





Mixing contributions from resonant trapped internal waves generated by bottom topography in an estuary

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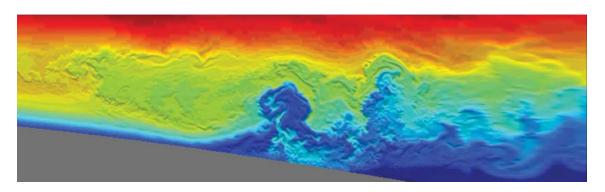
Session: NP7.1 | Extreme Internal Wave Events: Generation, Transformation, Breaking and Interaction with the Bottom Topography

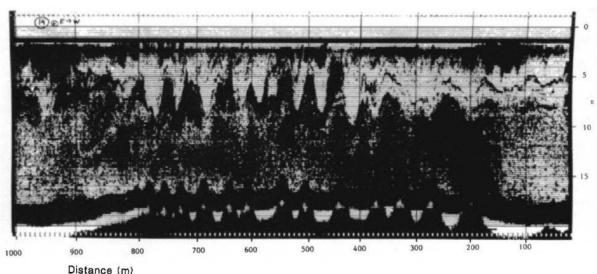


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Internal waves in estuaries







Upper image: Klymak, J., Legg, S., Alford, M., Buijsman, M., Pinkel, R., and Nash, J. (2012). The Direct Breaking of Internal Waves at Steep Topography. *Oceanography*, 25(2):150–159. Lower image: Pietrzak, J. D., Kranenburg, C. & Abraham, G. (1990). Resonant internal waves in fluid flow. *Nature, Springer Science and Business Media LLC, 344*, 844-847.

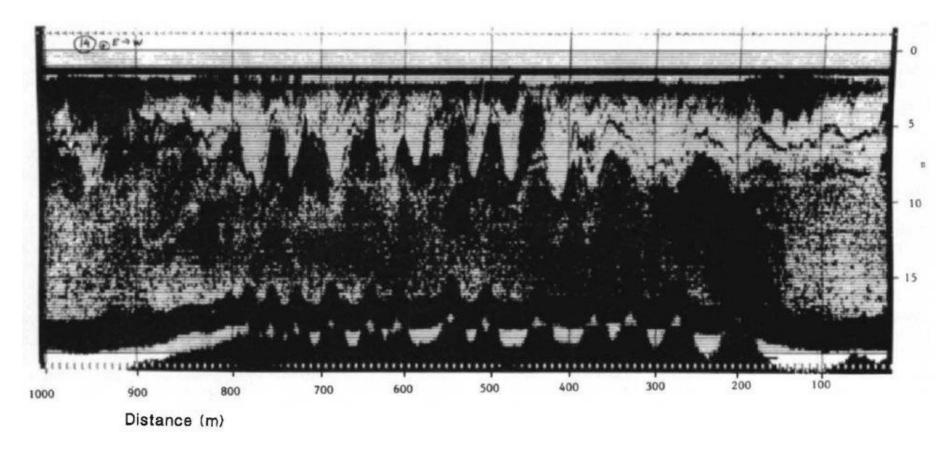
CONTEXT

Trapped internal waves in the Rotterdam Waterway





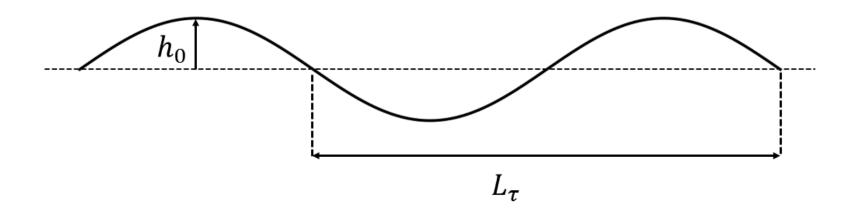
Trapped internal waves in the Rotterdam Waterway





CONTEXT

Analytical analysis

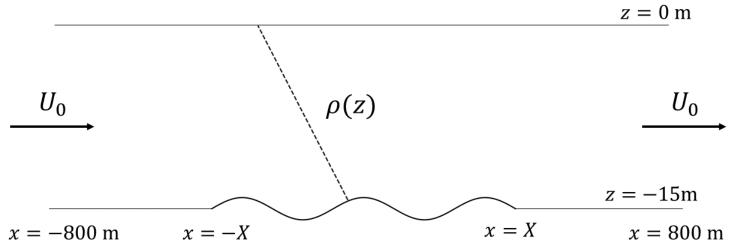


- Bottom topography amplitude $h_0 \rightarrow$ magnitude
- Bottom topography wave length $L_{\tau} \rightarrow$ magnitude and resonance condition



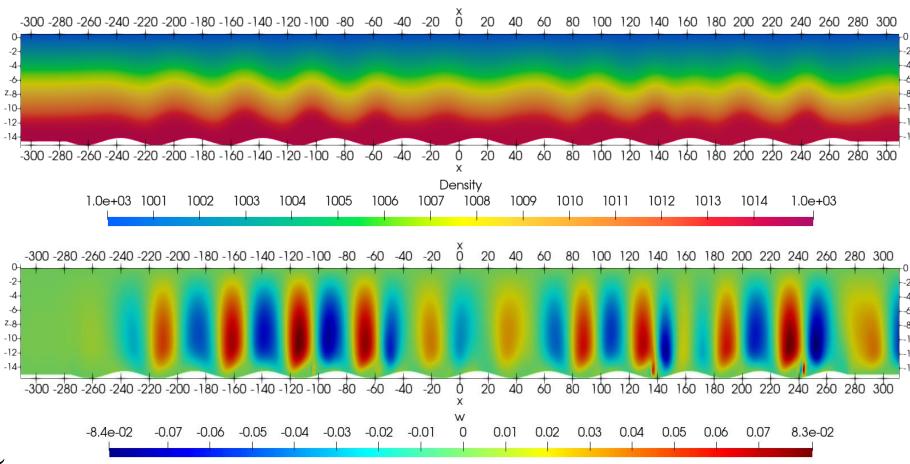
Set-up numerical simulation

- Fully non-hydrostatic finite element model (FINLAB¹)
- 2DV channel with a linearly stratified fluid
- Inflow & outflow boundary condition U_0 increases linearly in time



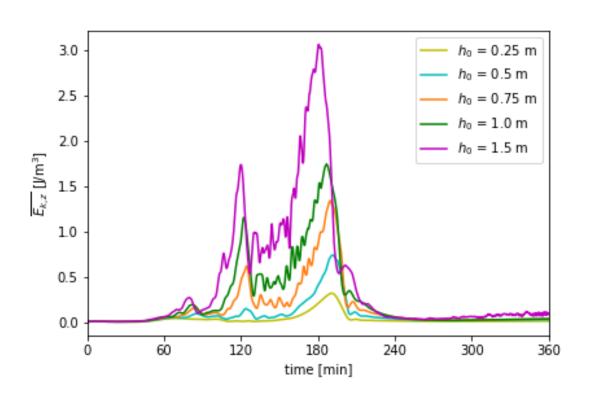


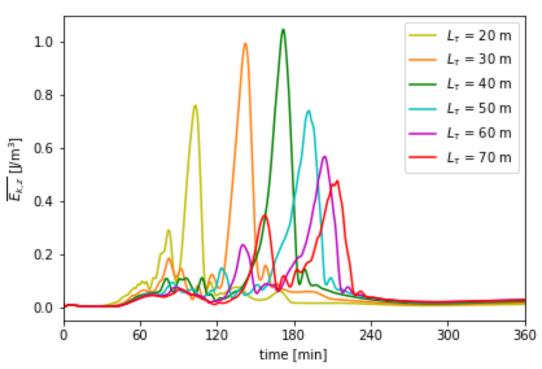
Mode 1 response





Variation in bottom topography parameters h_0 and $L_{ au}$



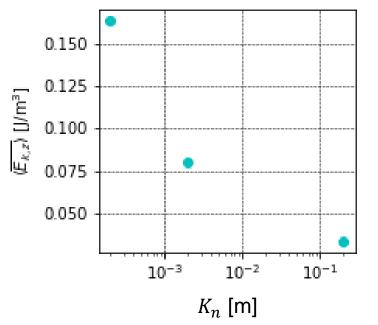


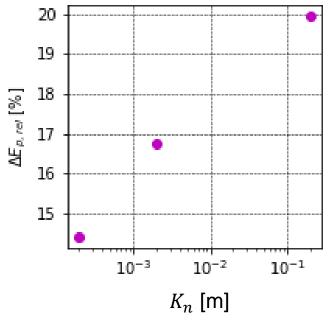


Mixing

Variations in Nikuradse bed roughness K_n

- $K_n \uparrow \rightarrow \text{friction } \uparrow$
- $K_n \uparrow \rightarrow \text{IW energy } \downarrow$
- $K_n \uparrow \rightarrow \Delta E_{p,rel} \uparrow$

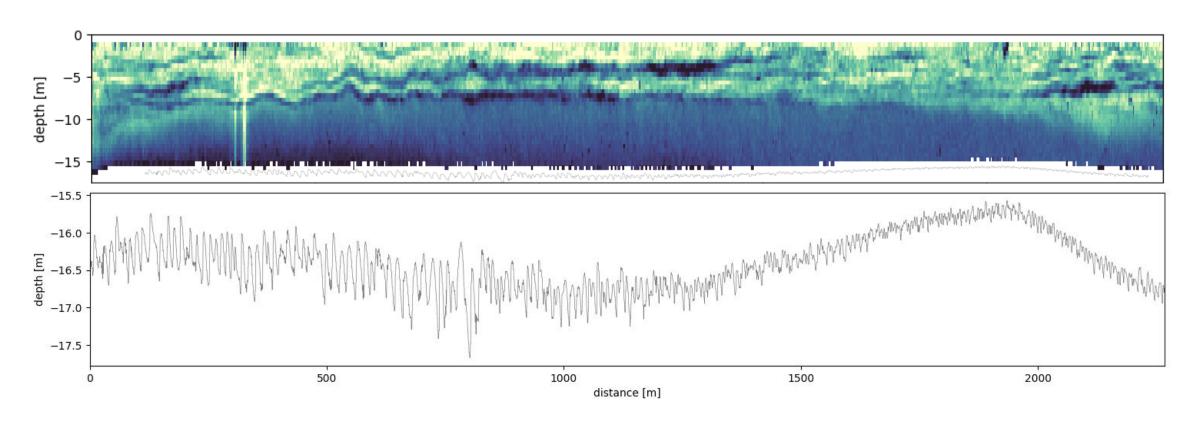


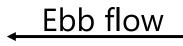


• Friction has more influence on $\Delta E_{p,rel}$ than internal wave energy



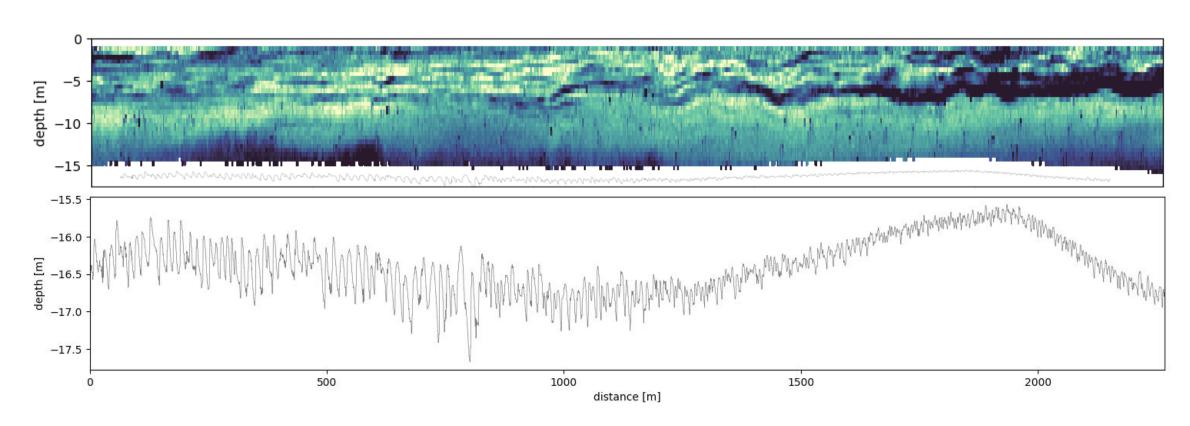
Measurements in the Rotterdam Waterway







Measurements in the Rotterdam Waterway







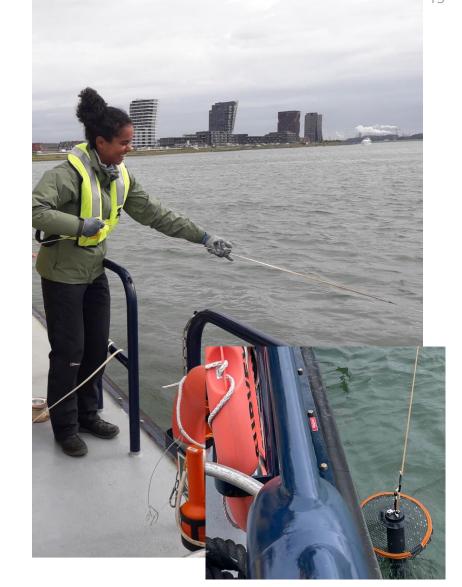
Conclusions

- For an accelerating flow case:
 - General response well described by analytical analysis;
 - Internal waves have a strong role near the bed due to bed friction;
- Estuarine internal waves observed in region with undular bottom topography.



Future work

- Model case with decelerating flow;
- Mixing contributions from propagating and/or breaking IWs;
- Analysis outside generation area;
- Comparison to field surveys of IWs and turbulent dissipation.











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