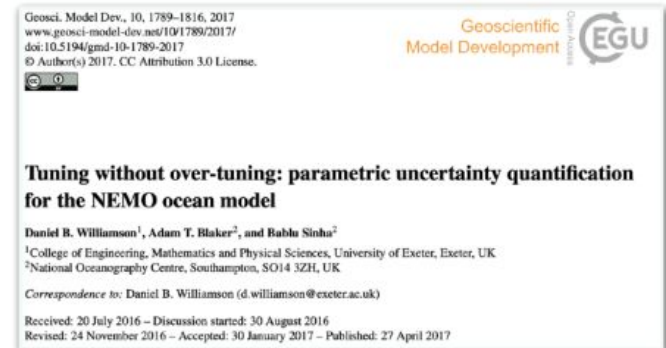
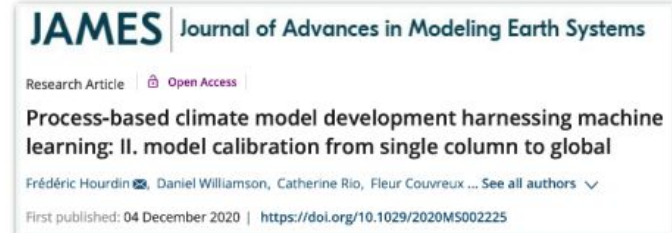
HM was used to tune **atmospheric models**, ex: LMDZ (Hourdin et al. 2020, Couvreur et al. 2020):

- * Using single-column models (SCMs) they afford to run several simulations with different set of parameters
- * Short timescales

Tuning ocean models:

HM was used to tune **ocean models**, ex: NEMO ORCA 2° (Williamsson et al. 2017):

- * Using an available ensemble of 400 NEMO simulations ran for 150 years.
- * Long timescales



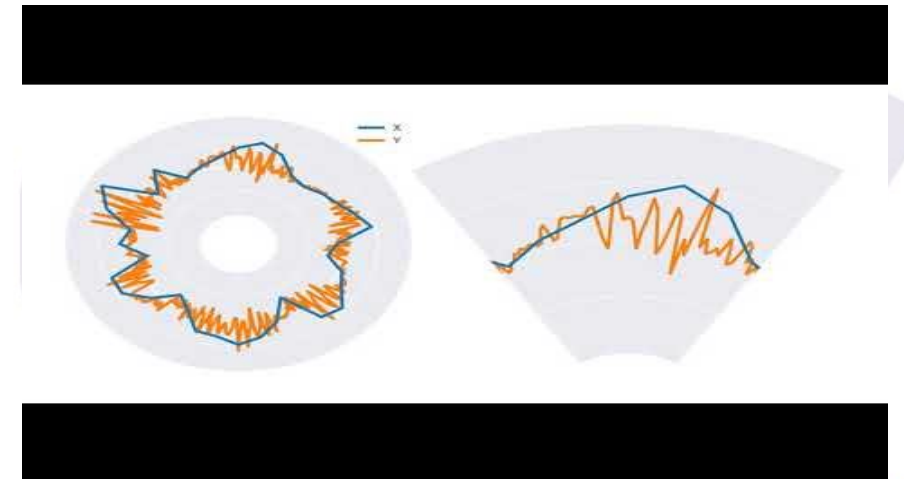
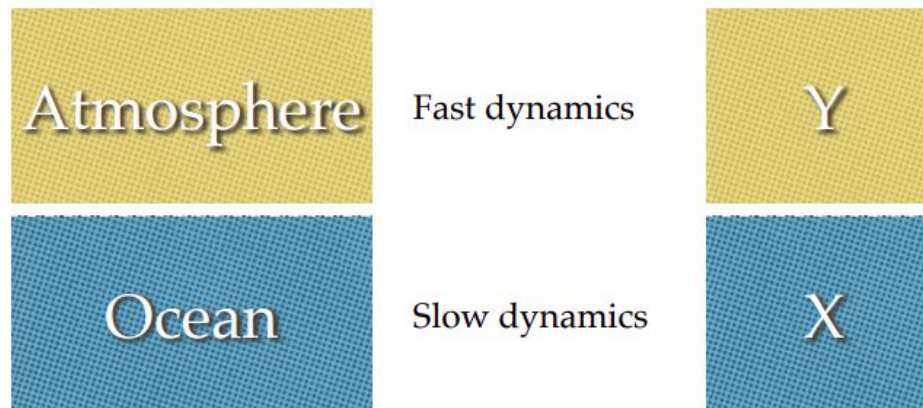
The Lorenz96 as a toy model

- * Periodic system of K ($k=1, \dots, K$) ODEs
- * **Two-level version:** add periodic variable Y with its own set of ODEs.
- * The X and Y ODEs are linked through coupling terms. Each X has J Y variables associated with it.

$$\frac{dX_k}{dt} = \underbrace{-X_{k-1}(X_{k-2} - X_{k+1})}_{\text{Advection}} \underbrace{-X_k}_{\text{Diffusion}} \underbrace{+F}_{\text{Forcing}} \underbrace{-\frac{hc}{b} \sum_{j=1}^J Y_{j,k}}_{\text{Coupling}}$$

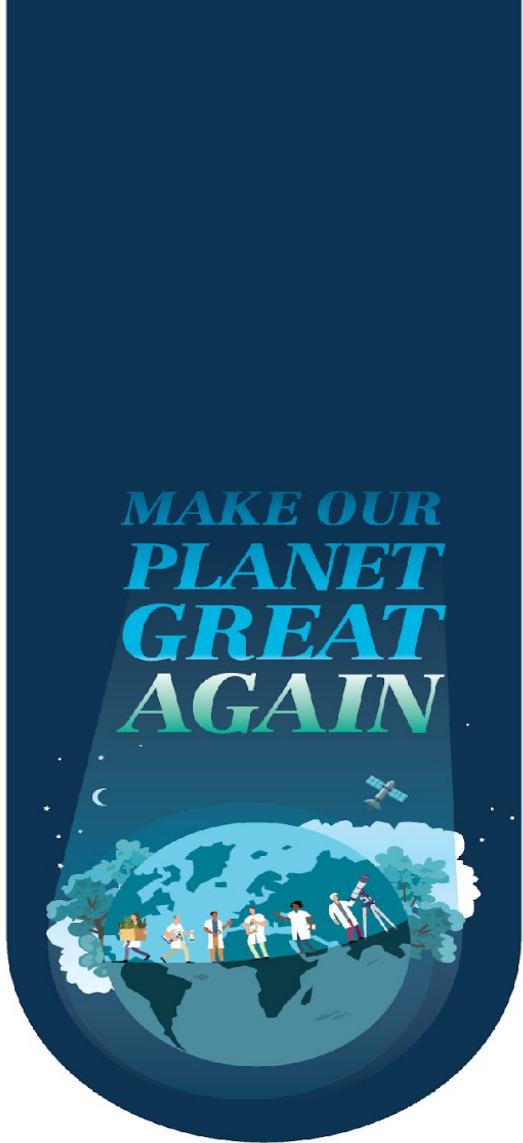
$$\frac{dY_{j,k}}{dt} = \underbrace{-cY_{j+1,k}(Y_{j+2,k} - Y_{j-1,k})}_{\text{Advection}} \underbrace{-cY_{j,k}}_{\text{Diffusion}} \underbrace{+\frac{hc}{b} X_k}_{\text{Coupling}}$$

Analogy with coupled ocean-atmosphere models:



Credits: Stephan Rasp

Experiment: HM for the tuning of parameters (F, h, c, b)



HM on the Lorenz96

- * **Metrics**: long-term time means to mimic climatological quantities
- * **Ground Truth**: perfect setting $K=36$ **X** variables each coupled with $J=10$ **Y** variable. $F=10, h=1, c=10, b=10$, chaotic behavior.
- * **HM code**: R + Python code
! Parallel computation + GPR models can be trained on **GPU**

$$f(X, Y) = \begin{pmatrix} X \\ \bar{Y} \\ X^2 \\ X\bar{Y} \\ \bar{Y}^2 \end{pmatrix}$$

Justified by energy conservation constraints, check Schneider et al. 2017 for details (ESM 2.0 paper)

180-dimensional vector

MAKE OUR
PLANET
GREAT
AGAIN



HM on the Lorenz96

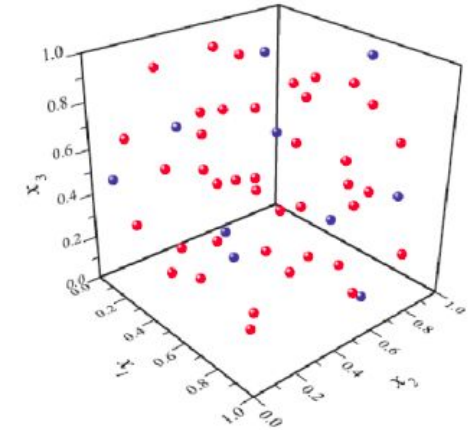
Initial guess of parameter space

| Params | Prior | True |
|--------|----------|------|
| F | [-20,20] | 10 |
| h | [-2,2] | 1 |
| c | [0,20] | 10 |
| b | [-20,20] | 10 |

40 samples
from a LHS



Space filling design



Run the L96 model

Build a training database
for the emulator:

`x_train.size=(40,4)`

`y_train.size=(40,180)`

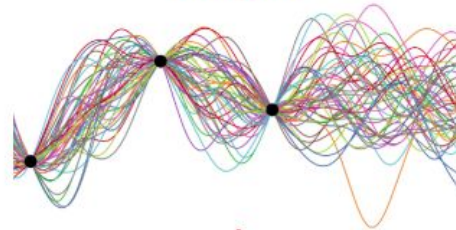
Use PCA

`y_train.size=(40,8)`

Here, one GP
Per output



Train the emulator then use it for
inference on a large number of
samples

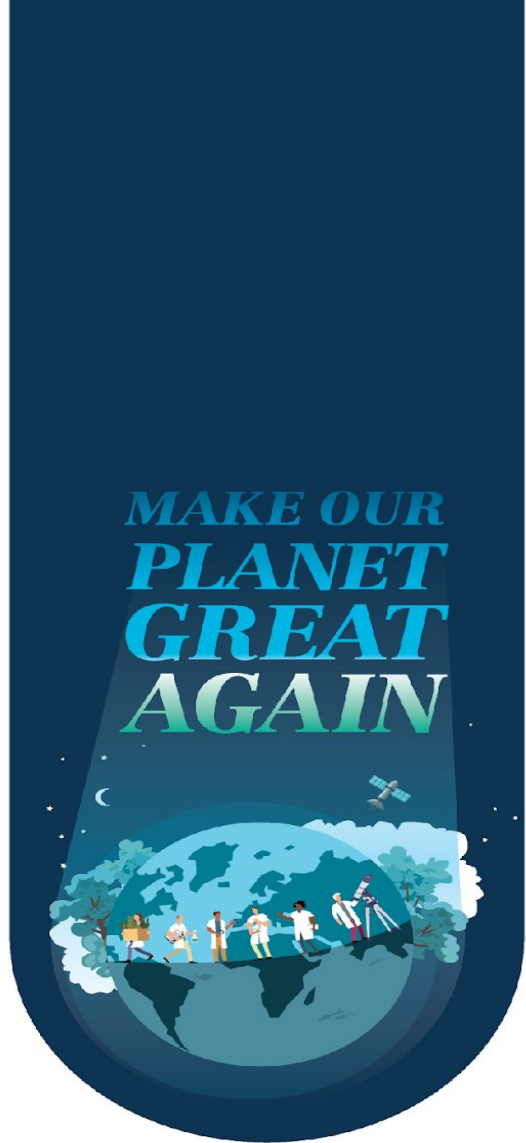


**Calculate
Implausibility**

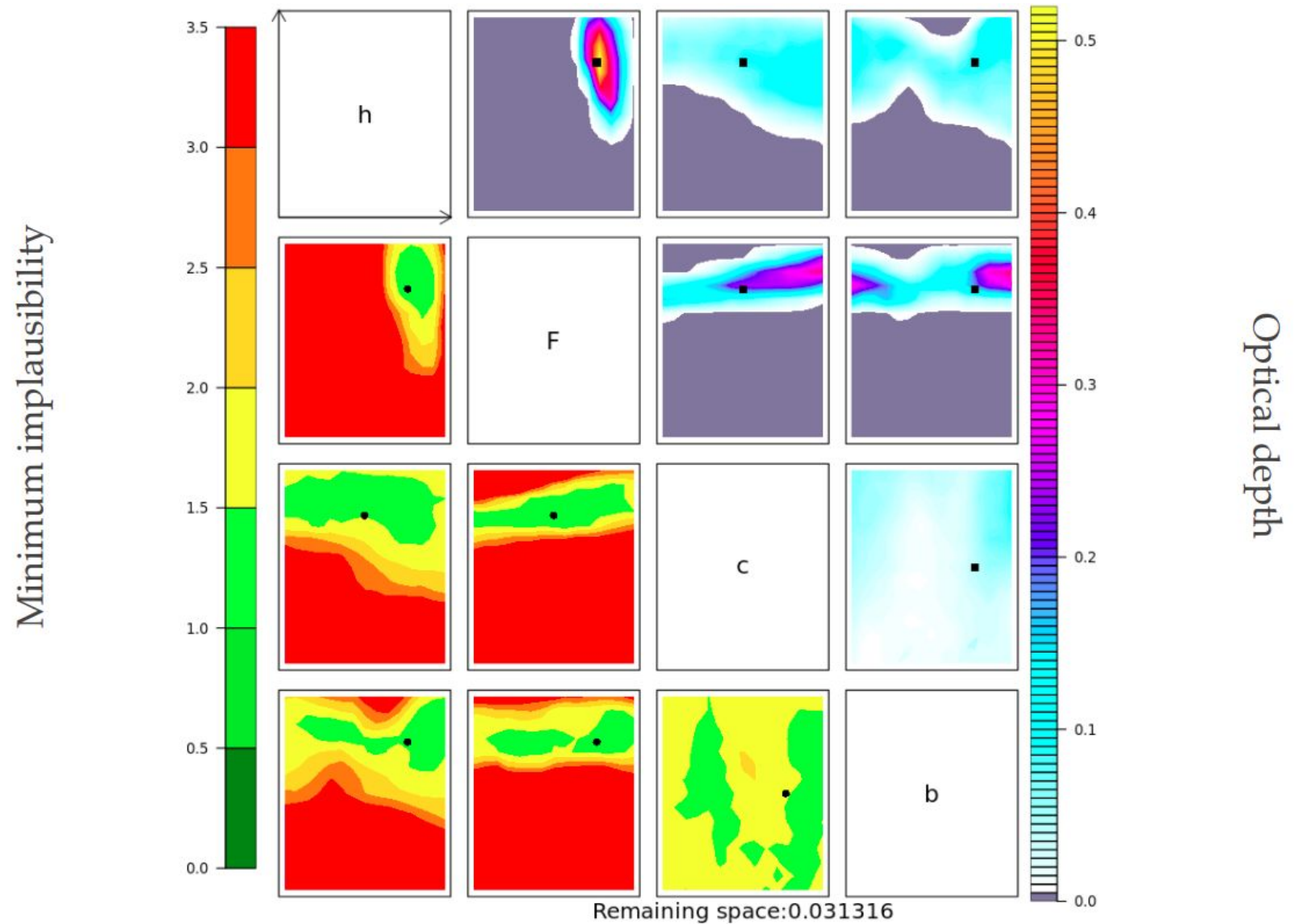
$$I(\theta) = \frac{|E[f(\theta)] - z|}{\sqrt{\text{Var}[f(\theta)]}}$$

MAKE OUR
PLANET
GREAT
AGAIN





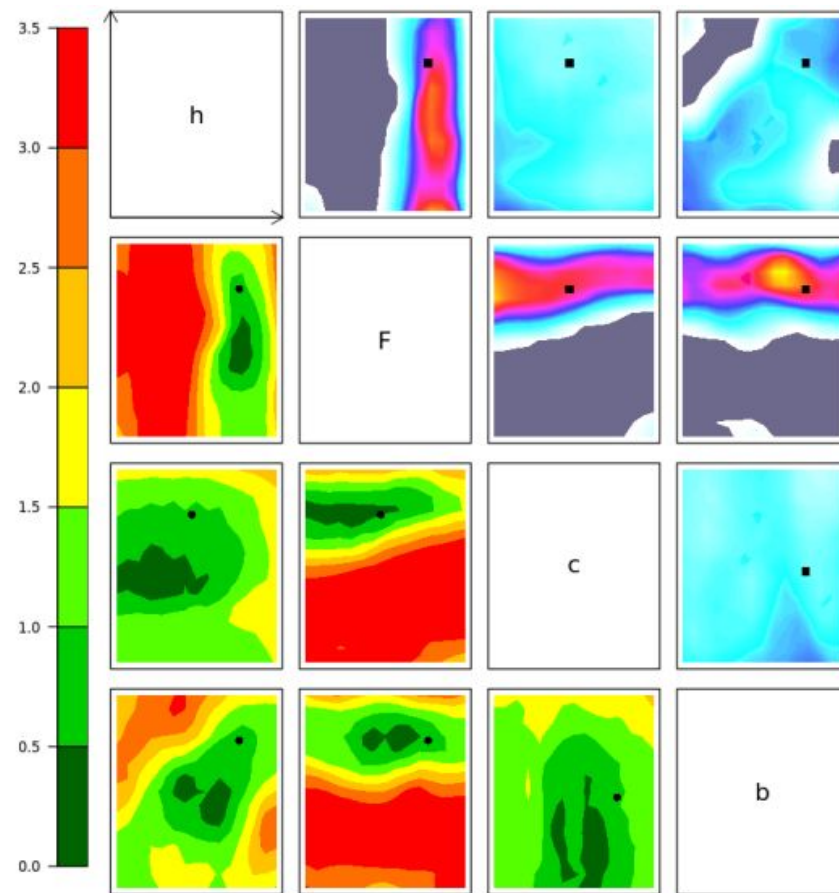
explaining NROY plots



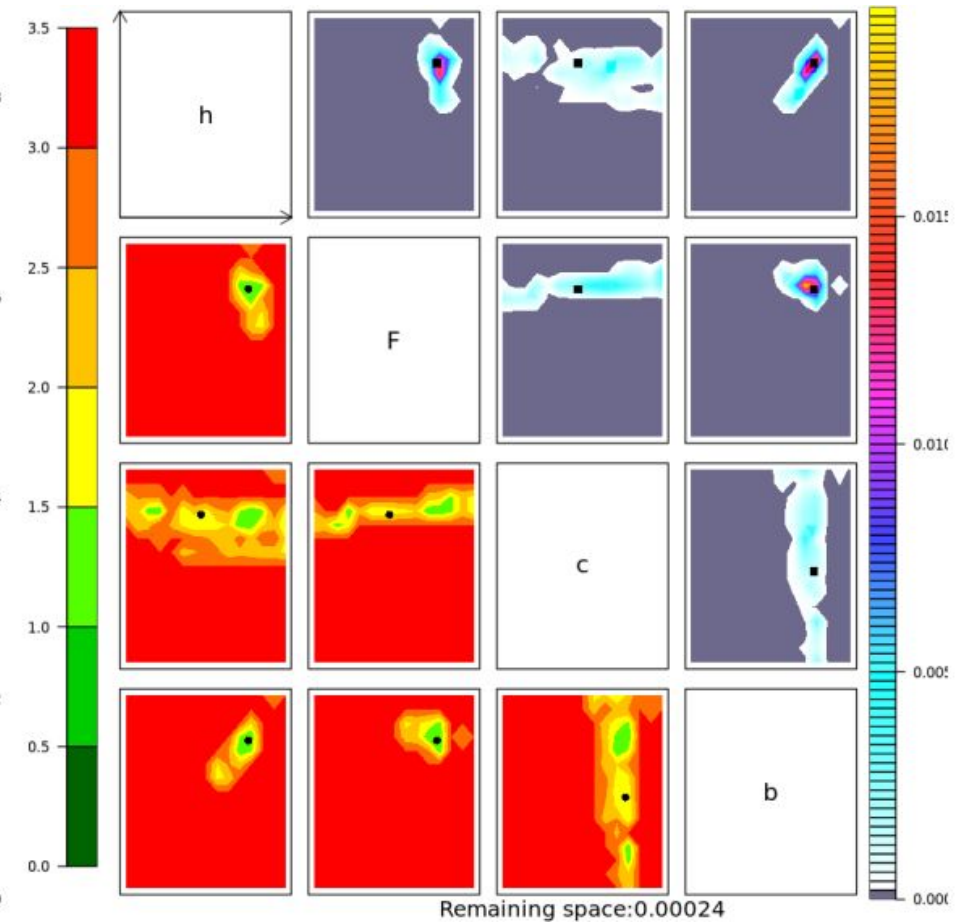
HM on the Lorenz96

MAKE OUR
PLANET
GREAT
AGAIN

| wave | NROY (%) | NbSim |
|-------------|----------|-------|
| 1 | 16.96 | 40 |
| 2 | 7.91 | 40 |
| 3 | 5.55 | 40 |
| 4 | 2.31 | 40 |
| 5 | 0.94 | 40 |
| 6 | 0.02 | 40 |
| Total = 240 | | |



wave 1



wave 6

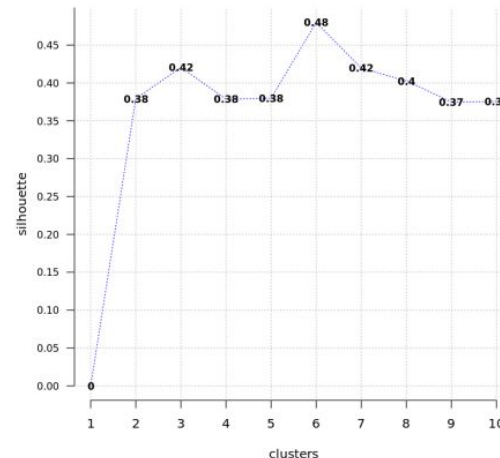
what to do with the NROY?

Open question, depends heavily on the computational budget

In case of a very short budget, an idea can be the use of **clustering** and selecting cluster centers

Here we use ***K-means*** and find six clusters

verification step where we make sure the six cluster centers belong to the last NROY



| | h | F | c | b |
|---|------|-------|-------|-------|
| 1 | 0.99 | 11.90 | 16.21 | 9.17 |
| 2 | 1.15 | 8.94 | 3.94 | 10.33 |
| 3 | 0.58 | 10.31 | 11.90 | 6.89 |
| 4 | 0.92 | 10.31 | 10.28 | 9.35 |
| 5 | 1.87 | 11.52 | 19.03 | 15.65 |

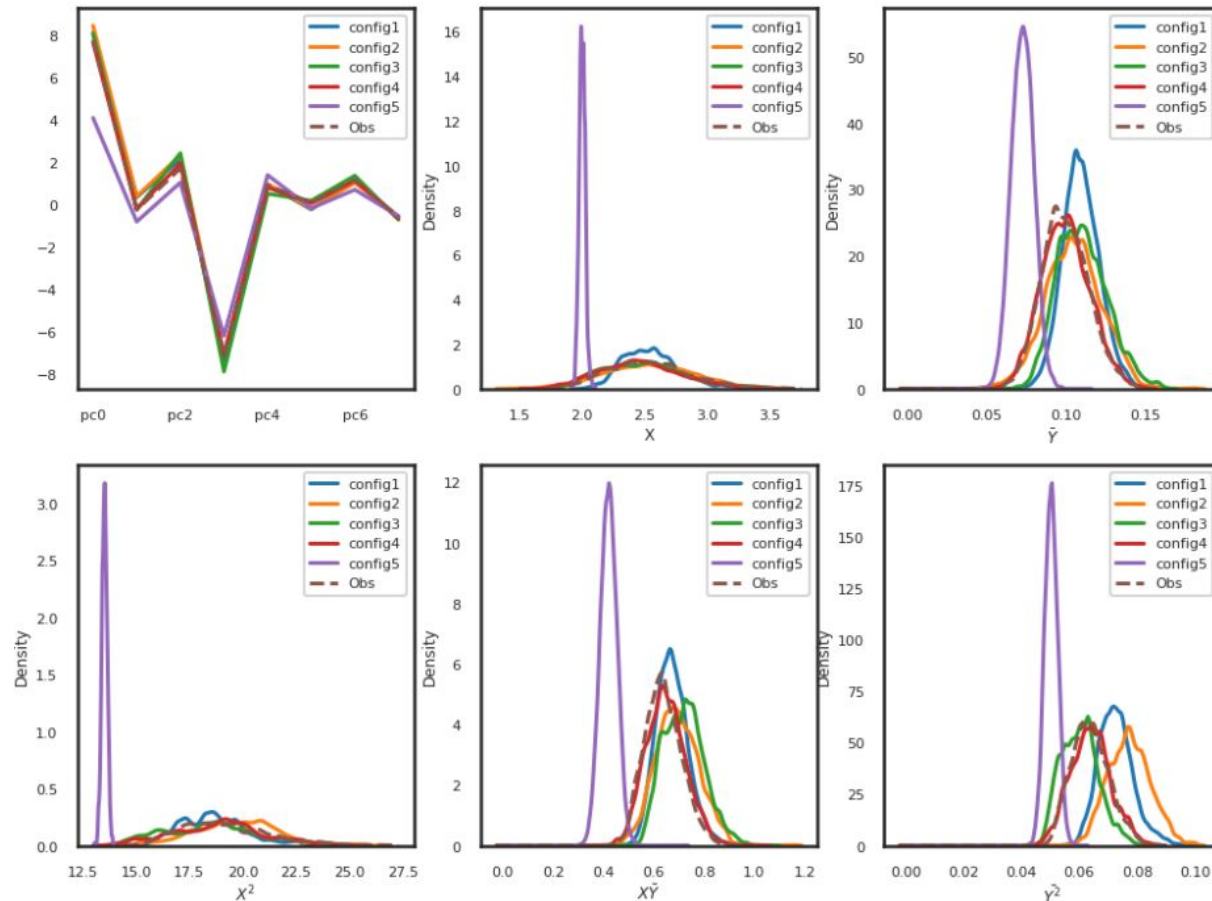
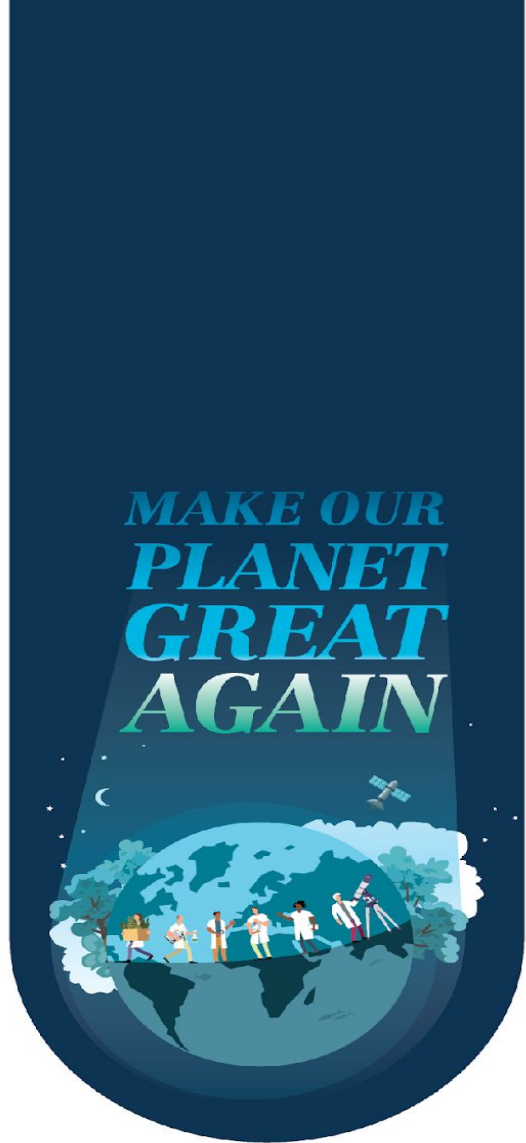
centers of clusters

MAKE OUR
PLANET
GREAT
AGAIN



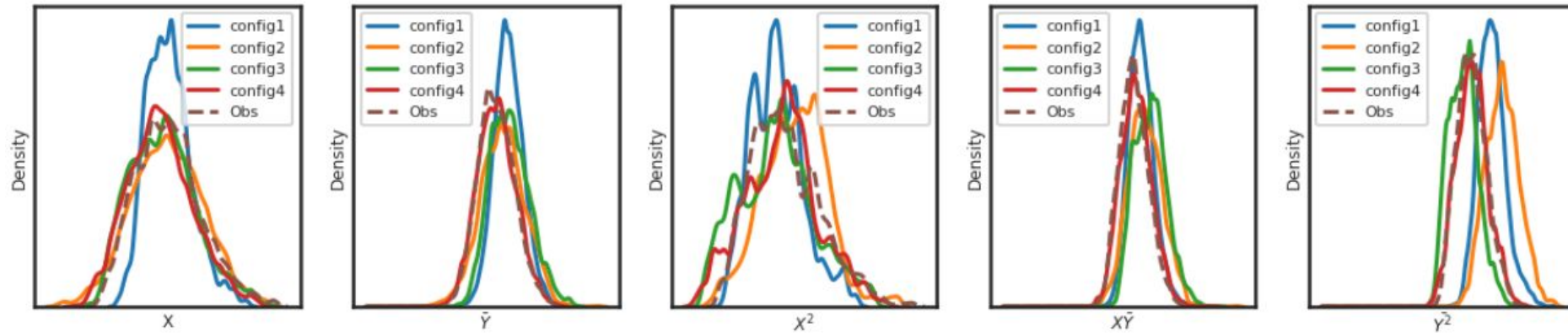
HM on the Lorenz96

We take the set of parameters and **run the real Lorenz96 simulation** then check the metrics and compare them with observations



HM on the Lorenz96

We take the set of parameters and **run the real Lorenz96 simulation then check the metrics and compare them with observations**



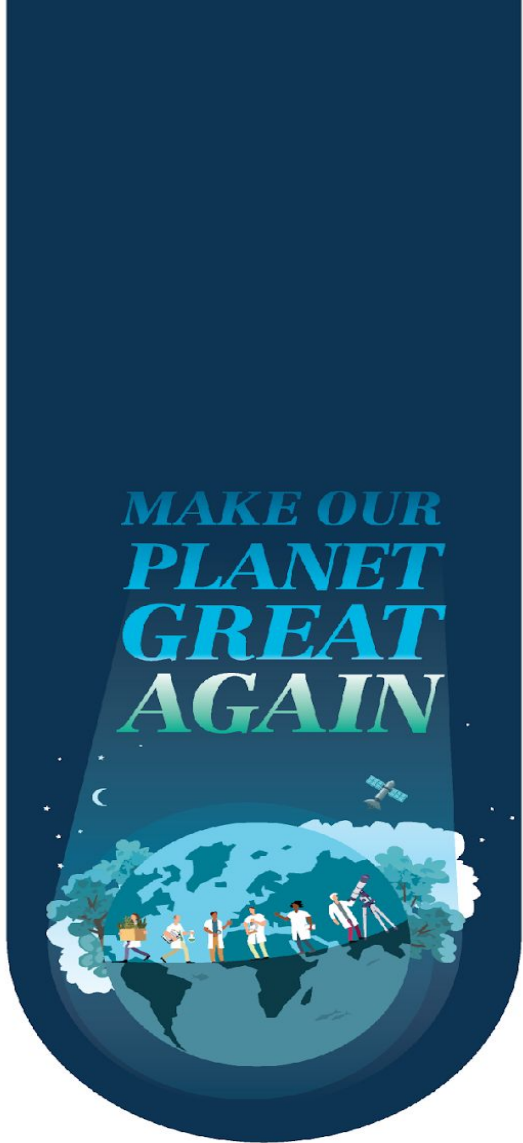
| | h | F | c | b | KL-div |
|---|------|-------|-------|-------|-------------|
| 1 | 0.99 | 11.90 | 16.21 | 9.17 | 0.13 |
| 2 | 1.15 | 8.94 | 3.94 | 10.33 | 0.09 |
| 3 | 0.58 | 10.31 | 11.90 | 6.89 | 0.15 |
| 4 | 0.92 | 10.31 | 10.28 | 9.35 | 0.01 |

MAKE OUR
PLANET
GREAT
AGAIN



Lessons learned

- History Matching is a powerful tool that can **assist (and not replace)** the expertise of domain-based tuning
- **Setting a computational budget in advance** is important and plays an important role in the final result
- Incorporate as much **domain expertise** as you can in the History Matching process
- There are still many open questions that could make History Matching more efficient for climate models (dimensionality reduction, non-convex NROY clusters, etc.)









Our review paper on Machine Learning for ocean science

MAKE OUR
PLANET
GREAT
AGAIN

ENVIRONMENTAL RESEARCH
LETTERS

TOPICAL REVIEW

Bridging observations, theory and numerical simulation of the ocean using machine learning

Maike Sonnewald^{1,2,3,9,*} , Redouane Lguensat^{4,5} , Daniel C Jones⁶ , Peter D Dueben⁷ , Julien Brajard^{5,8} 
and V Balaji^{1,2,4} 

¹ Princeton University, Program in Atmospheric and Oceanic Sciences, Princeton, NJ 08540, United States of America

² NOAA/OAR Geophysical Fluid Dynamics Laboratory, Ocean and Cryosphere Division, Princeton, NJ 08540, United States of America

³ University of Washington, School of Oceanography, Seattle, WA, United States of America

⁴ Laboratoire des Sciences du Climat et de l'Environnement (LSCE-IPSL), CEA Saclay, Gif Sur Yvette, France

⁵ LOCEAN-IPSL, Sorbonne Université, Paris, France

⁶ British Antarctic Survey, NERC, UKRI, Cambridge, United Kingdom

⁷ European Centre for Medium Range Weather Forecasts, Reading, United Kingdom

⁸ Nansen Center (NERSC), Bergen, Norway

⁹ Present address: Princeton University, Program in Atmospheric and Oceanic Sciences, 300 Forrestal Rd., Princeton, NJ 08540, United States of America

* Author to whom any correspondence should be addressed.

E-mail: maikes@princeton.edu

Keywords: ocean science, physical oceanography, observations, theory, modelling, supervised machine learning, unsupervised machine learning

