



# A new method for the attribution of breakpoints in segmentation of IWV difference time series



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# Introduction

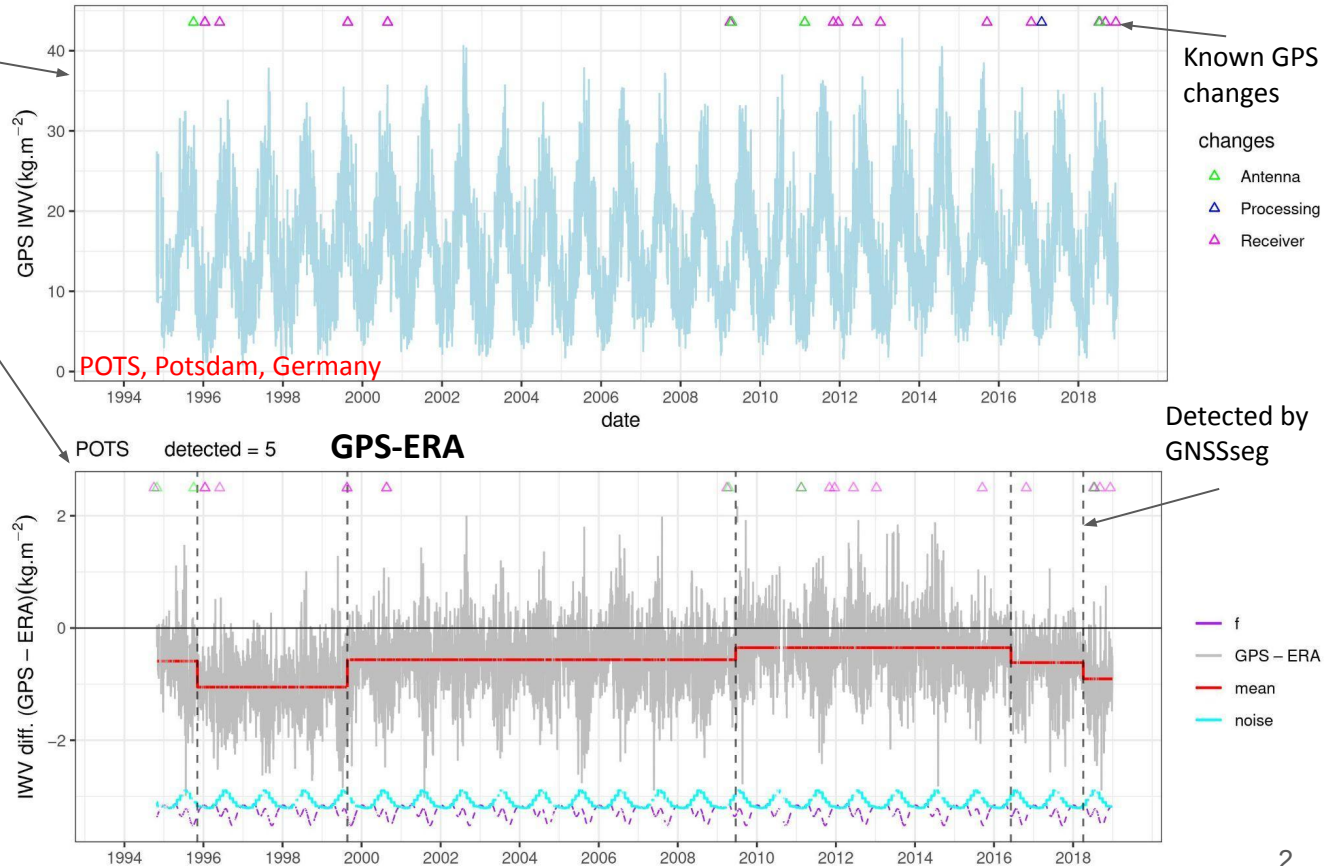
1. GPS series contains known equipment changes, but it's hard to see any induced IWV changes

2. Differenced series (GPS-ERA) is segmented using the GNSSseg method\*

**Problem: are the change-points due to GPS or to ERA ?**

3. Some detected change points are "close" to known equipment changes and others are not...

**=> Attribution = procedure used to chose between GPS and ERA**



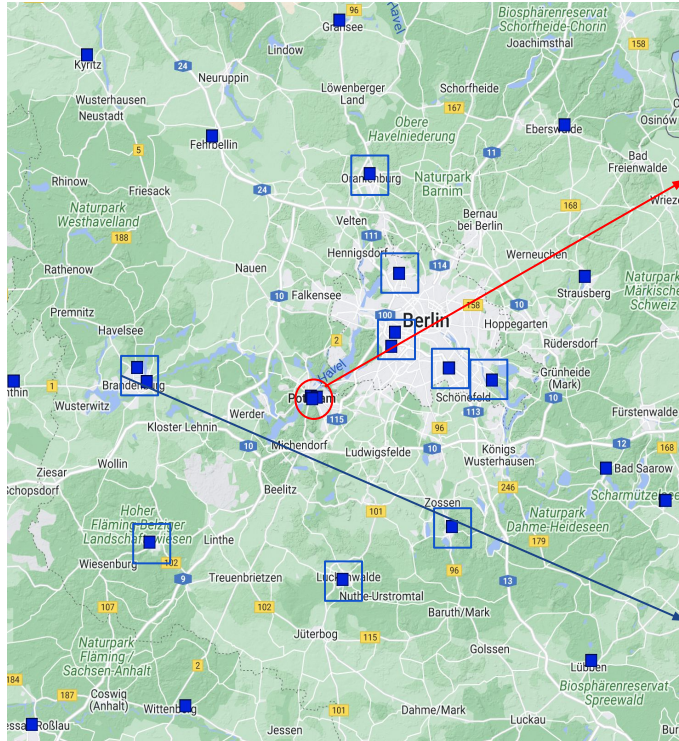
\* GNSSseg R package available on the CRAN

# Attribution method

## General idea:

1. Use data from **nearby stations** supposedly not affected by the same change-points
2. Each nearby station provides 2 additional series: GPS' and ERA'
3. Form **6 series of differences** : GPS-ERA, GPS-GPS', GPS-ERA', ERA-ERA', GPS'-ERA', GPS'-ERA.
4. Apply a **statistical test** for a change in the mean to the 6 series of differences in a +/- 1 year window around each detected change-point
5. Determine in which of the 4 series (GPS, ERA, GPS', or ERA') the change point occurred using a **predictive rule**.

# Select nearby station

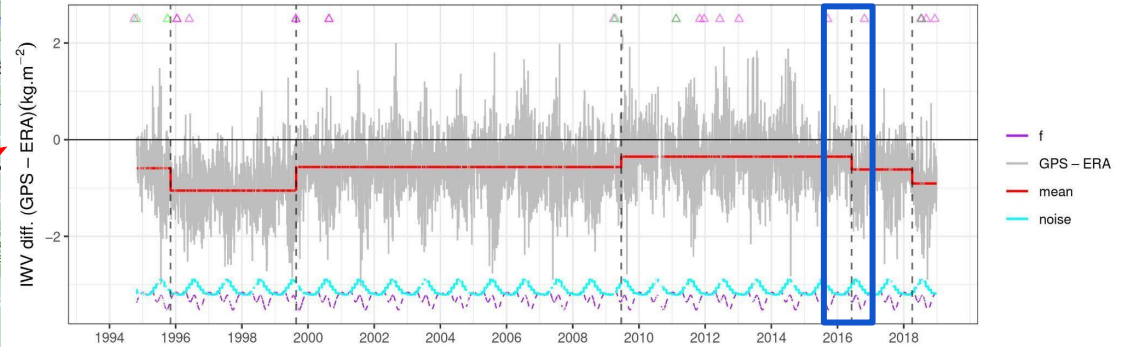


Horizontal distance: 33km

Vertical distance: 57m

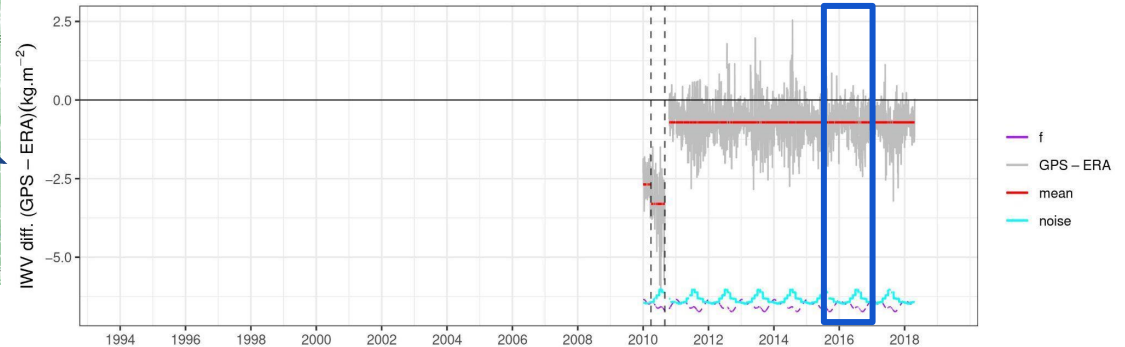
Main station: POTS

GPS - ERA

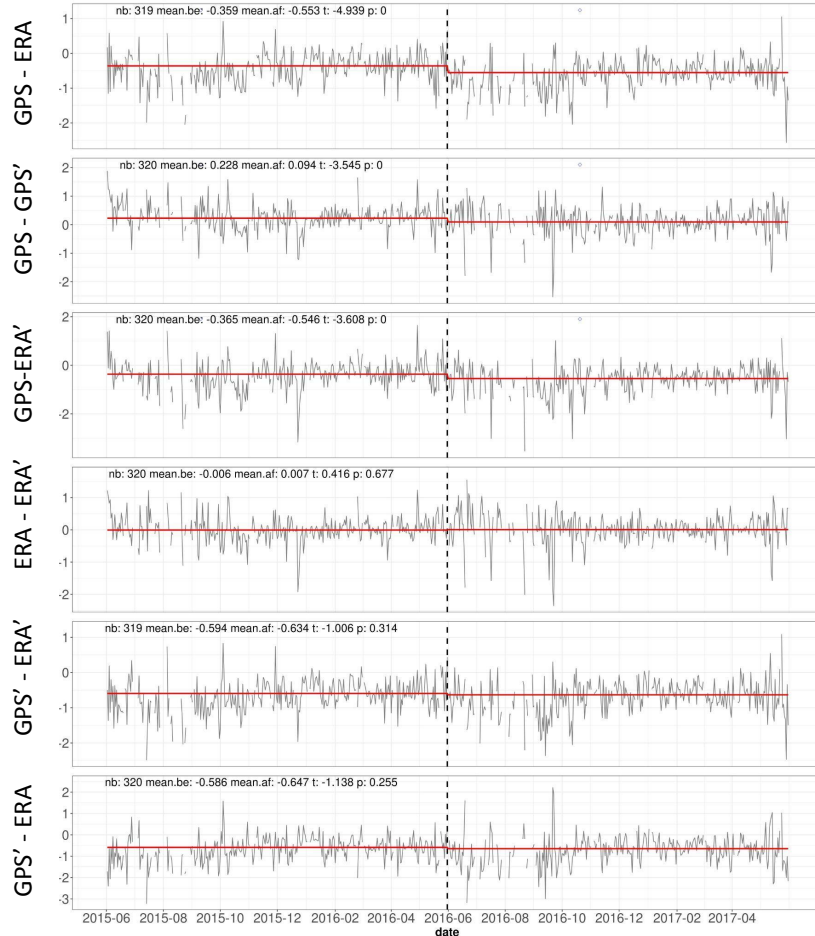


Nearby station: D001

GPS' - ERA'



# Form 6 series of differences and apply test



## Test results

### Look-up table

Truth				Test results					
A	B	C	D	1	2	3	4	5	6
GPS	ERA	GPS'	ERA'	GPS-ERA	GPS-GPS'	GPS-ERA'	ERA-ERA'	GPS'-ERA'	GPS'-ERA
-1	0	0	0	-1	-1	-1	0	0	0
-1	0	0	1	-1	-1	-1	-1	-1	0
-1	0	0	-1	-1	-1	0	1	1	0
-1	0	1	0	-1	-1	-1	0	1	1
-1	0	1	1	-1	-1	-1	-1	0	1
0	1	0	0	-1	0	0	1	0	-1
0	1	1	1	-1	-1	-1	0	0	0

solution

- The look-up table provides the correct solution given that the combination of 6 test results exists in the table.
- If the combination is not in the table a more sophisticated search is necessary, e.g. based on prior probabilities for each combination or a statistical predictive rule.

# Application to global GPS network

- Data sets:

- GPS = 81 IGS stations, CODE REPRO2015 solution
  - GPS' = 704 nearby stations\*, NGL repro3 solution
  - ERA, ERA' = ECMWF reanalysis ERA5
- 
- 156 breakpoints in 56 main stations can be tested with 1 to 10 nearby stations
- 
- 109 breakpoints have at least 1 nearby station with combination of 6 tests results in the table
- 
- Finally, 52% breakpoints are attributed to GPS and 48% are attributed to ERA.

## Perspectives

1. Work in progress:  
Build a predictive rule using supervised classification
2. Final objective:  
After attribution, correct offsets in GPS series

More information:

<https://meetingorganizer.copernicus.org/EGU22/EGU22-6390.html>

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**Thank you for your attention!**

\* Horizontal distance < 200km, vertical distance < 500m

# Supplemental material

# 1. GPS data sets used in this study

	<b><u>Main stations:</u></b> CODE REPRO2015	<b><u>Nearby stations:</u></b> NGL
Software	Bernese GNSS software v5.3	GipsyX Version 1.0
Strategy	Double-difference solution of a global network	PPP
Orbits, clocks, ERPs	CODE repro2 (1994.0-2015.0) + CODE final (2015.0-2019.0)	daily Repro3.0 (JPL)
Reference frame	IGb08	IGS14
Antenna calibration	igs08_1852.atx until 28 January 2017, igs14.atx from 29 January 2017	igs14_www.atx
Window length	72h	30 h
Elevation cutoff angle	3	7
Observations	GPS (1994.0-2002.0), GPS+GLONASS (2002.0-2019.0)	GPS
Observation sampling	3 min	5 min
Observation weighting	$1/\cos(z)^{**2}$	$1/\sin(z)$
Tropospheric model	6-hourly ECMWF analysis (provided by TUV). VMF1 mapping functions (hydrostatic and wet). Piece-wise linear model for ZWD with constraints: 5 m absolute and 5 m relative. Sampling : 2h (ZWD), 24h (gradients).	VMF1 gridded ECMWF tropo parameters from TU Vienna Mapping Function: VMF1 (hydrostatic and wet). Estimation: Zenith delay and gradients as random walk every 5 minutes
Tropo files	ZTD and gradient estimates provided in SINEX files (resampled to 01, 03,... 23 UTC)	ZTD and gradient estimates provided in SINEX files (0000, 0005,...2345 UTC)
Ambiguity resolution	Fixed	Fixed



## 2. Details of the attribution method

For each detected change-point in the main station:

Step 1: Select nearby stations and form 6 series of differences

- Search for nearby stations with limit distance of 200 km and height difference  $< 500\text{m}$ .
- Apply vertical correction(Bock et al., AMT, 2022) to the IWV series from the nearby stations  $\Rightarrow$  GPS' and ERA'.
- Check homogeneity of all series in the  $\pm 1$  yr window (if other change points were detected, reduce the window)
- Form the 6 series of differences
- Screen the series of difference to remove outliers
- Pair the data on the left and right of the change-point
- If the final number of points is lower than 100 on each side, discard this nearby station.

Step 2: Characterize series and apply weighted t-test

- Heteroskedasticity: estimate the monthly variance of the difference series over the  $\pm 1$  yr period with a robust estimator
- Autocorrelation: identify a stochastic model, ARMA of max order (1,1), for the difference series.
- Compute the t-statistic for the 6 differences series, taking into account the heteroskedasticity and autocorrelation, and test their significance.

Step 3: Apply a table search or a prediction rule for the results of the 6 tests

Step 4: Summarize the results for the given breakpoint if several nearby stations have been used.

## Step 2: Significance test on mean difference

- Use the weighted-t-test with the monthly variance. The weighted mean and the t-statistics can be computed as follow:

$$t = \frac{\hat{\mu}_1 - \hat{\mu}_2}{\sqrt{\frac{1}{\sum_{t \in I_1} \frac{1}{\sigma_t^2}} + \frac{1}{\sum_{t \in I_2} \frac{1}{\sigma_t^2}}}} \quad \hat{\mu}_1 = \frac{\sum \frac{Y_t}{\sigma_t^2}}{\sum_{t \in I_1} \frac{1}{\sigma_t^2}}, \quad \hat{\mu}_2 = \frac{\sum \frac{Y_t}{\sigma_t^2}}{\sum_{t \in I_2} \frac{1}{\sigma_t^2}}$$

- The variance  $\sigma_t^2$  is computed using a robust estimator
- The denominator in the t-statistic and is rescaled using the Effective Sample Size concept (Zwiers and von Storch, 1995):
- The ratio between the actual and the effective sample size is computed from the autocorrelation function:

$$\frac{n}{n_e} = 1 + 2 \sum_1^{n-1} \left(1 - \frac{h}{n}\right) \rho(h)$$

- The autocorrelation function  $\rho(h)$  is the theoretical ACF for the identified ARMA(1,1) model with model parameters estimated by maximum likelihood method (Box and Jenkins, 2017).

## Step 3: Table search

1. In total, there are 54 combinations of interest from GPS, ERA, GPS', ERA' (see left part of table)  
→ 46 different combinations of 6 differences including values -2, -1, 0, 1, 2 (see logical table)

2. From test results, the only possible values are -1, 0, 1  
→ 38 different combination of 6 test results can be detected

3. Remove the duplicate combinations in the *test results* table based on prior probabilities (see right part of table)

4. Use of the table: search for the combination in the *test result* table and deduce the corresponding ABCD values. If the combination is not in the table, search for the "nearest" one (e.g. with smallest number of differences). If several solutions exist, use again the prior probabilities to disentangle them.

Truth				Logical table						Test results						Prior joint probability			
A		B	C	D	1		2	3		4	5		6	P(A,B,C,D)					
GPS		ERA	GPS'	ERA'	GPS-ERA	GPS-GPS'	GPS-ERA'	ERA-ERA'	GPS'-ERA'	GPS'-ERA	GPS-ERA	GPS-GPS'	GPS-ERA'	ERA-ERA'	GPS'-ERA'	GPS'-ERA			
1	1	0	0	0	1	1	1	0	0	0	1	1	1	0	0	0	0.1944		
2	1	0	0	1	1	1	0	-1	-1	0	1	1	0	-1	-1	0	0.0108		
3	1	0	0	-1	1	1	1	1	1	0	1	1	1	1	1	0	0.0108		
4	1	0	1	0	1	0	1	0	1	1	1	0	1	0	1	1	0.0108		
5	1	0	1	1	1	0	0	-1	0	0	1	1	0	-1	0	1	0.0006		
6	1	0	1	-1	1	0	1	1	1	1	1	1	0	1	1	1	0.0006		
7	1	0	-1	0	1	1	1	0	-1	-1	-1	1	1	0	-1	-1	0.0108		
8	1	0	-1	1	1	1	0	-1	-1	-1	-1	1	1	0	-1	-1	0.0006		
9	1	0	-1	-1	1	1	1	1	0	-1	-1	1	1	1	1	0	0.0006		
10	0	-1	0	0	1	0	0	-1	0	0	1	1	0	0	-1	0	0.0108		
11	0	-1	0	1	1	0	-1	-1	-1	-1	1	1	0	-1	-1	1	0.0108		
12	0	-1	0	-1	1	0	1	0	1	1	1	1	0	1	0	1	0.1944		
13	0	-1	1	0	1	-1	0	-1	1	1	1	1	-1	0	-1	1	0.0006		
14	0	-1	1	1	1	-1	-1	-1	0	1	1	1	-1	-1	-1	0	0.0006		
15	0	-1	1	-1	1	-1	-1	1	0	1	1	1	-1	1	0	1	0.0108		
16	0	-1	-1	0	1	1	0	-1	-1	-1	0	1	1	0	-1	-1	0.0006		
17	0	-1	-1	1	1	1	-1	-1	-1	-1	0	1	1	-1	-1	-1	0.0006		
18	0	-1	-1	-1	1	1	1	1	0	0	0	1	1	1	0	0	0.0108		
19	-1	0	0	0	-1	-1	-1	-2	0	0	0	-1	-1	-1	0	0	0.1944		
20	-1	0	0	1	-1	-1	-2	-1	-1	-1	0	-1	-1	-1	-1	0	0.0108		
21	-1	0	0	-1	-1	-1	0	1	1	1	0	-1	-1	0	1	1	0.0108		
22	-1	0	1	0	-1	-1	-2	-1	0	1	1	1	-1	-1	0	1	0.0108		
23	-1	0	1	1	-1	-2	-2	-1	0	1	0	1	-1	-1	-1	0	0.0006		
24	-1	0	1	-1	-1	-2	0	1	2	1	1	1	-1	-1	0	1	0.0006		
25	-1	0	-1	0	-1	0	-1	0	-1	-1	-1	-1	-1	0	-1	-1	0.0108		
26	-1	0	-1	1	-1	0	-2	-1	-2	-1	-1	-1	-1	0	-1	-1	0.0006		
27	-1	0	-1	-1	-1	0	0	1	0	-1	-1	-1	0	0	1	0	0.0006		
28	0	1	0	0	-1	0	0	1	0	0	-1	-1	0	0	1	0	0.0108		
29	0	1	0	1	-1	0	-1	0	-1	-1	-1	-1	0	-1	-1	-1	0.1944		
30	0	1	0	-1	-1	0	1	2	1	-1	-1	-1	0	1	1	1	0.0108		
31	0	1	1	0	-1	-1	0	1	1	0	0	-1	-1	0	1	1	0.0006		
32	0	1	1	1	-1	-1	-1	0	0	0	0	-1	-1	-1	0	0	0.0108		
33	0	1	1	-1	-1	-1	1	2	2	0	0	-1	-1	1	1	1	0.0006		
34	0	1	-1	0	-1	1	0	1	-1	-2	-2	-1	1	0	1	-1	0.0006		
35	0	1	-1	1	-1	1	-1	0	-2	-2	-2	-1	1	-1	-1	-1	0.0108		
36	0	1	-1	-1	-1	1	1	2	0	-2	-2	-1	1	1	0	-1	0.0006		
37	1	-1	0	0	2	1	1	-1	0	1	1	1	1	1	0	1	0.0009		
38	1	-1	0	1	2	1	0	-2	-1	1	1	1	1	0	-1	1	0.0009		
39	1	-1	0	-1	2	1	2	0	1	1	1	1	1	0	1	1	0.0162		
40	1	-1	1	0	2	0	1	-1	1	2	1	1	0	1	-1	1	0.00005		
41	1	-1	1	1	2	0	0	-2	0	2	1	1	0	0	-1	0	0.00005		
42	1	-1	1	-1	2	0	2	0	2	2	1	1	0	1	0	1	0.0009		
43	1	-1	-1	0	2	2	1	-1	-1	0	1	1	1	-1	-1	-1	0.00005		
44	1	-1	-1	1	2	2	0	-2	-2	0	1	1	0	-1	-1	0	0.00005		
45	1	-1	-1	-1	2	2	2	0	0	0	1	1	1	0	0	0	0.0009		
46	-1	1	0	0	-2	-1	-1	1	0	-1	-1	-1	-1	-1	1	0	0.0009		
47	-1	1	0	1	-2	-1	-2	0	-1	-1	-1	-1	-1	-1	0	-1	0.0162		
48	-1	1	0	-1	-2	-1	0	2	1	-1	-1	-1	-1	0	1	1	0.0009		
49	-1	1	1	0	-2	-2	-1	1	1	0	-1	-1	-1	-1	1	1	0.00005		
50	-1	1	1	1	-2	-2	-2	0	0	0	-1	-1	-1	-1	0	0	0.0009		
51	-1	1	1	-1	-2	-2	0	2	2	0	-1	-1	-1	0	1	1	0.00005		
52	-1	1	-1	0	-2	0	-1	1	-1	-2	-1	-1	-1	-1	-1	-1	0.00005		
53	-1	1	-1	1	-2	0	-2	0	-2	-2	-1	-1	-1	0	-1	-1	0.0009		
54	-1	1	-1	-1	-2	0	0	2	0	-2	-1	-1	-1	0	1	0	0.00005		