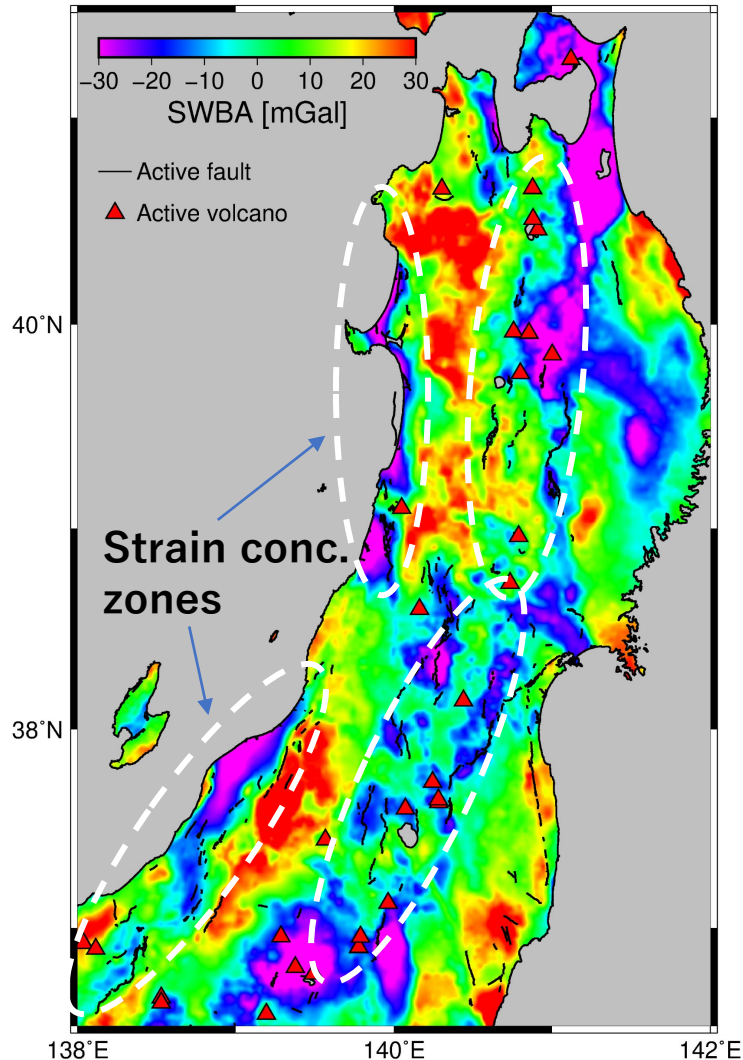


# Short-wavelength Bouguer anomaly and folding with disclination in the northeastern Japan

**Mitsuhiro HIRANO** & Hiroyuki NAGAHAMA

Department of Earth Sciences, Tohoku University, Sendai, Japan

# Short-wavelength Bouguer anomaly (SWBA) in the northeastern Japan



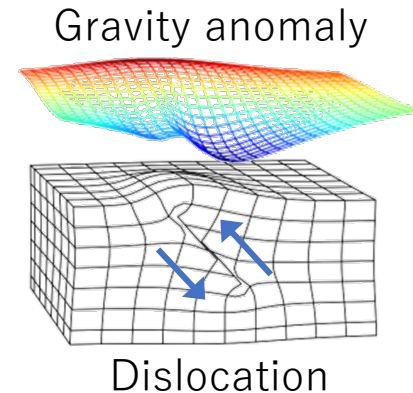
Hirano et al. (2022)

■ **Trend of active faults:** negative regions

■ **Its cause & Estimated anomaly:**

Cracks & volumetric strain  
due to fault dislocation

About -10 mGal for 3 million  
years



■ **Patterns**

Strain concentration zones with active faults  
and multi folding

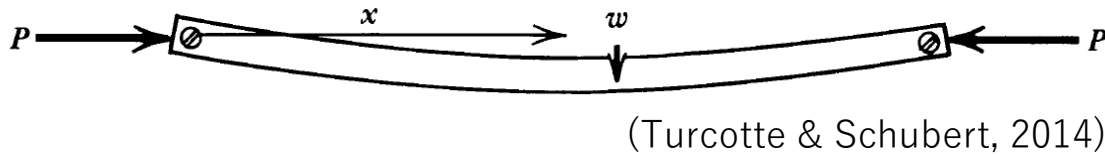
► Negative zones along the arc

■ **Objective:**

Discuss the SWBA from the geometrical  
viewpoint of folding with disclination

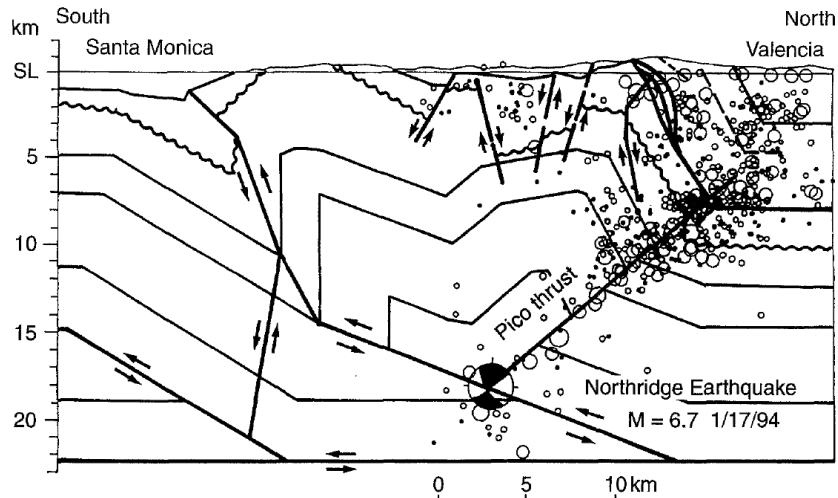
# Folding and Euler-Schouten curvature

■ **Euler-Schouten curvature** (Schouten, 1954):  $H_{ij}^\alpha \approx \frac{\partial w^\alpha}{\partial x^i \partial x^j}$  ( $w$ : deflection)



In the case,  $H \approx \frac{\partial^2 w}{\partial x^2}$

## ■ Folding and fault dislocation



(Davis & Namson, 1994; Nagahama, 1996)

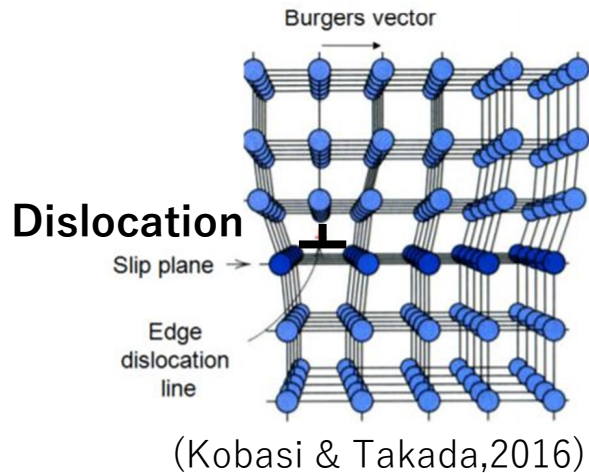
The density of earthquake occurrence  $N$  is proportional to the curvature of folding, (Nagumo, 1969)

$$N \propto \left| \frac{\partial^2 w}{\partial x^2} \right|$$

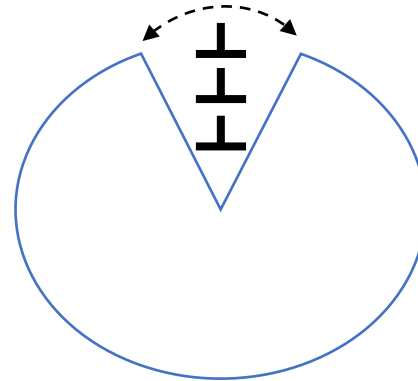
Fault dislocation accumulates at the regions with its high curvature (Nagahama, 1996).

# Disclination and Curvature in material space

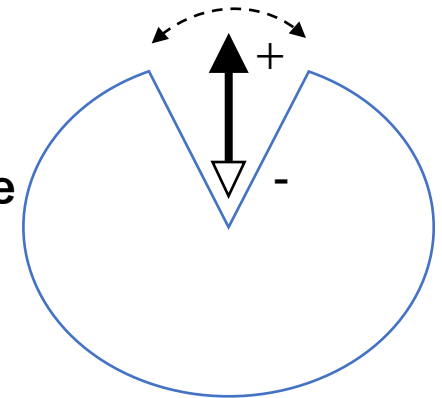
## ■ The Equivalence between dislocation and disclination (Kleinert, 2011)



The row of dislocation



Disclination dipole



Equivalence



## ■ Disclination and curvature in material space (Kondo, 1955)

### • Disclination density

$$\theta^{\alpha\beta} = \epsilon^{\alpha\nu\mu} \epsilon^{\beta\lambda\kappa} R_{\nu\mu\lambda\kappa} / 4 \quad (\epsilon^{\alpha\nu\mu} : \text{Levi-Civita symbol})$$

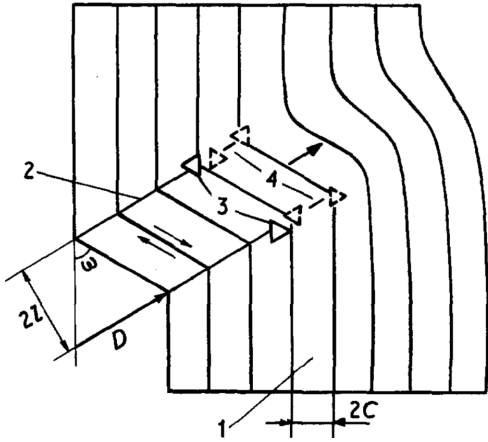
### • Riemann-Christoffel curvature (Gauss-Codazzi relation):

$$R_{\nu\mu\lambda\kappa} = \frac{1}{2} \Sigma_{\alpha} (H_{\mu\kappa}^{\alpha} H_{\nu\lambda}^{\alpha} - H_{\nu\kappa}^{\alpha} H_{\mu\lambda}^{\alpha})$$

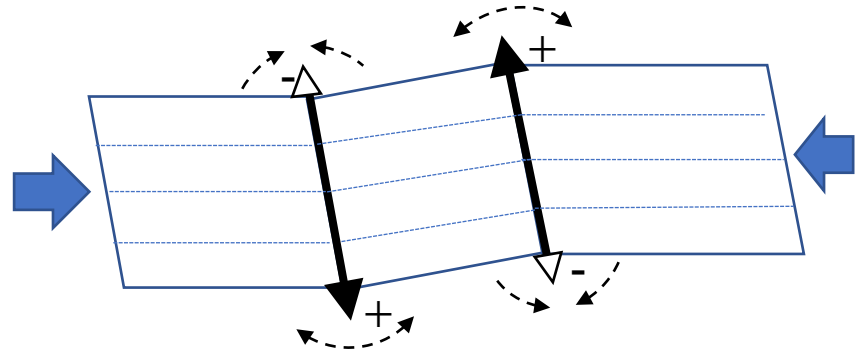
Euler-Schouten curvature

# Kink folding and Disclination

## ■ Kink band and Kink folding (Pertsev et al., 1981; Osaki et al., 2011)

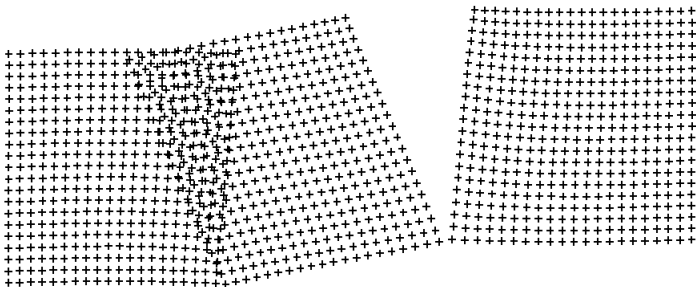


The Structures in non-homogeneous material with disclination dipoles



Angular folding with disclination dipoles

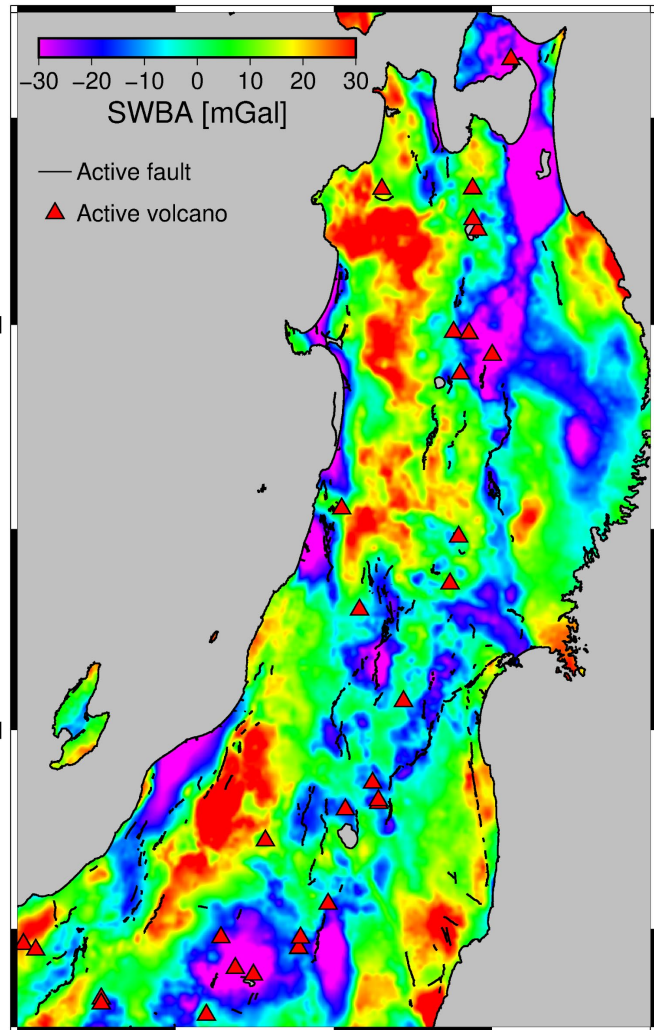
## ■ Displacement field with two disclination dipoles (Osaki et al., 2011)



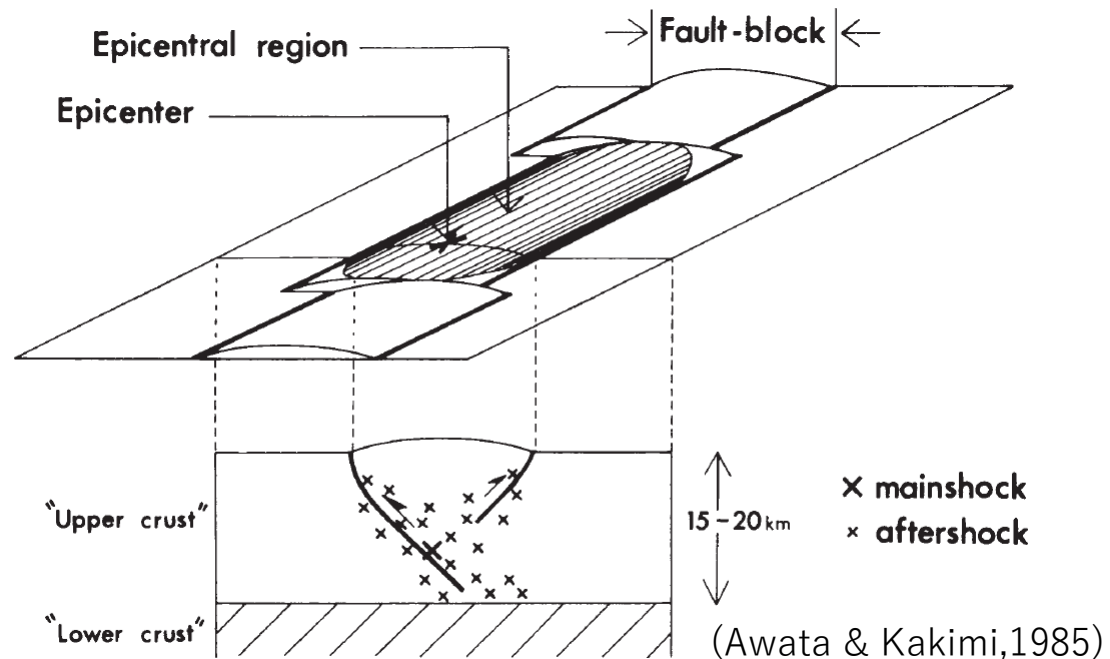
Mass-loss or mass-excess zones around disclination

(Osaki et al., 2011)

# Fault blocks can cause the positive and negative regions



138°E 140°E 142°E



Fault blocks can cause the mass-loss or mass-excess regions as well as Kink folding.

## ■ Conclusion

The positive and negative zones along the arc reflect the geometric condition of the crust with disclination.