

Guidance on optimal vertical covariance localization based on a convection-permitting 1000-member ensemble

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Motivation – Why vertical localization?

Ensemble-based background error covariances:

- Key component in convective-scale data assimilation
- Introduce flow-dependence
- Spread information in state space and determine observation weight

Problem: Sampling error due to under-sampling

Requires: Localization to mitigate spurious correlations
(e.g., distance-dependent damping of covariances)

Challenges for (vertical) localization:

- **Long-distance error correlations** with physical meaning
--> for example radiative effects of clouds or deep convection
- **Non-linear flow and rapid error growth**
--> localization on convective scales is non-trivial task

Our approach: Very large ensembles + subsampling for improving localization

Localization of error covariances

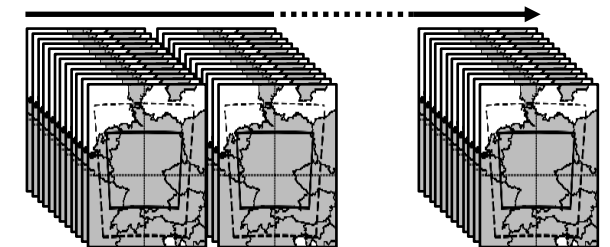
$$x_a = x_b + K(y - H x_b)$$

$$K = PH^T(HPH^T + R)^{-1}$$

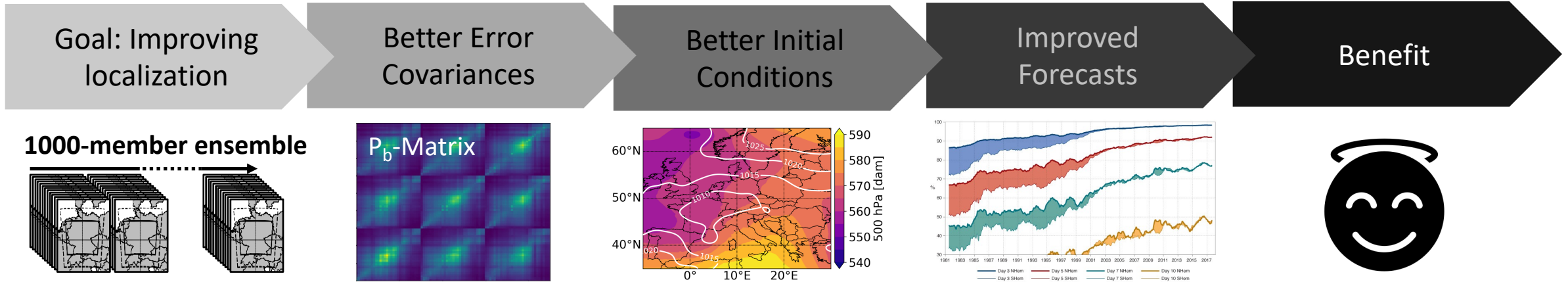
$$P = \frac{1}{N-1} \sum_{n=1}^N (x^n - \bar{x})(x^n - \bar{x})^T$$

$$P_{loc} = C \circ P$$

C: Localization matrix (model space)



Research goals - Vertical Localization



Research questions: Improving vertical localization based on 1000-member ensemble data-set

- How should an **optimal localiaztion** for vertical correlations be constructed?
- What are **optimal vertical localization scales/functions** for temperature, humidity or wind?
- How much **error reduction** can be achieved with different vertical localization approaches?

Convective-scale 1000-member ensemble simulation

1000-member ensemble

- **Model:** Japanese "SCALE-RM" model
- **Period:** 5 days / 10 forecasts in Mai/June 2016
- **Resolution:** 3 km grid spacing, 350x250 grid points with 30 levels
- **Boundary conditions:** Global GFS ensemble (20-member, NCEP)
+ 1000 random climatologically scaled perturbations

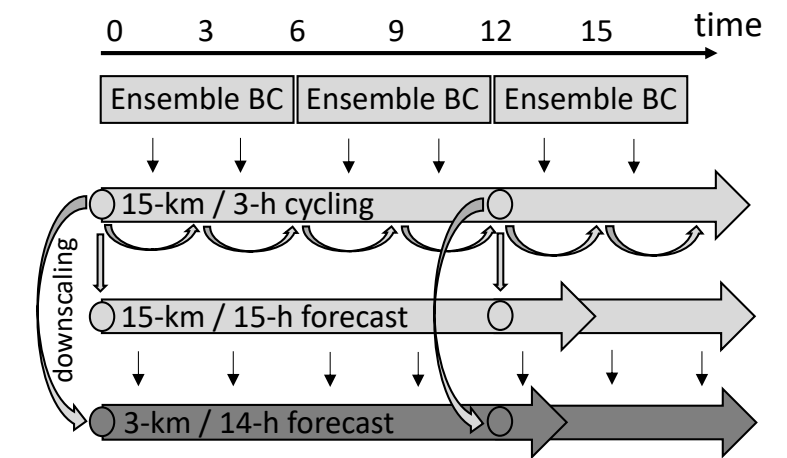
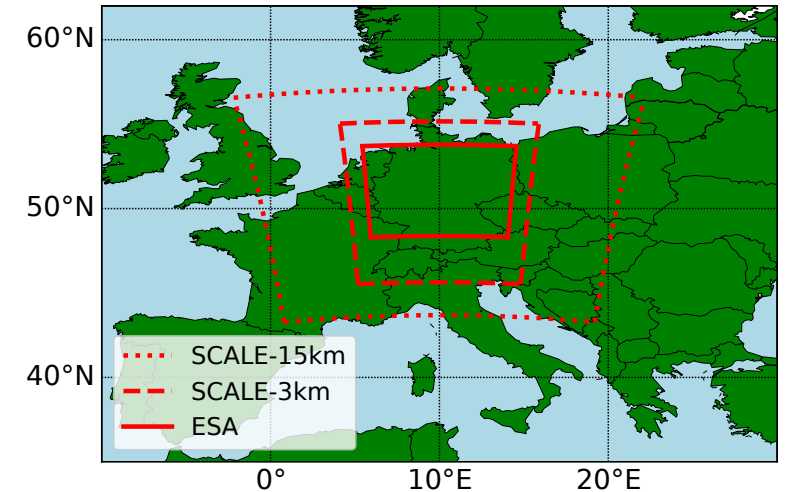
Experimental setting:

- 1000-member correlation as truth: r^{1000}
- 25 40-member subsample correlations: r^{40}
- 3h first guess background forecast for error correlations
- Focus on vertical correlations on 20 pressure levels

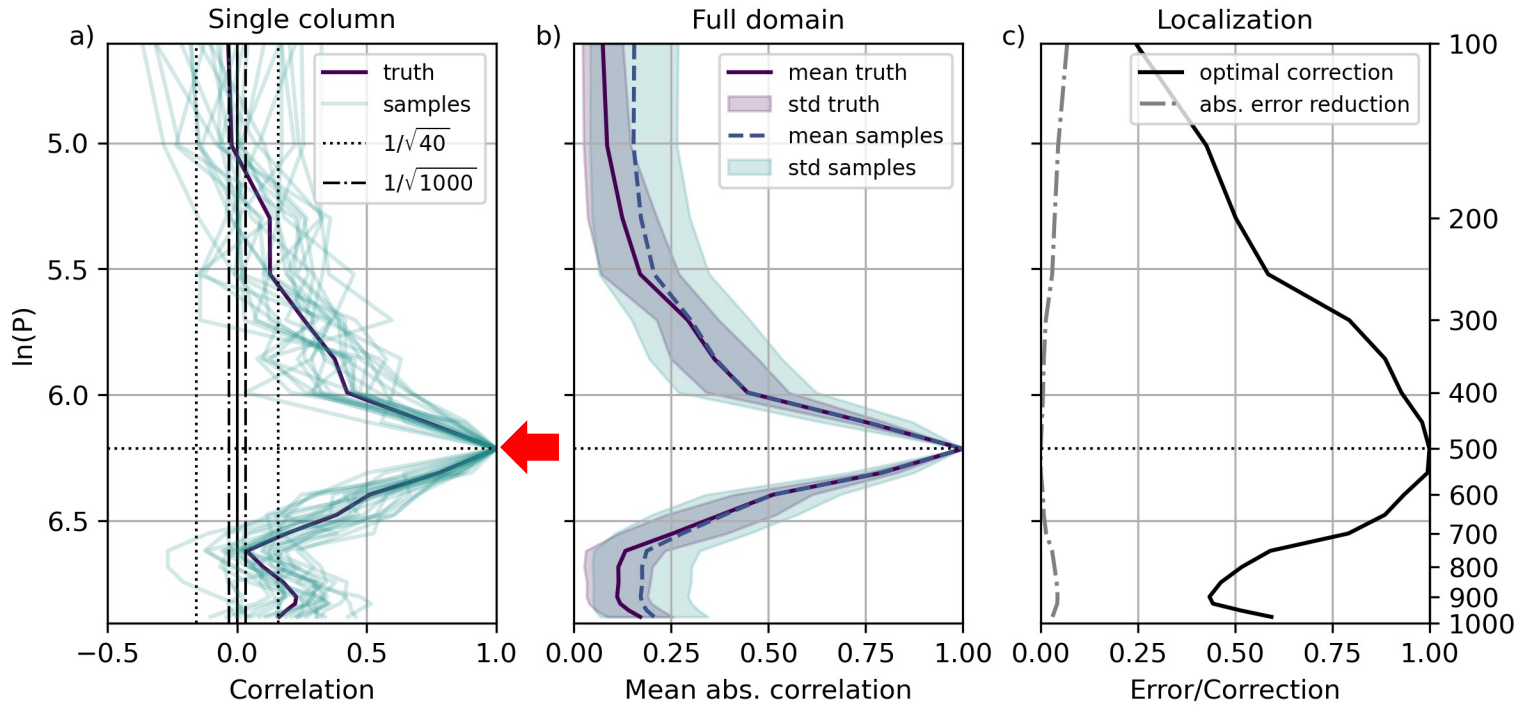
In collaboration with



Necker et al. 2020a (QJRM)
Necker et al. 2020b (MWR)



Goal: Finding empirical optimal localization α



Cost function $J \rightarrow$ opt. localization α
 „minimize root mean square difference between subsamples and 1000-m truth“

$$J(\alpha, t, p, A) = \sqrt{\sum_{s=1}^S \sum_{k=1}^K (\alpha r_{s,k}^{40} - r_k^{1000})^2}$$

J: Cost function t: time S: Subsamples
 α : opt. localization p: level K: Grid points
 r: correlation A: Variable pair

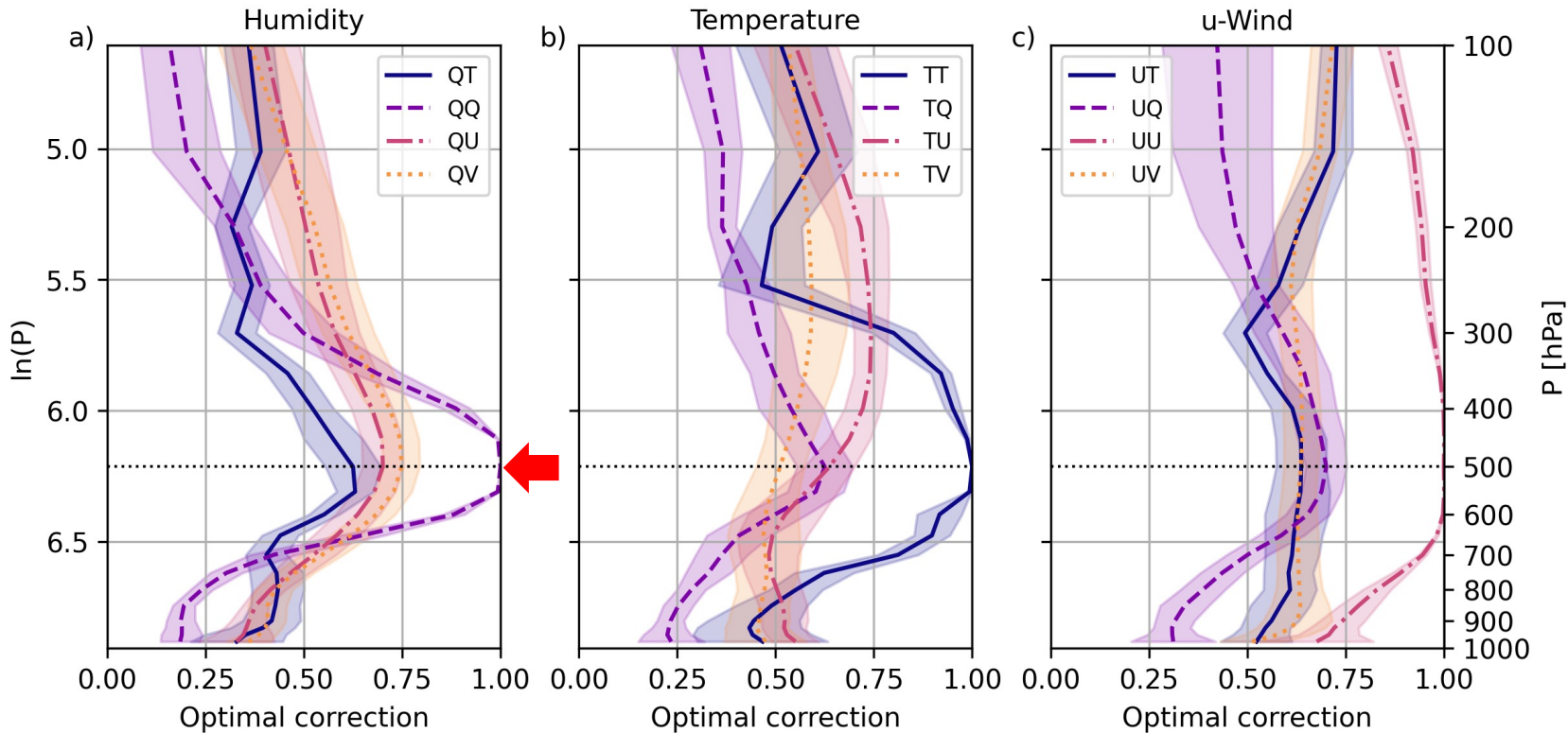
Optimal localization for vertical correlations

- Domain-uniform / non-adaptive loc.
- **Reference level 500hPa**
- **Temperature-Temperature correlations**

We focus on correlations as sampling error in variances is small

$$COV(x_1, x_2) = r(x_1, x_2) \sigma(x_1) \sigma(x_2)$$

Teaser result - Optimal vertical localization α



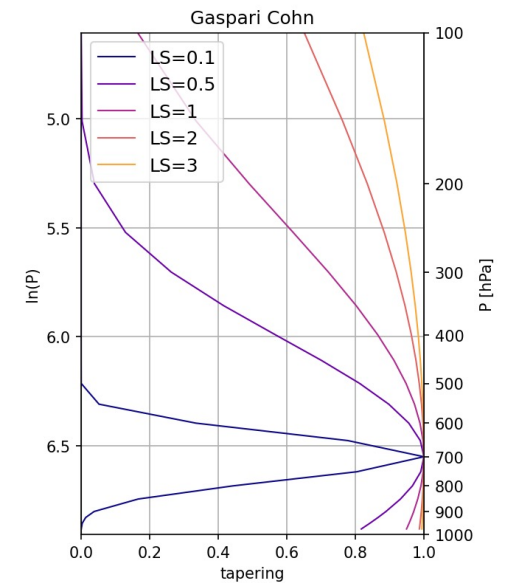
T: Temperature / Q: Spec. humidity / U: Zonal wind / V: Meridional wind

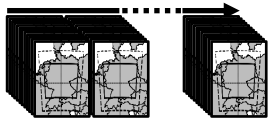
Shading: forecast-to-forecast variability

Reference level 500hPa

Conclusions

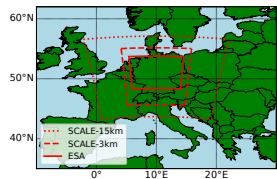
- Different localization scales: humidity, temperature, and wind
- Different requirements for self- and cross-correlations
- Different localization shapes: Exponential, Gaussian, or linear





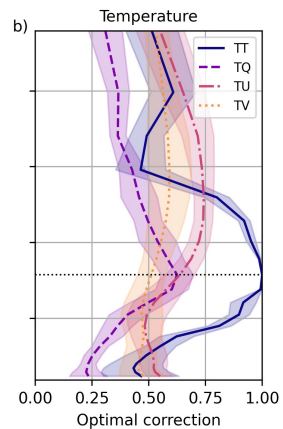
What can we learn from a convective-scale 1000-member ensemble?

- Quantify sampling errors and evaluate existing localization methods
- Derive optimal localization approaches independent of algorithmic constraints



Research Questions

- How should an **optimal localization** for vertical correlations be constructed?
- What are **optimal vertical localization scales/functions** for temperature, humidity or wind?
- How much **error reduction** can be achieved with different vertical localization approaches?



Necker et al. 2022 (NPG / Copernicus - Submission soon)

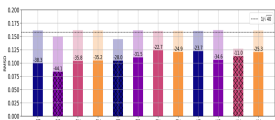
Guidance on how to improve vertical covariance localization based on a 1000-member ensemble.

Necker et al. 2020a (QJRMS) A convective-scale 1,000-member ensemble simulation and potential applications.

Q. J. R. Meteorol. Soc. 2020, 146, 1423– 1442. <https://doi.org/10.1002/qj.3744>

Necker et al. 2020b (MWR) Sampling Error Correction Evaluated Using a Convective-Scale 1000-Member Ensemble.

Mon. Wea. Rev., 148, 1229-1249. <https://doi.org/10.1175/mwr-d-19-0154.1>



Thank You!



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