





An optimized online version of NESTORE software package for the forecasting of strong aftershocks: an application to Italian clusters

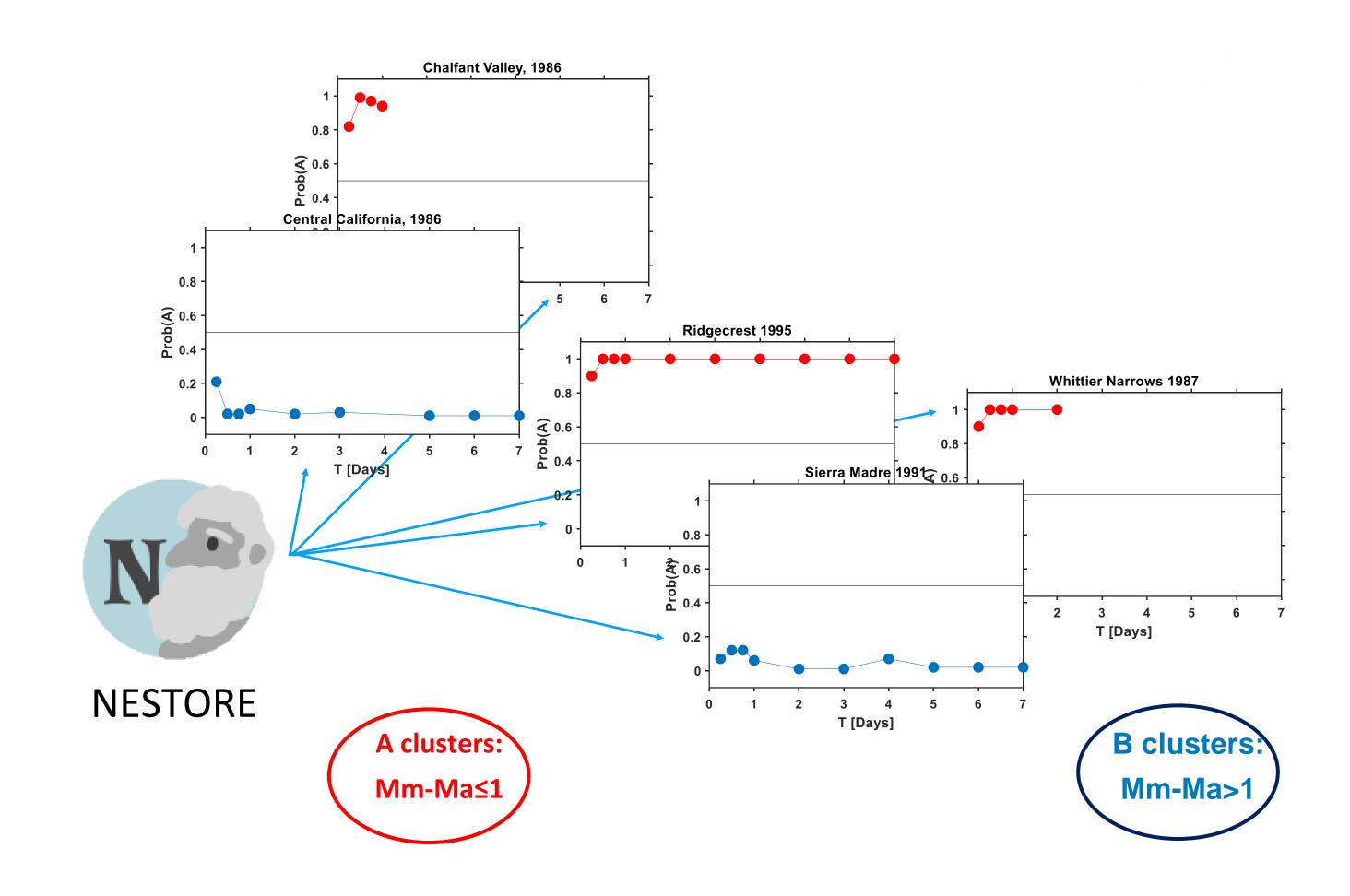
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NESTORE



- NESTORE (NExt STrOng Related Earthquake) is an algorithm based on machine learning approach
- It divides the clusters into two classes based on the difference in magnitude Dm between the o-mainshock (the first large shock e.g. M>4) and the strongest following earthquake (Type A: Dm≤1 Type B: Dm>1)
- NESTORE goal is type A clusters probabilistic forecasting based on features extracted from seismic catalogues in the first hours/days after the o-mainshock









NESTOREV1.0 Features



NUMBER AND SPATIAL DISTRIBUTION OF EVENTS

$$N_2(i) = \sum_i n_i \quad \text{if } m_i > M_m - 2$$

$$Z(i) = \frac{mean(10^{0.69m_i - 3.22})}{mean(r_{ij})}$$

SOURCE AREA TREND

$$S(i) = \sum_{i} 10^{(m_i - M_m)}$$

$$SLCum(i) = \sum_{i} abs[S(t_i) - S(t_{i-1}) \frac{i \cdot dt}{(i-1) \cdot dt}$$

$$SLCum2(i) = \sum_{i} abs[S([s_1 + (i-1) \cdot dt, s_1 + i \cdot dt]) - S([s_1 + (i-1) \cdot dt, s_1 + (i-1) \cdot dt, s_1 + (i-1) \cdot dt + d\tau]) \frac{dt}{d\tau}]$$

ENERGY AND MAGNITUDE TREND

$$Q(i) = \frac{\sum_{i} E_{i}}{E_{m}}$$

$$QLCum(i) = \sum_{i} abs[Q(t_i) - Q(t_{i-1}) \frac{i \cdot dt}{(i-1) \cdot dt}$$

$$V_m(i) = \sum_i |m_i - m_{i-1}|$$

$$QLCum2(i) = \sum_{i} abs[Q([s_1 + (i-1) \cdot dt, s_1 + i \cdot dt]) - Q([s_1 + (i-1) \cdot dt, s_1 + (i-1) \cdot dt + d\tau]) \frac{dt}{d\tau}]$$

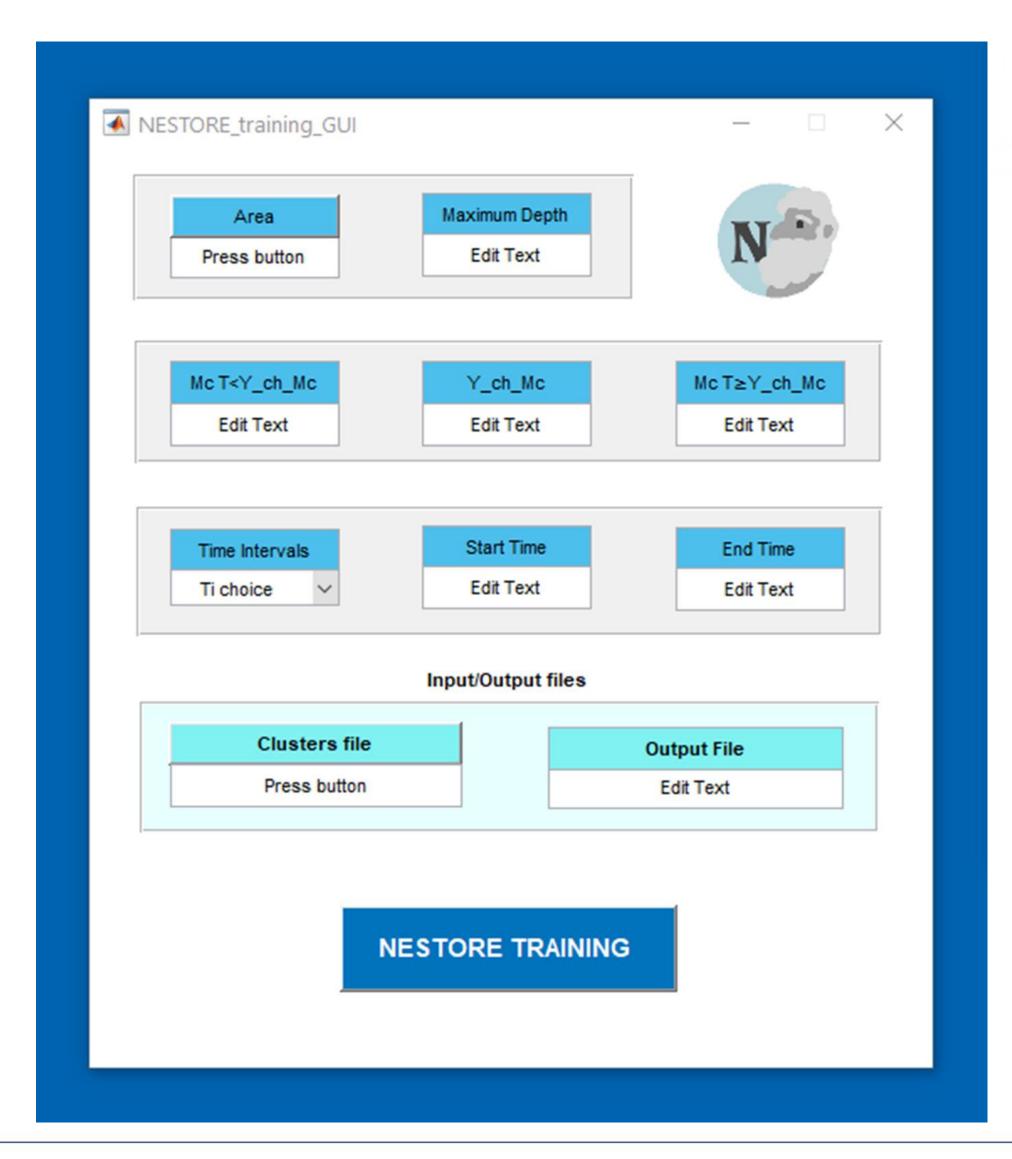






NESTOREV1.0 modules

- > NESTOREv1.0 software package consists of four main parts:
 - cluster identification module
 - training module
 - testing module
 - NRT classification (1 cluster)
- > All modules can be launched separately by command line, a dedicated user interface (GUI) is being developed too





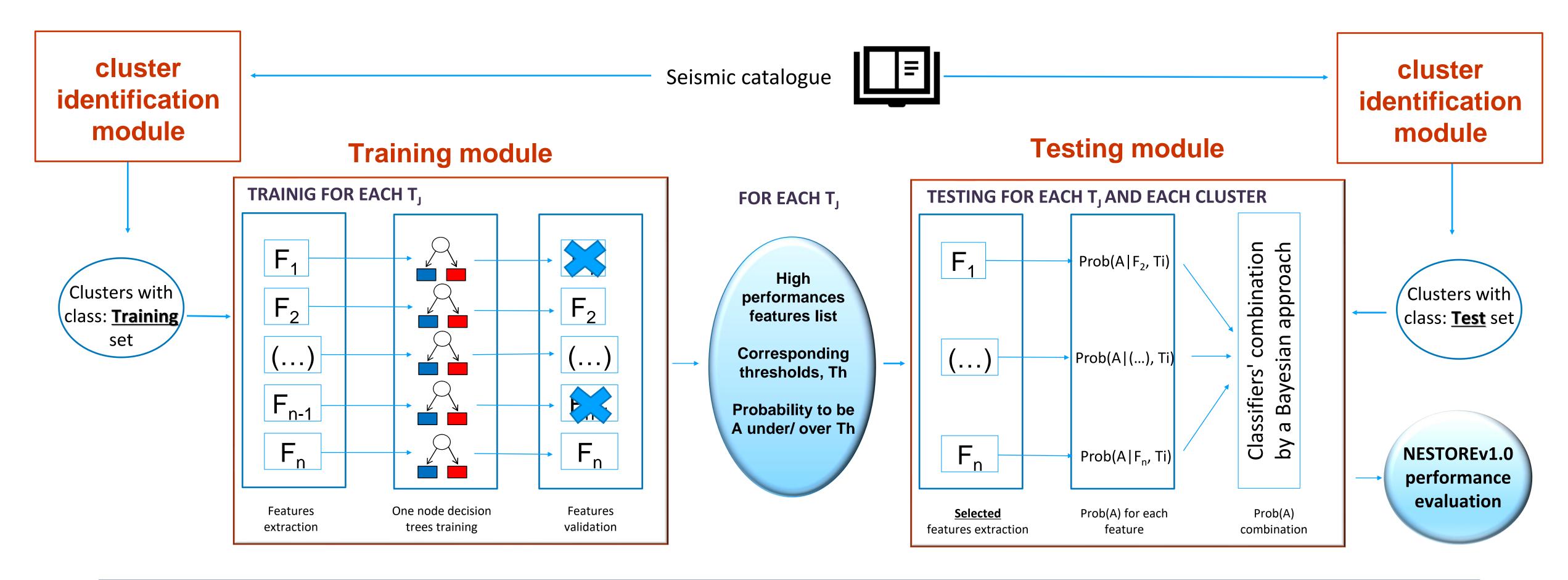




NESTOREV1.0 – TRAINING and TESTING



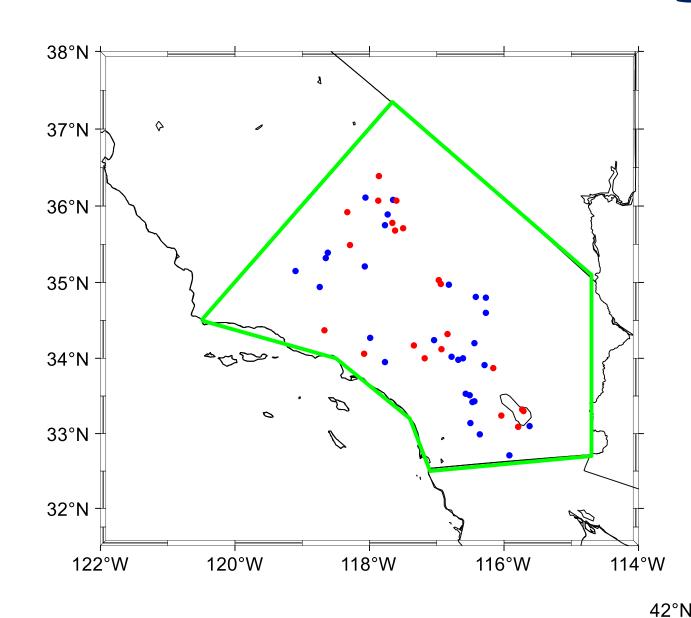
- NESTOREv1.0 analyses the seismic data at increasing time intervals T=[0.25,0.5,0.75,1,2,...,7] days (T_i) after the mainshock.
- After the training NESTORE can supply the probability to have an A cluster at time intervals T_i for new clusters





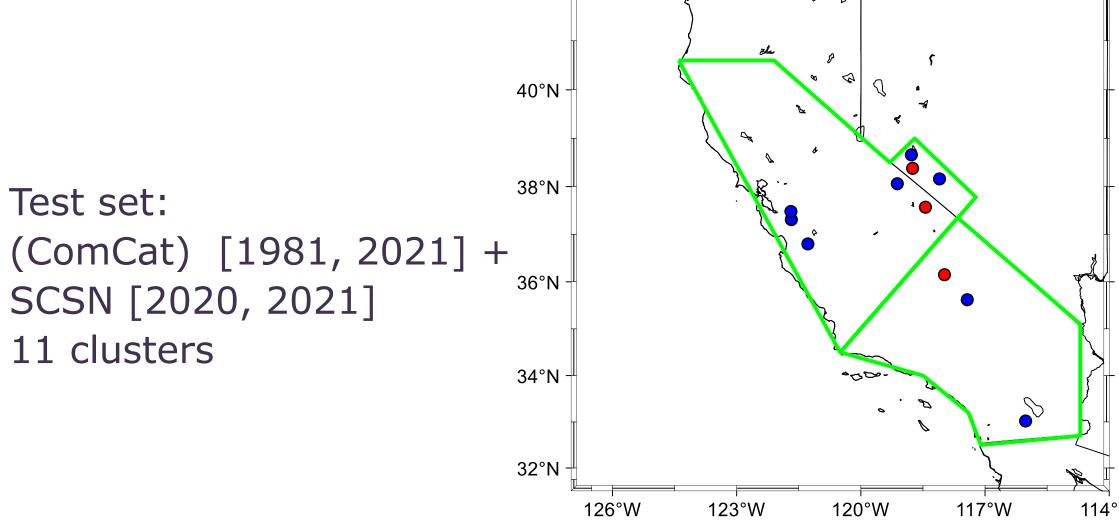


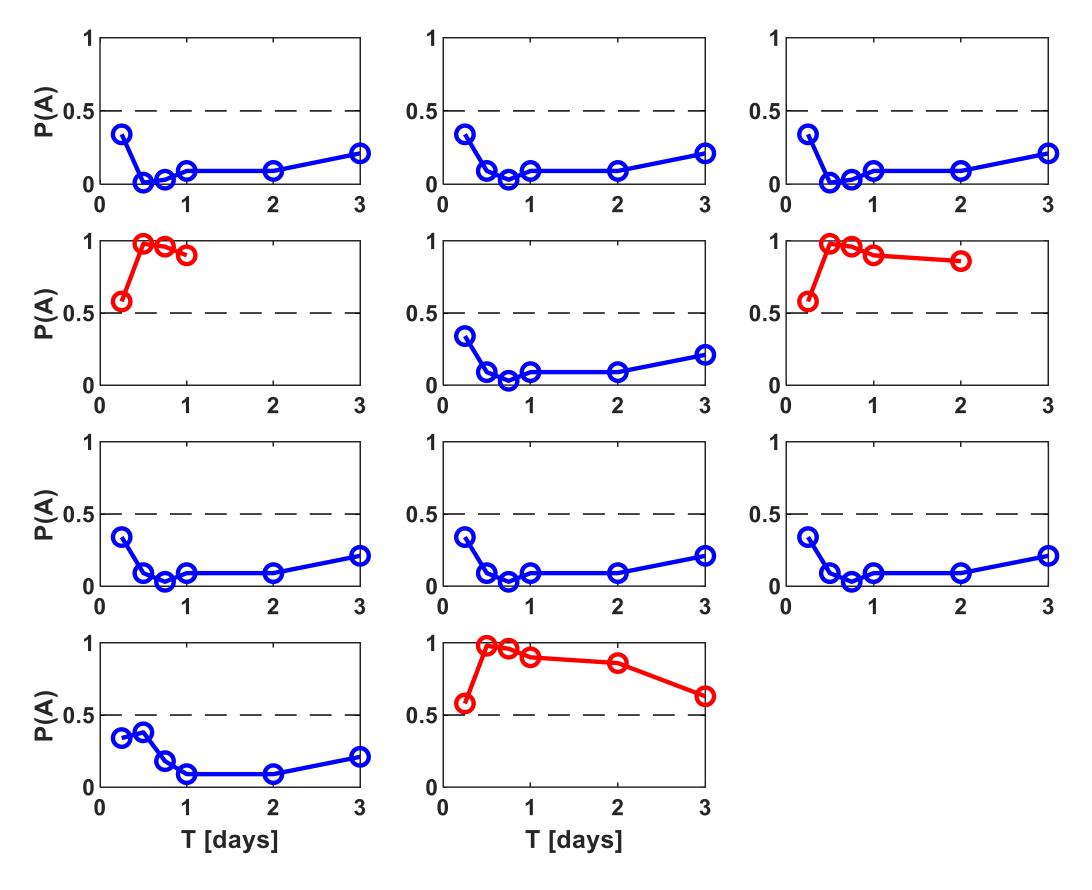
Training and testing NESTORE v1.0 in California



Dots: clusters mainshock location (50 clusters); red: type A clusters; blue: type B clusters.

Training set: SCSN [1981, 2020) 50 clusters



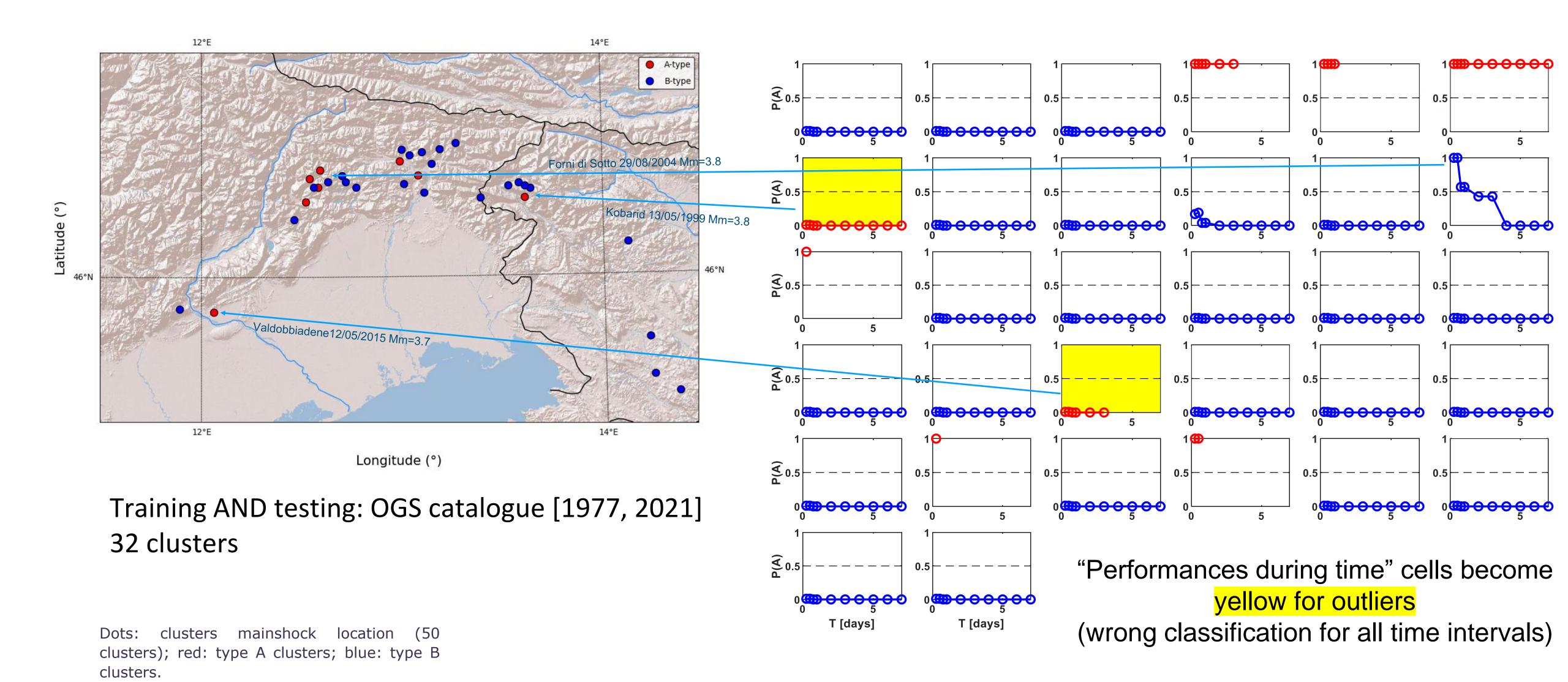


Performances during time





Self-test on NE Italy - Western Slovenia

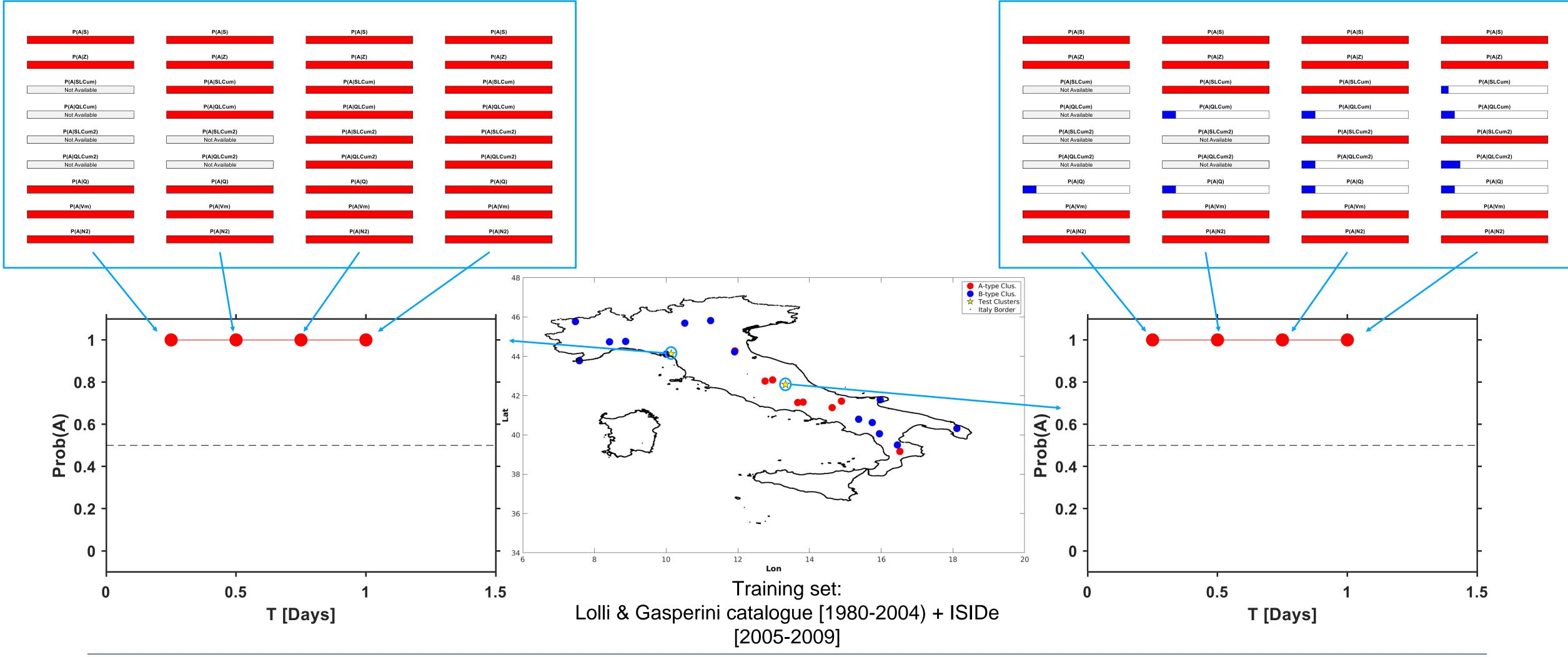






NRT classification Italy

June 21, 2013













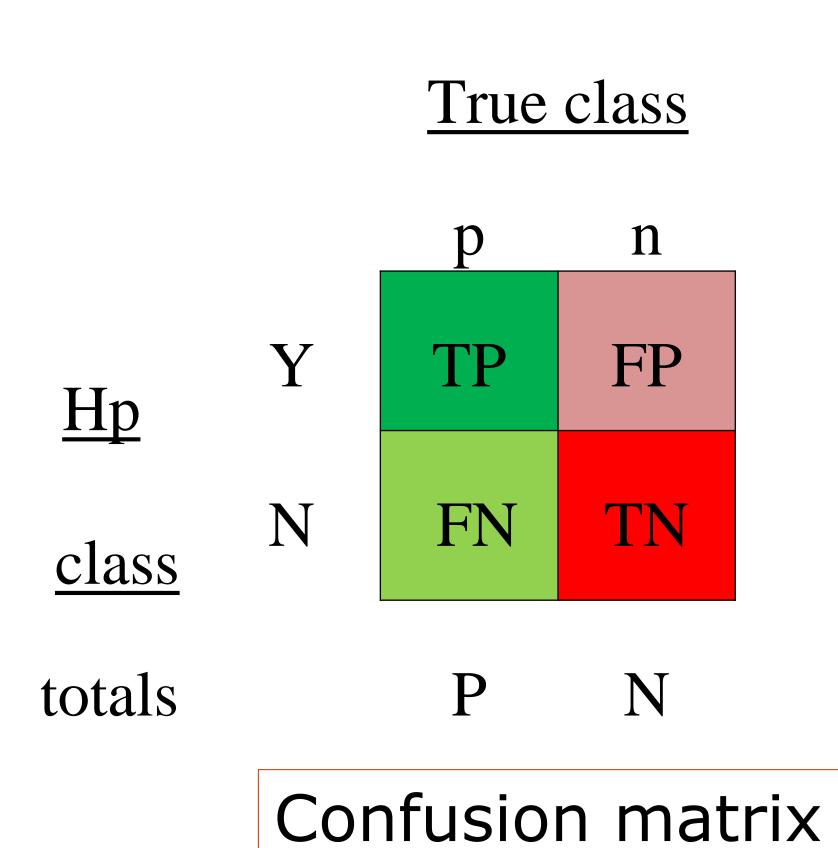


For further details

- Gentili S. and Di Giovambattista R. (2017). Pattern recognition approach to the subsequent event of damaging earthquakes in Italy. Physics of the Earth and Planetary Interiors, 266, 1-17.
 - https://www.researchgate.net/publication/314126252_Pattern_recognition_approach_to_the_subsequent_event_of_damaging_earthquakes_in_Italy
- Gentili S. and Di Giovambattista R. (2020). Forecasting strong aftershocks in earthquake clusters from northeastern Italy and western Slovenia. Physics of the Earth and Planetary Interiors, 303, 106483. https://arxiv.org/ftp/arxiv/papers/2005/2005.02779.pdf
- Gentili S. and Di Giovambattista R. (2022). Forecasting strong subsequent earthquakes in California clusters by machine learning. Physics of the Earth and Planetary Interiors, 327, 106879. https://www.sciencedirect.com/science/article/pii/S0031920122000401



Confusion matrix



$$Recall = TPR = \frac{TP}{P}$$

$$Precision = \frac{TP}{Y}$$

$$Accuracy = \frac{TP + TN}{P + N}$$

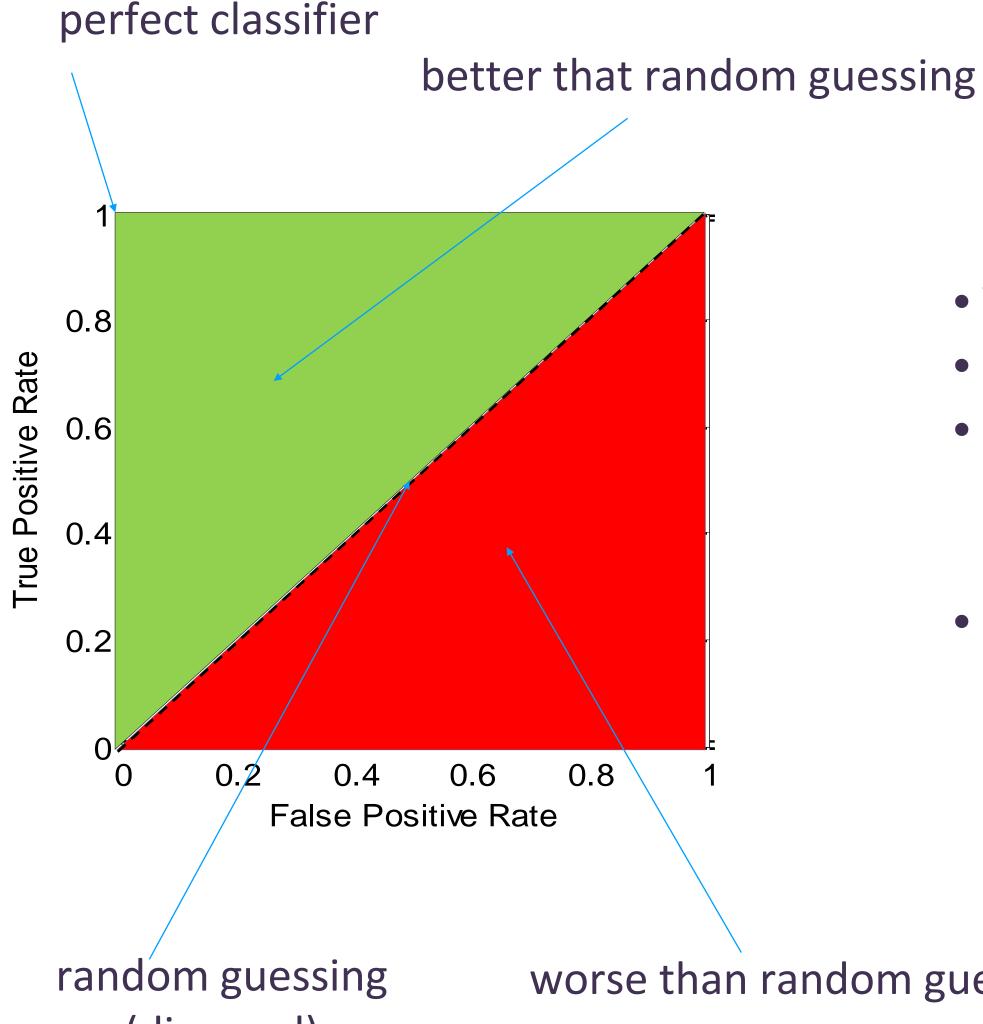
$$FPR = \frac{FP}{N}$$

Informedness = TPR - FPR





ROC



- True Positive Rate= True(A) / All(A)
- False Positive Rate= False(B)/ All(B)
- A discrete classifier produces a point of coordinates (False Positive Rate, True Positive Rate) in the ROC graph.
- One point in ROC space is better than another if it is closer to the point (0,1)

(diagonal)

worse than random guessing







Classifiers combination

- For each T_i, only the feature selected during the training set are extracted
- The thresholds are compared with the value of the feature to estimate the probability pi that the cluster is A for each feature
- The values of p_i are combined by using a Bayesian approach

$$P(A|D_1 \dots D_N) = \frac{[N(B)]^{N-1} \prod_{n=1}^{N} p_n}{[N(B)]^{N-1} \prod_{n=1}^{N} p_n + [N(A)]^{N-1} \prod_{n=1}^{N} (1 - p_n)}$$



