

Observation of acoustic normal modes of the atmosphere after the 2022 Hunga-Tonga eruption.

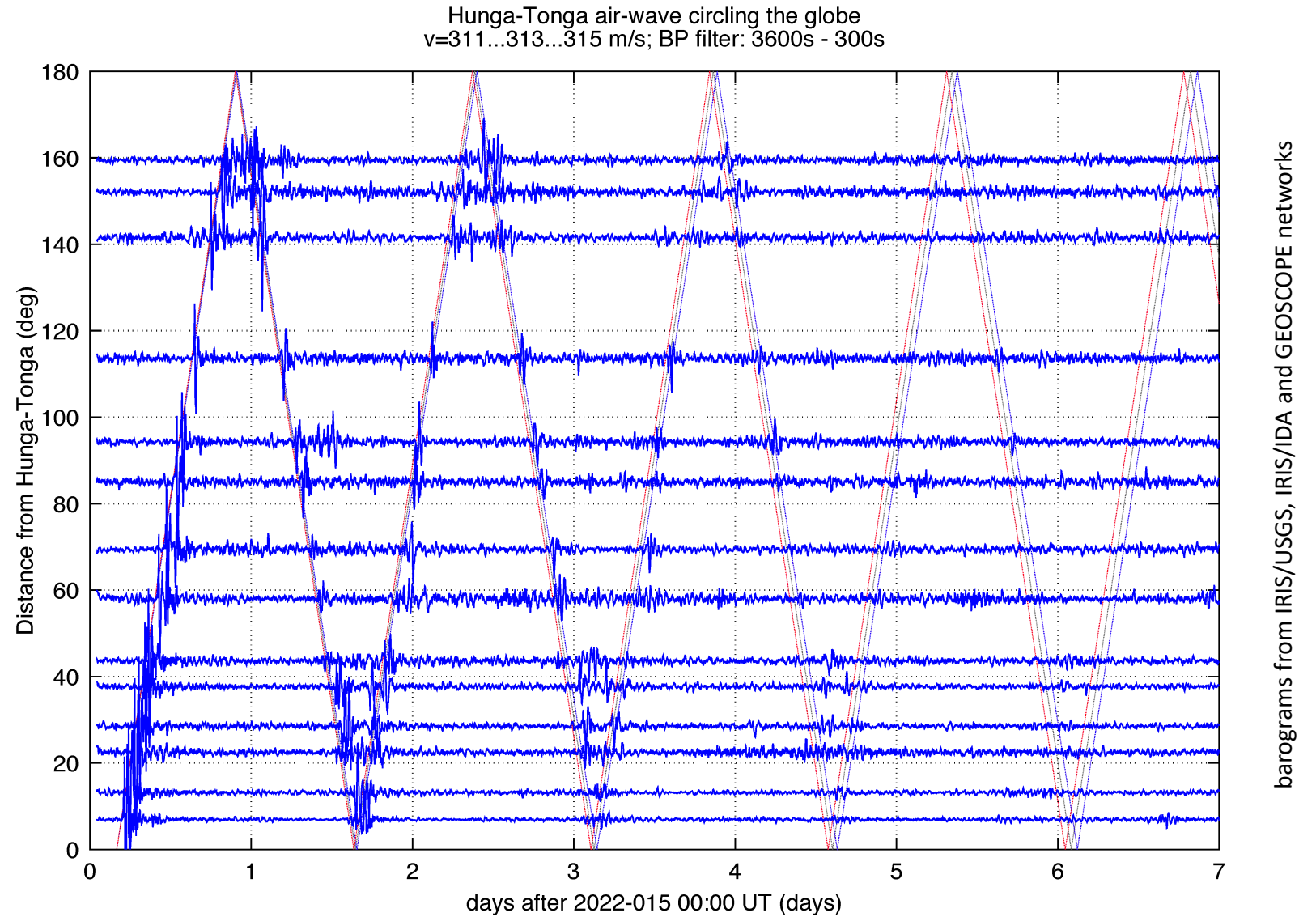


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EGU22-13581

Lamb waves in the atmosphere orbiting the Earth multiple times.

Group velocity $u=313$ m/s

Orbital period: 35.5 hrs

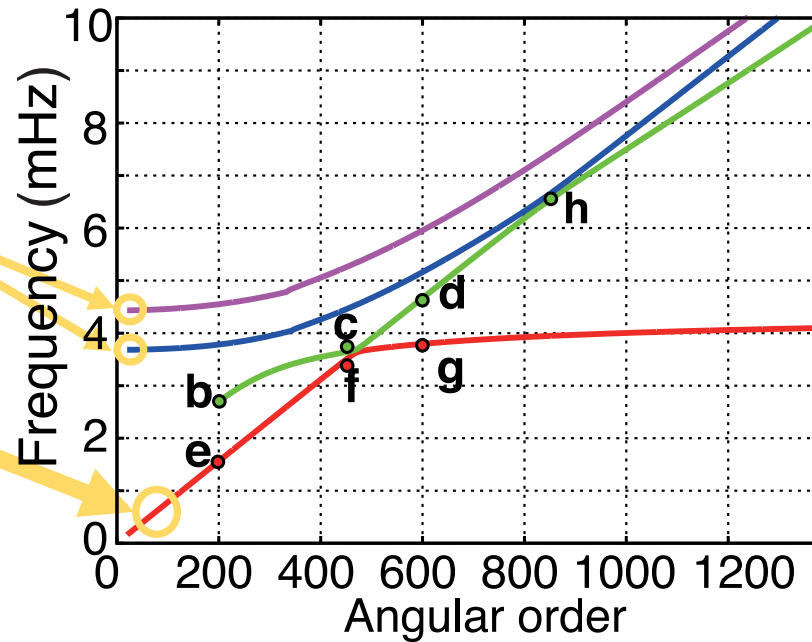
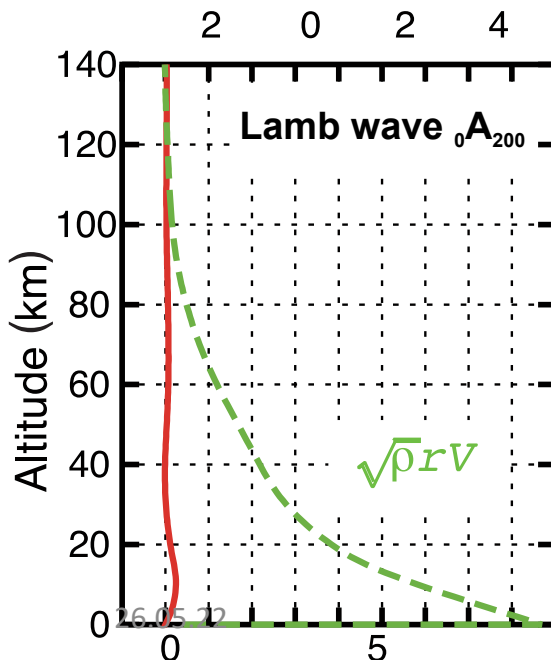


Dispersion diagram for the atmosphere

(Nishida et al., Geophys. J. Int., 2014, Background Lamb waves in the atmosphere)

Vertical acoustic modes:
excite bi-chromatic Rayleigh waves
(eg. Widmer&Zürn, GRL, 1992)

globe circling Lamb waves
(horizontally polarized)



Nomenclature

Fundamental acoustic modes

— h —

First overtones of acoustic modes

—

Lamb waves

— e — f — d — h —

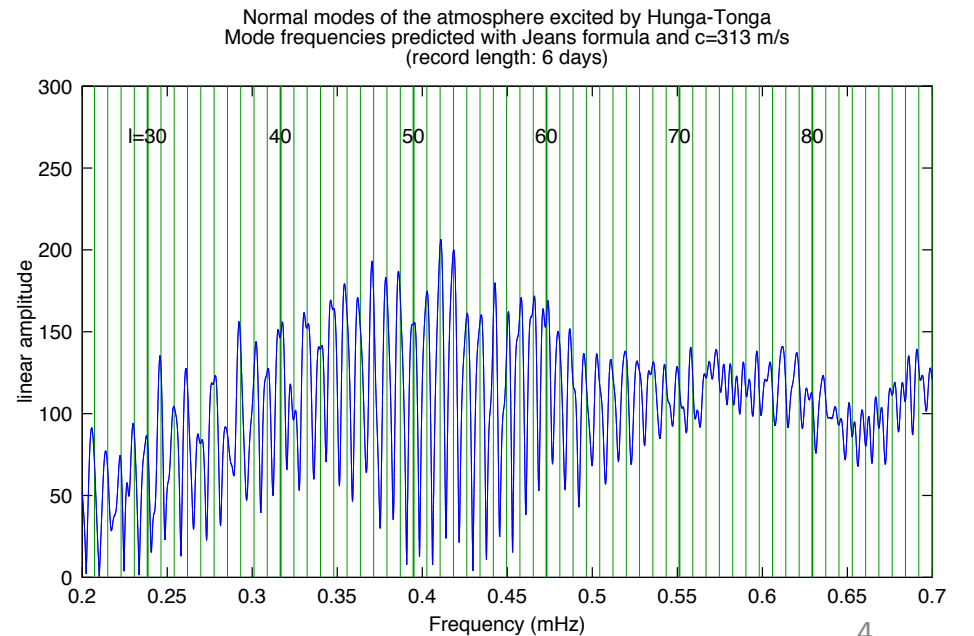
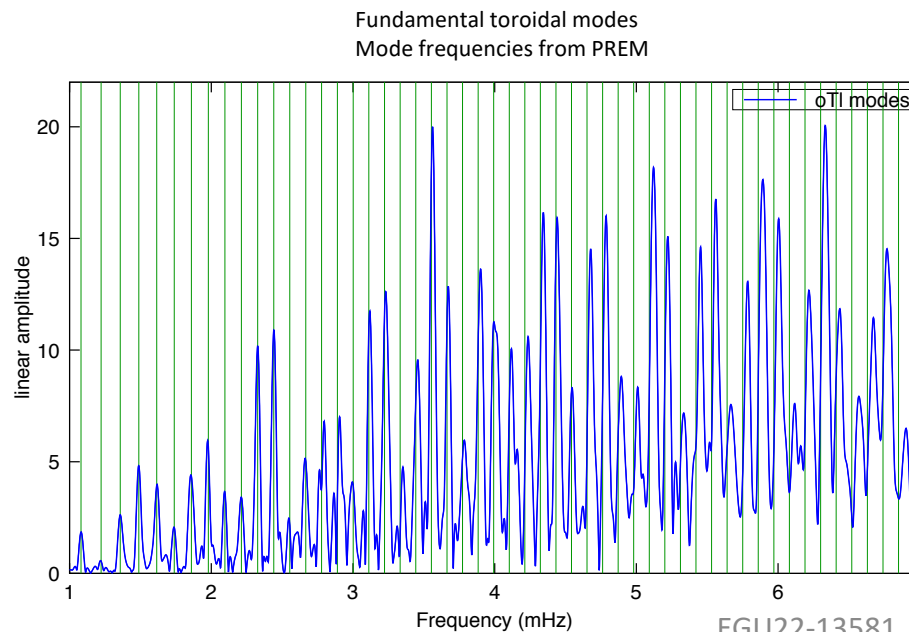
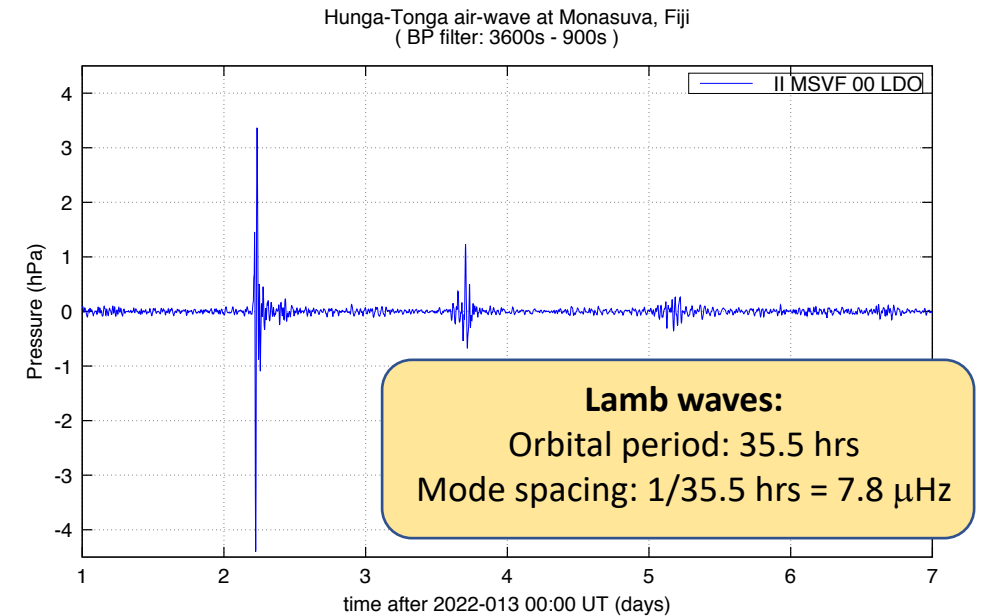
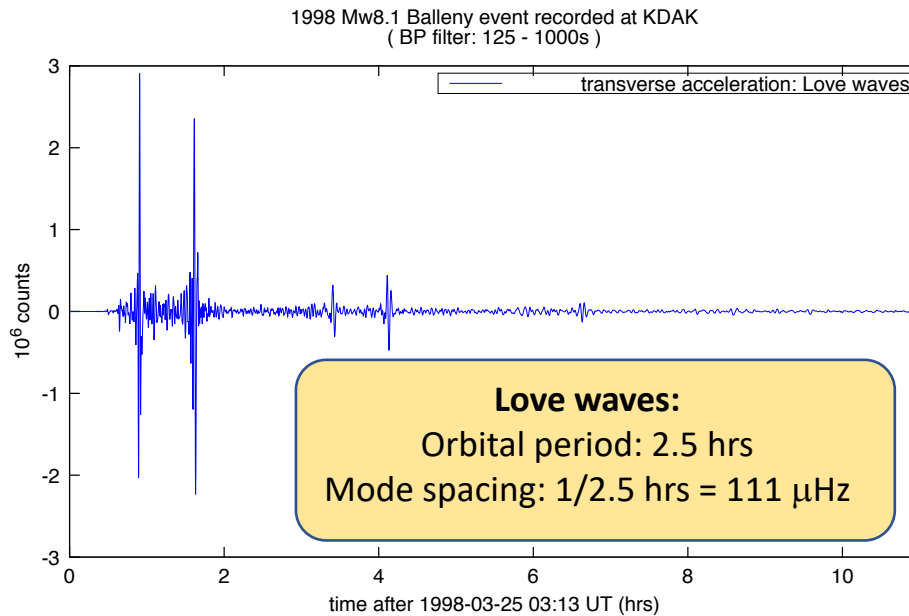
Thermospheric gravity wave

— b — c — g —

For Lamb waves $u=c$ and hence we can use Jeans Formula to predict mode frequencies for any angular order.

$$k = \frac{\ell + 1/2}{R} = \frac{\omega_\ell}{c}$$

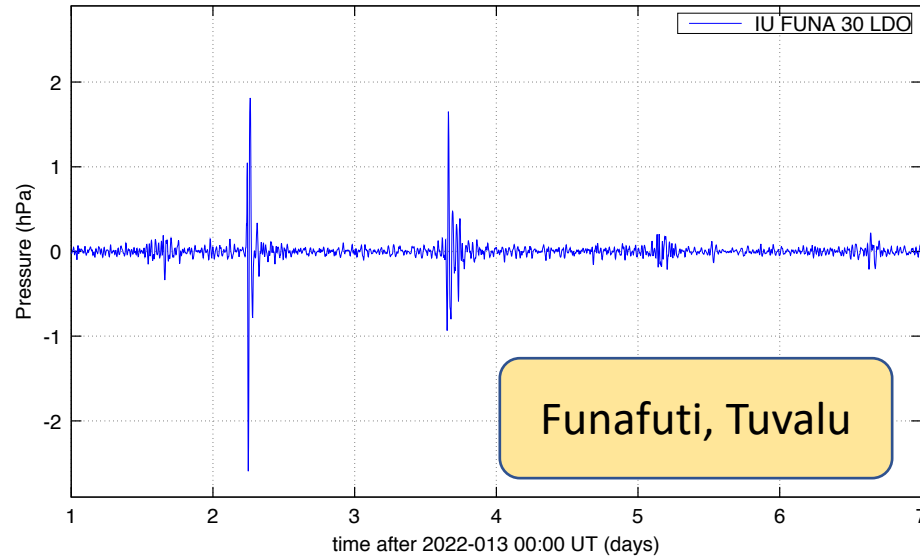
Analogy between Love- and Lamb-waves



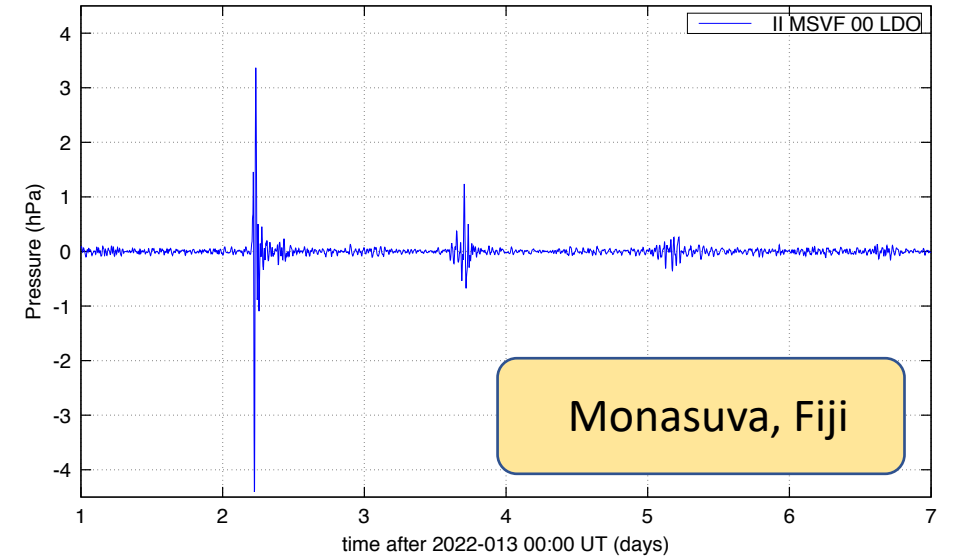
Note: large peak frequency shifts away from predicted mode frequencies.

This renders interpretation of peak frequencies difficult.

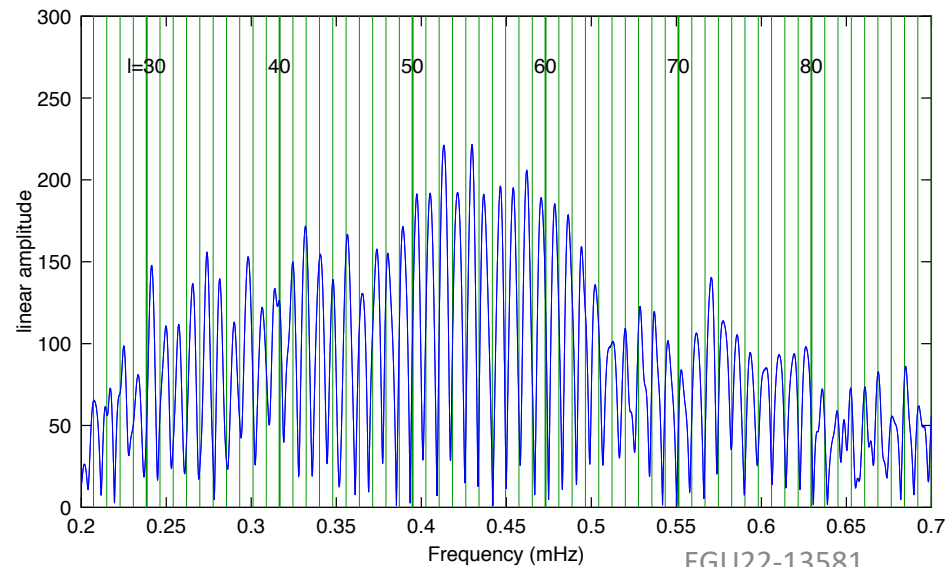
Hunga-Tonga air-wave at Funafuti, Tuvalu
(BP filter: 3600s - 900s)



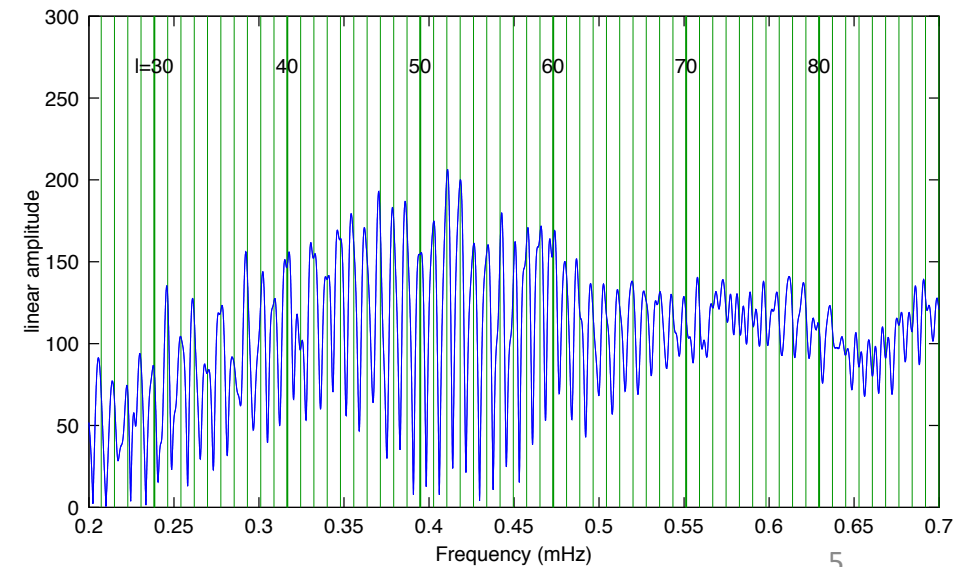
Hunga-Tonga air-wave at Monasuva, Fiji
(BP filter: 3600s - 900s)



Normal modes of the atmosphere excited by Hunga-Tonga
Mode frequencies predicted with Jeans formula and $c=313$ m/s
(record length: 6 days)



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Mode frequencies predicted with Jeans formula and $c=313$ m/s
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Conclusions

Honga Tonga has excited globe circling Lamb waves.

These can be observed for at least 4 full orbits, where one orbit takes ~ 35.5 hours.

Constructive and destructive interference between waves that have left the source in opposite direction leads to a global pattern of standing waves: normal modes of the atmosphere.

On favorable source-receiver great circles these modes can be observed as discrete peaks in the Fourier spectra of barograms between 0.2 – 0.7 mHz.

The observed spacing between adjacent modes of $7.8 \mu\text{Hz}$ ($=1/35.5$ hrs) confirms our normal mode hypothesis.

Heterogeneities in the global atmosphere (wind, temperature,...) lead to large peak frequency shifts such that spectral peaks cannot be unambiguously attributed to a particular spherical harmonic degree.