



Scalewise Universal Relaxation to Isotropy of Inhomogeneous Atmospheric Boundary Layer Turbulence

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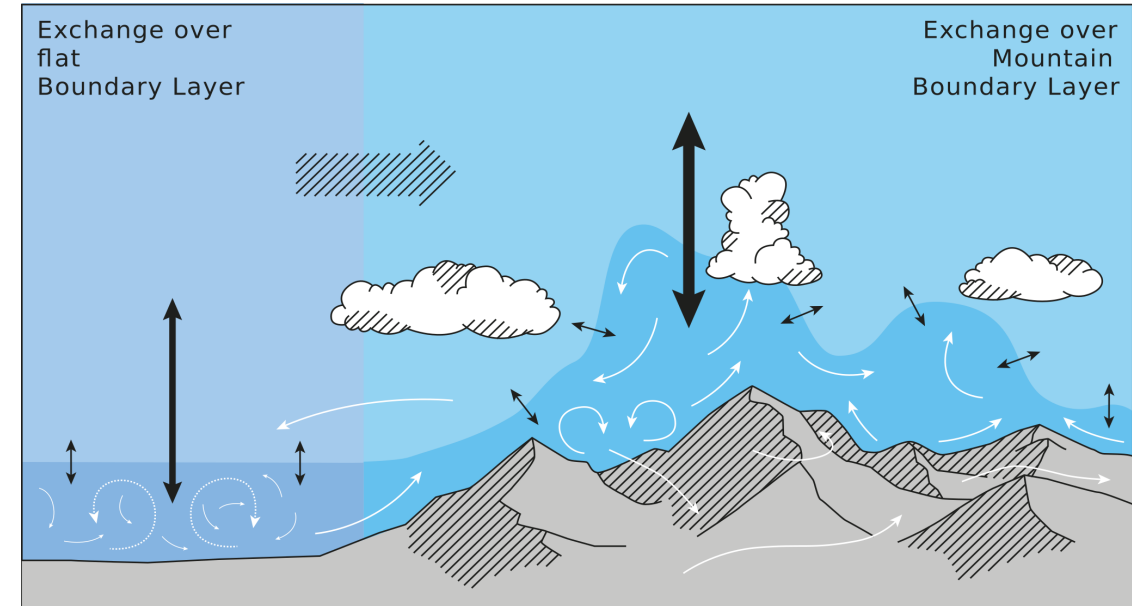
Motivation

Atmospheric turbulence:

- $Re \sim 10^9$
- wide inertial subrange (several decades)
- Tendency towards isotropy

Production scales of turbulence are anisotropic:

- Buoyancy
- Shear
- Terrain-induced pressure perturbations
- Streamline curvature
- Additional length scales (LLJ)



What is the effect of terrain and flow complexity on turbulence cascade?

Data from 20 turbulence towers: flat - mountain top

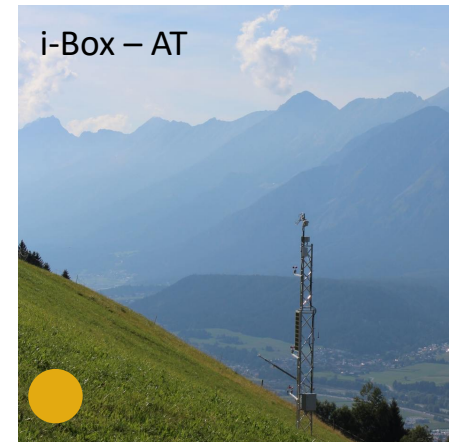
AHATS – CA



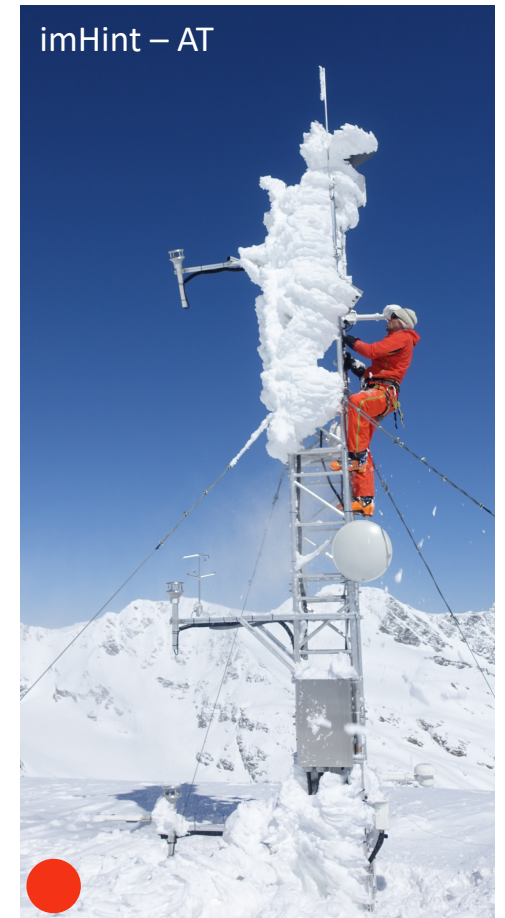
T-Rex – CA



i-Box – AT



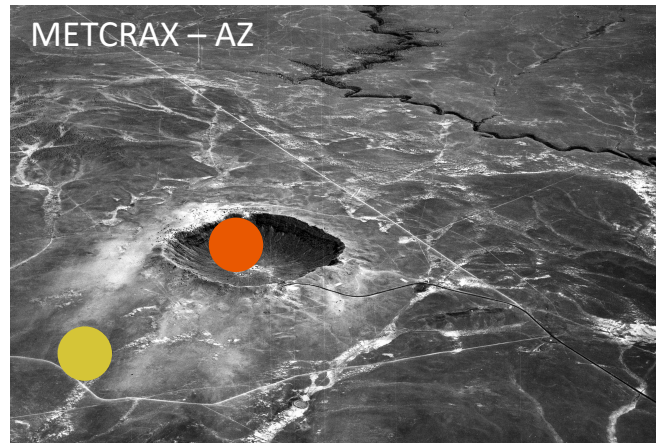
imHint – AT



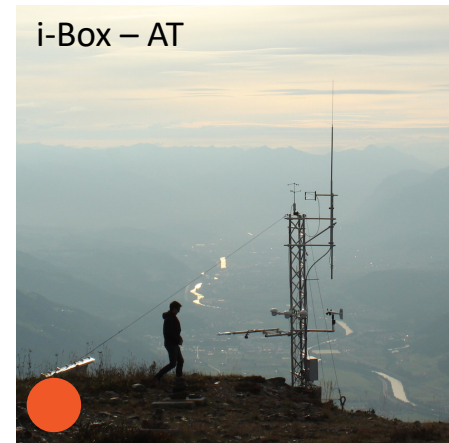
Cabauw – NL



METCRAX – AZ



i-Box – AT



AHATS
CASES-99

Cabauw
IPAQs

T-RexC
i-Box0

i-Box1
FAR

NEAR
RIM

T-RexW
FLR

i-Box10
i-Box27

SSW2
SSW4

i-BoxTop
ImHint

Determining scalewise anisotropy

- Wavelet decomposition of Reynolds stress tensor

- At each scale:

→ Invariant analysis of the anisotropy tensor
(Lumley & Newmann 1977, Banerjee et al. 2007)

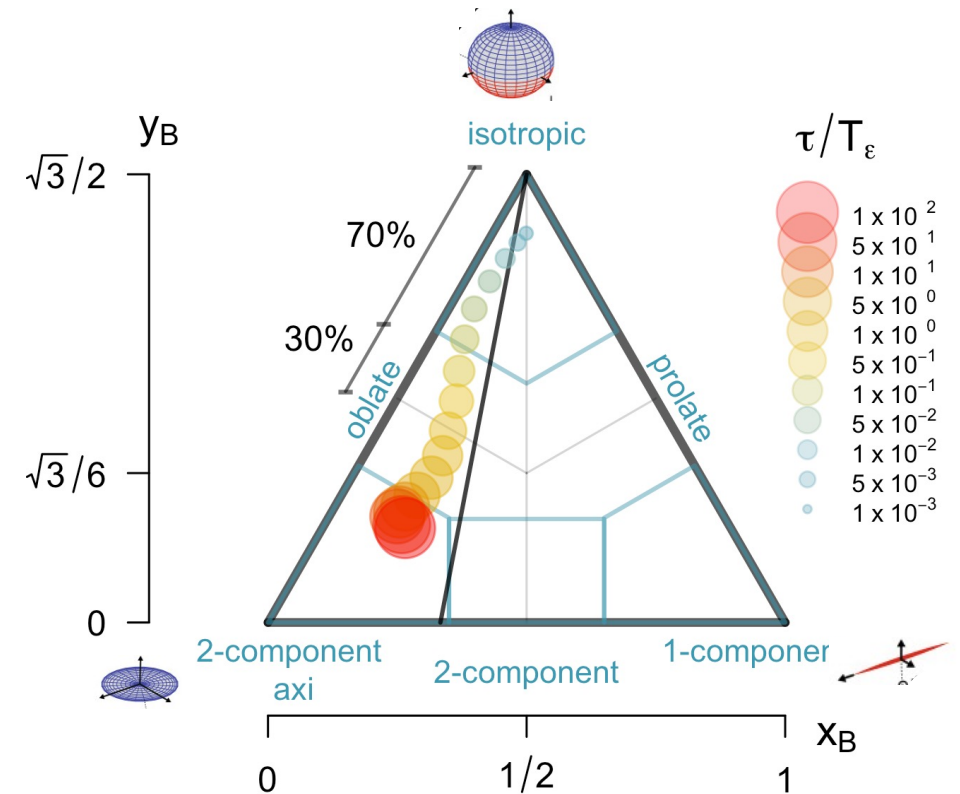
$$x_B = \lambda_1 - \lambda_2 + \frac{1}{2}(3\lambda_3 + 1)$$

$$y_B = \frac{\sqrt{3}}{2}(3\lambda_3 + 1)$$

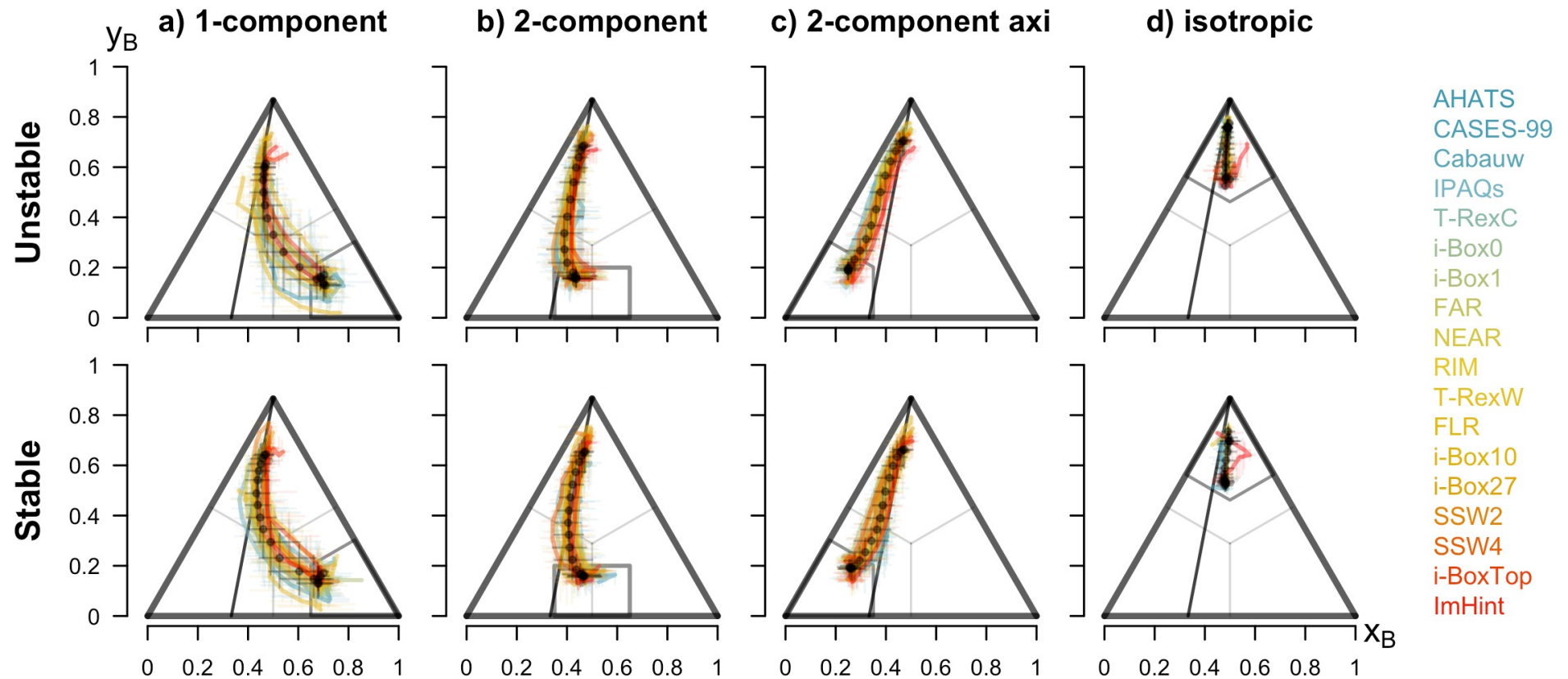
→ Cluster according to bulk anisotropy and stratification

→ Average trajectories for each dataset

→ Ensemble trajectories from all datasets

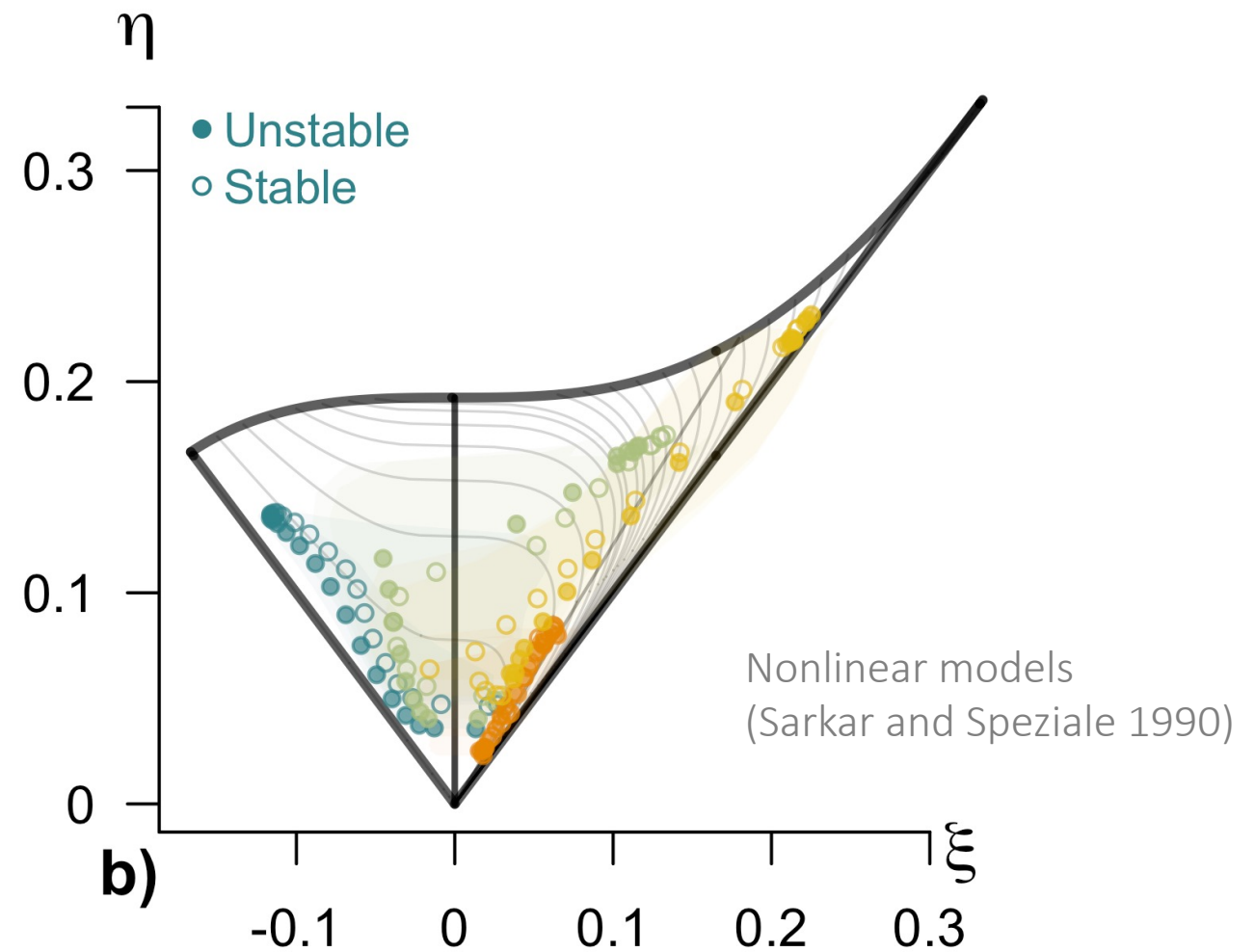
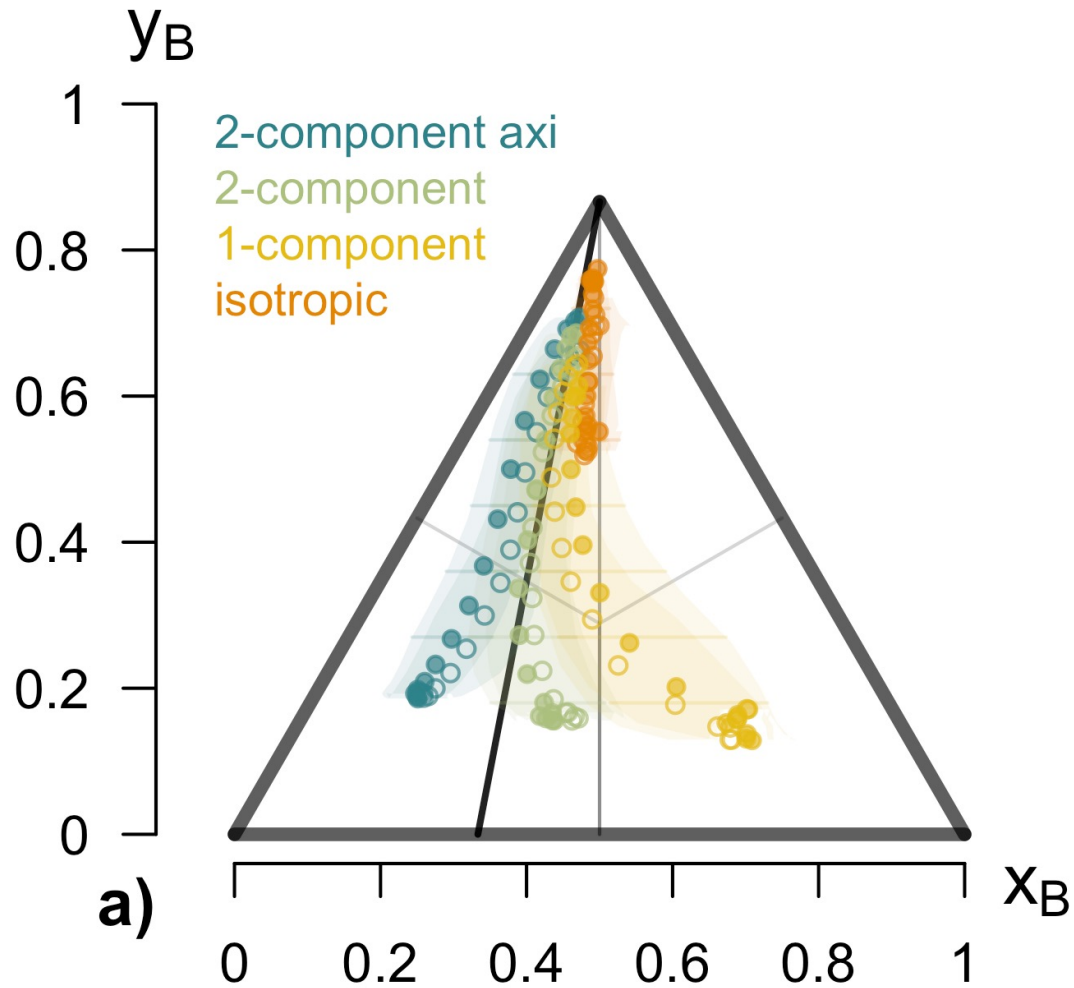


Relaxation to isotropy: does not depend on terrain complexity

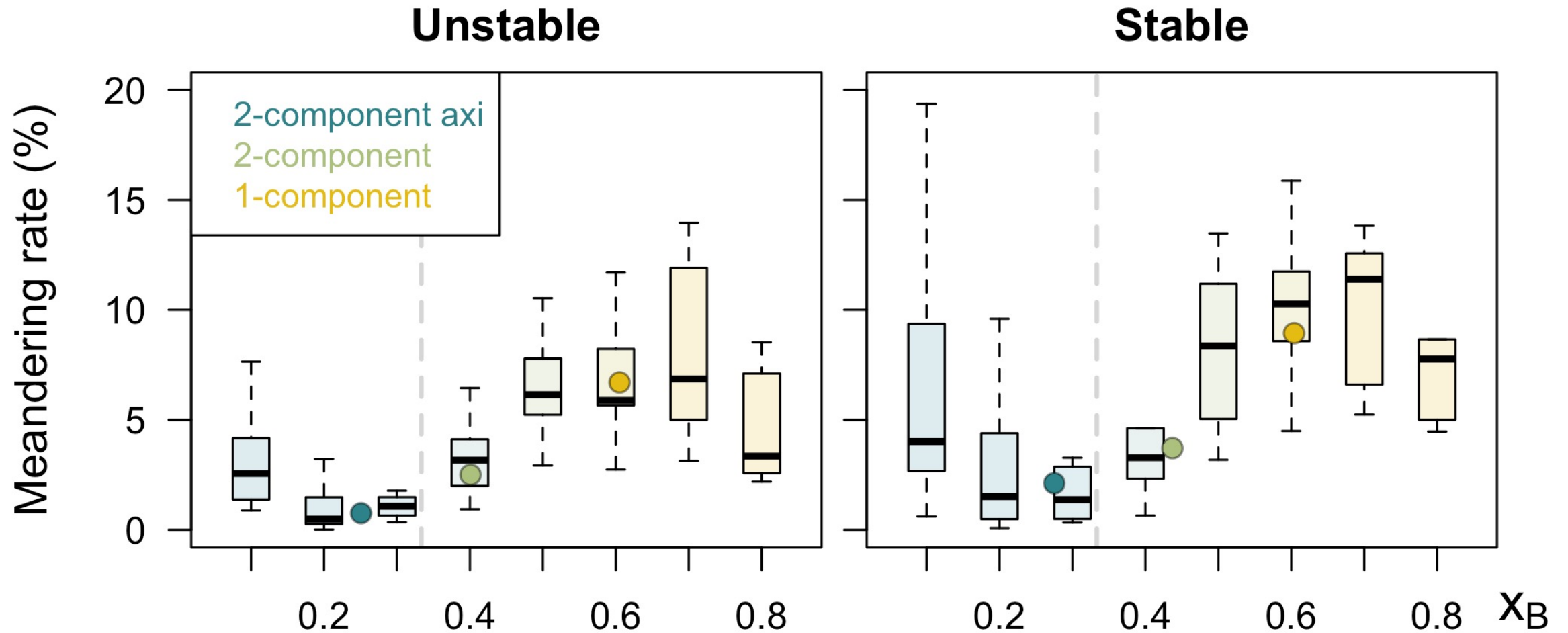


- Same shape of trajectories in each cluster
- Minimal variation between data sets

Relaxation to isotropy: weakly depends on stratification



Relaxation to isotropy: is non-linear



Relaxation to isotropy: speed depends on initial anisotropy

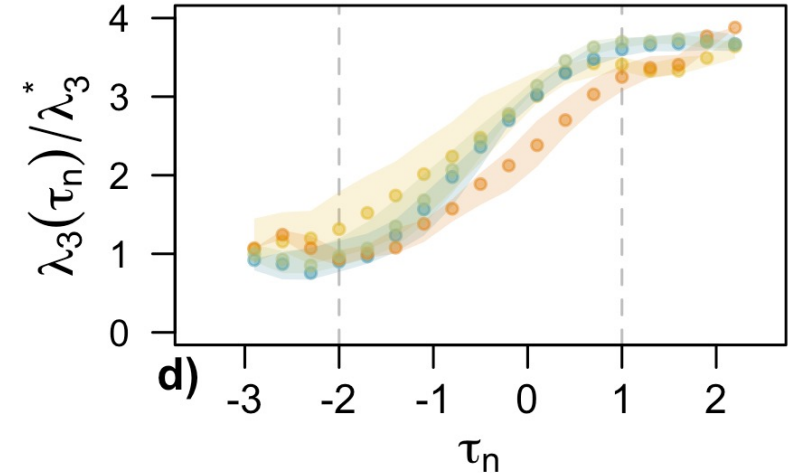
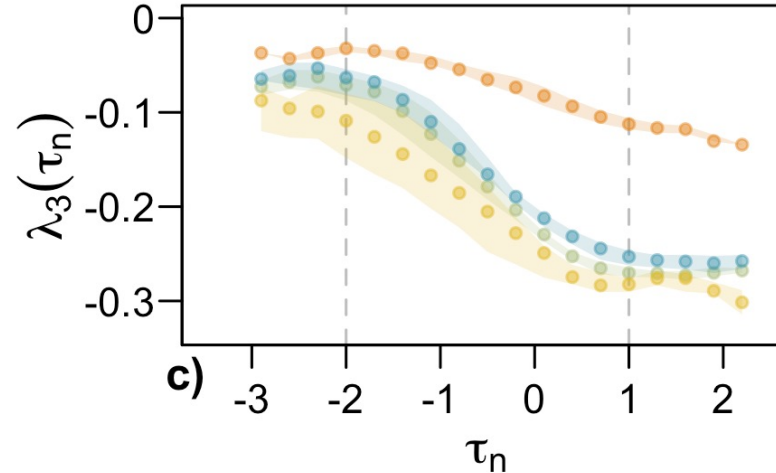
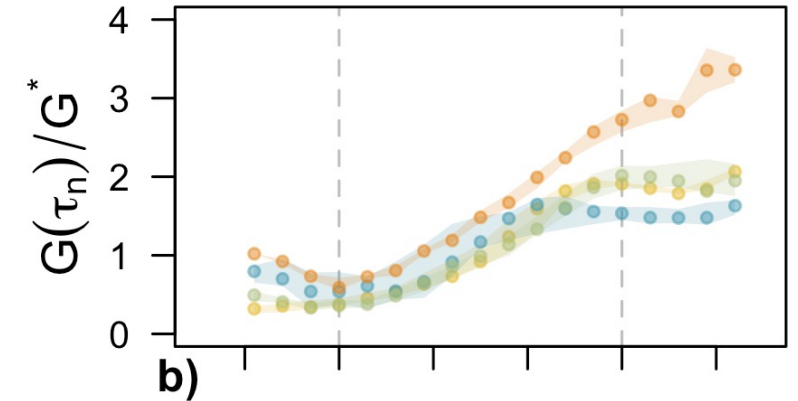
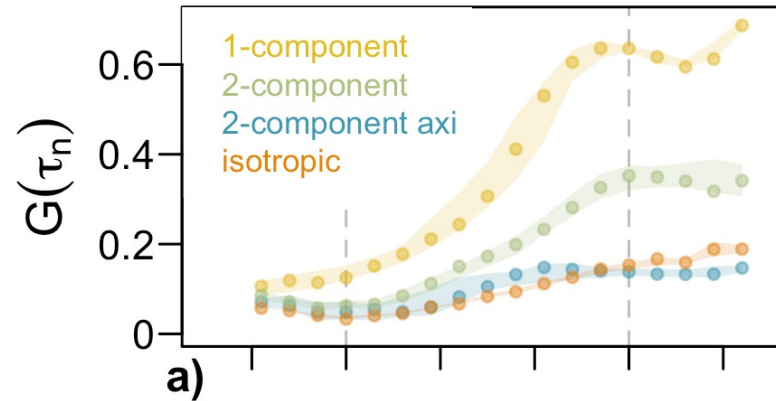
$$x_B = G + \frac{1}{2}(3\lambda_3 + 1)$$

$$y_B = \frac{\sqrt{3}}{2}(3\lambda_3 + 1)$$

We can develop a scaling for speed of trajectories

$$G^* \sim \lambda_1$$

$$\lambda_3^* \sim \lambda_3$$



Conclusions

- Bulk anisotropy sets a universal path towards isotropy at smallest scales
- Anisotropy encodes all relevant information on complexity: both stratification, and terrain and flow complexity
- Anisotropy invariant map imposes controls on trajectories
- Outlook: inclusion of anisotropy can improve Monin-Obukhov similarity scaling

Stiperski I, Katul GG, Calaf M (2021) Universal return to isotropy of inhomogeneous atmospheric boundary layer turbulence. *PRL*, 126, 194501

Funding from the European Research Council (ERC) under the European Union's Horizon 2020 research and innovation programme (Grant agreement No. 101001691: Unicorn)