

COMPARISON OF THE PERFORMANCE OF PCA-NN MODELS FOR TEC OVER THE IBERIAN PENINSULA:

THE ROLE OF SPACE WEATHER PARAMETERS AS PREDICTORS FOR TEC

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Photography encouraged



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ABSTRACT

The total electron content (TEC) over the Iberian Peninsula was modeled using a PCA-NN models based on the decomposition of the observed TEC series using the principal component analysis (PCA) and reconstruction of the daily mean TEC and daily PCA modes' amplitudes by different types of neural networks (NN) using several types of space weather parameters as predictors. Lags of 1 and 2 days between the TEC and space weather parameters are used.

Two main goals are set:

1. To find a NN configuration(s) that produces forecasts of reasonable quality with minimal amount of input data
2. To find a best set of space weather parameters that work as predictors for PCA-NN models

Here we present preliminary results related to the **second goal**: PCA-NN models with different sets of predictors are compared. Among predictors we consider proxies for the solar UV and XR fluxes, number of the solar flares of different types, parameters of the solar wind and of the interplanetary magnetic field, geomagnetic indices, solar wind coupling functions and TEC series themselves.

TOC

- PCA-NN models for TEC
- Data
 - TEC
 - SW predictors
 - Different groups of SW predictors
 - Correlated SW predictors
 - “Auto-regression” introduction
- NN Configuration
- Selection of the best sets of SW predictors and optimization of hyperparameters
- Performance of the PCA-NN model
- Conclusions
- Acknowledgements

PCA-NN MODELS FOR TEC



PCA-BASED MODELS

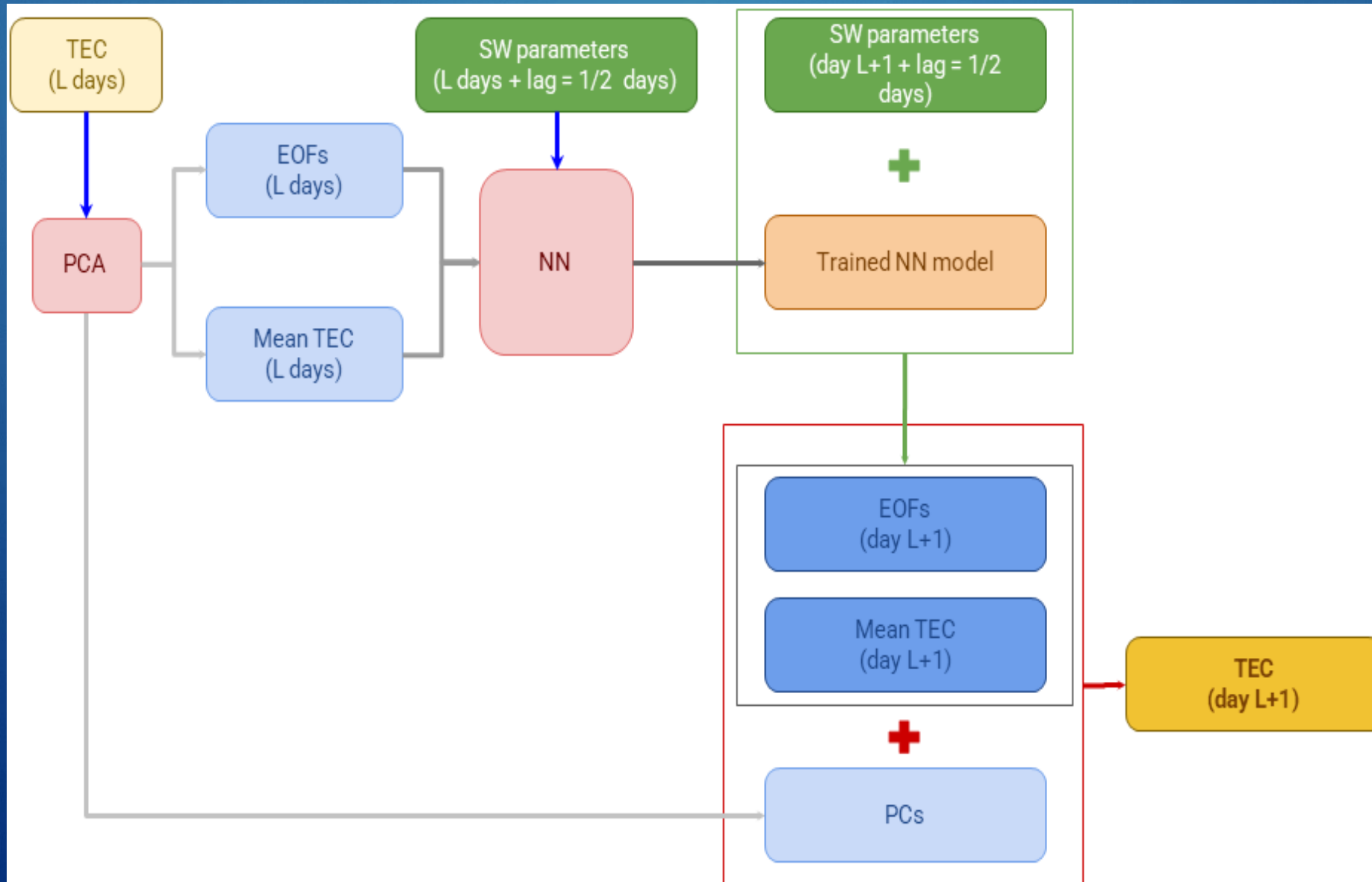
- The total electron content (TEC) over the Iberian Peninsula was modeled using a PCA-NN model based on
 1. decomposition of the observed TEC series using the principal component analysis (PCA)
 2. reconstruction of the daily mean TEC and daily PCA modes' amplitudes by, for example, regression models (PCA-MRM models^{*}) or neural networks (PCA-NN models) using several types of space weather parameters (SW) as predictors.
- Lags of 1 and 2 days between the TEC and SW predictors are used

^{*} A. L. Morozova, T. Barata, T. Barlyaeva (2022) PCA-MRM model to forecast TEC at middle latitudes, *Atmosphere*, 13(2), 323; <https://doi.org/10.3390/atmos13020323>

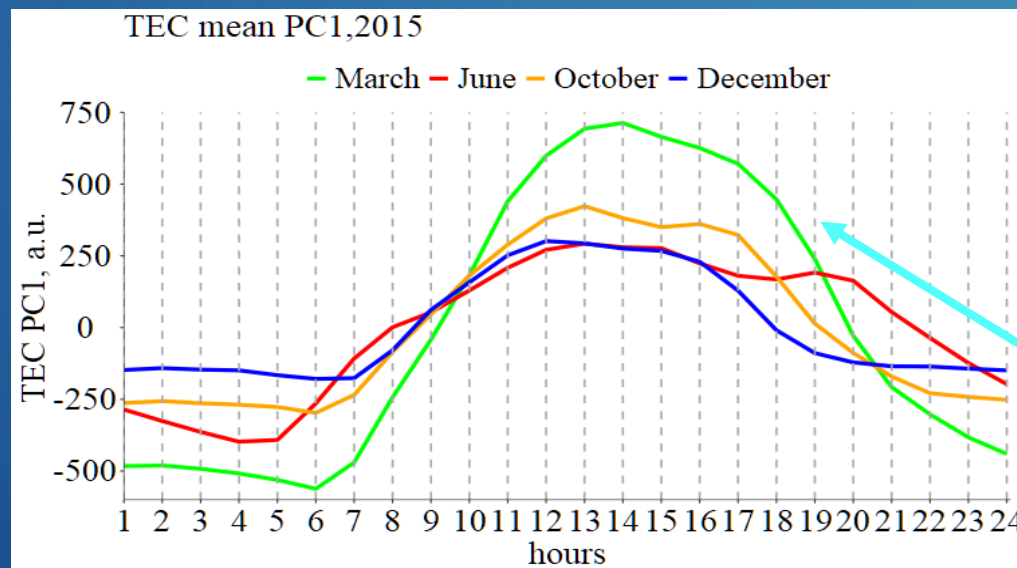


PCA-NN MODEL

$L = 31$ days



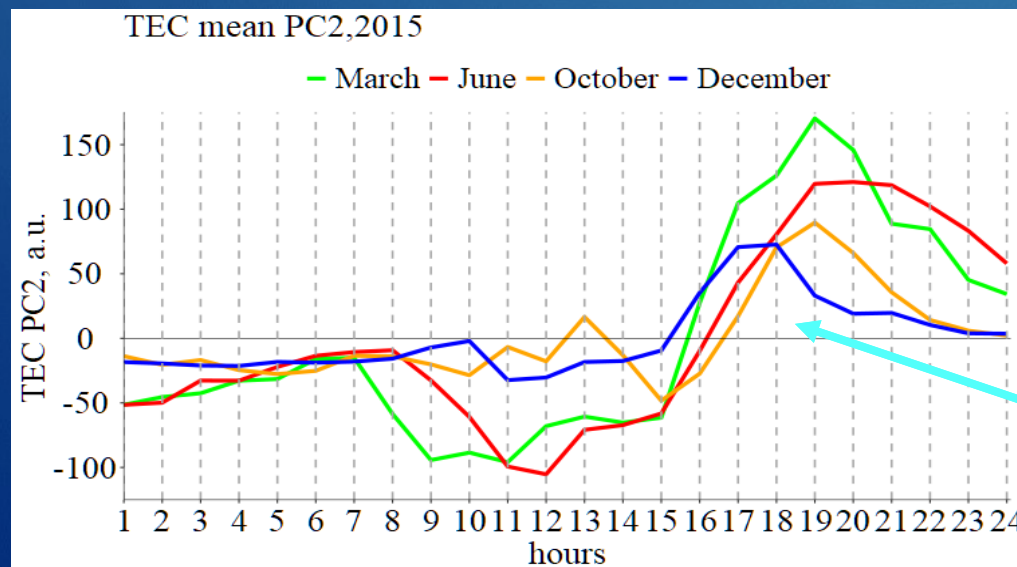
TEC PCA MODES 1 AND 2



Mode 1 (PC1 & EOF1):

Explains 77-95% of the TEC variations for different months

PC1 = regular daily variation due to the changes of the insolation



Mode 2 (PC2 & EOF2):

Explains 1.5-8.4% of the TEC variations for different months

PC2 = shallow minimum of TEC around the noon and a maximum in the late afternoon



PCA-BASED MODELS

- The main feature of the PCA-based models is that the TEC series is decomposed into several PCA modes which represent TEC daily variations of different types
- The amplitude of each of the mode for each day is described by the EOF coefficients
 - The EOF coefficients can be modelled using space weather parameters as predictors using, e.g., multiple regression models (MRM) or neural networks (NN)
- The advantage of the PCA-based models is that there is no need for any assumption on the phase and amplitude or seasonal/regional features of TEC daily variations: the daily variations of correct shapes are extracted automatically by PCA from the input TEC data



DATA



DATA: TEC

- Vertical TEC measured at Lisbon airport, Portugal (39° N, 9° W) by a GNSS receiver with SCINDA firmware
- Time interval: 01.01.2015- 31.12.2015
- Time resolution: 1h data
- TEC series: daily mean TEC, EOF1, EOF2



DATA: SPACE WEATHER PARAMETERS (SW PREDICTORS)

- Solar wind parameters:
 - Pressure (p), density (n), velocity (v)
- Interplanetary magnetic field:
 - Full interplanetary magnetic field (scalar B), GSM components (B_x, B_y, B_z)
- Coupling functions*: $d\Phi_{MP}/dt$, E_{WAV} , E_{WV} , ε_3 , E_{KLV} , E_{KL} , $v \cdot B_S$, E_{SR} , E_{TL}
- Geomagnetic indices:
 - Dst, ap, AE, local K_{COI}-index (Coimbra Geomagnetic Observatory, Portugal)
- Proxies for the solar UV & XR fluxes:
 - UV: Mg II composite series or F10.7 index
 - XR: Solar EUV Experiment (TIMED mission)
 - Daily number of solar flares of classes $\leq C$ and M, and the number of all flares N
- Time resolution: 1 d data

* Newell, P. T., T. Sotirelis, K. Liou, C.-I. Meng, and F. J. Rich (2007), A nearly universal solar wind-magnetosphere coupling function inferred from 10 magnetospheric state variables, *J. Geophys. Res.*, 112, A01206, doi:10.1029/2006JA012015



SPACE WEATHER PARAMETERS: CORRELATED PREDICTORS

- Some of the SW predictors correlate with each other
- Highest correlations:
 - n & p ($|r| = 0.75$)
 - Dst & ap & AE & K_{coi} ($|r| = 0.75 \div 0.85$)
 - $Mg II$ & $F10.7$ & XR ($|r| \geq 0.82$)
 - Number of C and all flares ($|r| = 0.98$)
 - $(d\Phi_{MP}/dt, E_{WAV}, E_{WV}, \varepsilon_3, E_{KLV}, E_{KL}, v \cdot B_S, E_{SR}, E_{TL})$ vs (K_{coi}, ap, AE) ($|r| \geq 0.75$)

To test: Can we use correlated predictors?



TEC SERIES: AUTO-REGRESSION

- Lag1 autocorrelation coefficients
 - Daily mean TEC: $\alpha_1 = 0.91$
 - EOF1 : $\alpha_1 = 0.14$
 - EOF2 : $\alpha_1 = 0.38$
- Hypothesis to test: Adding lagged TEC series as the NN input parameters could improve NN forecasting skills for daily mean TEC and EOF2, but not for EOF1



NN MODELS: CONFIGURATION



PCA-NN MODEL – PREVIOUS RESULTS

- NN algorithm: feedforward NN with the resilient backpropagation with weight backtracking (ready-to-use package `neuralnet` (R))
- The input dataset length $L = 31$ days
- SW predictors are submitted as lagged series (lag = 1 and 2 days) together (for X predictors there are $2 \cdot X$ input series)
- “Monte-Carlo approach”: a number (e.g., 100) of NN models of the same architecture were trained on the same input dataset and were used to make a forecast for the day $L+1$; the final forecast is the arithmetic average of 100 forecasts



PCA-NN MODEL – CURRENT QUESTIONS

? Best set of SW predictors for the daily mean TEC and EOFs series

? Can correlated SW predictors be used

? Can TEC series be used as predictors

? Best NN configuration (hyperparameters) that produces forecasts of reasonable quality with minimal number of SW predictors for the daily mean TEC and EOFs series



SELECTION OF THE BEST SETS OF SW PREDICTORS & OPTIMIZATION OF HYPERPARAMETERS





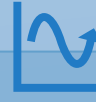


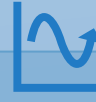
BEST NN ARCHITECTURE AND BEST SETS OF SW PREDICTORS

(no solar wind coupling functions, no auto-regression)

	Daily mean TEC	EOF1	EOF2
NN (layers & nodes)	(12,6,4)	(6,4)	(8,4,2)
Predictors	6 predictors	3 predictors	4 predictors
Best predictors	MgII Dst N. C flares ap AE XR	AE MgII Dst	AE Dst F10.7 v
r	0.91	0.31	0.33
MAE/RMSE (TEC _u)	1.82/2.40	0.03/0.04	0.13/0.18









BEST NN ARCHITECTURE AND BEST SETS OF SW PREDICTORS (+ solar wind coupling functions, no auto-regression)

	Daily mean TEC	EOF1	EOF2
NN (layers & nodes)	(14,7,3) (14,6,4) (14,4,2)	(8,4)	(10,8,4)
Predictors	7 predictors	4 predictors	5 predictors
Best predictors	MgII Dst N. C flares ap AE XR E _{SR} or E _{KLV} or E _{WV}	AE MgII Dst E _{SR}	AE Dst F10.7 v E _{SR} or E _{TL}
r	0.91 	0.29 	0.32 
MAE/RMSE (TEC_u)	1.84/2.42 	0.03/0.04 	0.14/0.18 



BEST NN ARCHITECTURE AND BEST SETS OF SW PREDICTORS (no solar wind coupling functions, + auto-regression)

	Daily mean TEC	EOF1	EOF2
NN (layers & nodes)	(14,7,3) (14,6,4) (14,4,2)	(8,4)	(10,8,4)
Predictors	7 predictors	4 predictors	5 predictors
Best predictors	MgII Dst N. C flares ap AE XR Daily mean TEC	AE MgII Dst EOF1	AE Dst F10.7 v EOF2
r	0.93 	0.28 	0.39 
MAE/RMSE (TEC_u)	1.73/2.40 	0.03/0.04 	0.13/0.17 



Legend:

About the same skills



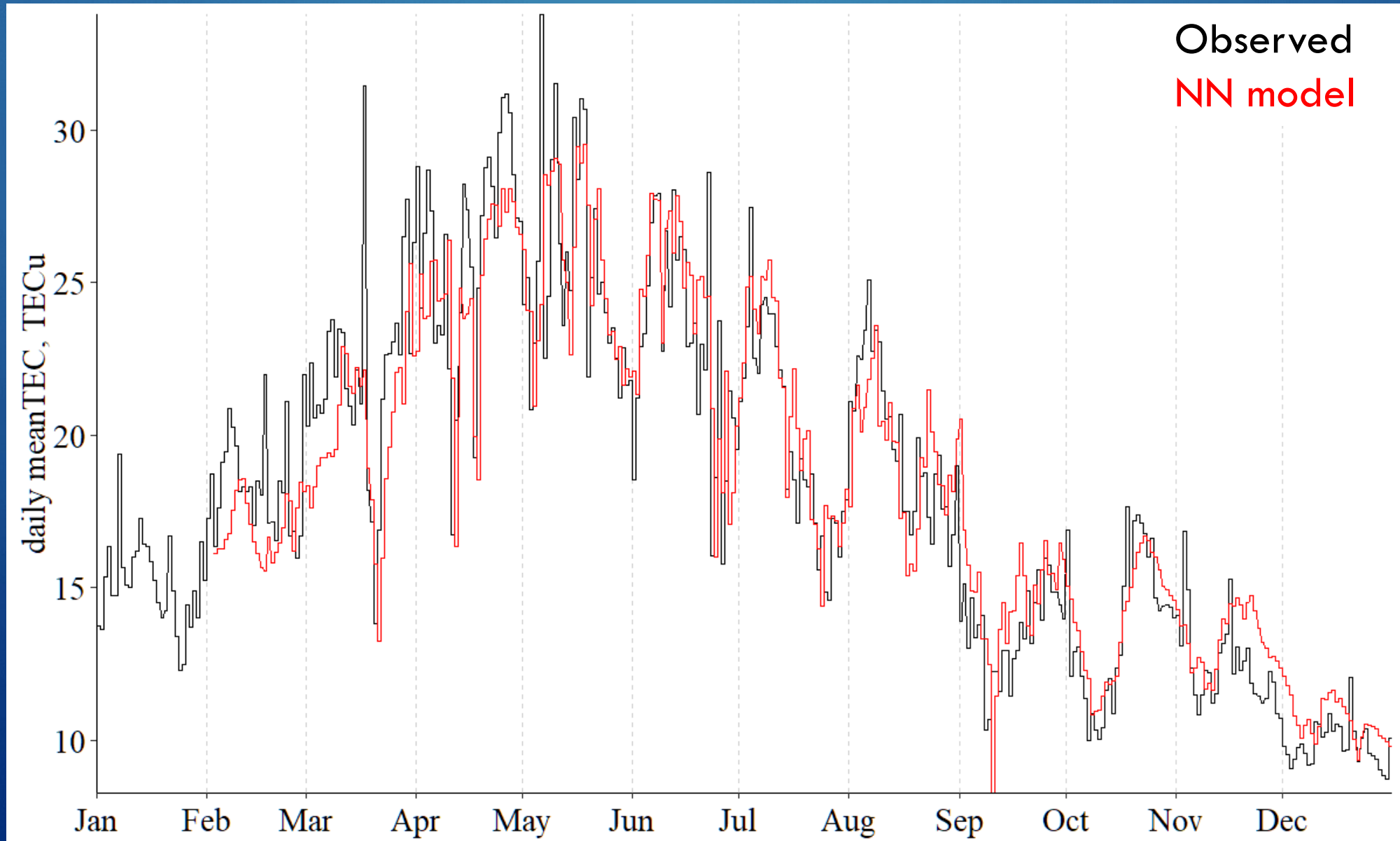
Worse skills



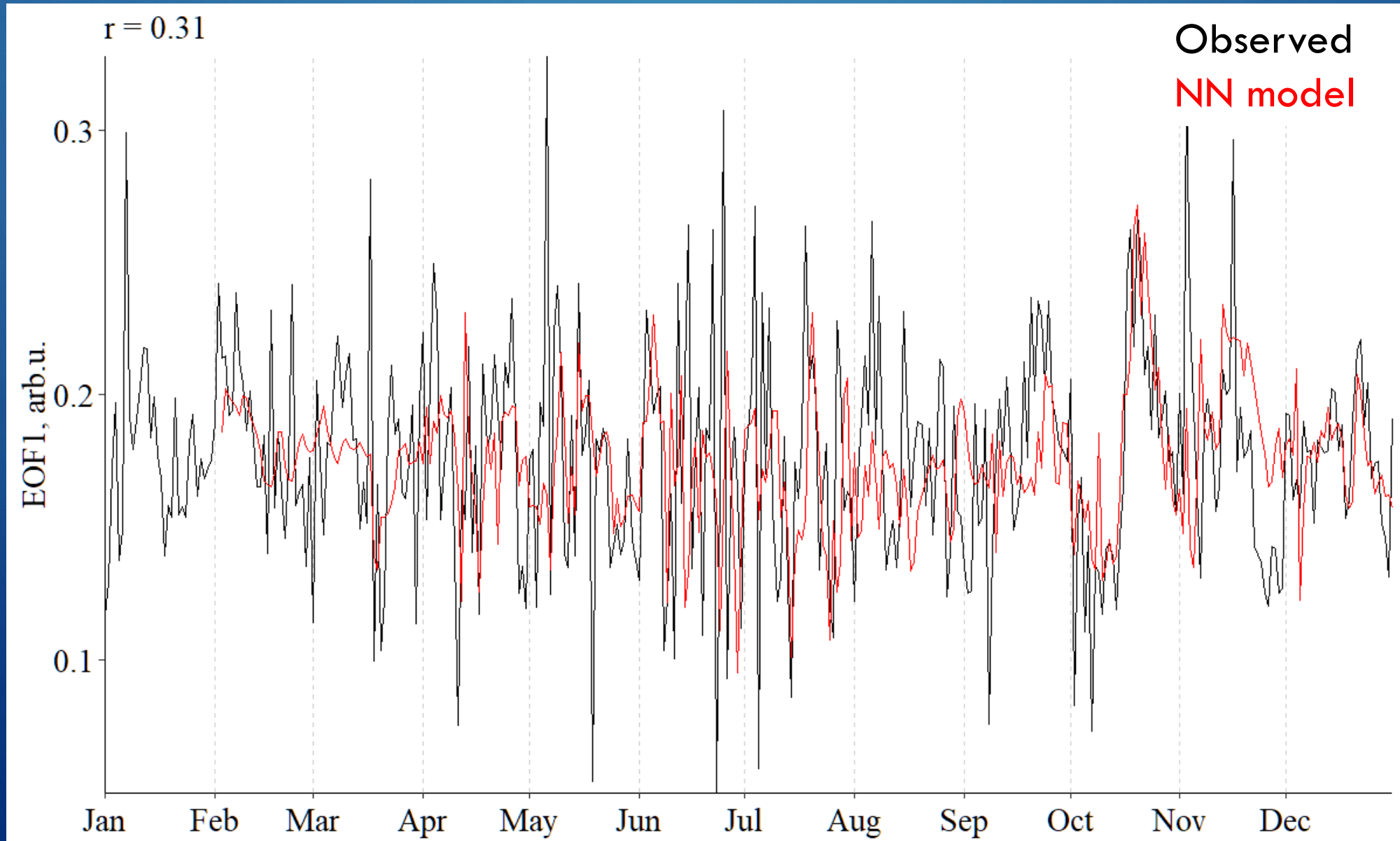
Better skills



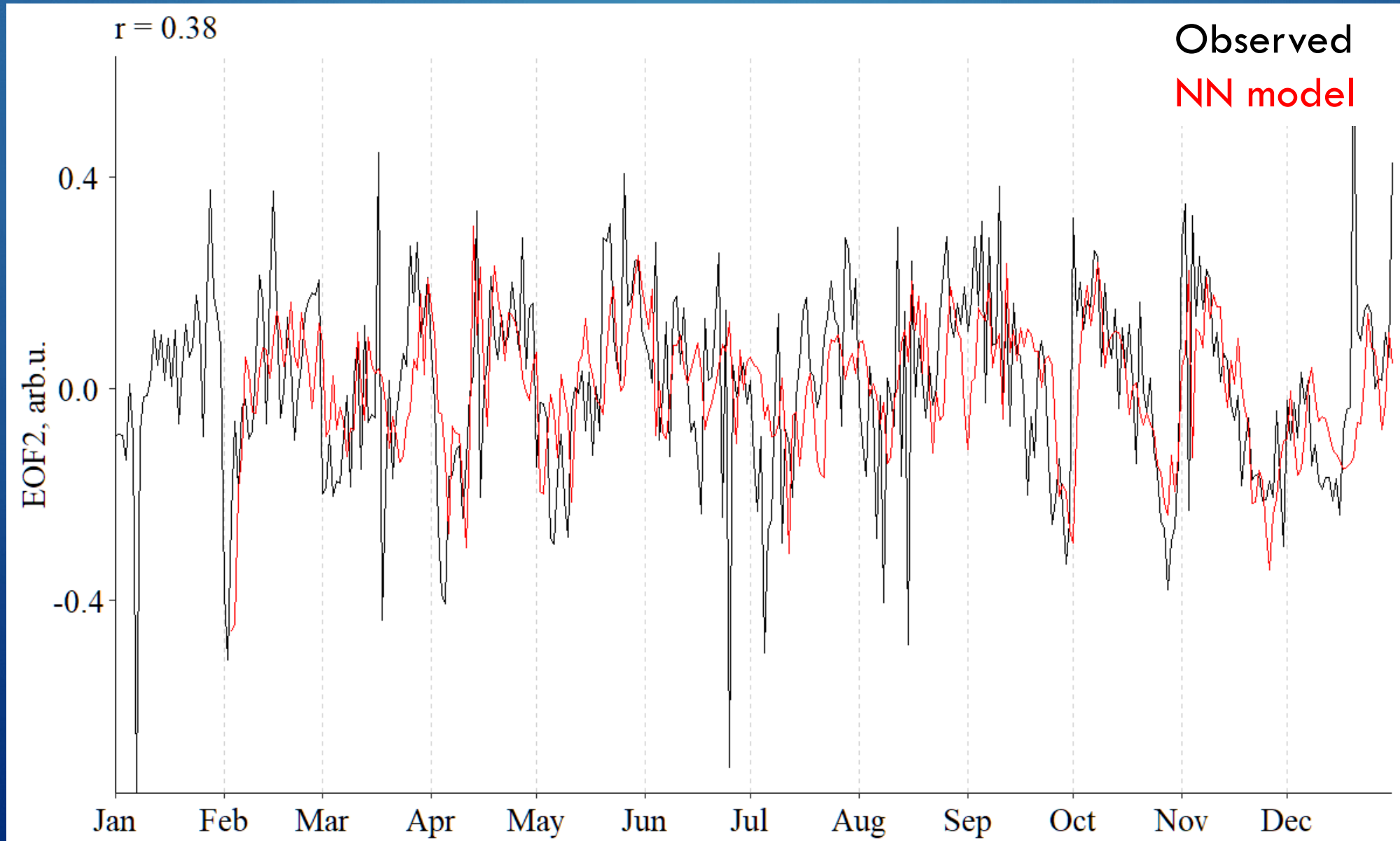
COMPARISON OF PC-NN FORECASTS AND OBSERVATIONS: daily mean TEC: forecasted vs observed



COMPARISON OF PC-NN FORECASTS AND OBSERVATIONS: EOF1: forecasted vs observed



COMPARISON OF PC-NN FORECASTS AND OBSERVATIONS: EOF2: forecasted vs observed



PCA-NN MODEL: FINAL CONFIGURATION

- SW predictors:
 - Geomagnetic indices
 - Proxies of the solar UV & XR fluxes/number of the flares
 - Only for the daily mean TEC and EOF2 – auto-regressive component
 - Only for EOF2 – solar wind velocity
- NN with 2 or 3 layers
- The forecasting quality of NN for EOF1 and EOF2 is lower than for the daily mean TEC due to their higher day-to-day variability



BEST NN ARCHITECTURE AND BEST SETS OF SW PREDICTORS

	Daily mean TEC	EOF1	EOF2
NN (layers & nodes)	(14,7,3) (14,6,4) (14,4,2)	(6,4)	(10,8,4)
Predictors	7 predictors	3 predictors	5 predictors
Best predictors	MgII Dst N. C flares ap AE XR Daily mean TEC	AE MgII Dst	AE Dst F10.7 v EOF2
r	0.93	0.31	0.39
MAE/RMSE (TEC_U)	1.73/2.40	0.03/0.04	0.13/0.17



PERFORMANCE OF THE PCA-NN MODEL

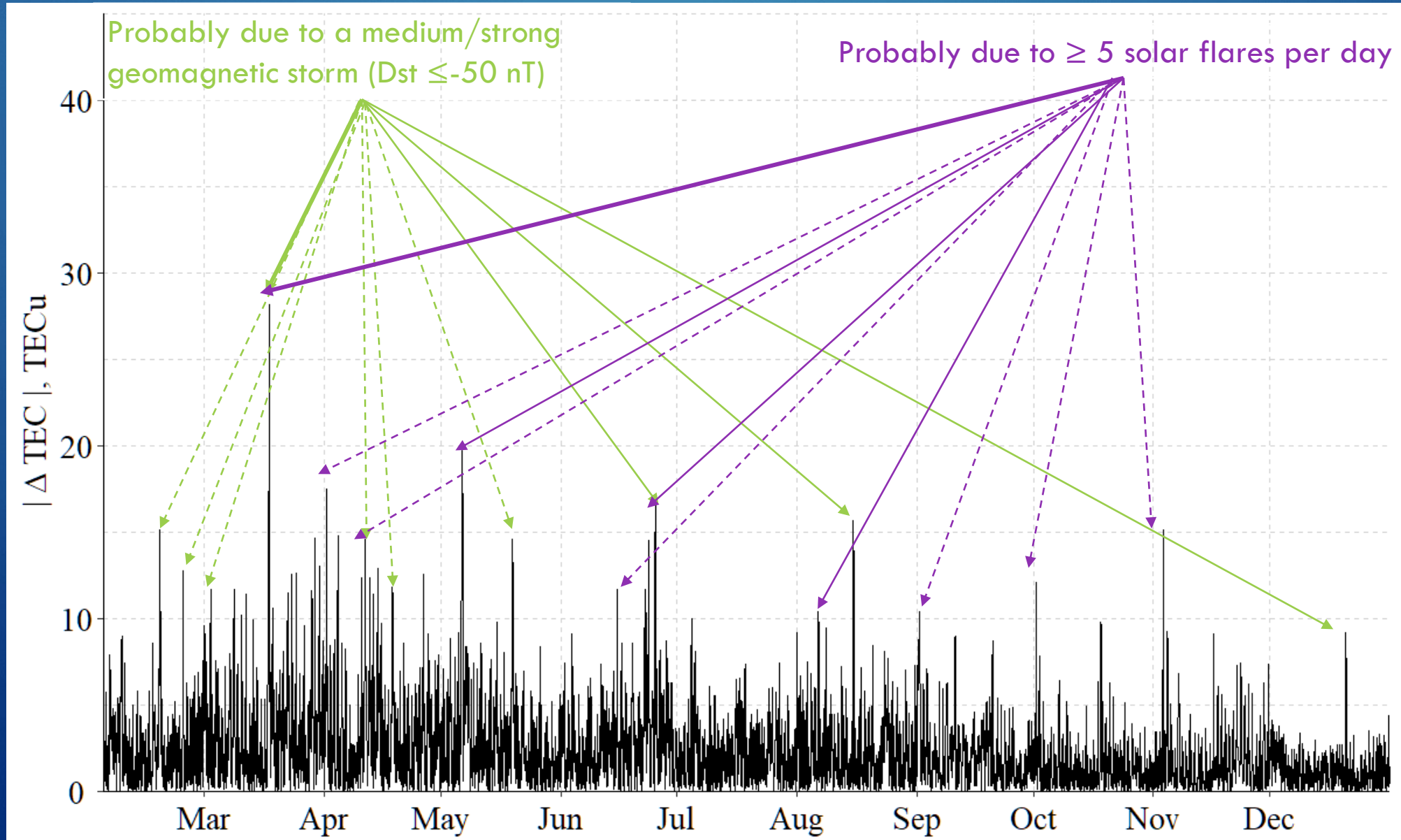


PCA-NN MODEL: FORECASTS FOR 1h TEC SERIES

- Forecast errors are higher during days of geomagnetic storms or days with high number of the solar flares



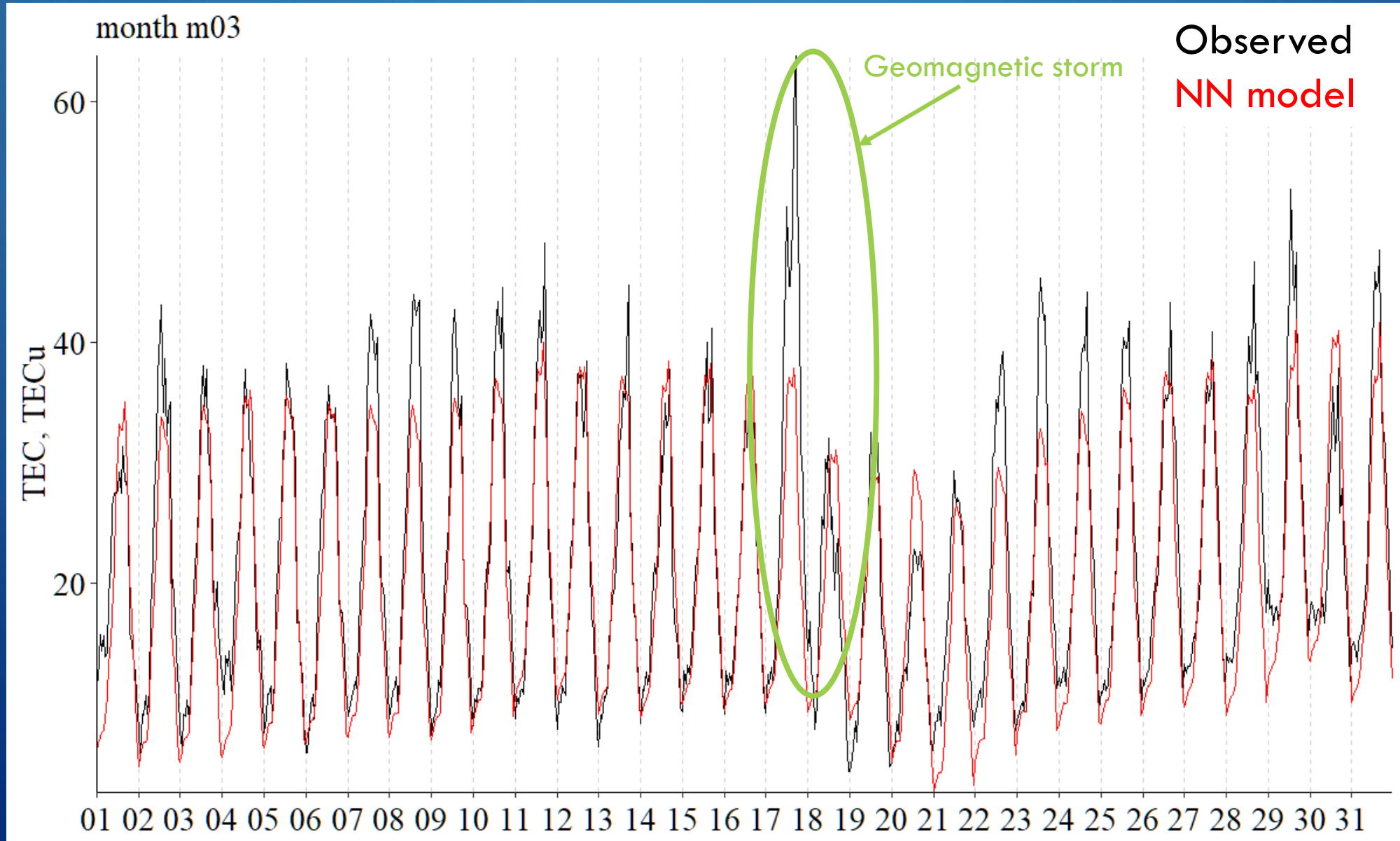
COMPARISON OF PC-NN FORECASTS AND OBSERVATIONS: 1h TEC: absolute errors



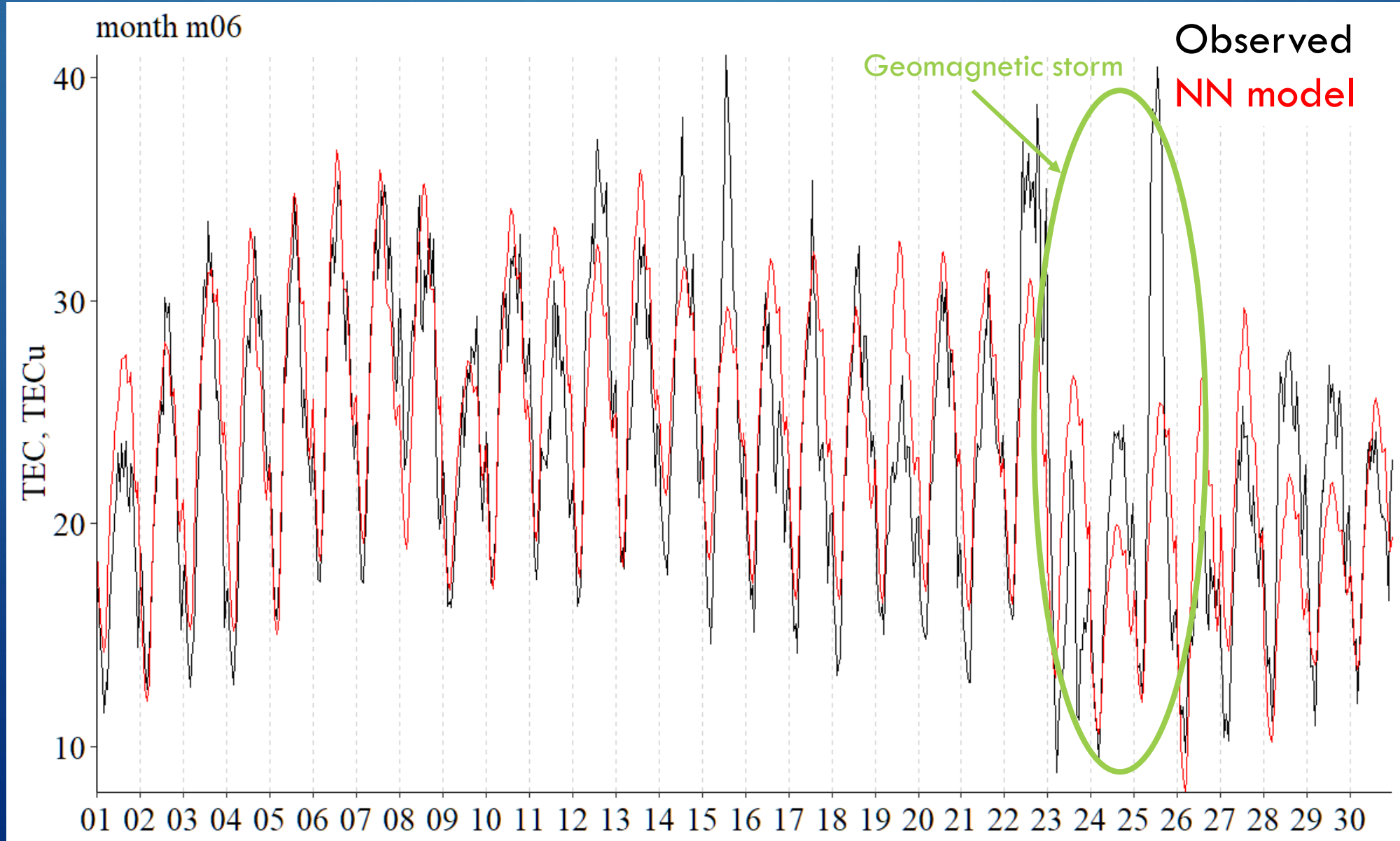
EXAMPLES FOR SOME MONTHS OF 2015



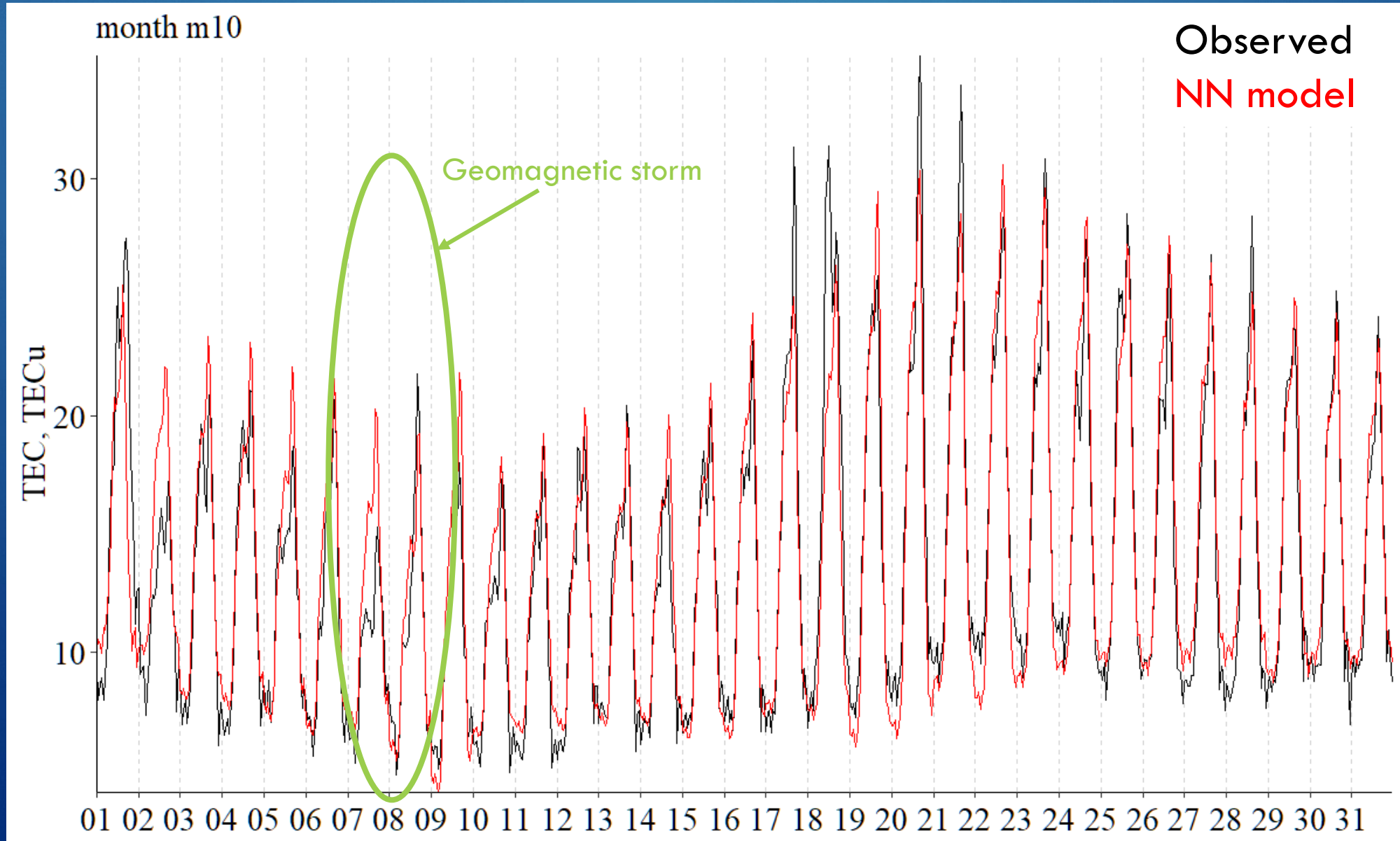
COMPARISON OF PC-NN FORECASTS AND OBSERVATIONS: 1h TEC, March 2015



COMPARISON OF PC-NN FORECASTS AND OBSERVATIONS: 1h TEC, June 2015



COMPARISON OF PC-NN FORECASTS AND OBSERVATIONS: 1h TEC, October 2015



COMPARISON OF TEC_{OBS} AND TEC_{REC}

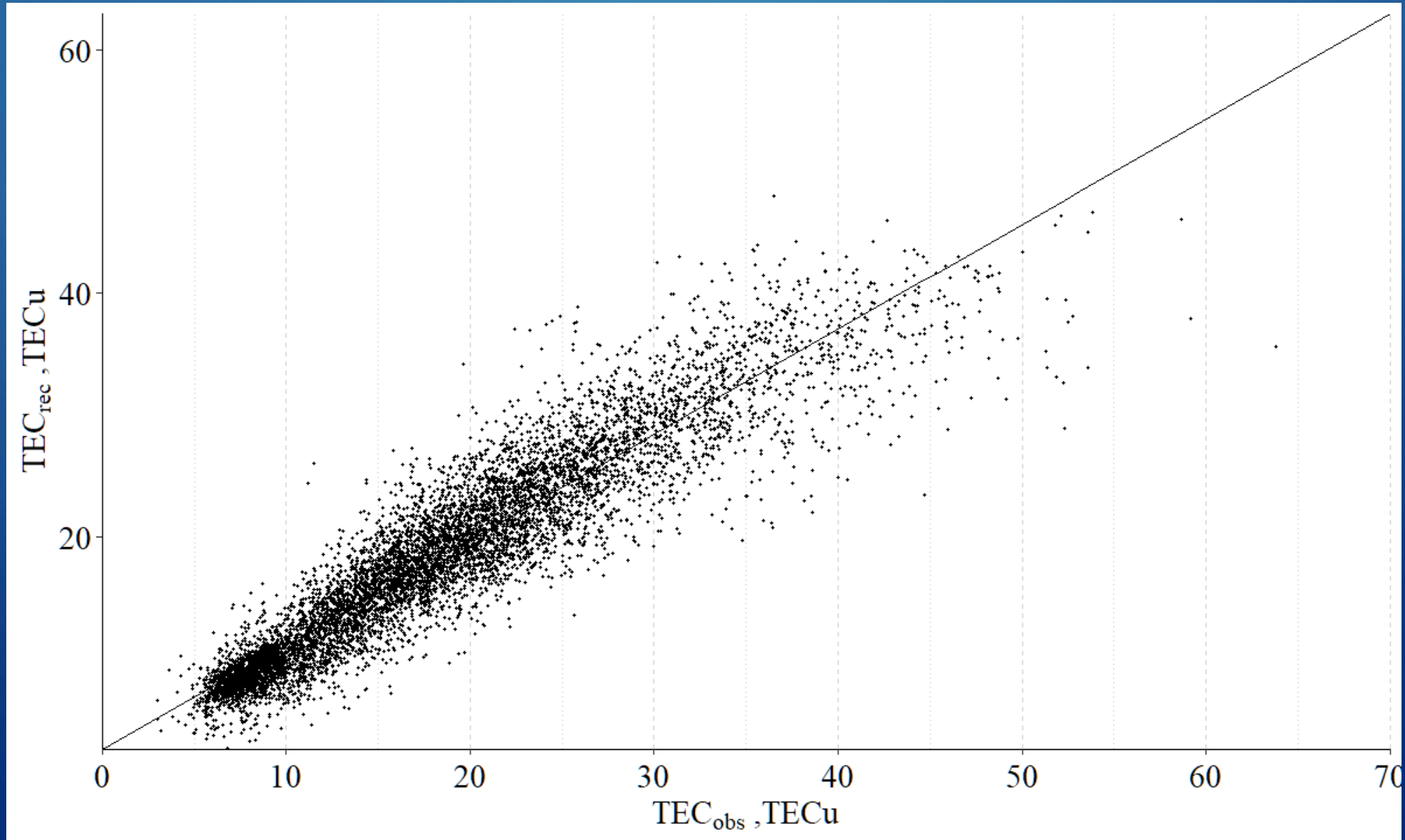


COMPARISON OF TEC_{OBS} AND TEC_{REC}

- Correlation between the observed (TEC_{obs}) and the forecasted (TEC_{rec}) series:
 - Daily mean TEC: $r = 0.93$
 - 1h TEC: $r = 0.93$
 - 1h TEC – daily mean TEC: $r = 0.94$
- PCA-NN forecasting skills:
 - MAE
 - Daily mean TEC: 1.7 TECu
 - 1h TEC: $r = 2.5$ TECu
 - 1h TEC – daily mean TEC: $r = 1.7$ TECu
 - RMSE
 - Daily mean TEC: 2.2 TECu
 - 1h TEC: $r = 3.45$ TECu
 - 1h TEC – daily mean TEC: $r = 2.4$ TECu
 - MaxE
 - Daily mean TEC: 9.5 TECu
 - 1h TEC: $r = 28.3$ TECu
 - 1h TEC – daily mean TEC: $r = 18.9$ TECu



COMPARISON OF PC-NN FORECASTS AND OBSERVATIONS: 1h TEC: reconstructed (forecasted) vs observed

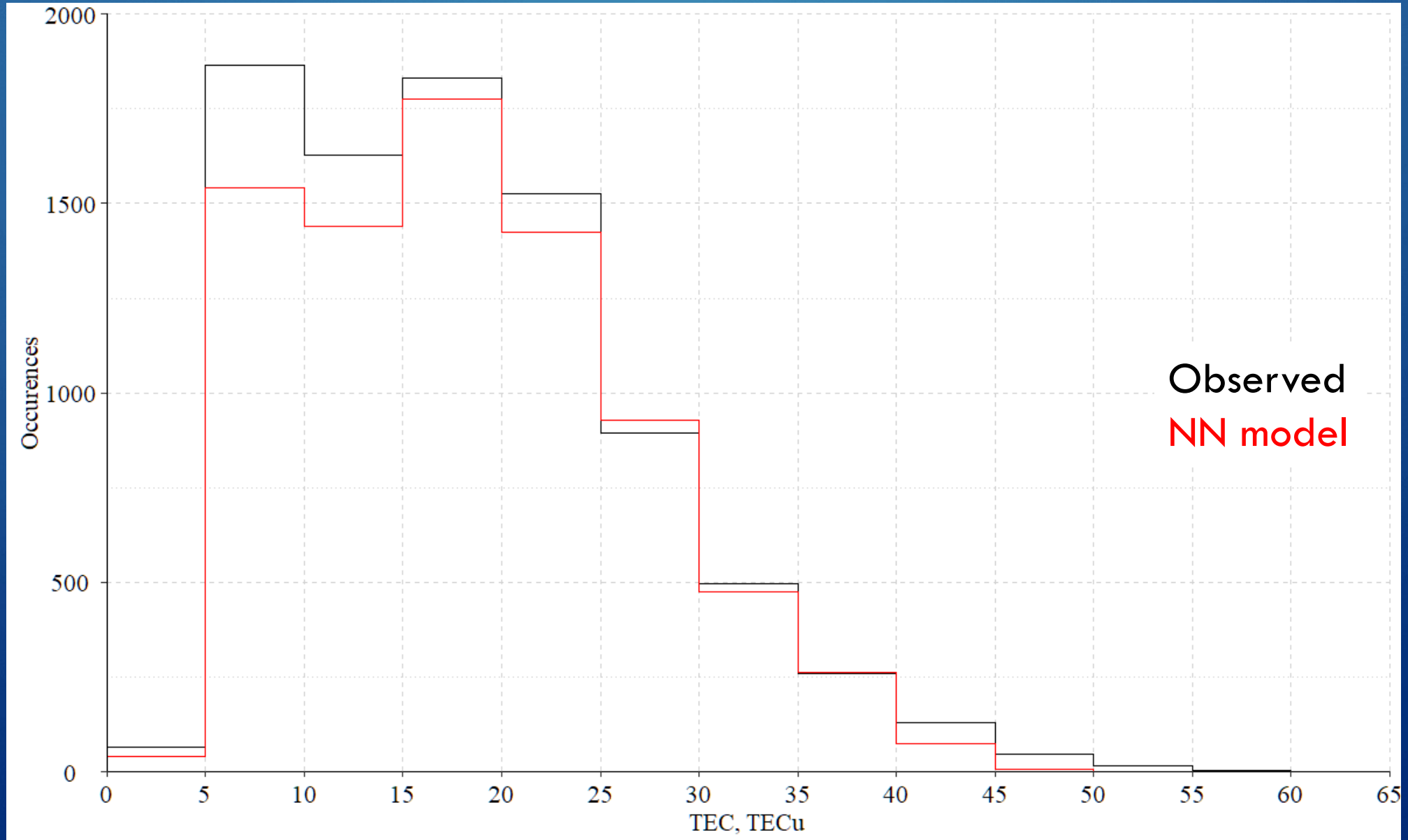


COMPARISON OF TEC_{OBS} AND TEC_{REC}

- Occurrences of certain TEC values are about the same for the observed and forecasted series
- In most cases the differences between TEC_{obs} and TEC_{rec} do not exceed 5 TECu, however:
 - For the nights & quiet days ($TEC \leq \sim 20$ TECu) the PCA-NN model over-estimates TEC by ~ 5 TECu more frequently than under-estimates TEC by ~ 5 TECu
 - For more disturbed days ($TEC > \sim 20$ TECu) the PCA-NN model under-estimates TEC by ~ 5 TECu more frequently than over-estimates TEC by ~ 5 TECu

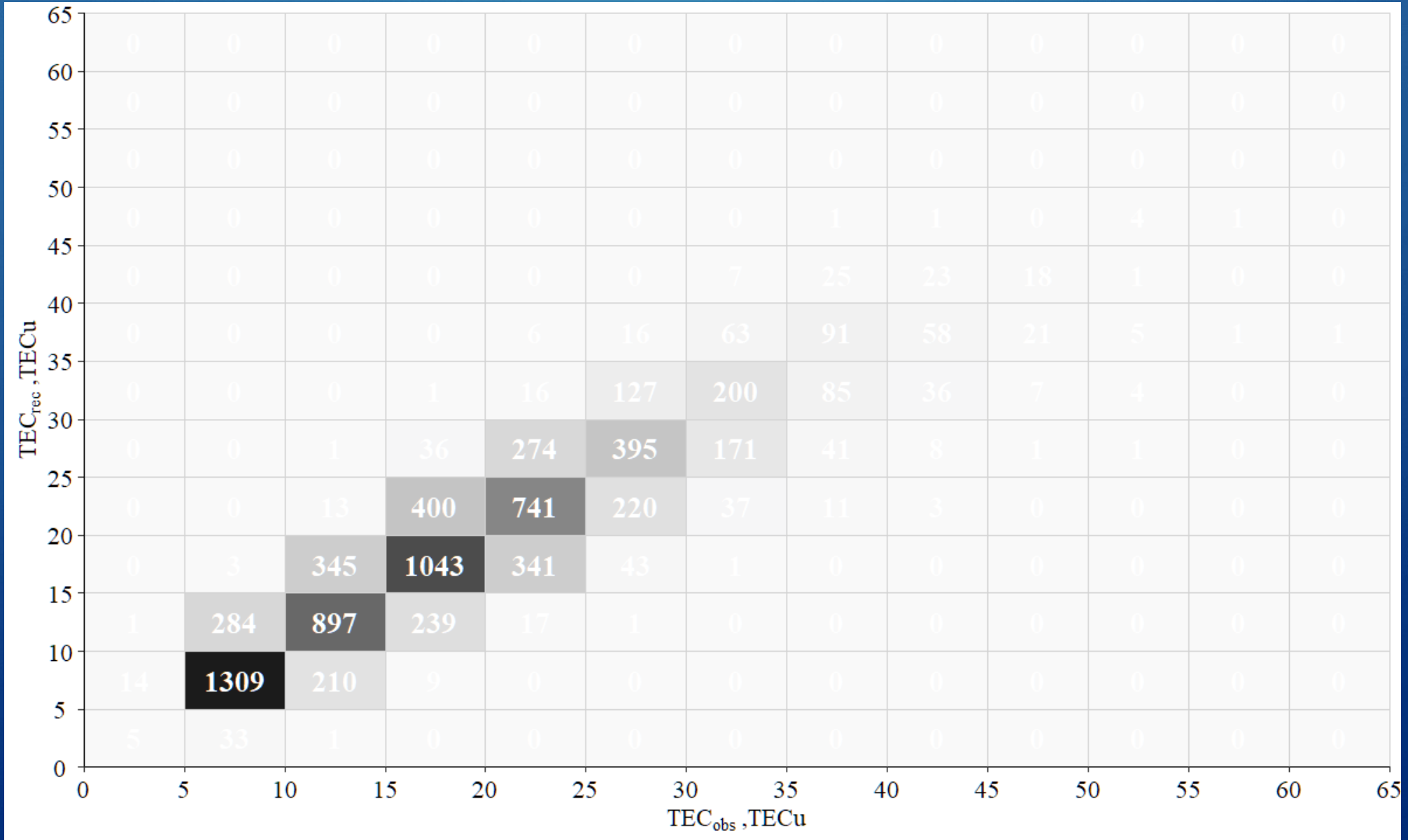


COMPARISON OF PC-NN FORECASTS AND OBSERVATIONS: 1h TEC: occurrences for the forecasted & observed values



COMPARISON OF PC-NN FORECASTS AND OBSERVATIONS:

1h TEC: occurrences for the forecasted vs observed values



CONCLUSIONS



- SW predictors
 - Best sets of SW predictors for PCA-NN models:
 - Daily mean TEC – 7 predictors (including daily mean TEC)
 - EOF1 – 3 predictors
 - EOF2 – 5 predictors (including EOF2)
 - Most important predictors:
 - Dst, AE, solar UV proxies – used for all TEC parameters
 - daily mean TEC & EOF1 \Leftrightarrow Mg II; EOF2 \Leftrightarrow F10.7
 - The use of correlated predictors may improve the prediction quality
 - Solar wind coupling functions do not improve NN forecasts
- NN with small number of layers perform better (only 2 or 3 layers for 6 to 14 input SW series)
- Highest errors are observed for days with strong geomagnetic storms ($Dst \leq -50$ nT) and/or many solar flares (≥ 5 per day)



ACKNOWLEDGEMENTS

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