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Taiwan

A Stochastic Rainfall Generator Suitable for Modeling Future Compound Disasters Associated with Heavy Rainfall

Rainfall Variability – Influence on Urban Flood



Journal of Hydrology
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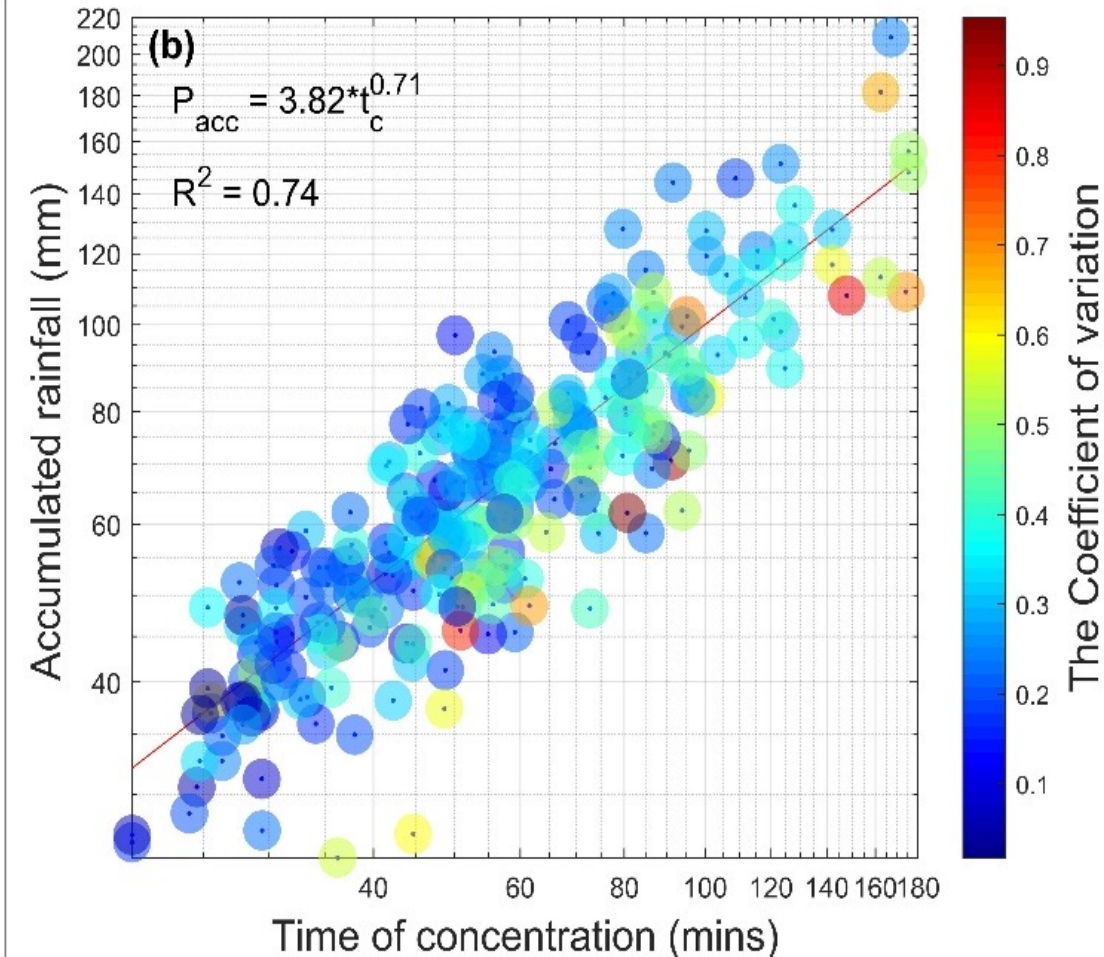
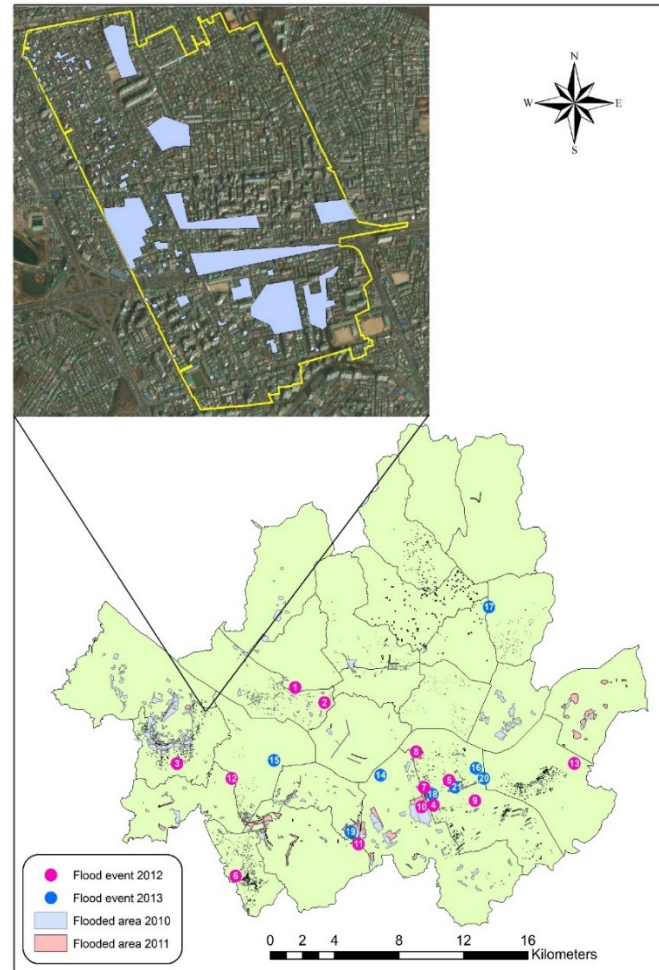
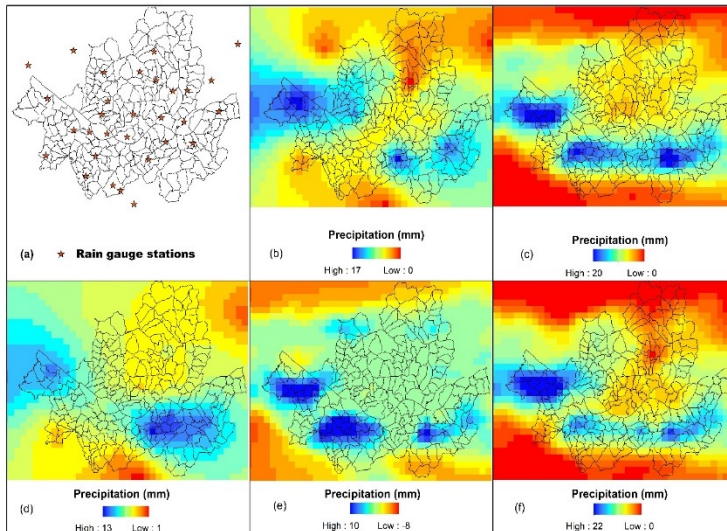


Research papers

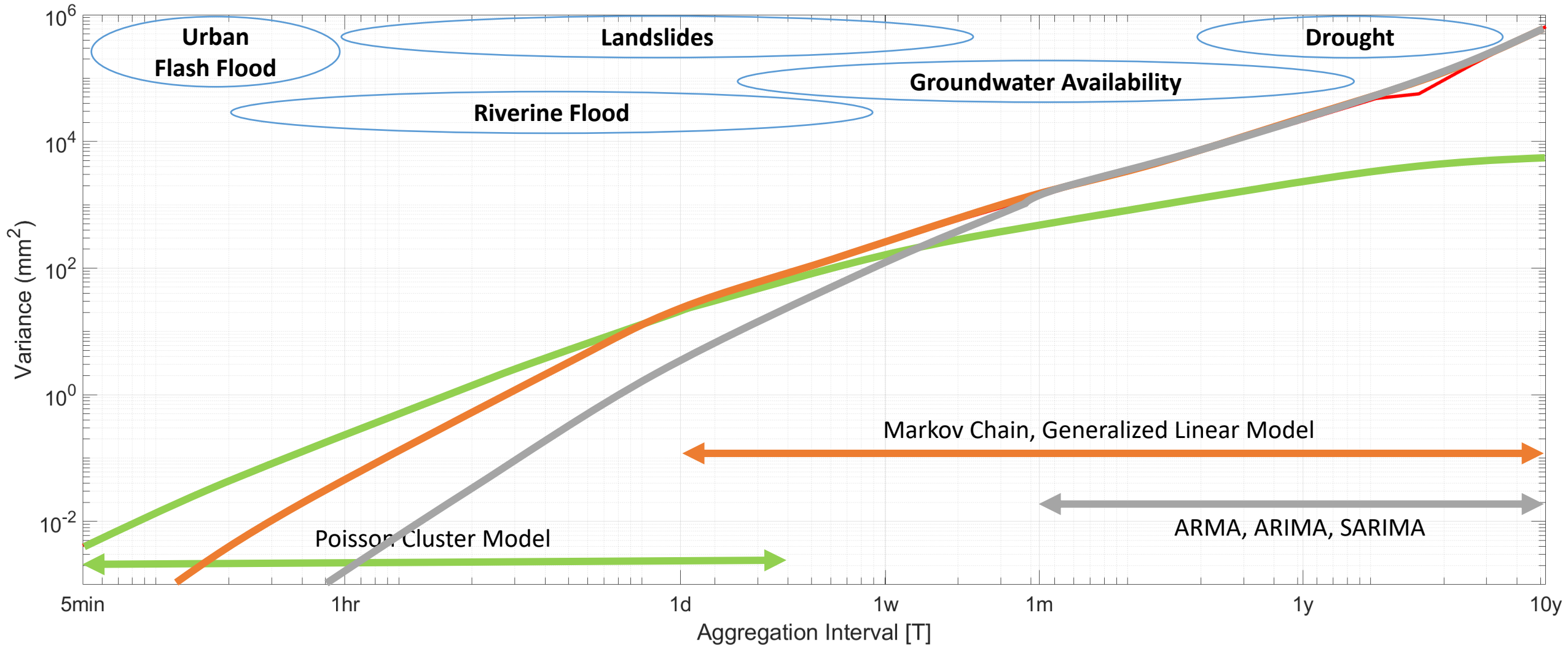
Determination of flood-inducing rainfall and runoff for highly urbanized area based on high-resolution radar-gauge composite rainfall data and flooded area GIS data

Duc Anh Dao, Dongkyun Kim , Soohyun Kim, Jeongha Park

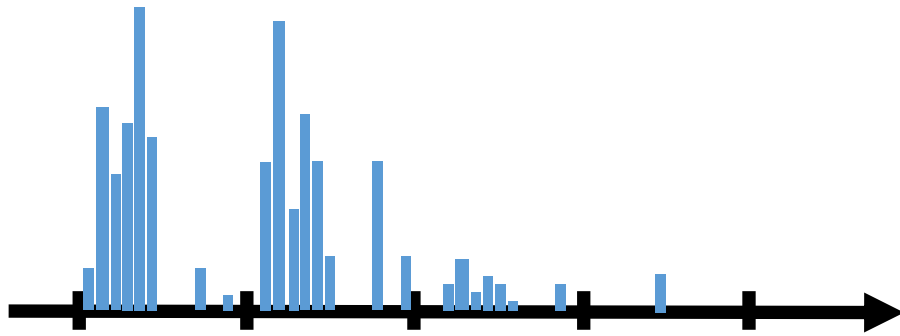
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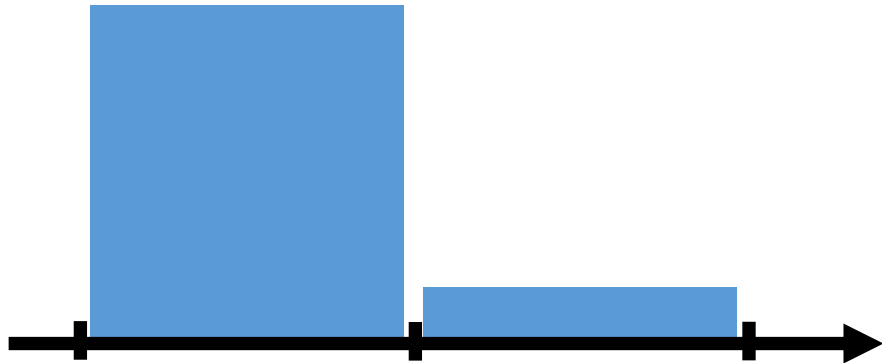
Rainfall Model for Holistic Framework



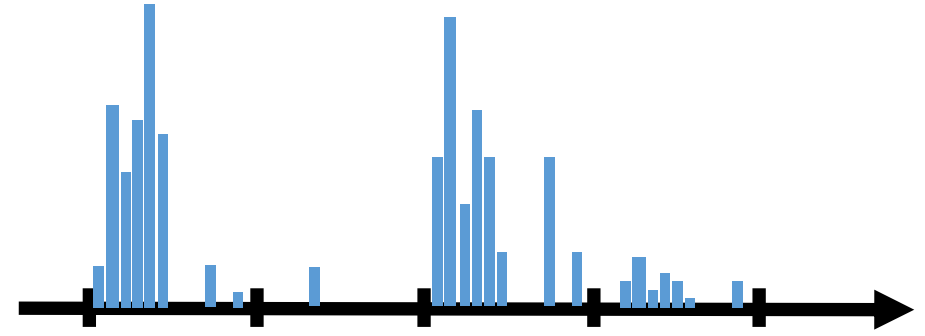
Good Memory



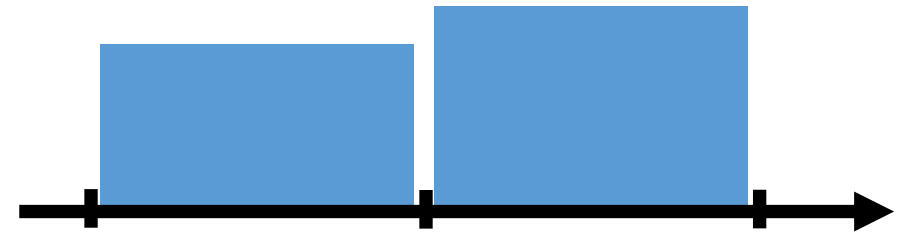
Greater Variability



Bad Memory



Less Variability



$$Var(Y^{(nh)}) = nVar(Y^{(h)}) + \sum_{i=1}^n \sum_{j=1, j \neq i}^n Cov(Y_i^{(h)}, Y_j^{(h)})$$

Poisson Cluster Rainfall Model

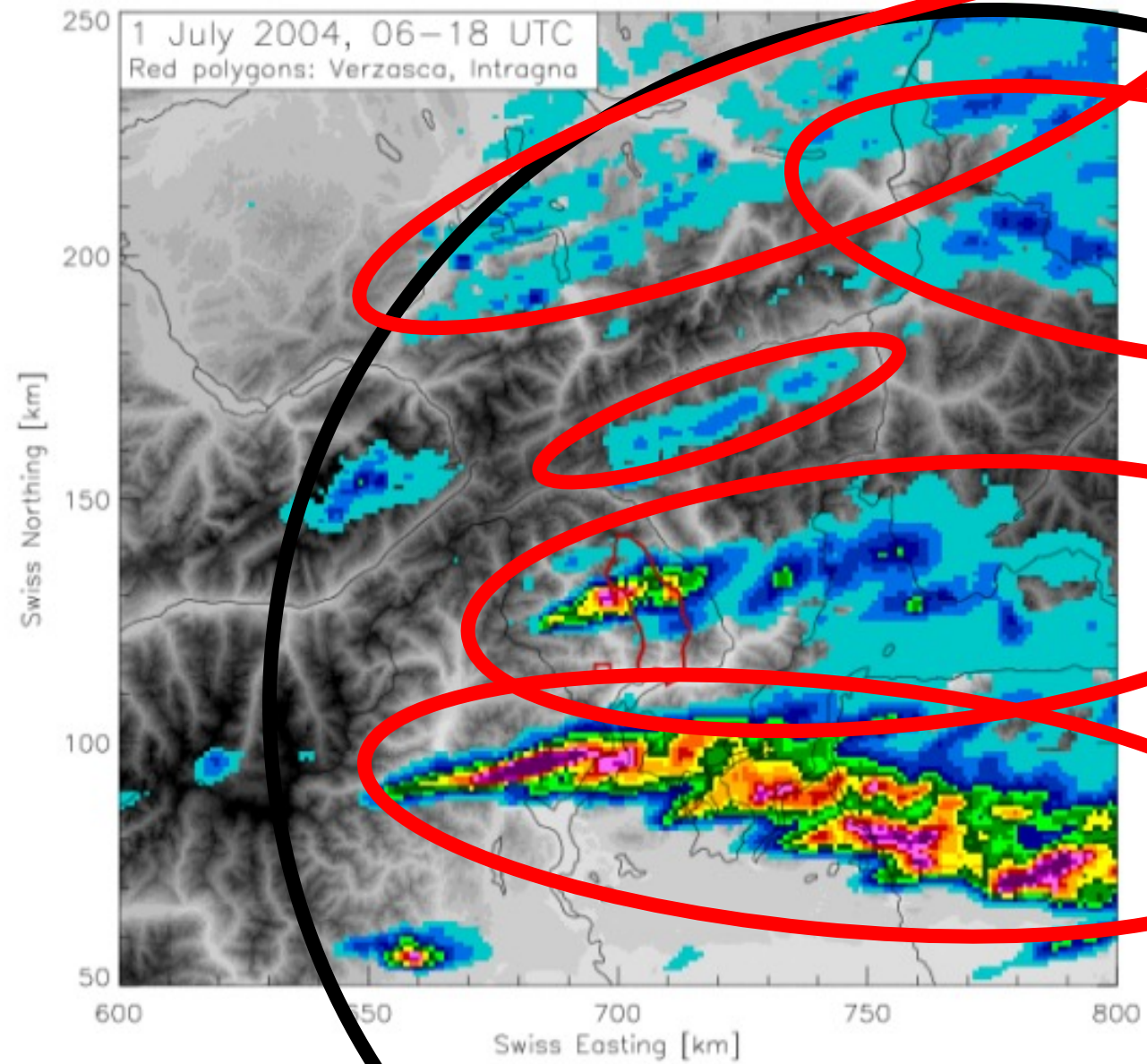
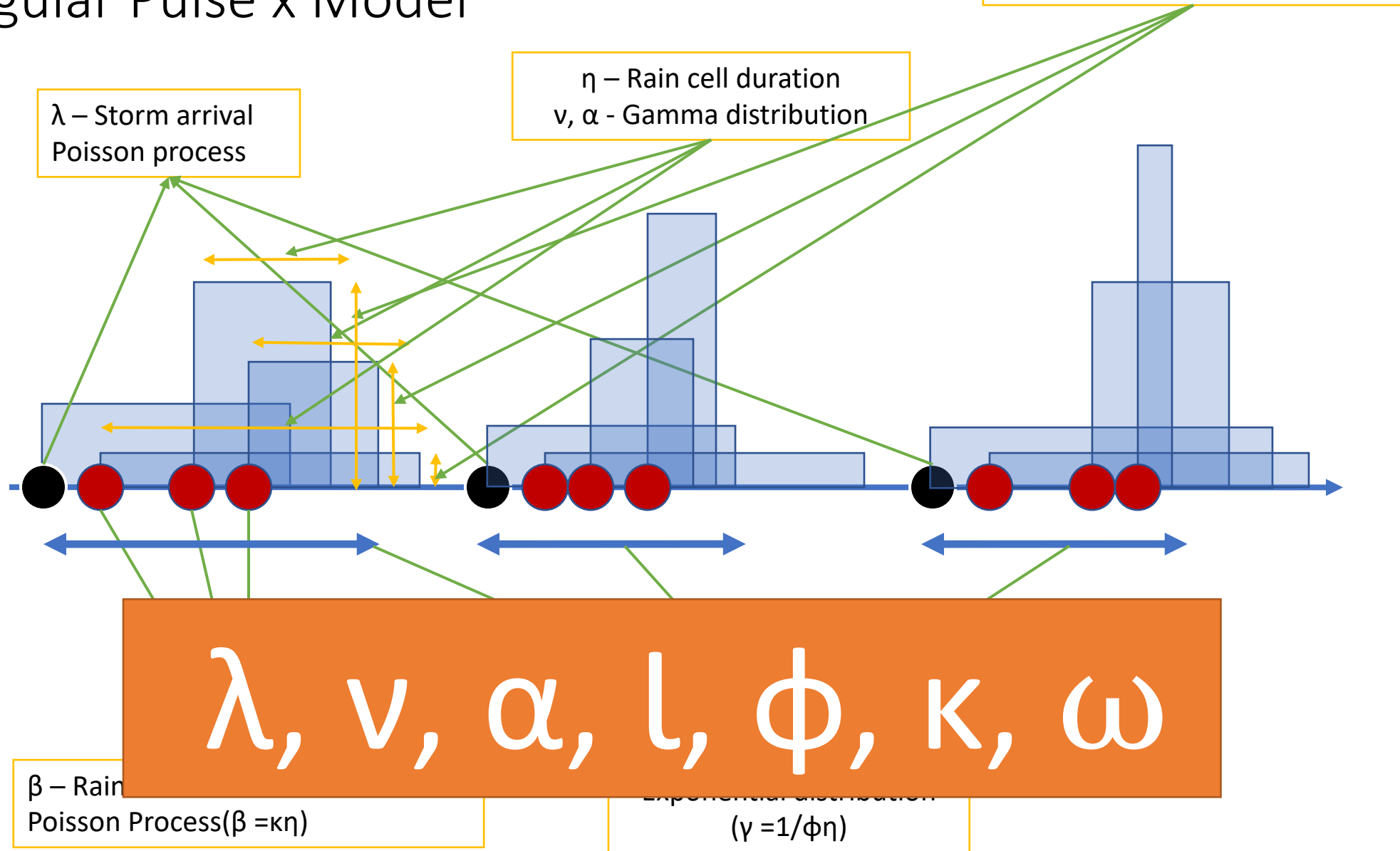


Image Source: <http://www.meteoswiss.admin.ch/web/en/research/projects/rain.html>



Randomized Bartlett Lewis Rectangular Pulse x Model



Parameter Calibration

How to get..
 $\lambda, \nu, \alpha, \iota, \phi, \kappa, \omega$

$$E[Y_t^{(T)}] = \lambda \mu \mu_c \frac{\nu}{\alpha - 1} T$$

$$\begin{aligned} \text{Var}[Y_t^{(T)}] &= \frac{2 \nu^{2-\alpha} T}{\alpha - 2} \left(k_1 - \frac{k_2}{\phi} \right) - \frac{2 \nu^{3-\alpha}}{(\alpha - 2)(\alpha - 3)} \left(k_1 - \frac{k_2}{\phi^2} \right) \\ &+ \frac{2}{(\alpha - 2)(\alpha - 3)} \left[k_1 (T + \nu)^{3-\alpha} - \frac{k_2}{\phi^2} (\phi T + \nu)^{3-\alpha} \right] \end{aligned}$$

$$\begin{aligned} \text{Cov}[Y_t^{(T)}, Y_{t+s}^{(T)}] &= \frac{k_1}{(\alpha - 2)(\alpha - 3)} \{ [T(s - 1) + \nu]^{3-\alpha} + [T(s + 1) + \nu]^{3-\alpha} - 2(Ts + \nu)^{3-\alpha} \} \\ &+ \frac{k_2}{\phi^2 (\alpha - 2)(\alpha - 3)} \{ 2(\phi Ts + \nu)^{3-\alpha} - [\phi T(s - 1) + \nu]^{3-\alpha} - [\phi T(s + 1) + \nu]^{3-\alpha} \} \end{aligned}$$

$$\begin{aligned} P(\text{zero rainfall}) &= \exp \left\{ -\lambda T - \frac{\lambda \nu}{\phi (\alpha - 1)} \left[1 + \phi (\kappa + \phi) - \frac{1}{4} \phi (\kappa + \phi)(\kappa + 4\phi) \right. \right. \\ &\quad \left. \left. + \frac{\phi (\kappa + \phi)(4\kappa^2 + 27\kappa\phi + 72\phi^2)}{72} \right] \right. \\ &\quad \left. + \frac{\lambda \nu}{(\alpha - 1)(\kappa + \phi)} \left(1 - \kappa - \phi + \frac{3}{2} \kappa \phi + \phi^2 + \frac{\kappa^2}{2} \right) \right. \\ &\quad \left. + \frac{\lambda \nu}{(\alpha - 1)(\kappa + \phi)} \left[\frac{\nu}{\nu + (\kappa + \phi)T} \right]^{\alpha-1} \frac{\kappa}{\phi} \left(1 - \kappa - \phi + \frac{3}{2} \kappa \phi + \phi^2 + \frac{\kappa^2}{2} \right) \right\} \end{aligned}$$



European Journal of Operational Research

Volume 213, Issue 1, 16 August 2011, Pages 15-23



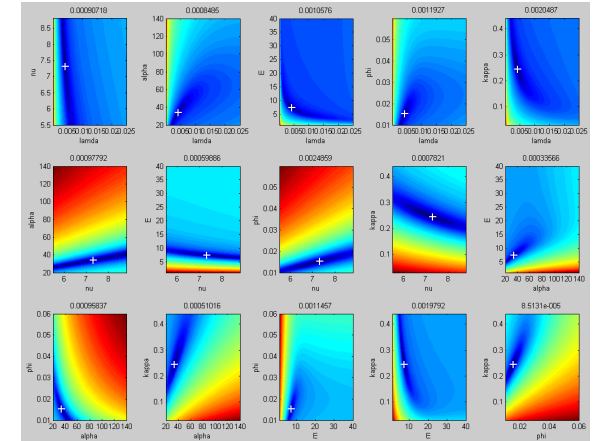
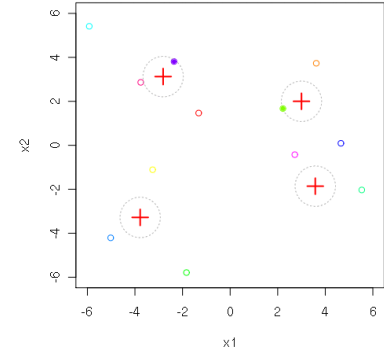
Discrete Optimization

Enhanced speciation in particle swarm optimization for multi-modal problems

Huidae Cho ^a✉, Dongkyun Kim ^a✉, Francisco Olivera ^a✉, Seth D. Guikema ^b✉

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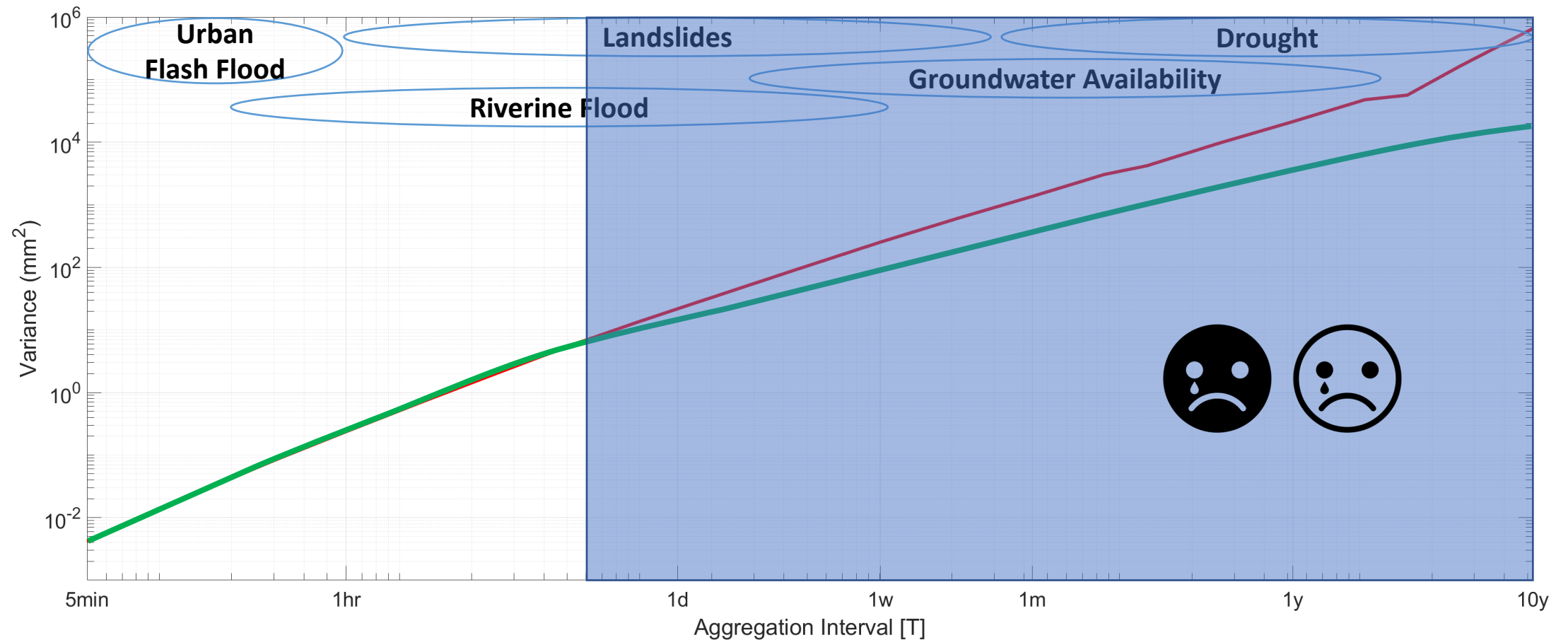


$$S(h) = \frac{\lambda \mu_c \mu_x^3 \sum_{k=1}^{k=8} Q_k(\phi, \kappa, f_1, f_2, 0)}{(1 + 2\phi + \phi^2)(\phi^4 - 2\phi^3 - 3\phi^2 + 8\phi - 4)\phi^3} \text{ for } \alpha > 4$$

$$\begin{aligned} S(h) &\approx \frac{\lambda \mu_c \mu_x^3}{(1 + 2\phi + \phi^2)(\phi^4 - 2\phi^3 - 3\phi^2 + 8\phi - 4)\phi^3} \\ &\quad \left[\frac{\nu^\alpha \eta_0^{\alpha-1} h^3}{\Gamma(\alpha)(\alpha-1)} (2\kappa^2(\phi^7 - 3\phi^6 + \phi^5 + 3\phi^4 - 2\phi^3) + f_2(\phi^9 - 6\phi^7 + 9\phi^5 - 4\phi^3) \right. \\ &\quad \left. + 3\kappa f_1(\phi^8 - \phi^7 - 5\phi^6 + 5\phi^5 + 4\phi^4 - 4\phi^3)) \right. \\ &\quad \left. + \sum_{k=1}^{k=8} Q_k(\phi, \kappa, f_1, f_2, \eta_0) \right] \text{ for } 1 < \alpha \leq 4 \end{aligned}$$

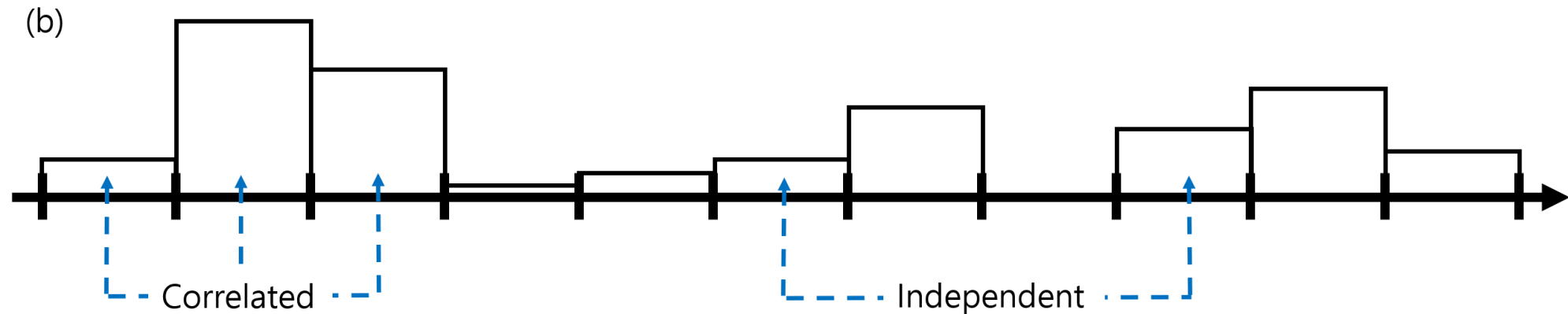
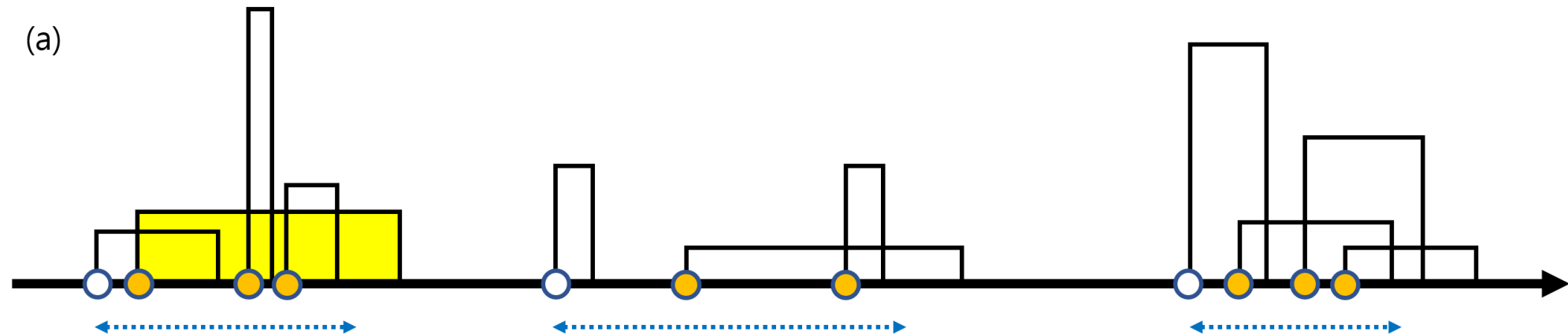
$$S(h) = \infty \text{ for } \alpha \leq 1$$

Issue of the Poisson Cluster Rainfall Model

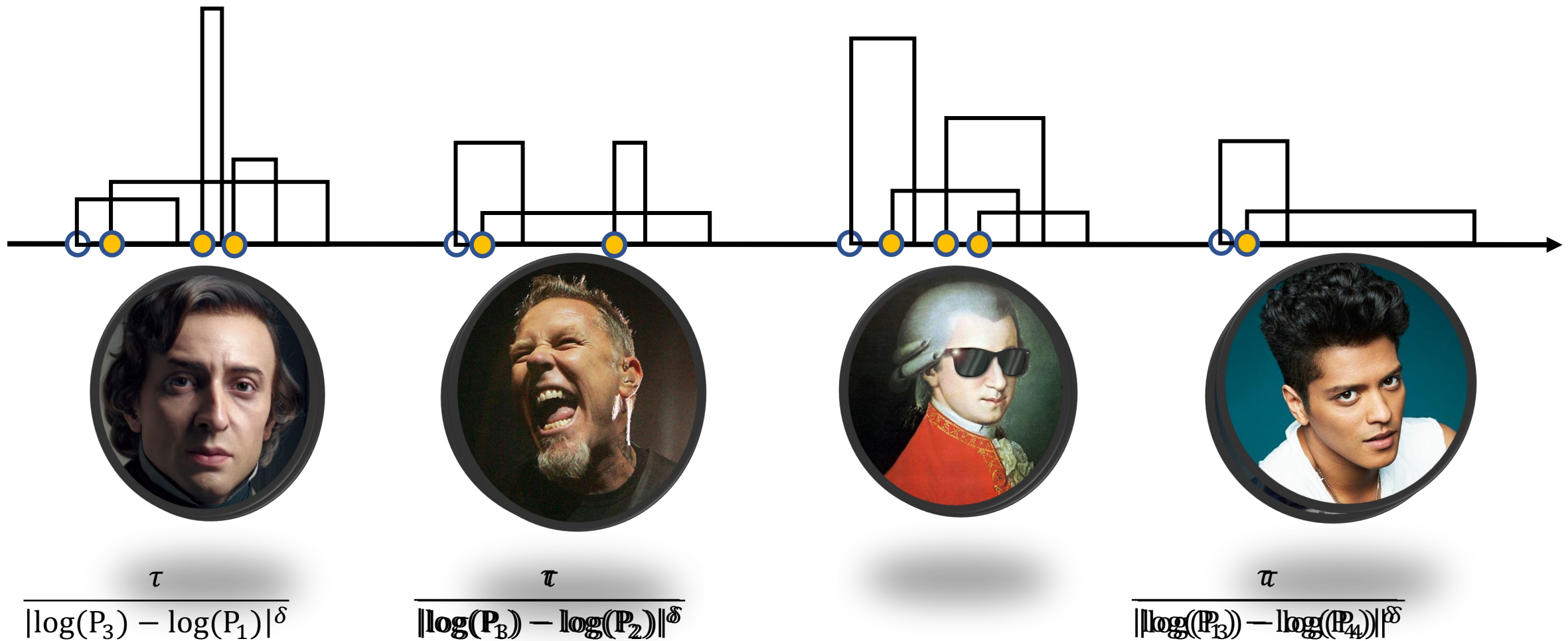


Issue of the Poisson Cluster Rainfall Model

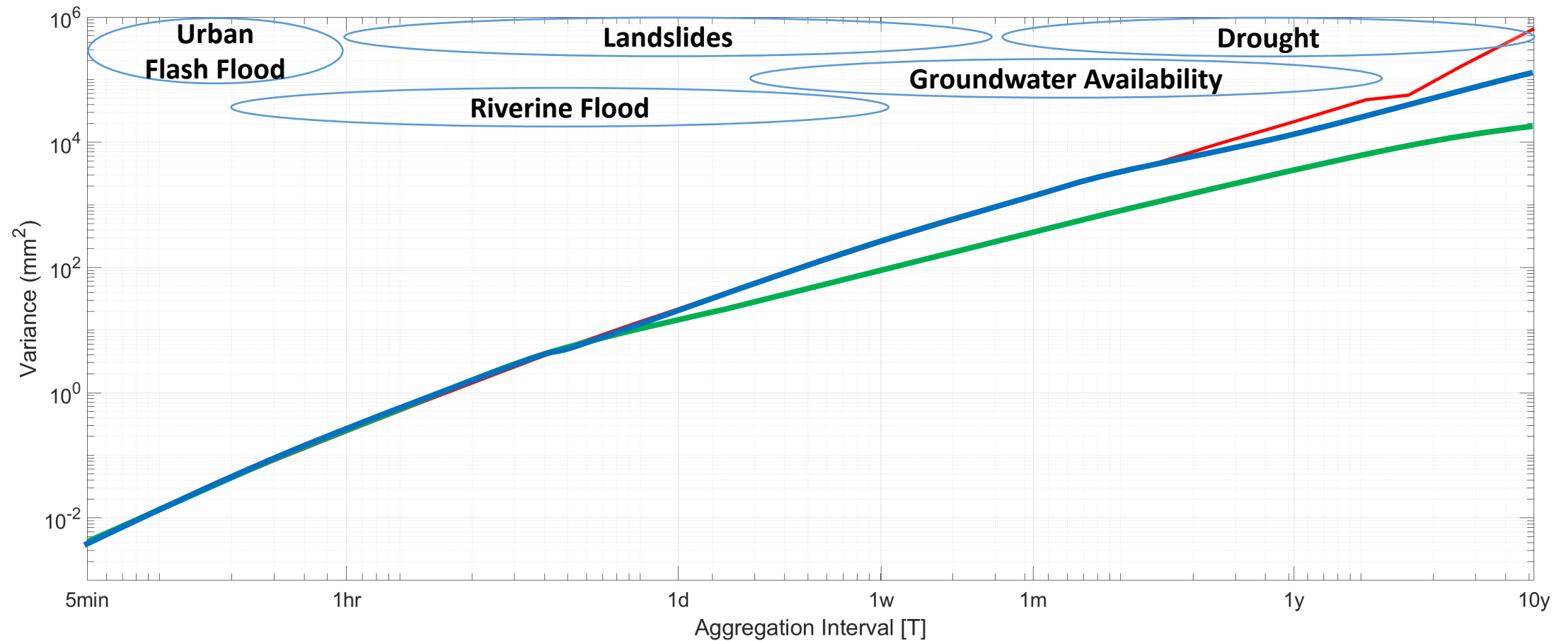
○ Poisson process of rainstorm arrival \longleftrightarrow Storm activity time ● Poisson process of rain cell arrival □ Rain cell



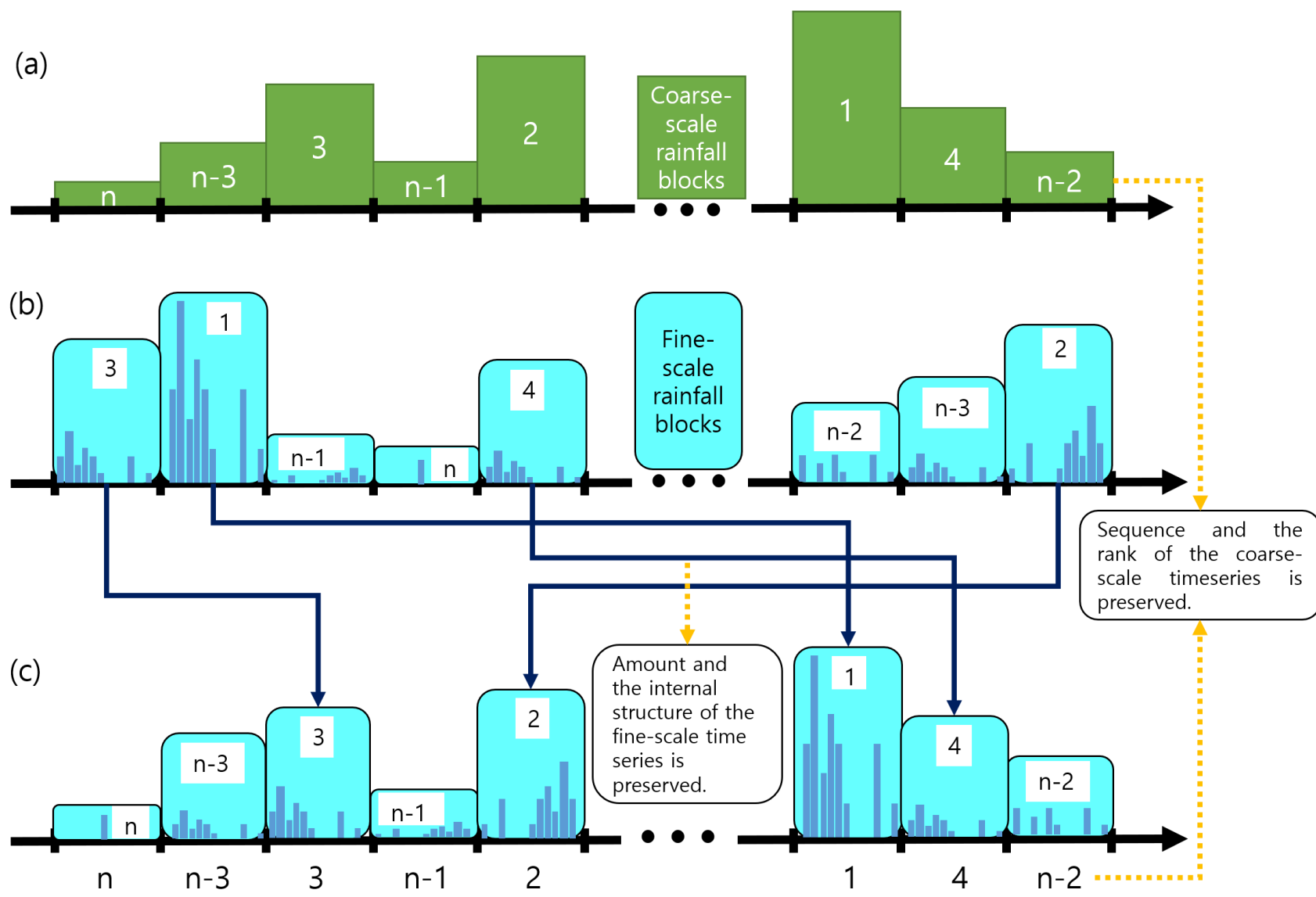
Poisson Cluster – Shufflex2 Model



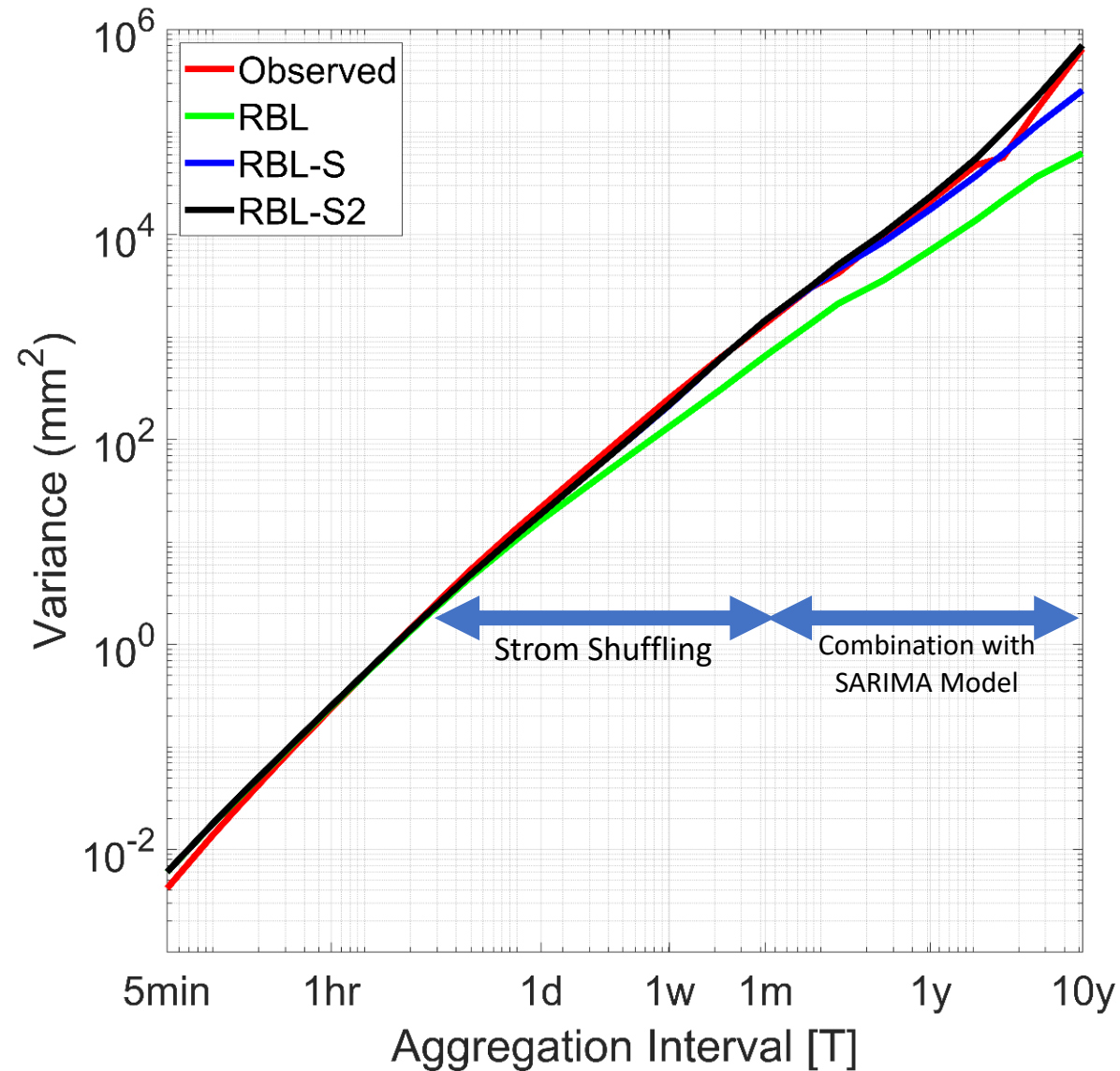
Poisson Cluster – Shufflex2 Model

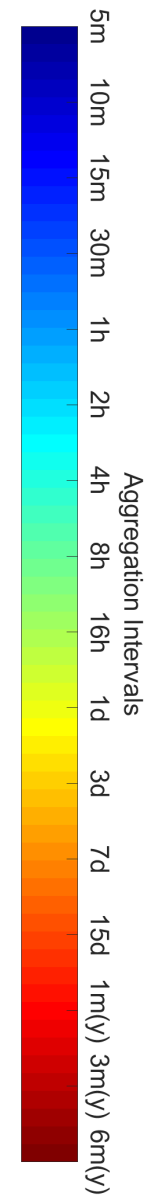
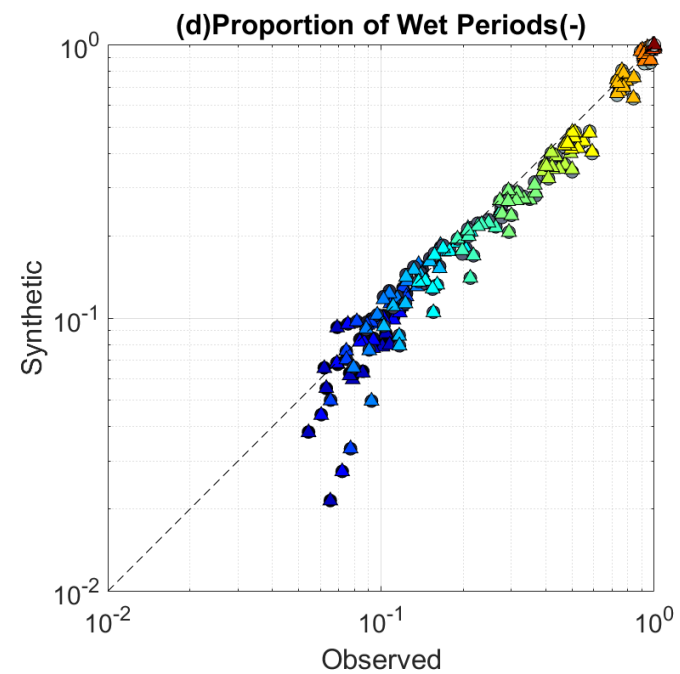
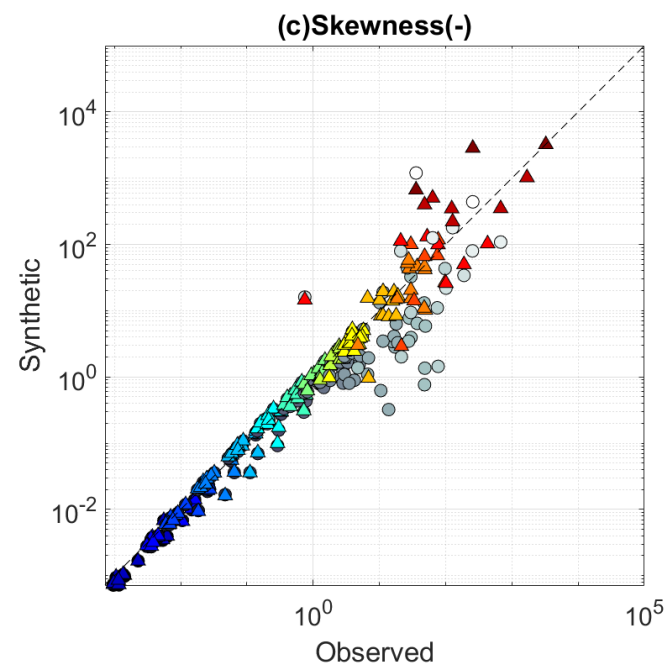
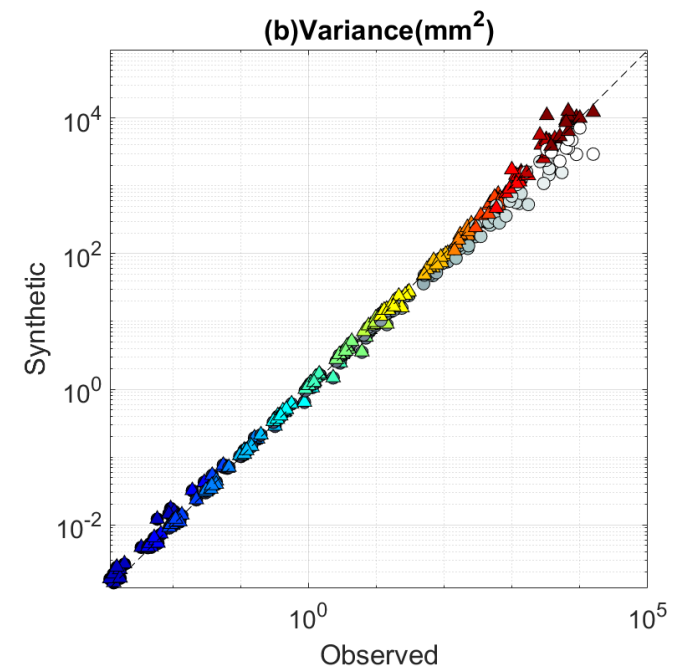
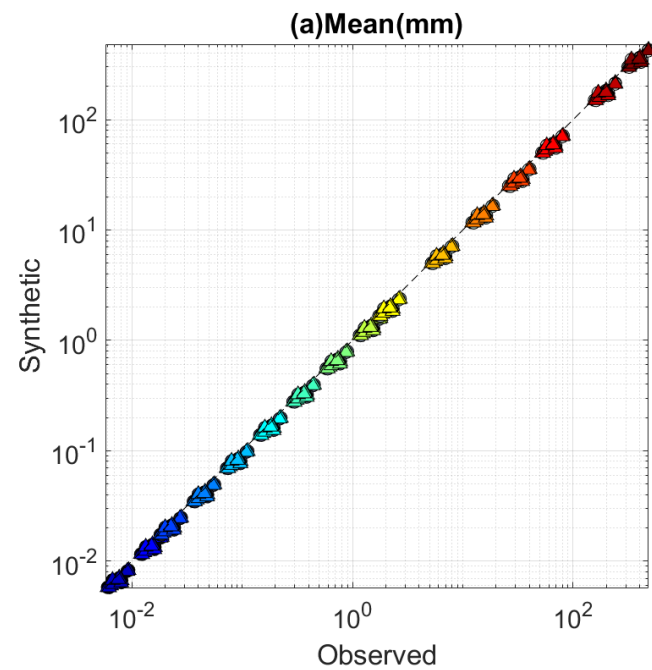


Poisson Cluster – Shufflex2 Model

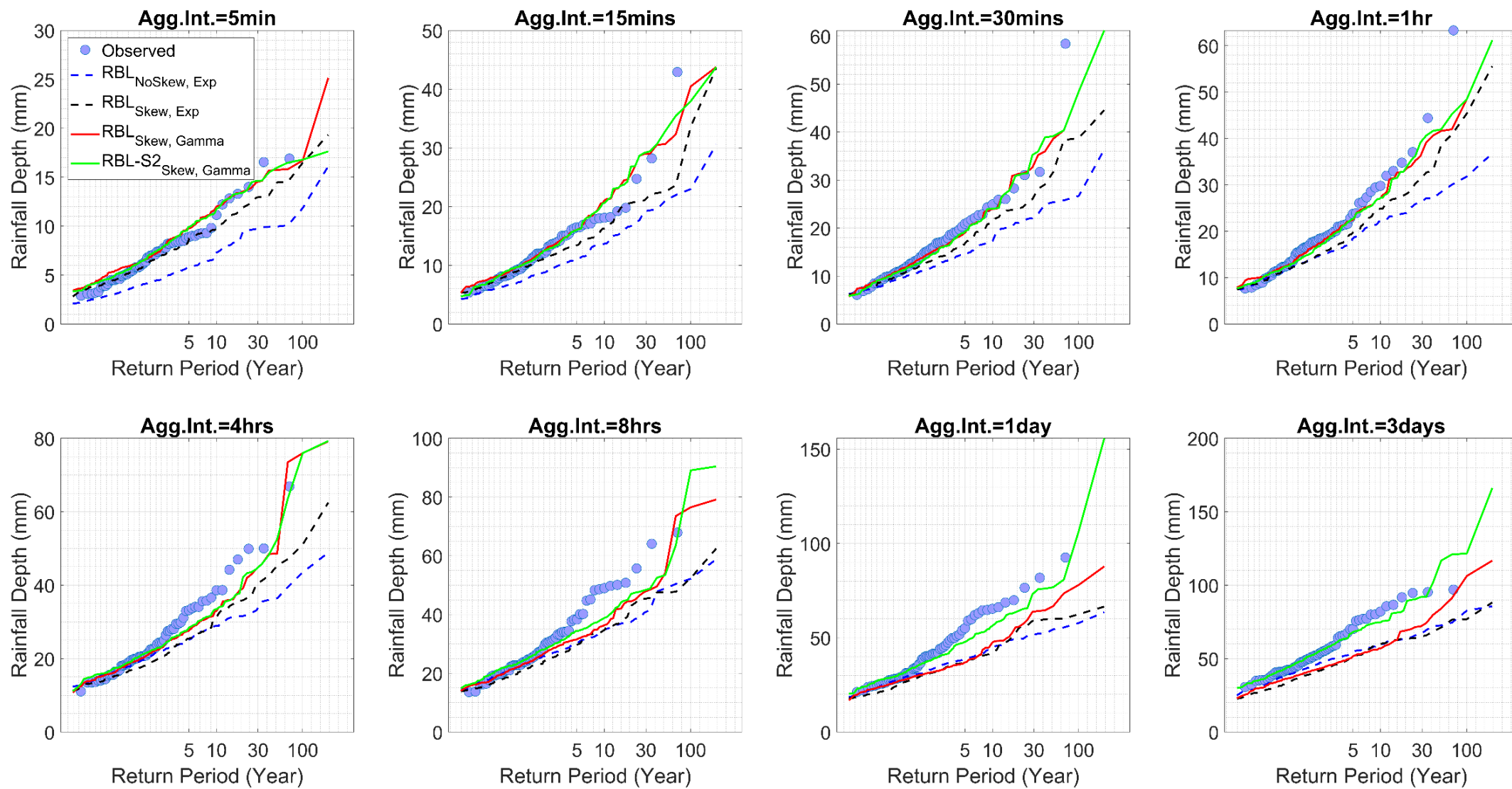


Poisson Cluster – Shufflex2 Model

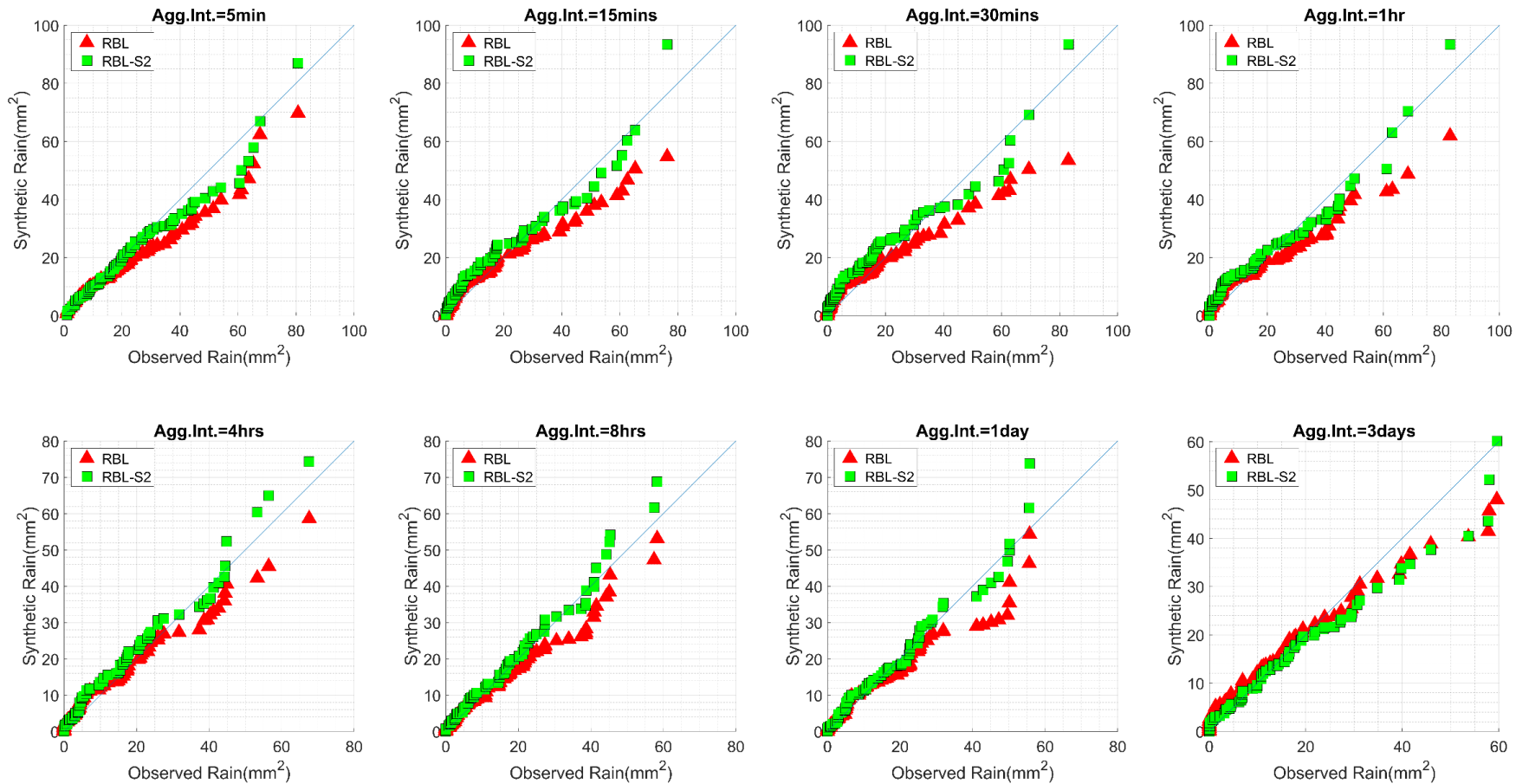




Extreme Value Reproduction

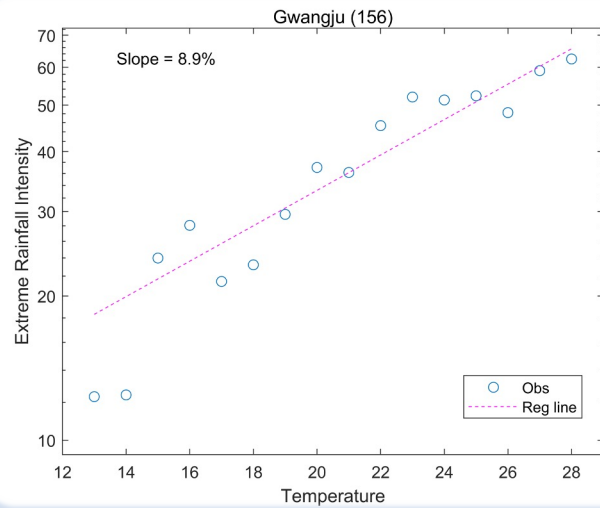


Past-7day Rainfall Reproduction (for continuous hydrologic modeling)



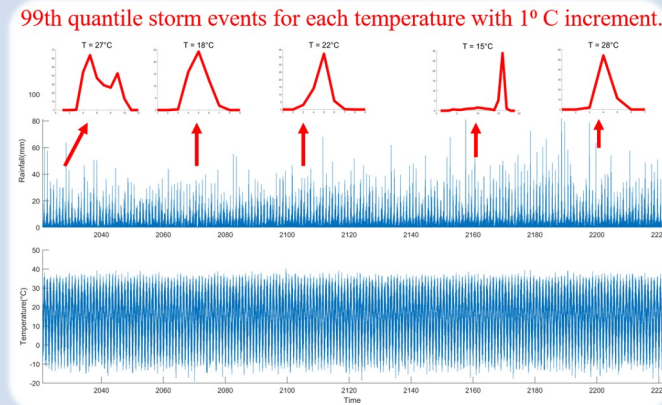
Model Extension for Climate Change

1



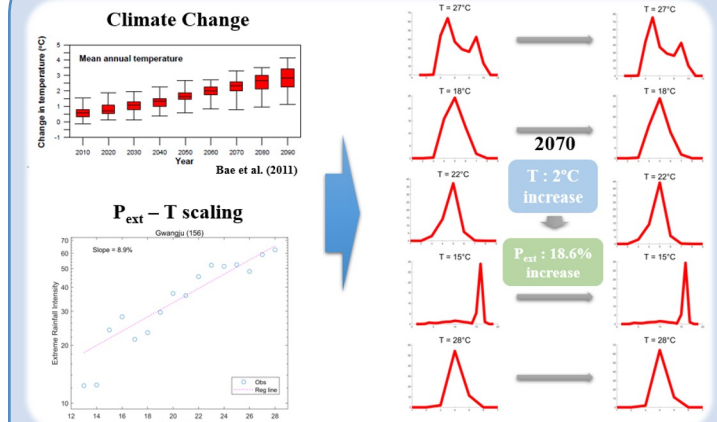
Obtain C-C relationships from observed rainfall

2



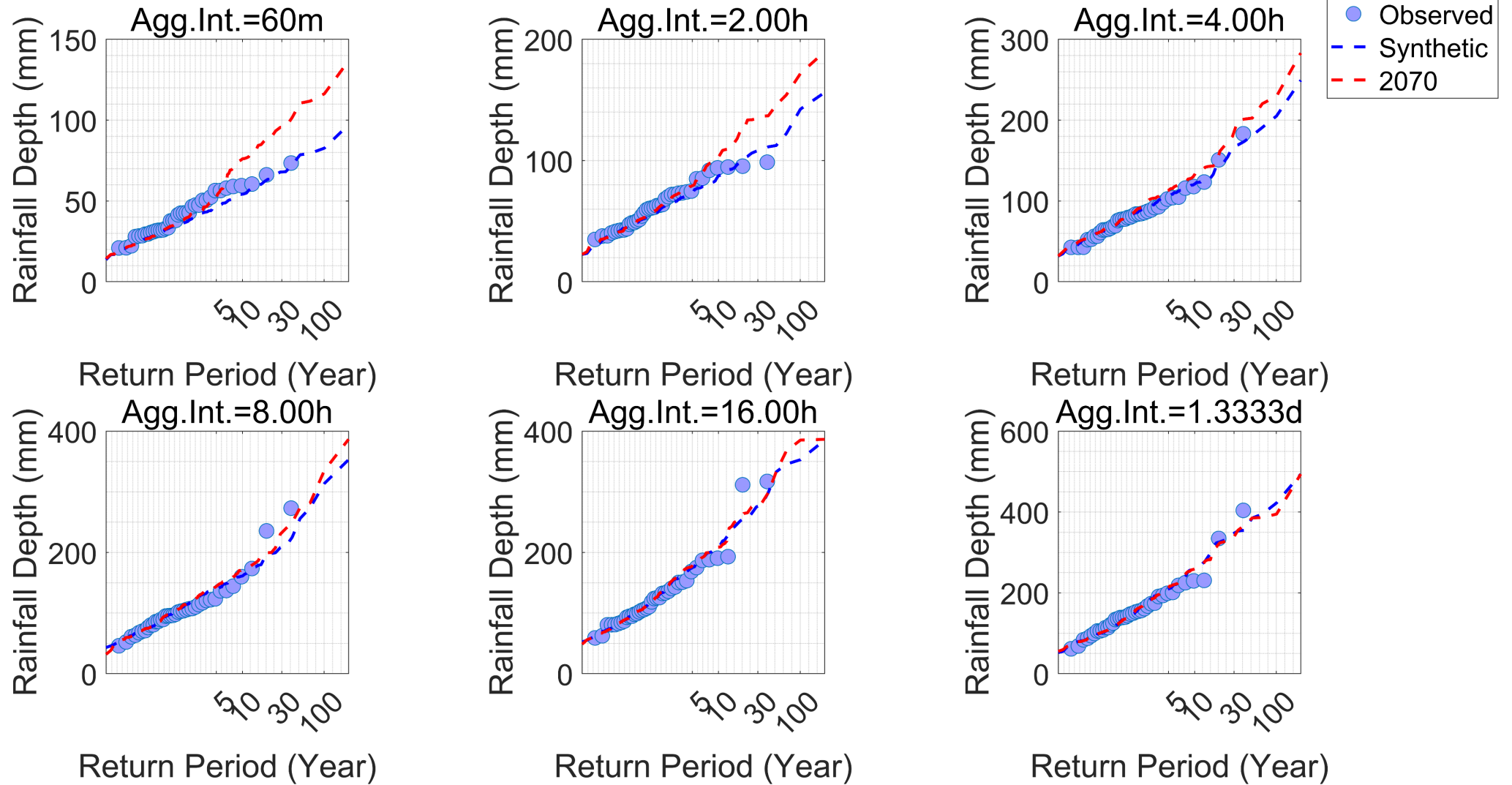
Extract Extreme Events from Synthetic Rainfall

3

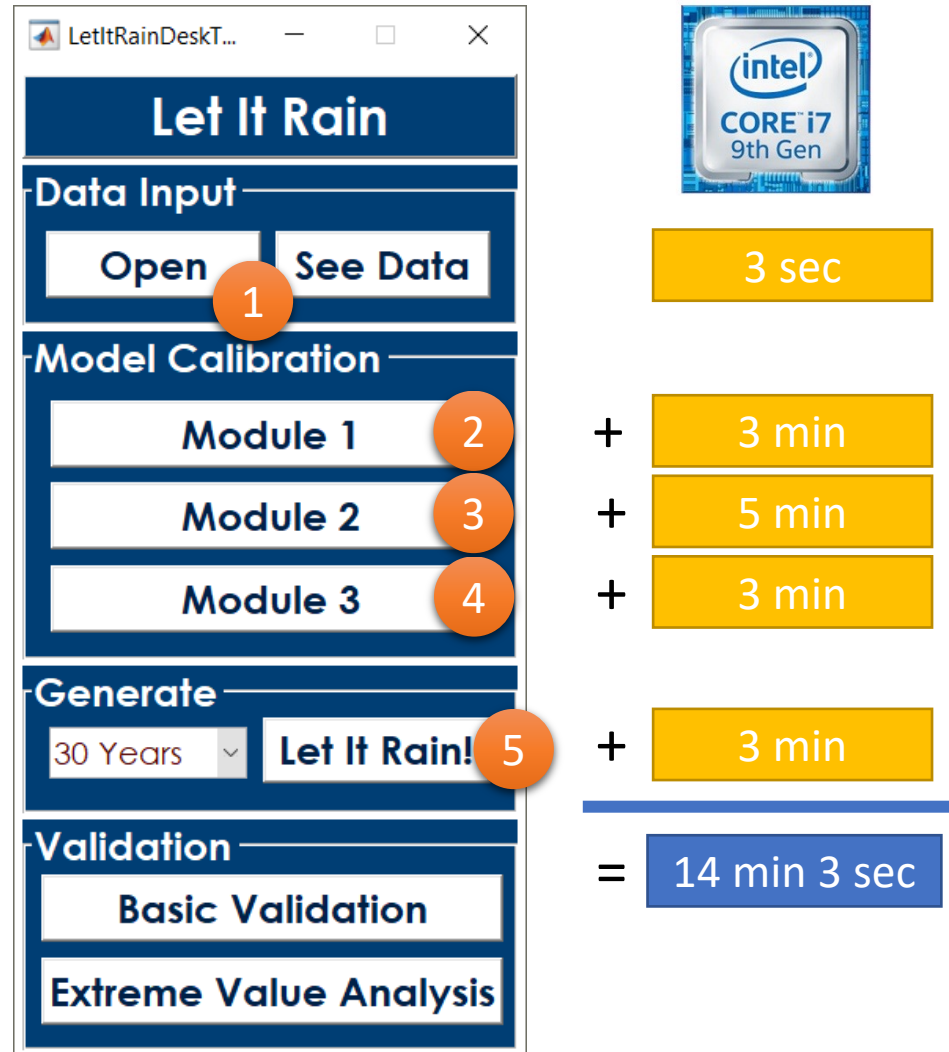


Scale extreme rain events

Extreme Value for Future Period



So what? I know it's good. How can I use it?
www.hihydrology.com



The image shows a screenshot of the 'Let It Rain' software interface on the left and a performance breakdown on the right. The software interface has a title bar 'LetItRainDeskT...' and a main title 'Let It Rain'. It is divided into five sections: 'Data Input' with 'Open' and 'See Data' buttons; 'Model Calibration' with 'Module 1', 'Module 2', and 'Module 3' buttons; 'Generate' with a '30 Years' dropdown and a 'Let It Rain!' button; and 'Validation' with 'Basic Validation' and 'Extreme Value Analysis' buttons. Orange circles with numbers 1 through 5 are placed over the 'Open', 'Module 1', 'Module 2', 'Module 3', and 'Let It Rain!' buttons respectively. To the right, an Intel Core i7 9th Gen processor icon is shown above a list of tasks and their durations: '3 sec', '+ 3 min', '+ 5 min', '+ 3 min', '+ 3 min', and a final result '= 14 min 3 sec'.

Task	Duration
Open	3 sec
Module 1	+ 3 min
Module 2	+ 5 min
Module 3	+ 3 min
Let It Rain!	+ 3 min
Total	= 14 min 3 sec

Conclusion

- Rainfall memory governs the rainfall variability throughout the timescales.
- Ignoring it in rainfall modeling will eventually entail underestimation of the assessed risks.
- A model was developed to resolve this issue.
- The shuffling algorithm can be applied to all types of rainfall models to preserve memory.

Thank you!



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Research papers

A stochastic rainfall model that can reproduce important rainfall properties across the timescales from several minutes to a decade

Dongkyun Kim ^a , Christian Onof ^b

