



Universiteit Utrecht



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# **Characterizing** microstructures of Earth materials: **Reconstructing** higher-order correlation functions using deep generative adversarial networks (GANs)

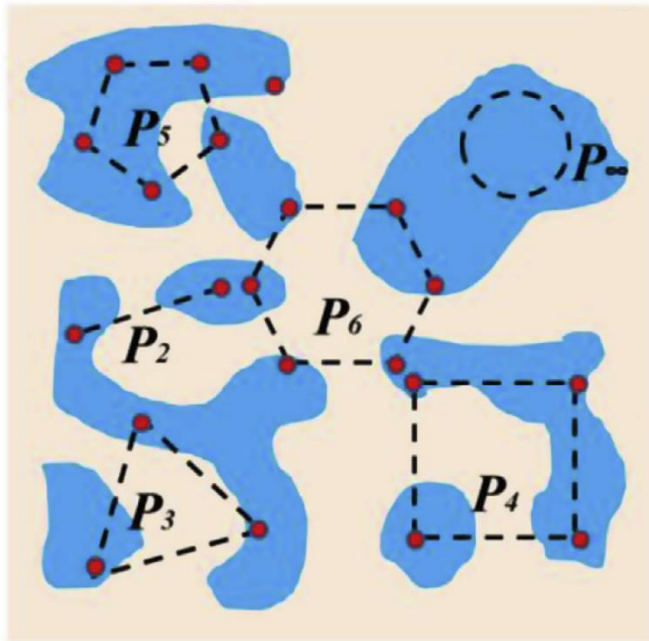
**Hamed Amiri**

Ivan Vasconcelos, Oliver Plümper , Yang Jiao

# Characterization

- ❖ Statistical representation of geomaterials using spatial correlation functions.

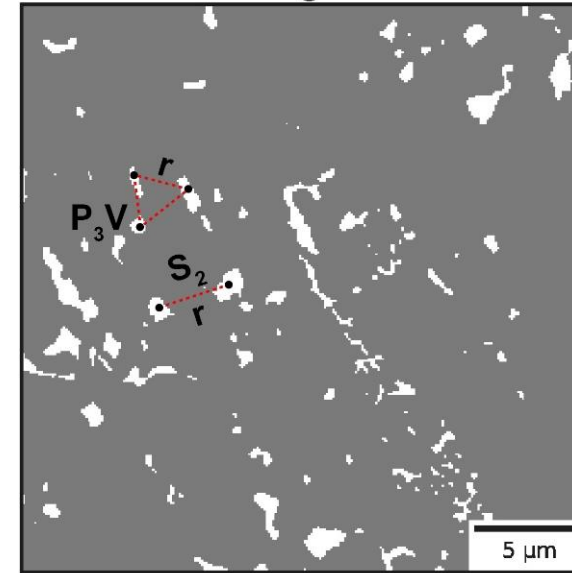
Statistical microstructure descriptors (SMDs)



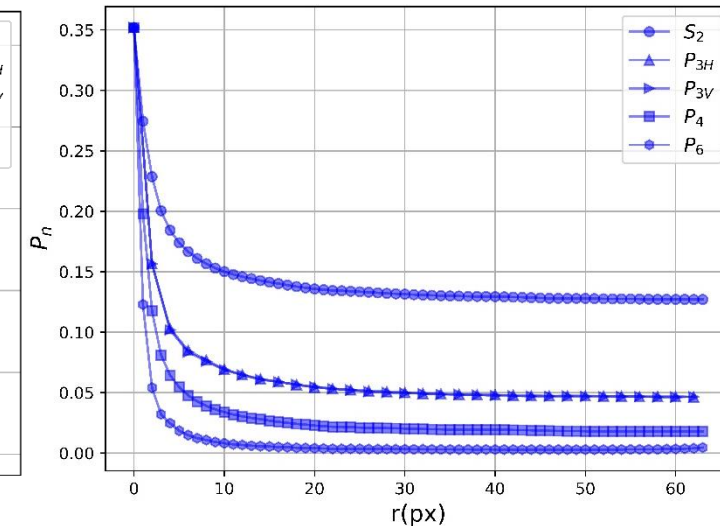
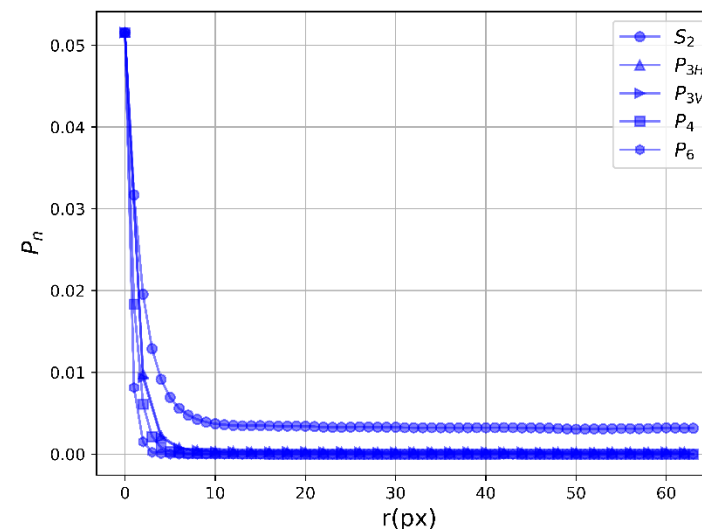
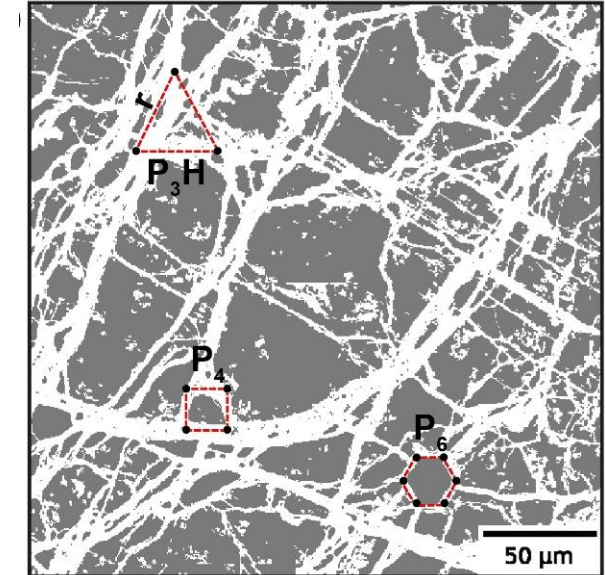
(Chen et al., 2019)

Probability of  $n$  random points of distance  $r$  to lie in the same phase of interest

Meta-igneous



Serpentinite

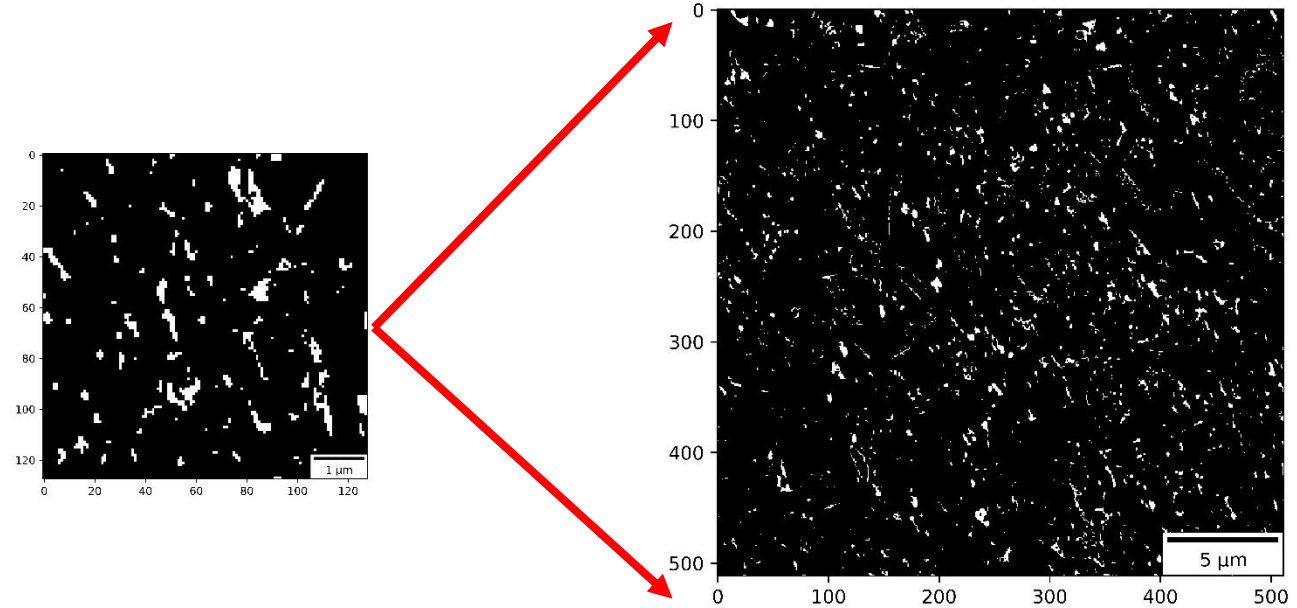


# Image reconstruction

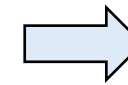
- ❖ **Image reconstruction** is the process of generating **statistically equivalent** microstructures but with **larger size** and/or **additional dimensions**.

## Why image reconstruction?

- ✓ Upsampling and upscaling.



✓ High-resolution  
✗ Small field of view



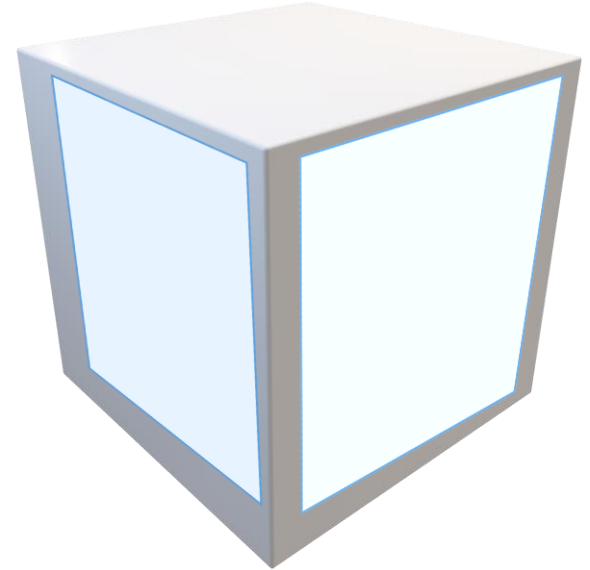
✓ High-resolution  
✓ Representative size

# Image reconstruction

❖ **Image reconstruction** is the process of generating **statistically equivalent** microstructures but with **larger size** and/or **additional dimensions**.

## Why image reconstruction?

- ✓ Upsampling and upscaling.
- ✓ 2D to 3D reconstruction



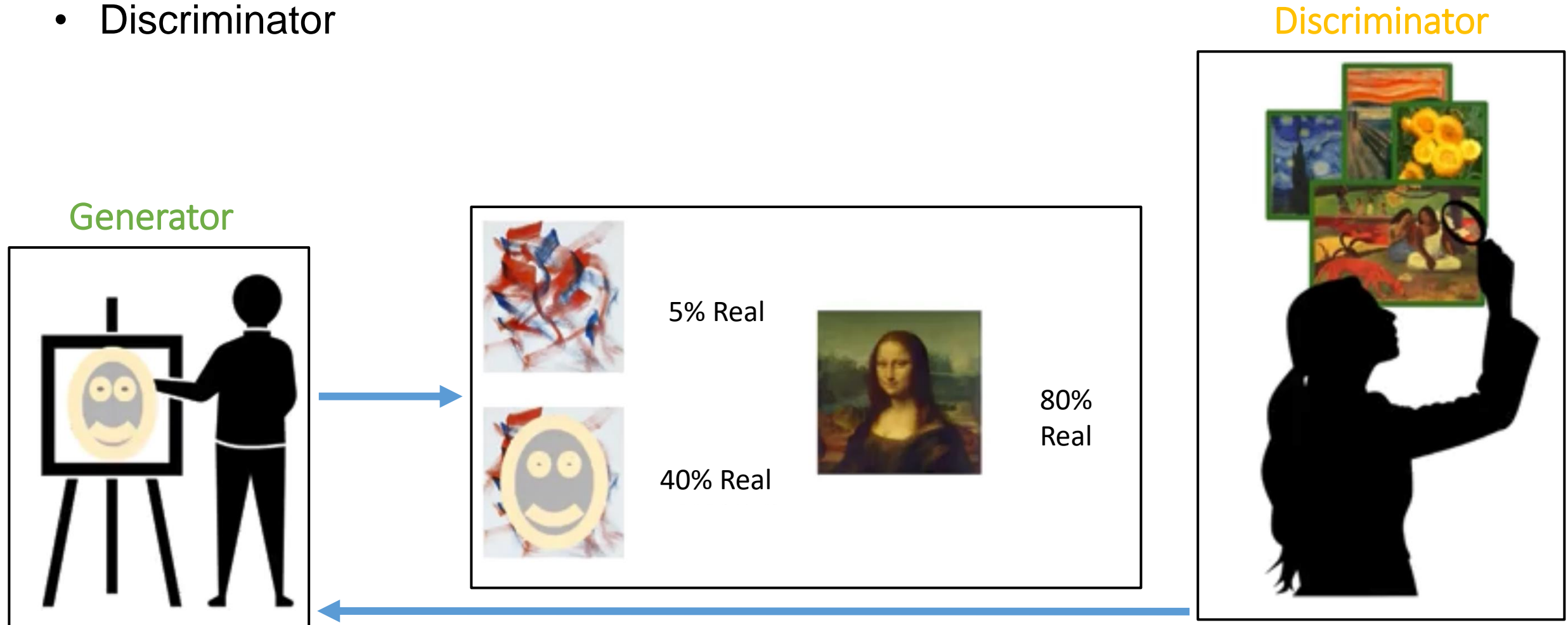
## Methods:

- ✓ Stochastic: two-point correlation + optimization method (simulated annealing).
- ✓ **Deep-learning based generative models:** Generative adversarial network (GAN).

# Generative adversarial network (GAN)

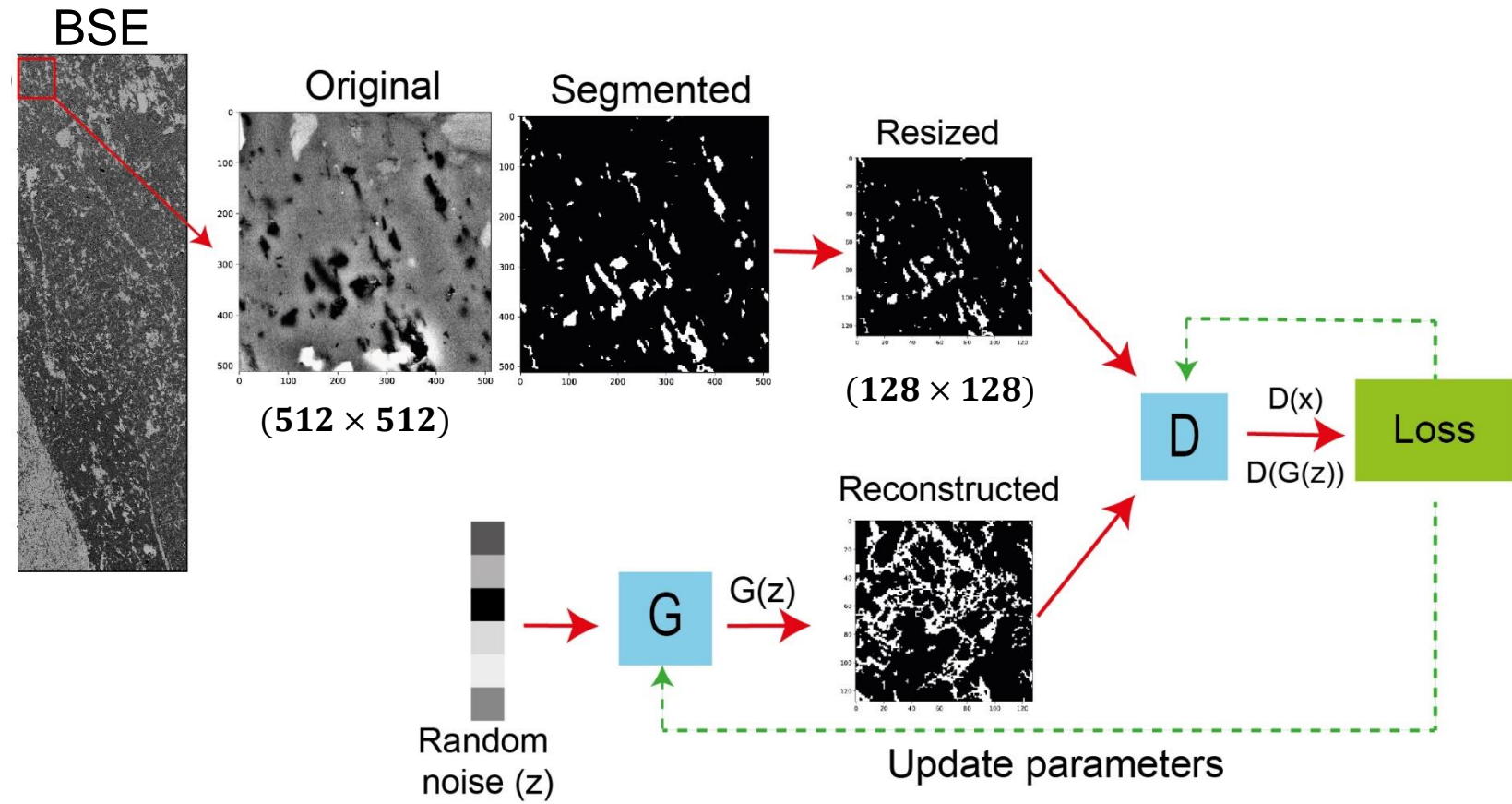
## ❖ 2 convolutional neural networks (CNN):

- Generator
- Discriminator





# Generative adversarial network (GAN)



Non-cooperative game (Minimax game)

Wasserstein loss with  
Gradient penalty (WGAN-GP):

$$\min_G \max_C E(c(x) - E(c(g(z))) + \underbrace{\lambda E(\|\nabla(c(\hat{x}))\|_2 - 1)^2}_{\text{Regularization term}})$$

(Gulrajani et al., 2017)

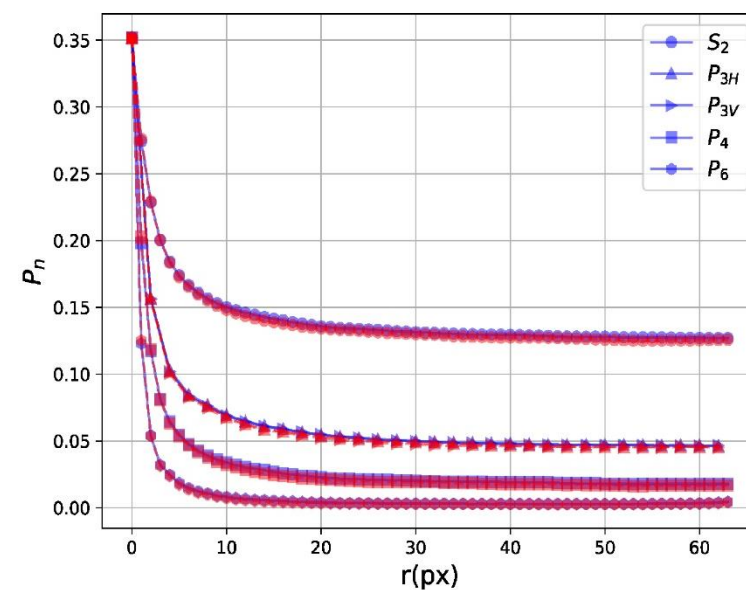
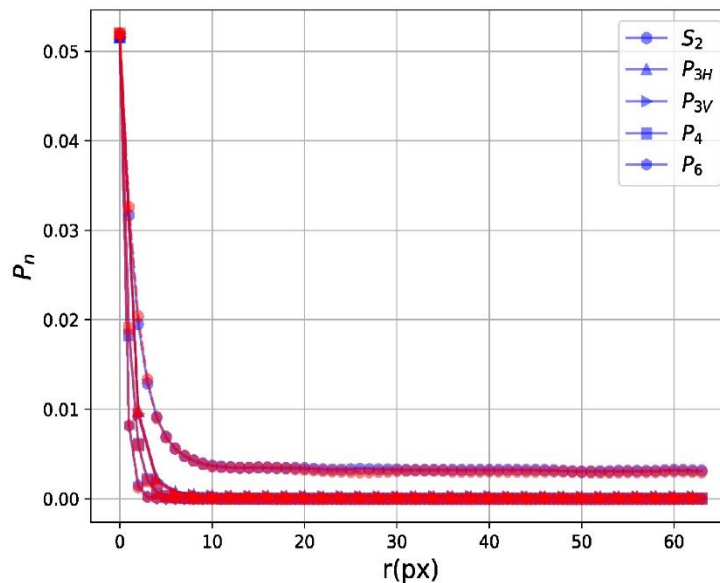
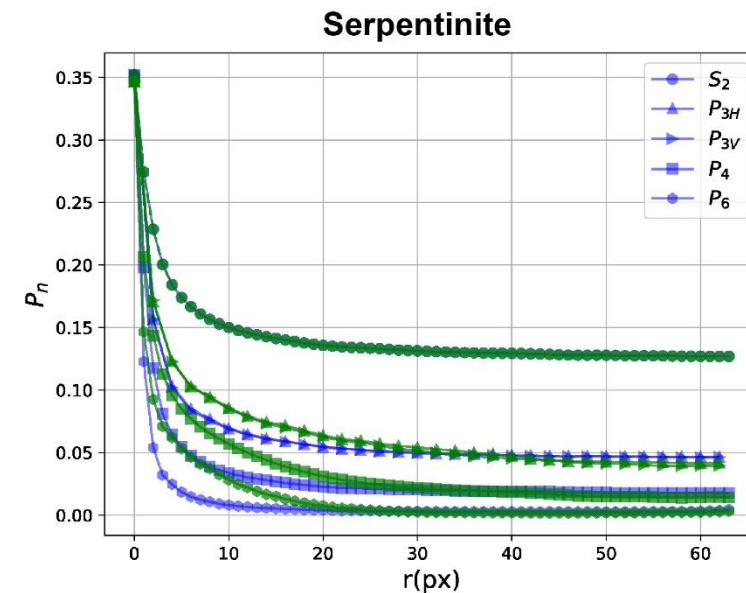
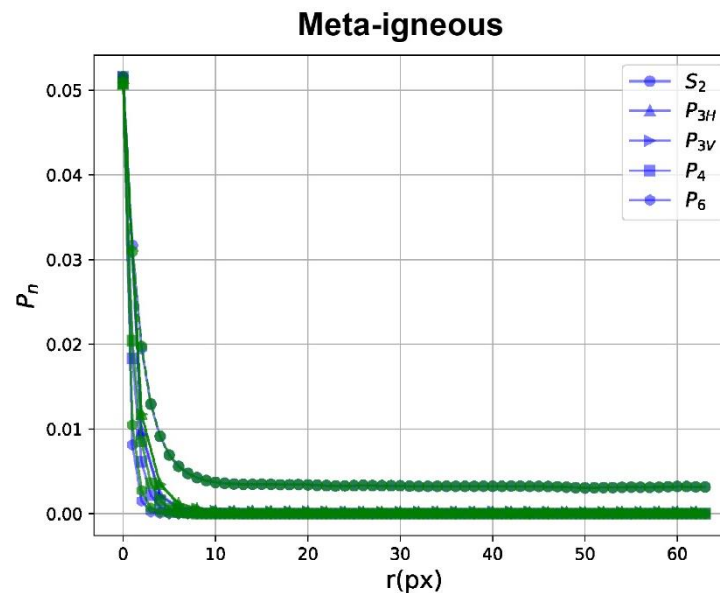
# WGAN-GP vs Stochastic

Stochastic reconstruction

$S_2$  + Simulated annealing

WGAN-GP

Trained with thousands of images



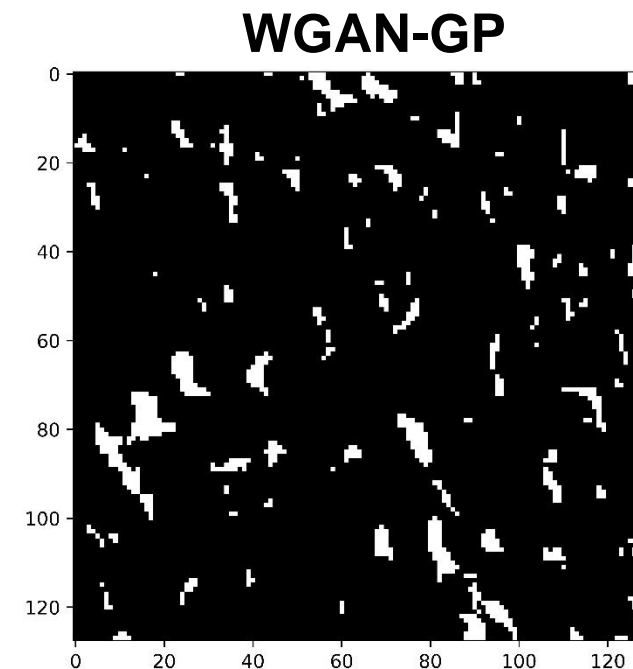
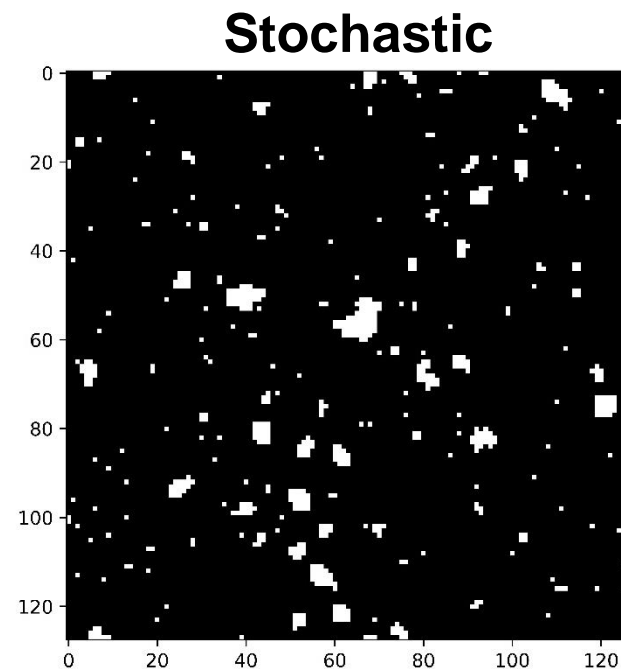
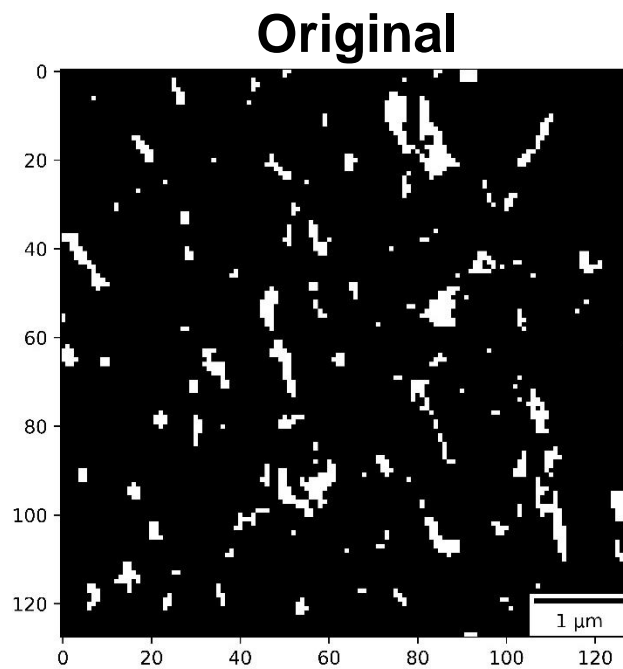
Blue: Original

Green: Stochastic

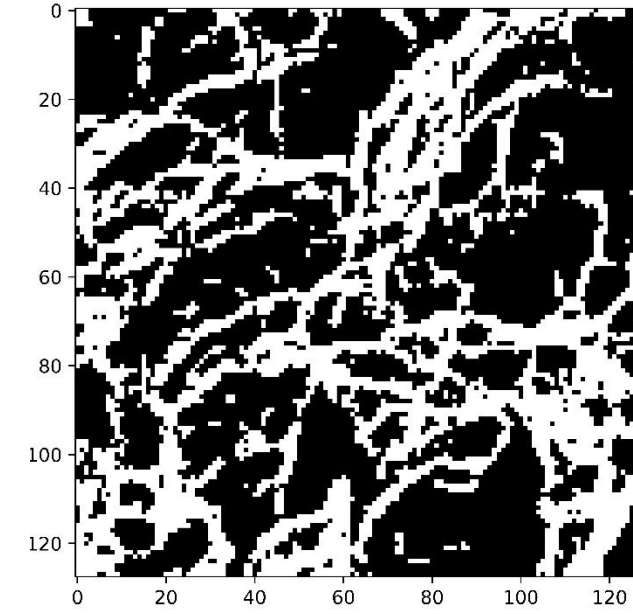
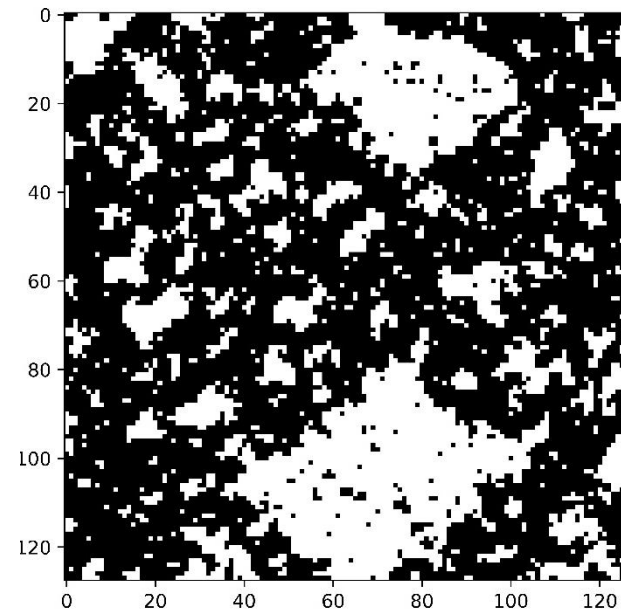
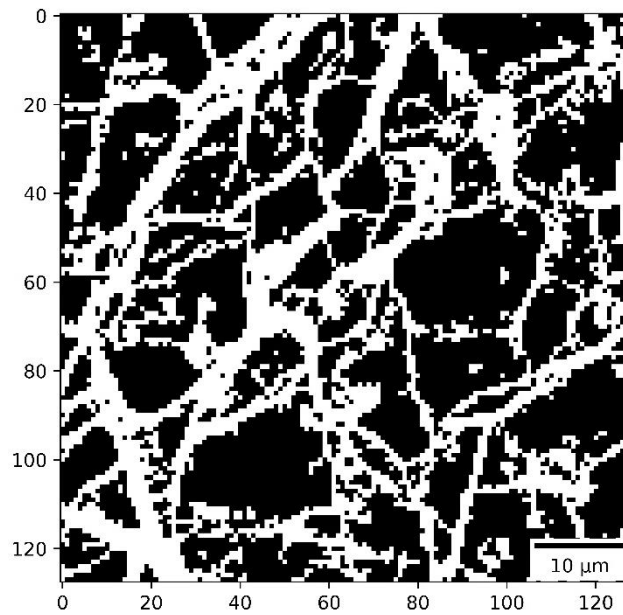
Red: Our WGAN-GP

# WGAN-GP vs Stochastic method

Meta-igneous  
Pore network



Serpentinite  
fracture network





# Conclusion

- ❖ Spatial correlations should be coupled with image reconstruction, especially in the case of **anisotropic heterogeneous** microstructures and when **transport modelling** is the next step!
- ❖ Github: <https://github.com/hamediat/GeoWGAN-GP>
- ❖ Images are freely accessible:  
<https://public.yoda.uu.nl/geo/UU01/ACSDR4.html>