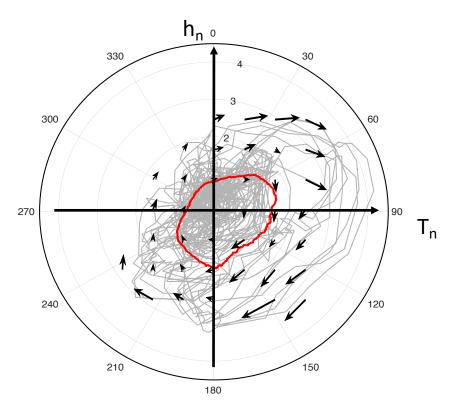
Asymmetries in the ENSO phase space



Dietmar Dommenget and Maryam Al-Ansari

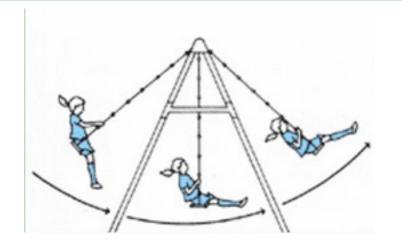
submitted to Climate Dynamics

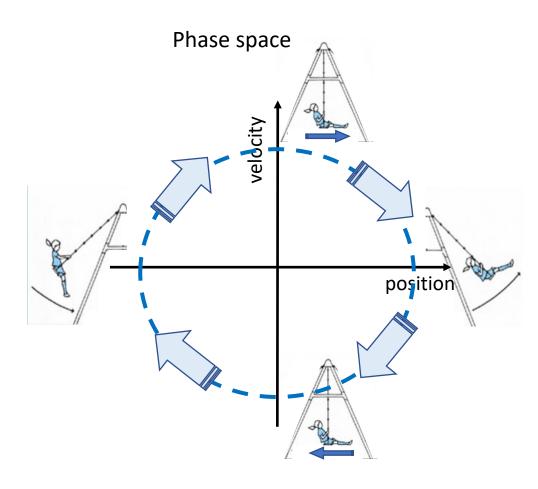




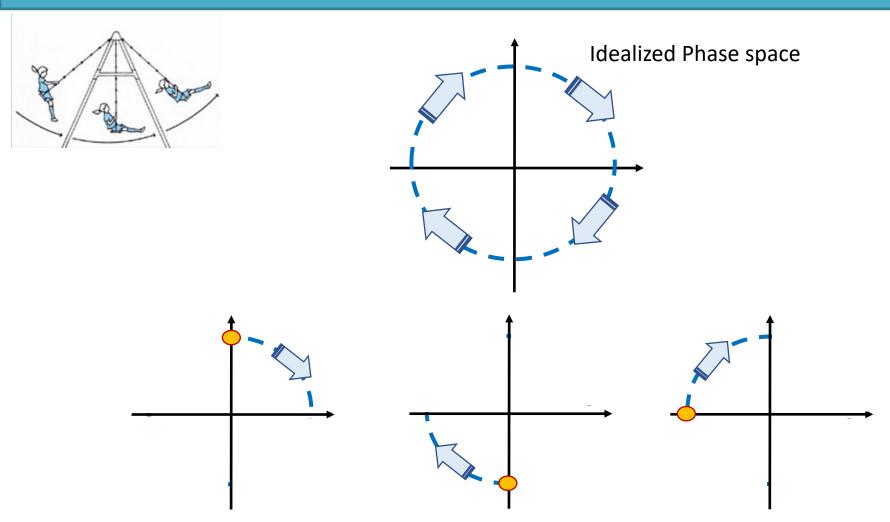


- Motivation
- The ENSO phase space
- Observed ENSO phase space
- Linear & Non-linear Recharge Oscillator
- Predictions

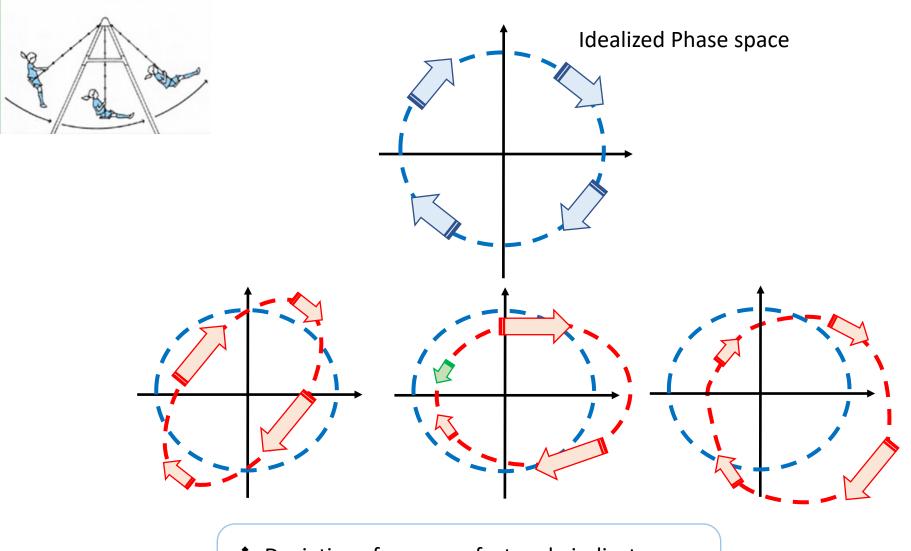




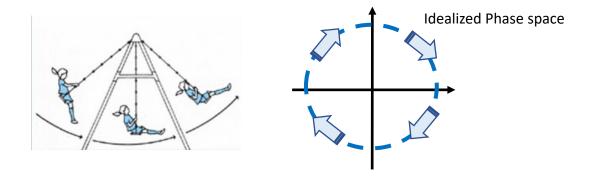
- ❖ The physical phase space illustrates an oscillation.
- It presents the system as a cycle.



❖ A cycle with clear tendencies implies predictability



Deviations from a perfect cycle indicate interesting dynamics

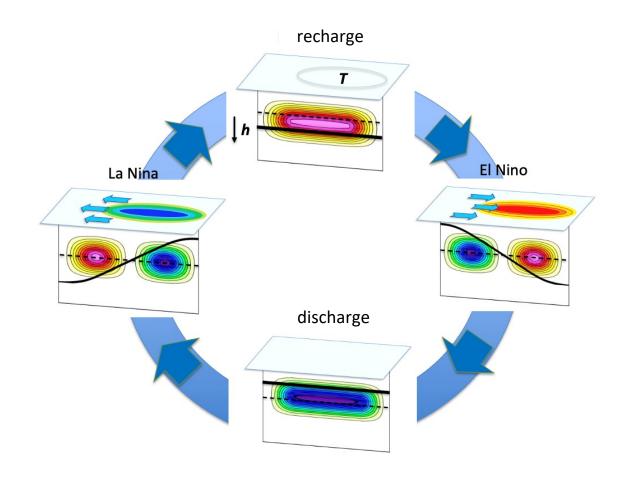


What is a Climate Mode?

- ❖ A Physical climate mode has a phase space with two variables x and y with an out-of-phase relationship
- The mode has clear propagation through all phase of the cycle in clockwise direction
- This is the essence of a predictable oscillator

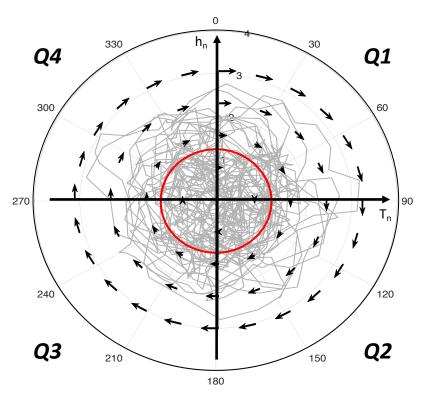
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The ENSO phase space



- ❖ The ENSO phase space is based on the *Recharge Oscillator* model of ENSO
- ❖ A cycle between upper ocean heat content (thermocline depth; h) and SST (T)

The idealized Recharge Oscillator model



radius = strength (S) angle = phase

= 100yrs sample of T and h

= mean **S** as function of phase

→ = mean tendencies

$$\frac{dT(t)}{dt} = \underbrace{a_{11}}T(t) + \underbrace{a_{12}}h(t) + \underbrace{Rt}$$

$$\frac{dh(t)}{dt} = a_{21}T(t) + a_{22}h(t) + Rh$$

 a_{11} , a_{22} = damping/growth rate

 a_{12} , a_{21} = delayed negative feedback (coupling)

Rt, Rh = noise forcing

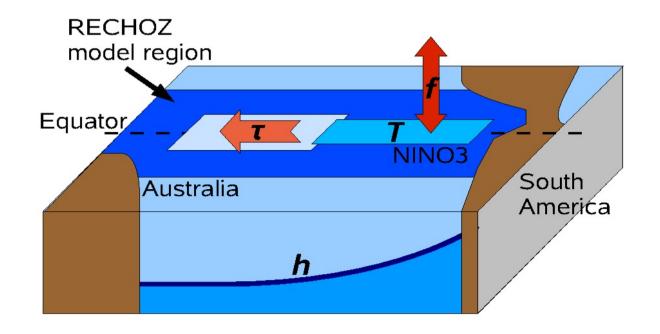
Idealized: $a_{11} = a_{22} \ a_{12} = -a_{21} \ Rt = Rh$

integrate stochastic model for 10⁴yrs of **T** and **h** statistics

❖ The idealized *Recharge Oscillator* model is symmetric / all phase are the same

- Motivation
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The observed ENSO phase space



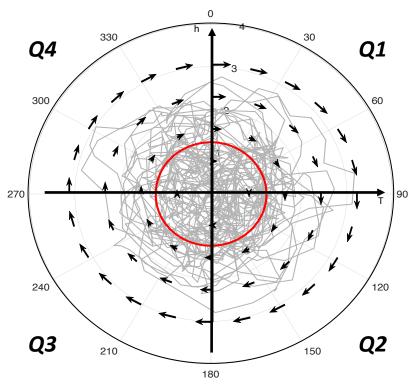
T = NINO3 SST anomalies

h = Z20 isotherm of whole eq. Pacific

Data: combined TAO-observations, ocean reanalysis (SODA, CHOR-RL/AS) 1980-2015

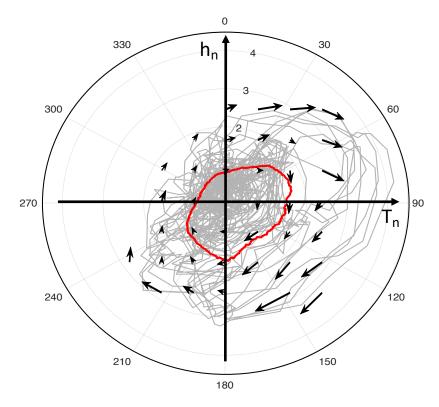
The observed ENSO phase space

idealized *Recharge Oscillator*



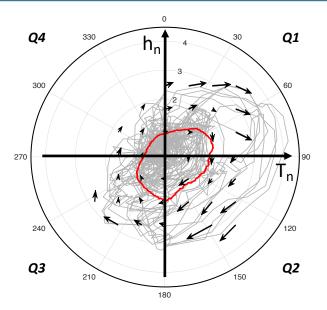
radius = strength (S)
angle = phase
= mean S as function of phase
= mean tendencies

Observed **T** and **h**

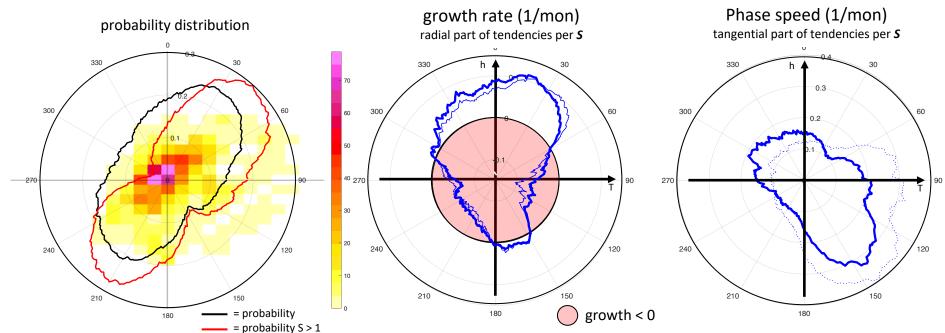


- The observed ENSO phase space has strong asymmetries.
- Both in *probabilities* and in *tendencies*

The observed ENSO phase space



- probabilities are shifted away from Q4.
- growth rate is largest in the recharge state and negative during El Nino / La Nina
- Phase transition is fastest after El Nino and close to zero during La Nina states.



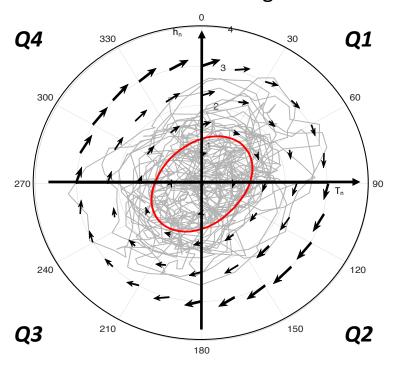
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Recharge Oscillator model

Use linear and non-linear Recharge Oscillator model to understand observed ENSO phase space asymmetries

Observed linear Recharge Oscillator model

Observed linear Recharge Oscillator



radius = strength (S)
angle = phase
= 100yrs sample of T and h
= mean S as function of phase
= mean tendencies

$$\frac{dT(t)}{dt} = \underbrace{a_{11}}T(t) + \underbrace{a_{12}}h(t) + \underbrace{Rt}$$

$$\frac{dh(t)}{dt} = \underbrace{a_{21}}T(t) + \underbrace{a_{22}}h(t) + \underbrace{Rh}$$

a₁₁, a₂₂ = damping/growth rate
 a₁₂, a₂₁ = delayed negative feedback (coupling)
 Rt, Rh = noise forcing

fit to observed **T** and **h**

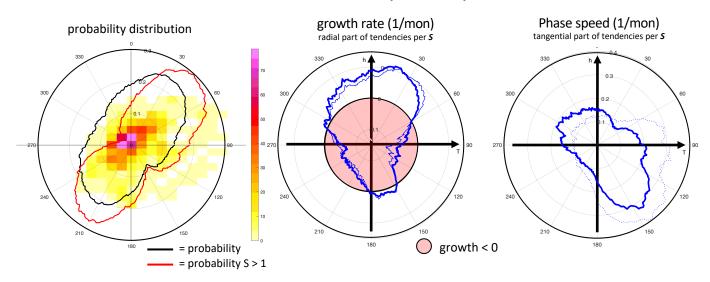
Normalized observed ReOsc model parameters				
a _{11n} = -0.115 mon ⁻¹	a _{12n} = 0.17 mon ⁻¹	$stdv(\zeta_T) = 0.29 \text{ mon}^{-1}$		
a _{22n} = +0.019 mon ⁻¹	a _{21n} = -0.16 mon ⁻¹	$stdv(\zeta_h) = 0.25 \text{ mon}^{-1}$		

integrate model with white noise forcing for 10⁴ yrs.

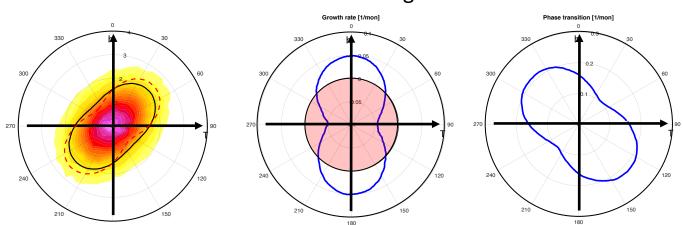
- ❖ It is asymmetric in the growth rate *T* and *h*
- ❖ It is symmetric in all other parts
- The ENSO phase space is phase-depending

Observed linear Recharge Oscillator model

observed ENSO phase space



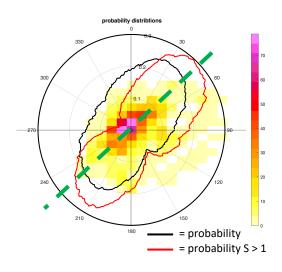
Observed linear Recharge Oscillator



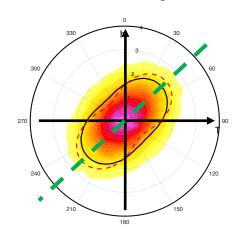
- The linear model can capture some of the phase space characteristics
- It is symmetric for opposite phases
- In-phase correlation between T and h explains most of the observed structures
- Some asymmetries are not captured.

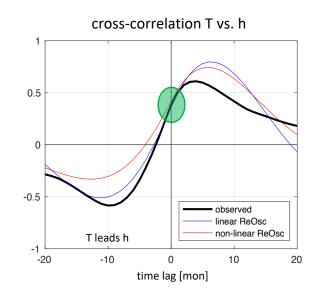
Observed Thermocline Depth Estimates

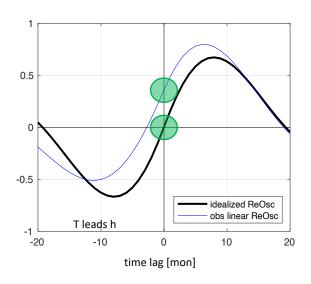
observed ENSO phase space



Observed linear Recharge Oscillator



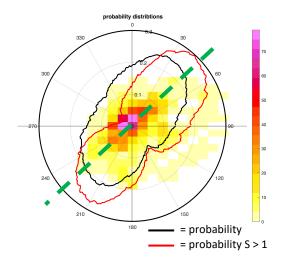




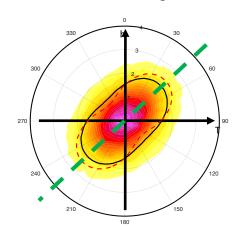
- In-phase correlation between T and h explains most of the observed structures
- In ReOsc model growth rates of T/h are strongly asymmetric
- This is not the idea of the ReOsc model
- There is likely a problem with the thermocline estimate (Z20-based)

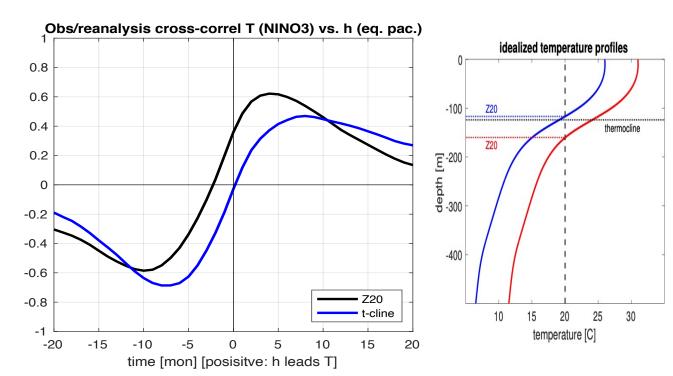
Observed Thermocline Depth Estimates

observed ENSO phase space



Observed linear Recharge Oscillator





The thermocline depth behaves better in the ReOsc concept than Z20.

A Non-linear Recharge Oscillator model

linear model

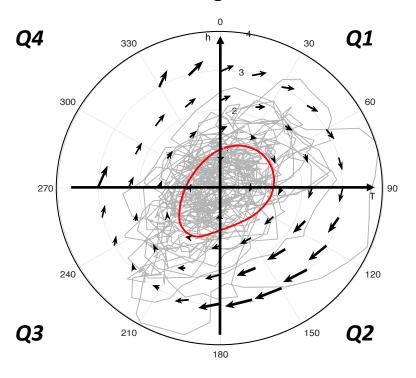
$$\frac{dT(t)}{dt} = \underbrace{a_{11}}_{T}T(t) + \underbrace{a_{12}}_{h}h(t) + Rt$$

$$\frac{dh(t)}{dt} = \underbrace{a_{11}}_{T}T(t) + \underbrace{a_{12}}_{h}h(t) + Rt$$

a₁₁, a₂₂ = damping/growth rate
 a₁₂, a₂₁ = delayed negative feedback (coupling)
 Rt, Rh = noise forcing

A Non-linear Recharge Oscillator model

Non-linear Recharge Oscillator



radius = strength (S)
angle = phase
= 100yrs sample of T and h
= mean S as function of phase
= mean tendencies

non-linear model

$$\frac{dT(t)}{dt} = a_{11-}T^{2}(t) + a_{11-}T(t) + a_{11-}h(t) + Rt$$

$$\frac{dh(t)}{dt} = a_{21}T(t) + a_{22}h(t) + Rh$$

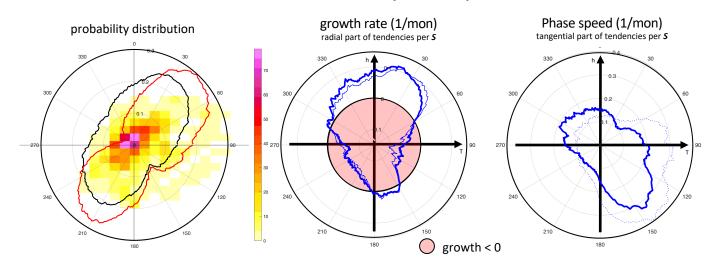
$$a_{11-0}$$
, a_{11-1} , a_{11-2} , a_{22} = damping/growth rate a_{12} , a_{21} = delayed negative feedback (coupling) Rt, Rh = noise forcing
$$a_{11-0} = -0.035 \text{ K mon}^{-1}$$
 a_{11-1} = -0.188 mon⁻¹.
 a_{11-2} = 0.058 K⁻¹mon⁻¹

integrate model with white noise forcing for 10⁴ yrs.

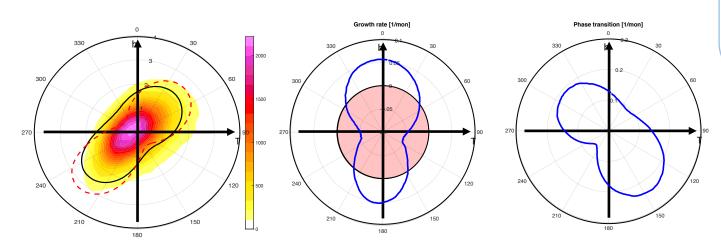
- assume quadratic function for growth of T
- Consistent with non-linear wind-SST (stronger feedback for negative T)

A Non-linear Recharge Oscillator model

observed ENSO phase space



Non-linear Recharge Oscillator



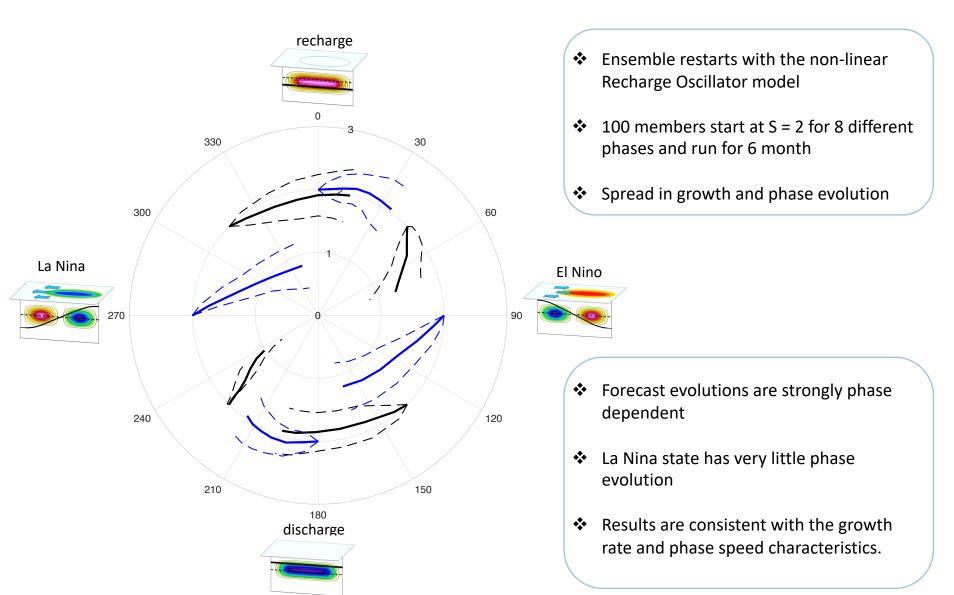
- The non-linear model can capture some of the non-linear characteristics
- Some asymmetries are not captured.

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Predictions

Predictability

Non-linear Recharge Oscillator



- Motivation
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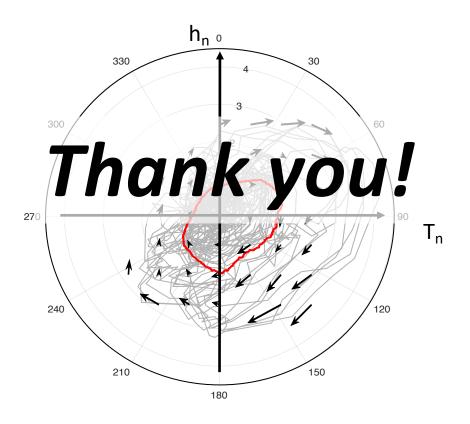
Summary

- The ENSO phase space is a good concept for understanding ENSO dynamics as a cycle
- It allows to define growth rate and phase speed as function of ENSO phase
- The observed ENSO phase space has strong asymmetries in probabilities, growth rates and phase speed
- \clubsuit Most of it is due to in-phase correlation between T and h -> artifact of estimating h?
- Non-linear growth rate of *T* can explain much of the non-linearity, but not all of it

Outlook

- The physical phase space is a good concept for any climate mode (.e.g, MJO)
- Analysis of *growth rate* and *phase speed* as function of phase helps to understand the dynamics of a climate mode
- A positive phase speed in all phases indicate a true oscillator

Asymmetries in the ENSO phase space



Dietmar Dommenget and Maryam Al-Ansari

soon to be published in Climate dynamics, keep fingers crossed!







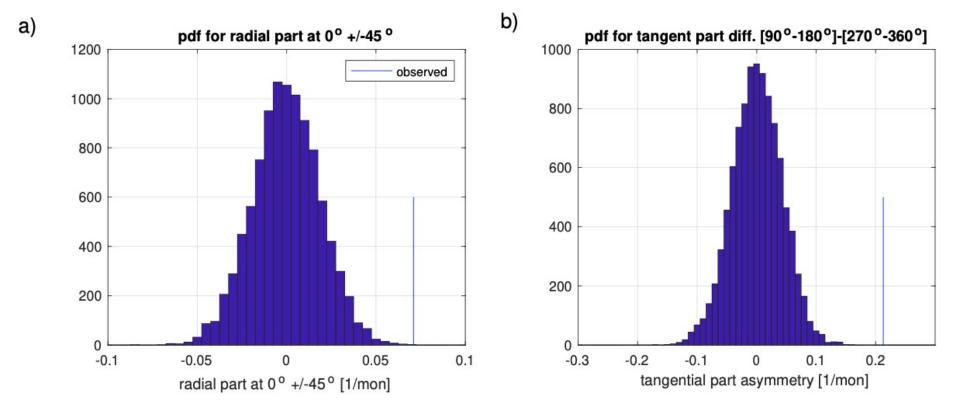


Figure 7: (a) Probability distribution for the radial tendency part at 0° +/-45° for the idealized ReOsc model and the observed value (blue vertical line). (b) Probability distribution for the difference of the tangential tendency part between [90°- 180°] minus [270°- 360°] for the idealized ReOsc model and the observed value (blue vertical line).

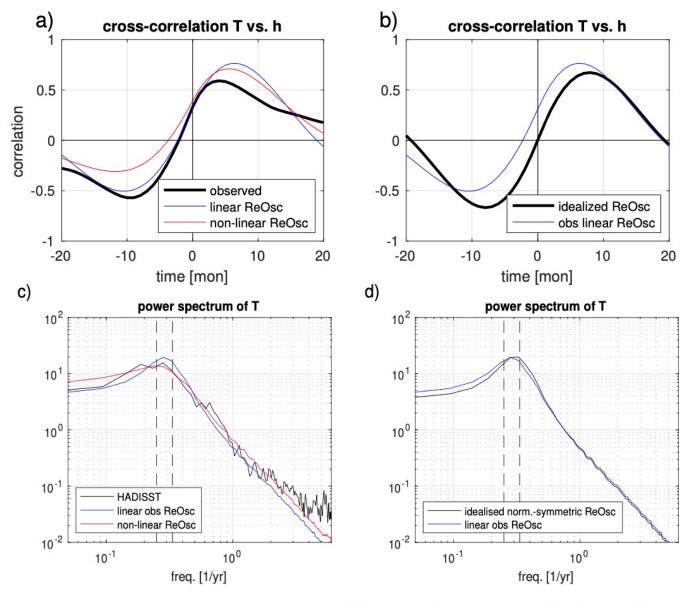
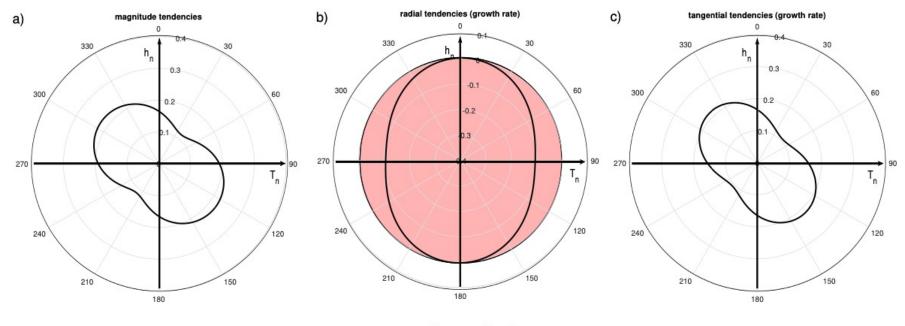


Figure 4: upper: cross-correlation between T and h for the observations and ReOsc models fitted to observations (a) and for an idealized ReOsc model (b). Negative lag time indicate T is leading the time evolution of h. Lower: power spectrum of T for observations (c) and for an idealized ReOsc model (d). The vertical dashed lines mark the periods of 3yrs and 4yrs.

observed linear ReOsc



non-linear ReOsc

