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# Analysis of the growth rate of heliospheric magnetic flux rope instabilities

Bachelor's Thesis



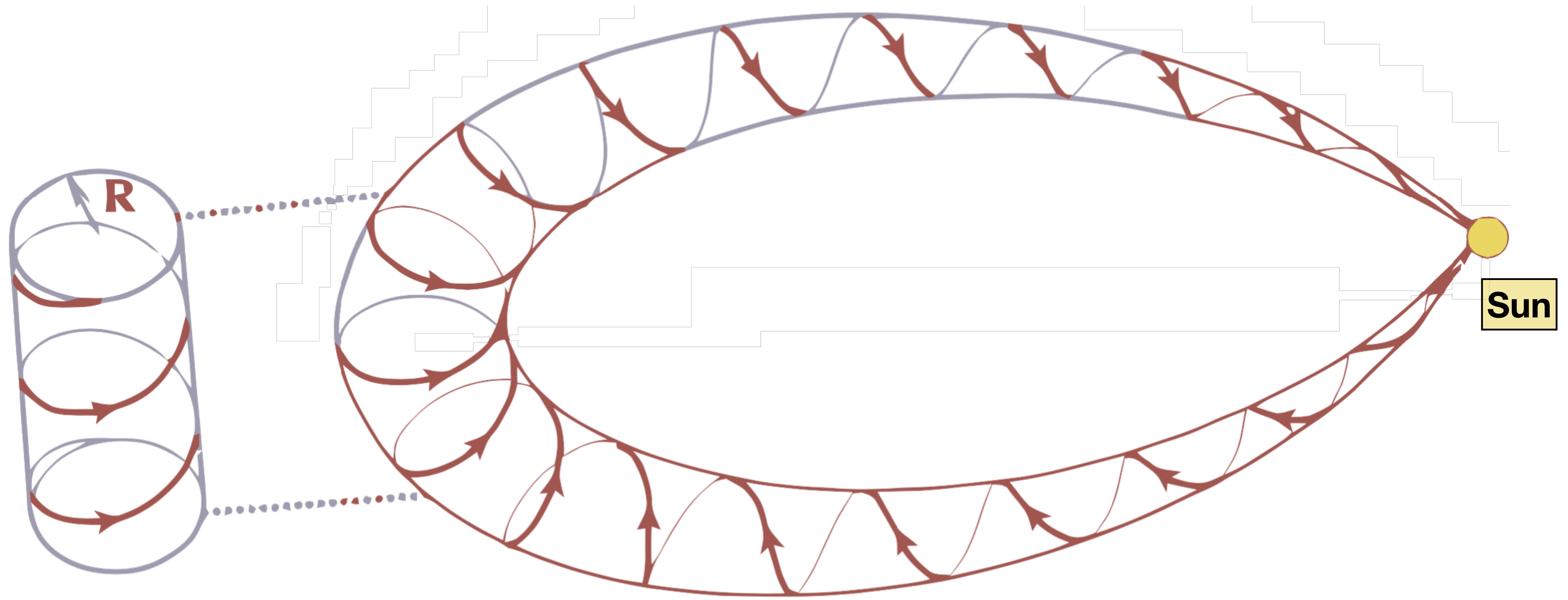
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1. Plasma instabilities in MFRs
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# 1. Plasma instabilities in MFRs

# Coronal mass ejections (CMEs)

## Magnetic flux ropes (MFRs) in magnetic clouds



Schematic representation of a magnetic cloud and its flux rope structure, with its cylindrical approximation. Original from Demoulin & Dasso (A&A, 2009).

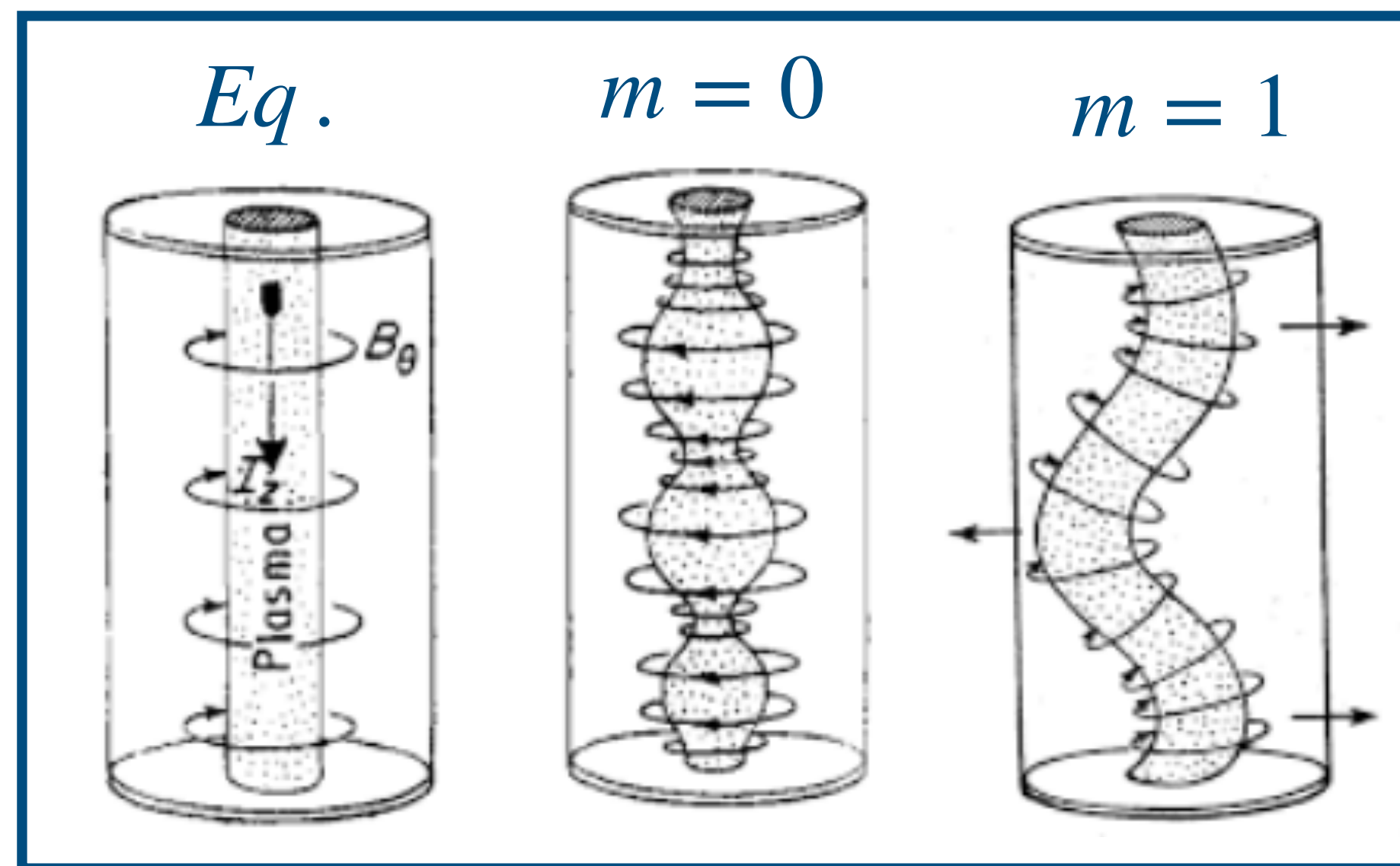


# Plasma instabilities in MFRs

- We consider Fourier displacements:

$$\xi(r, \theta, z) = \tilde{\xi}(r) e^{i m \theta + k z}$$

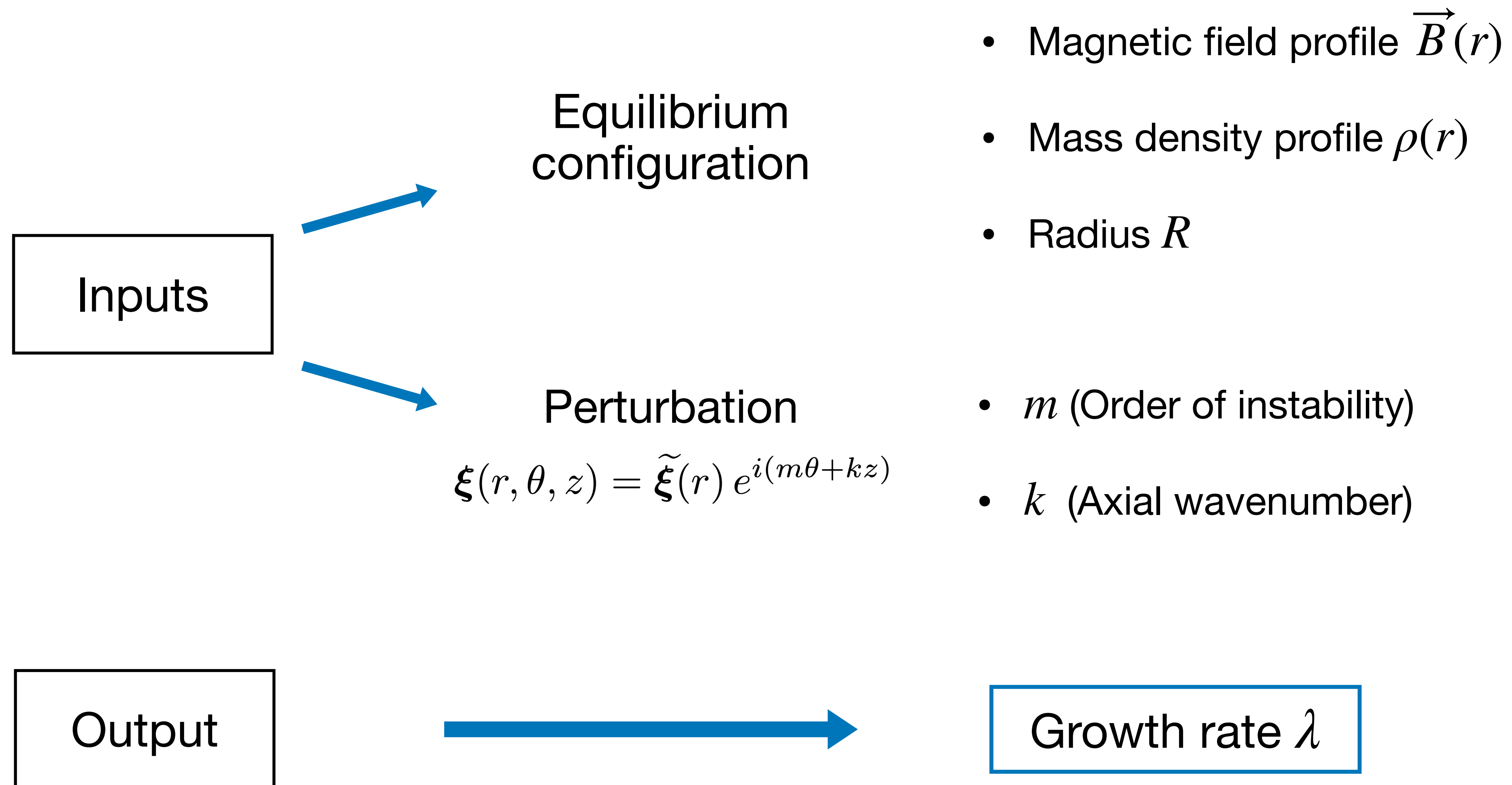
- The azimuthal wave number  $m$  determines the order of the instability:



Cylindrical plasma equilibrium and instabilities of different order  $m$ .  
Extracted from Sadouni (ApJ, 2020).

# Goals of this work

- Generalize Linton et. al. (ApJ, 1996) to study instabilities of any order  $m$
- Compare the growth rates of such instabilities
- Understand the effect of twist and Lorentz forces on flux rope instabilities



## 2. Magnetic field modeling

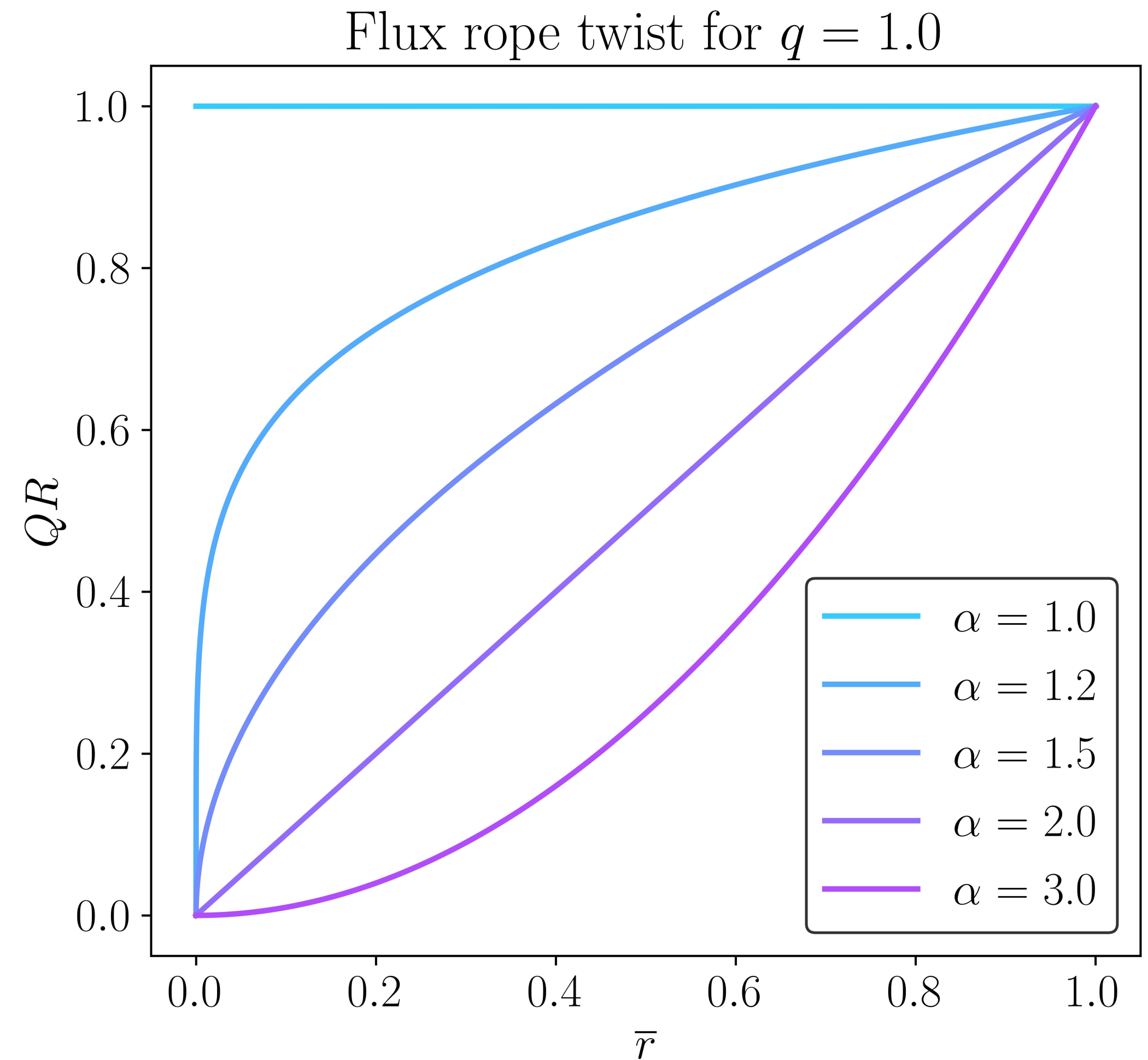
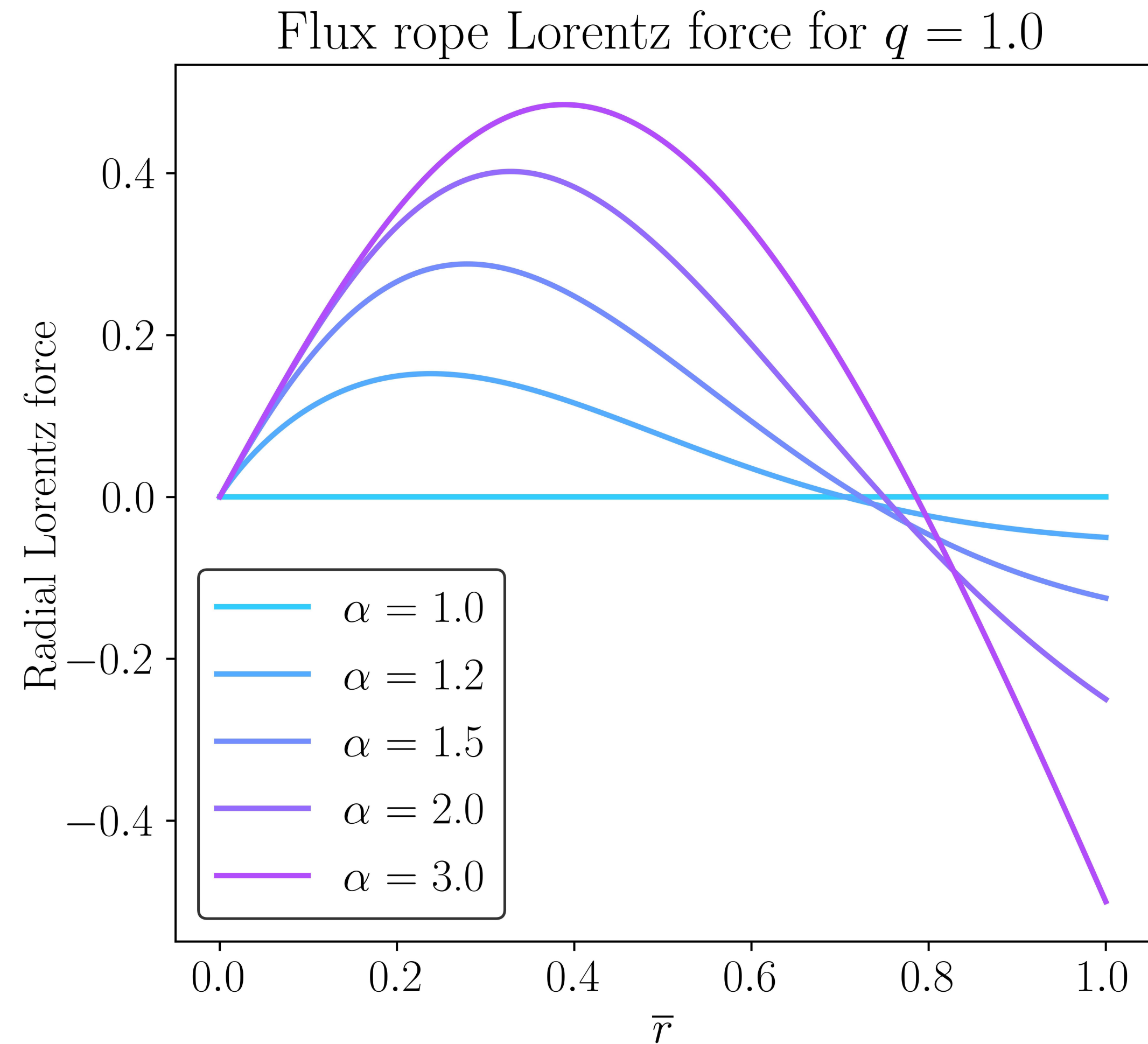
# The modified Gold-Hoyle model

- Given the parameters  $q$  and  $\alpha$ :

$$B_z(\bar{r}) = \frac{B_0}{1 + q^2 \bar{r}^2}, \quad B_\theta(\bar{r}) = q \bar{r}^\alpha B_z(\bar{r})$$

- For  $\alpha = 1$ , we recover the Gold-Hoyle force-free model with uniform twist  $q$ .
- $q$  is the *twist parameter*.
- $\alpha$  is the *force parameter*.

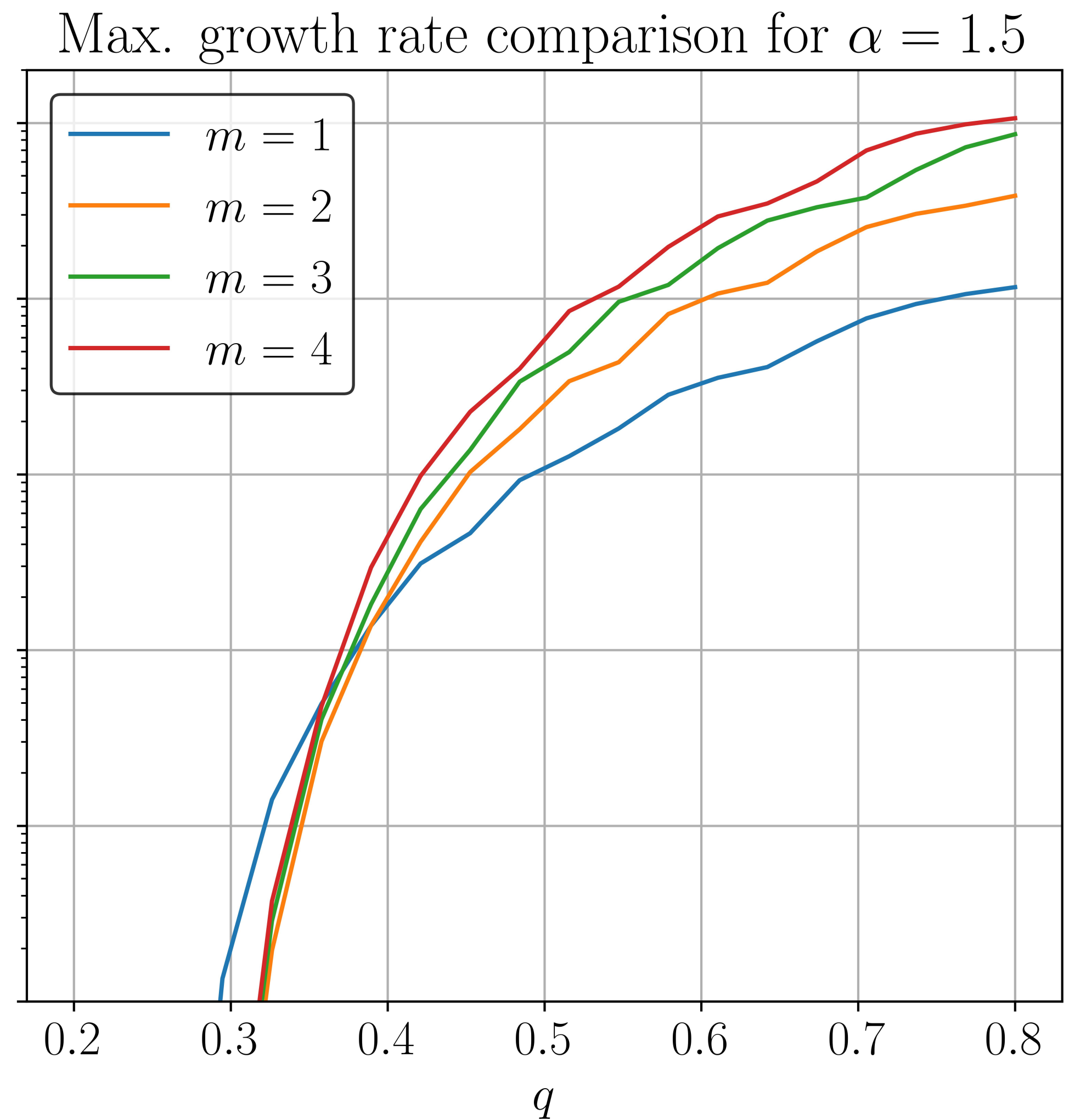
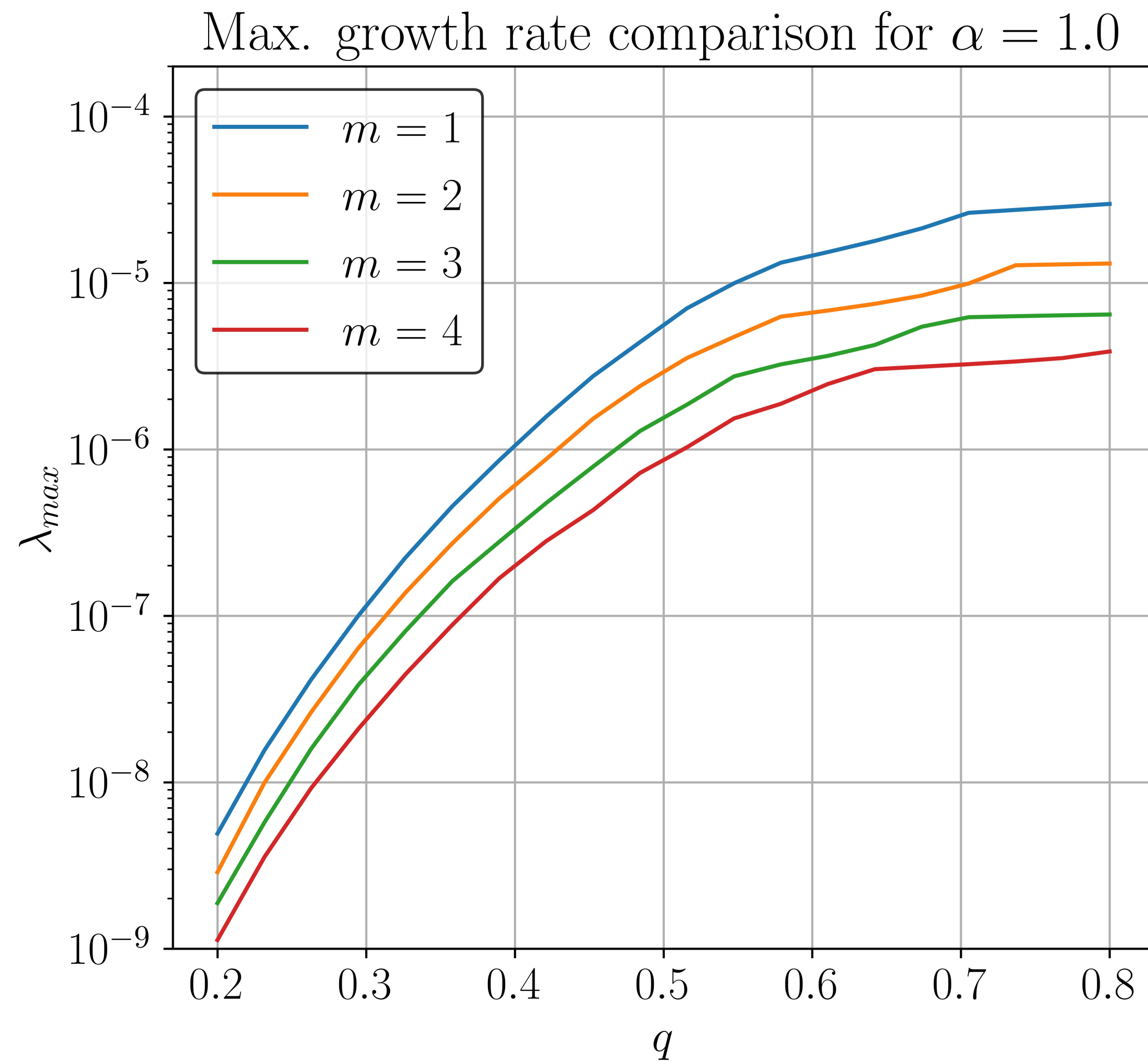
# The modified Gold-Hoyle model



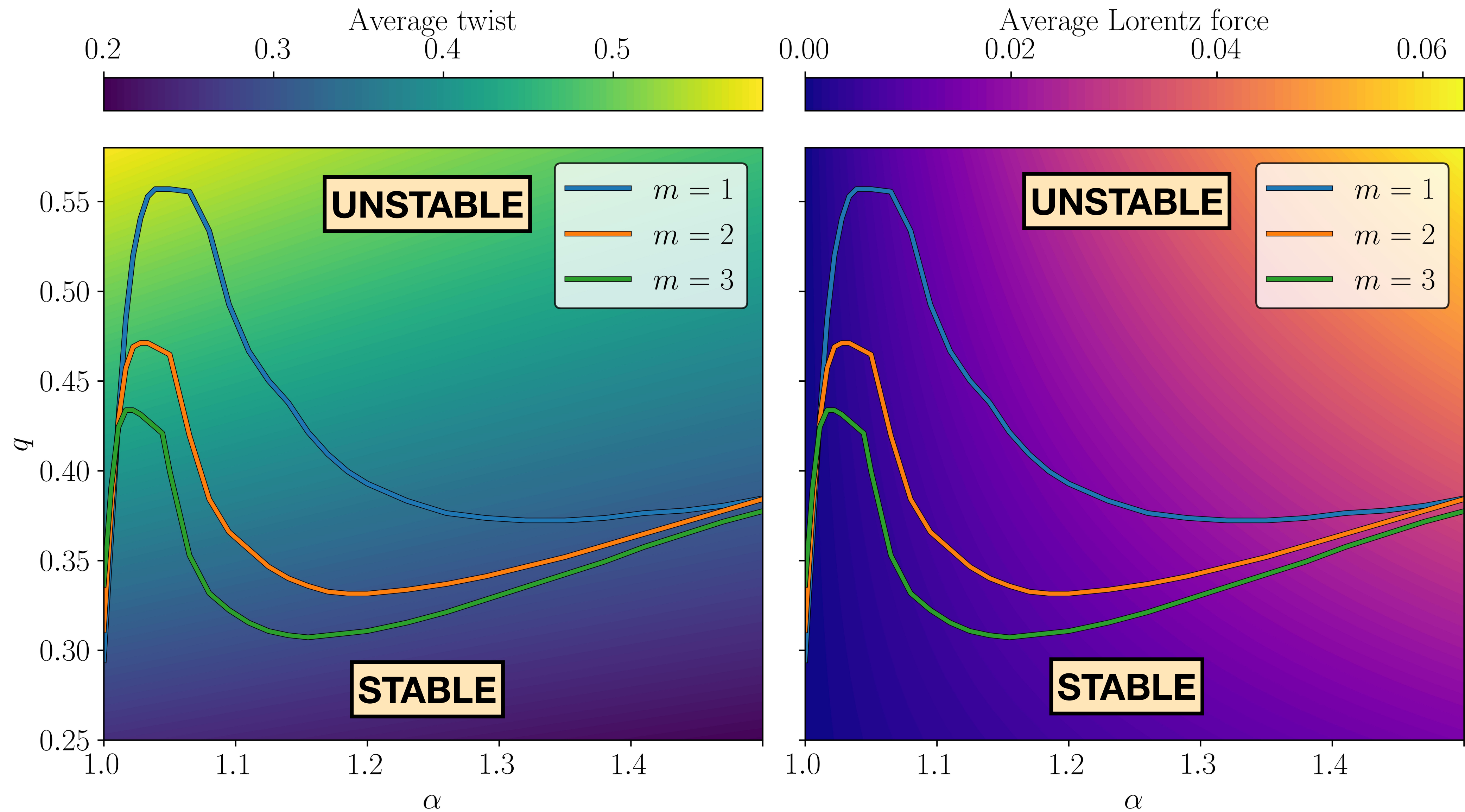
# 3. Presentation of results



# Plotting the maximum growth rate

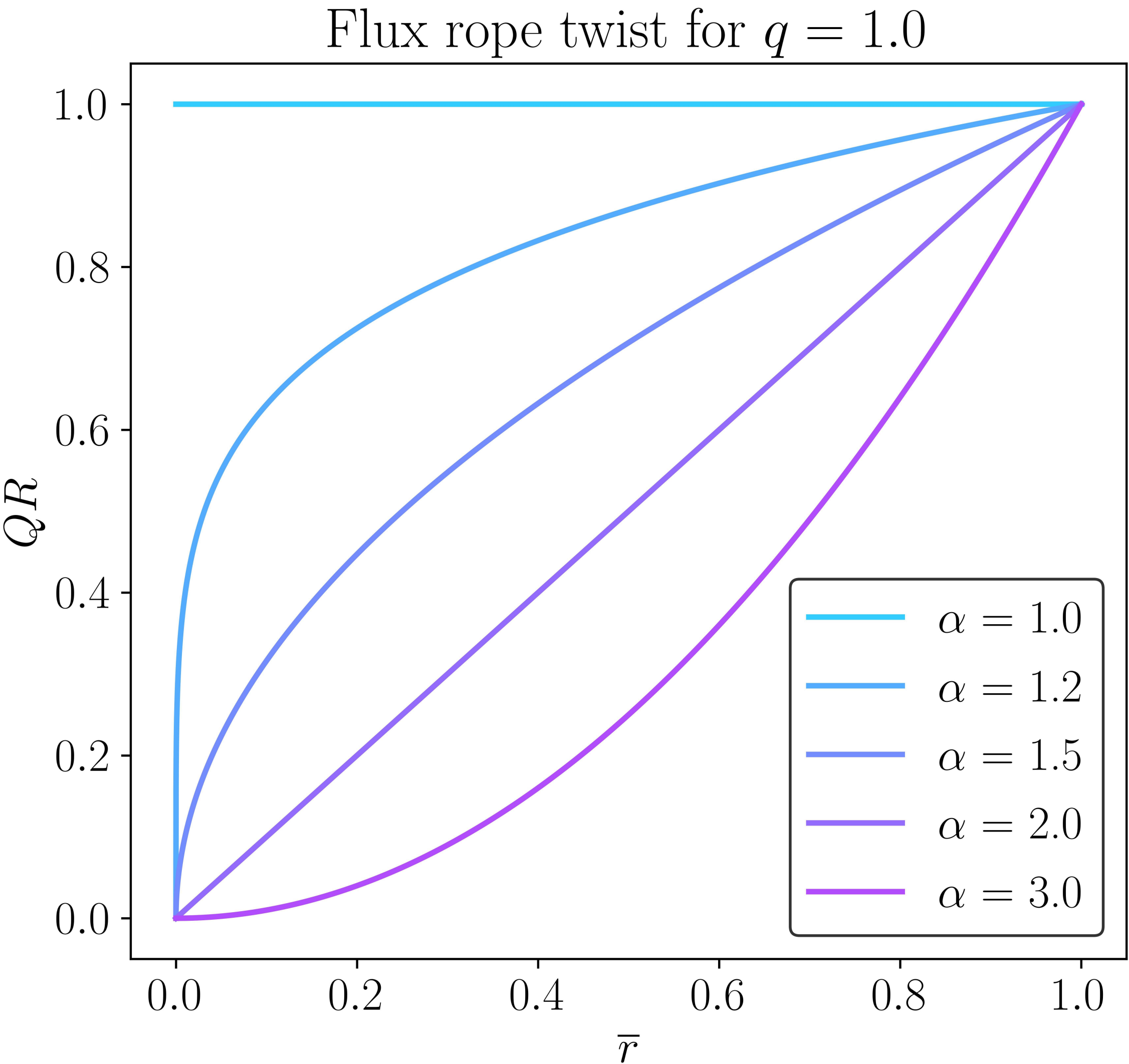
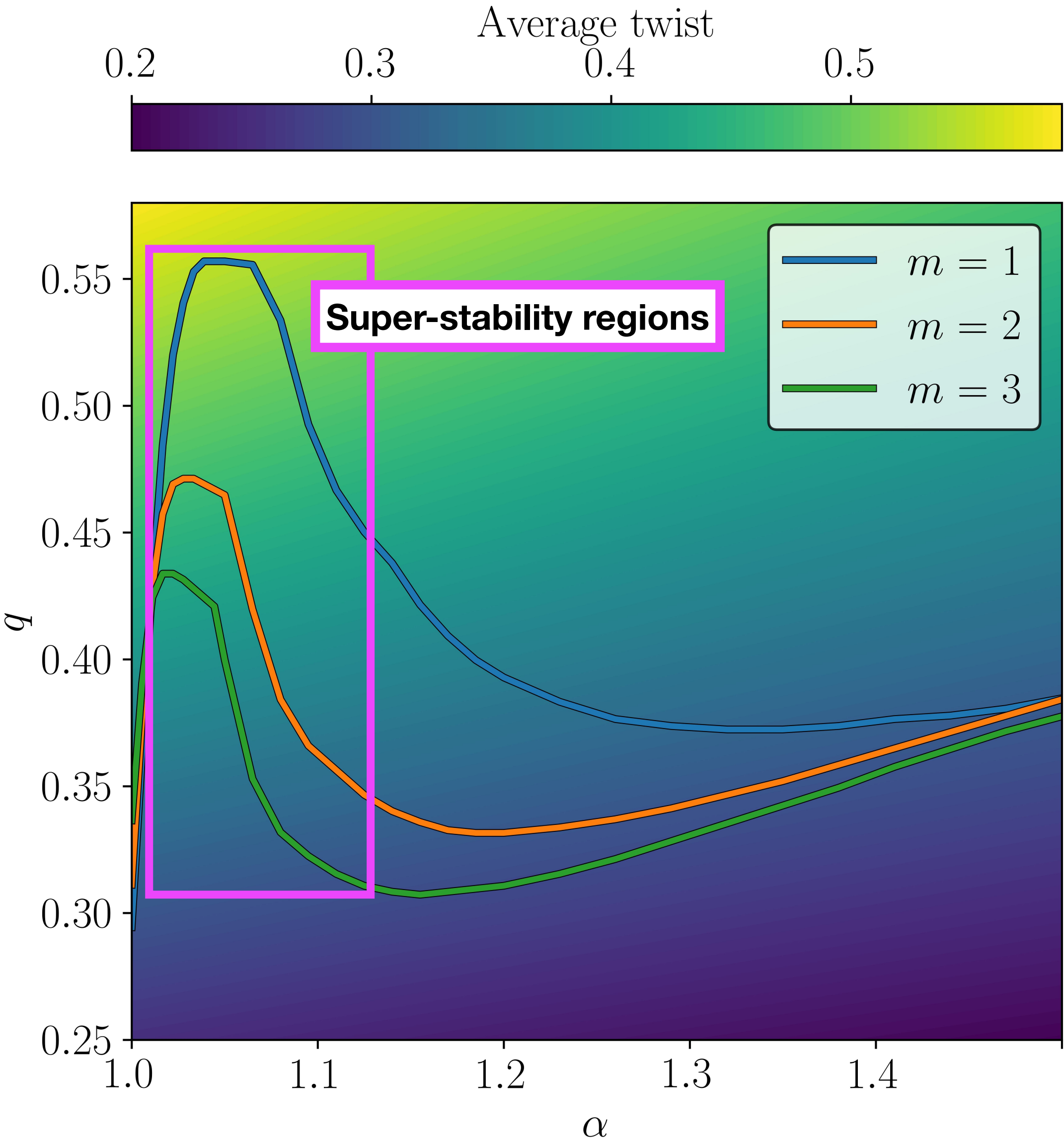


# Stability curves





# Superstability



## 4. Key takeaways

# Key takeaways

- Linton's equations have been generalized to instabilities of any order  $m$ .
- $m = 0$  is always stable, but instabilities were found for  $m \neq 0$ , for  $k \approx -mq$ .
- More rapid instabilities take place in highly twisted MFRs.
- The kink instability seems to dominate in force-free structures.
- When Lorentz forces come into play, there can be an instability inversion.
- For simplicity, big assumptions have been made.

**Thank you.**

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**This presentation participates in OSPP**

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**Outstanding Student & PhD  
candidate Presentation contest**