

Static Gravity Field Recovery and Accuracy Analysis

Based on Reprocessed GOCE Level 1b

Gravity Gradient Observations

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GOCE



GRACE

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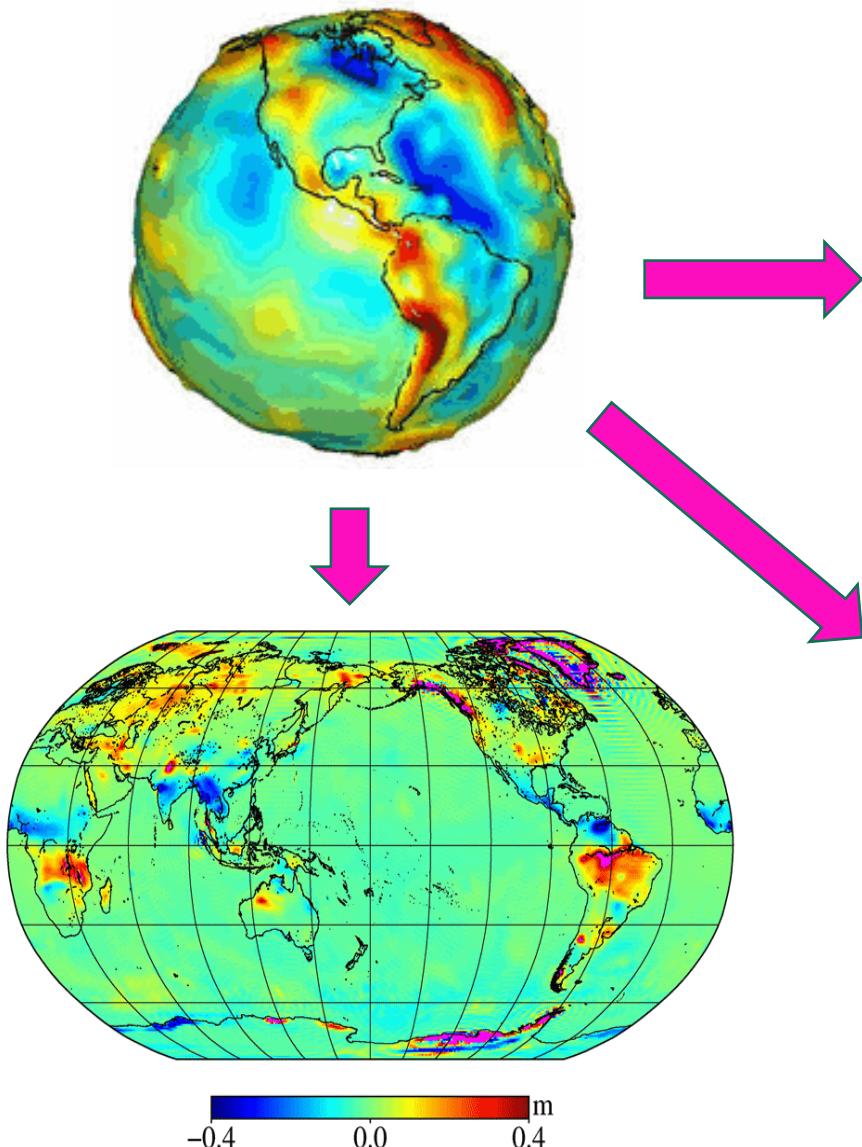
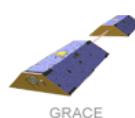
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➤ Introduction

Application of gravity field model

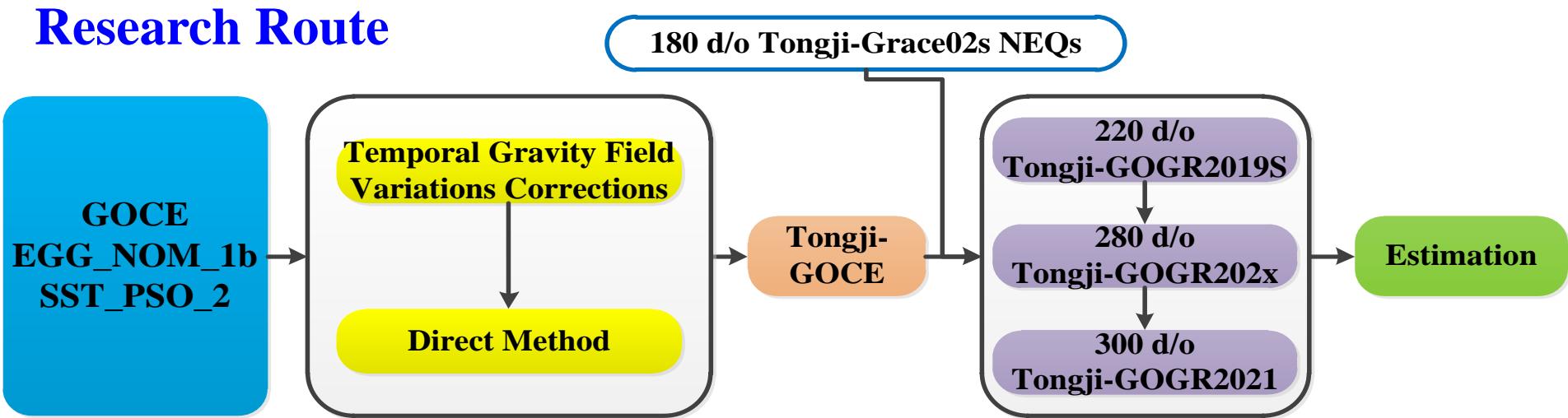




➤ Introduction



Research Route



Tab.1 Model Solutions

Solution	Tongji-GOGR2019S	Tongji-GOGR202x	Tongji-GOGR2021
d/o	220	280	300
GOCE	$\text{SGG} \approx 2a$	$\text{SGG} \approx 1148 \text{ d}$	SGG Mission Period
GRACE	180d/o Tongji-Grace02s NEQs		
Method	Direct Method		
Ref. Model	GIF48	Tongji-GOGR2019S	Tongji-GOGR202x
Other	No Constraint	Kaula Constraint	Kaula Constraint



➤ Theory of Satellite Gravity Recovery



$$V(\theta, \lambda, r) = \frac{GM_{\oplus}}{r} \left[1 + \sum_{n=2}^N \left(\frac{R}{r} \right)^n \sum_{m=0}^n \left(\bar{C}_{n,m} \cos m\lambda + \bar{S}_{n,m} \sin m\lambda \right) \bar{P}_{n,m} (\cos \theta) \right]$$

$$\rightarrow V_r, V_\theta, V_\lambda, V_{rr}, V_{\theta\theta}, V_{\lambda\lambda}, V_{r\theta}, V_{r\lambda}, V_{\theta\lambda} \quad \rightarrow \quad V_{xx}, V_{yy}, V_{zz}, V_{xy}, V_{xz}, V_{yz}$$

$$V_{xx}, V_{yy}, V_{zz}, V_{xz} \quad \rightarrow \quad \boldsymbol{v}_{SGG} = \mathbf{A}_{SGG} \boldsymbol{\delta u} - \mathbf{y}_{SGG}$$

Combination of GOCE SGG and GRACE

Tongji-Grace02s

$$\left(\frac{\sigma_0^2}{\sigma_{SGG}^2} \mathbf{N}_{SGG} + \frac{\sigma_0^2}{\sigma_{GRACE}^2} \mathbf{N}_{GRACE} + \alpha \mathbf{K}_{kaula} \right) \boldsymbol{\delta u} = \left(\frac{\sigma_0^2}{\sigma_{SGG}^2} \mathbf{w}_{SGG} + \frac{\sigma_0^2}{\sigma_{GRACE}^2} \mathbf{w}_{GRACE} \right)$$

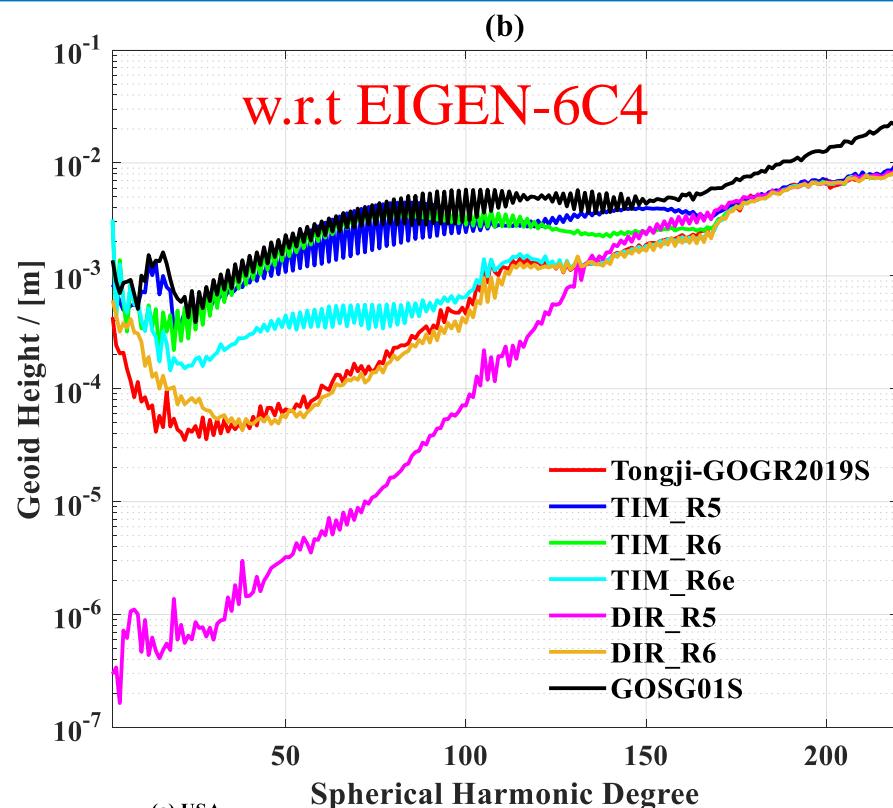
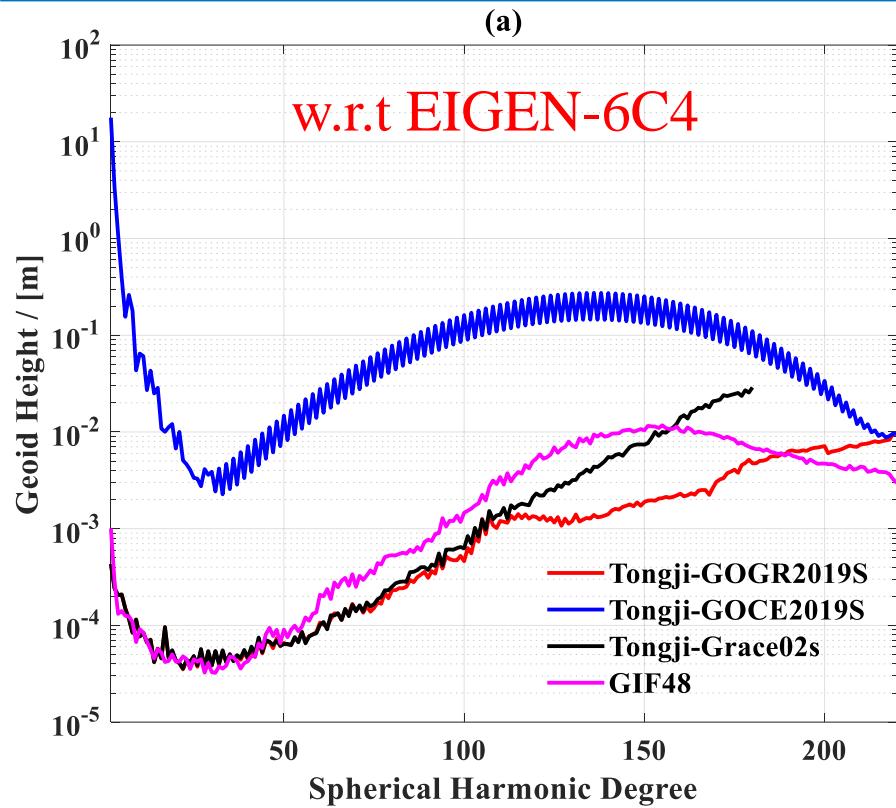
GOCE

$$\hat{\sigma}_i^2 = \frac{\mathbf{v}_i^T \mathbf{P}_i \mathbf{v}_i}{n_i - \text{tr}(\mathbf{N}_i^{-1} \mathbf{N}_i)}$$

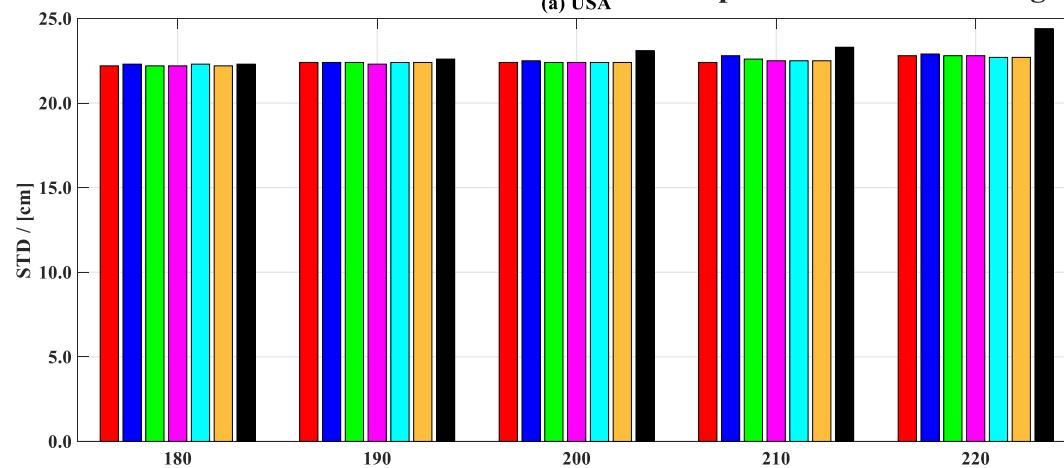
$$\sigma_0 = 0.02m$$



➤ Combined Recovery and Accuracy Analysis

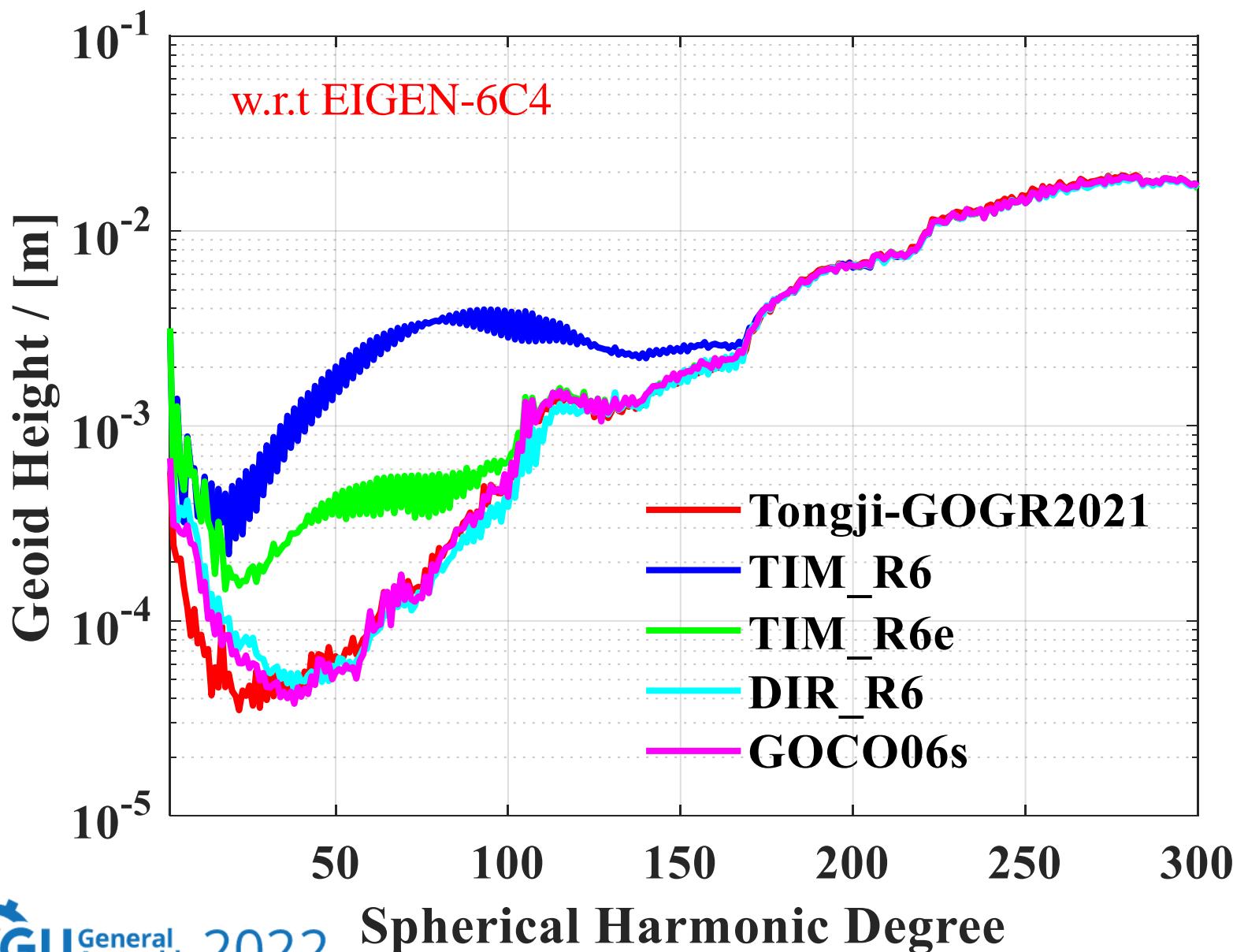
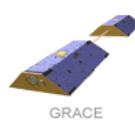


- Tongji-GOGR2019S
- TIM_R5
- TIM_R6
- TIM_R6e
- DIR_R5
- DIR_R6
- GOSG01S



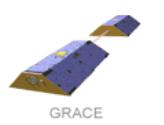


➤ Combined Recovery and Accuracy Analysis

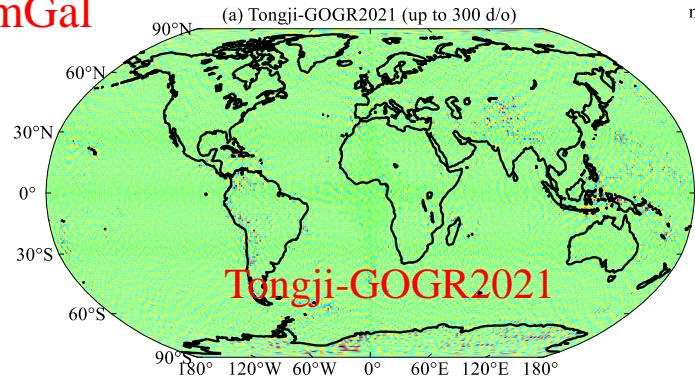




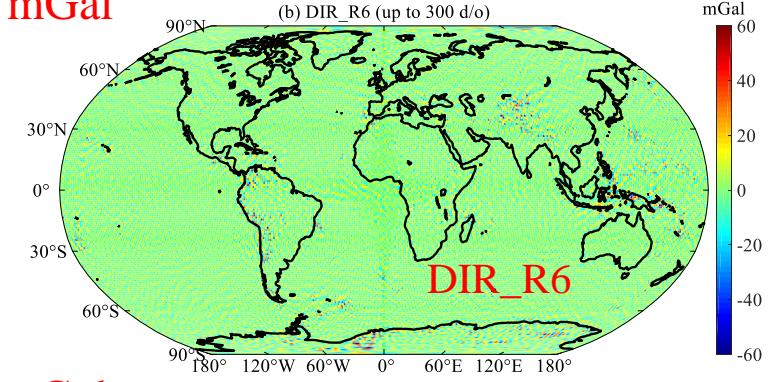
► Combined Recovery and Accuracy Analysis



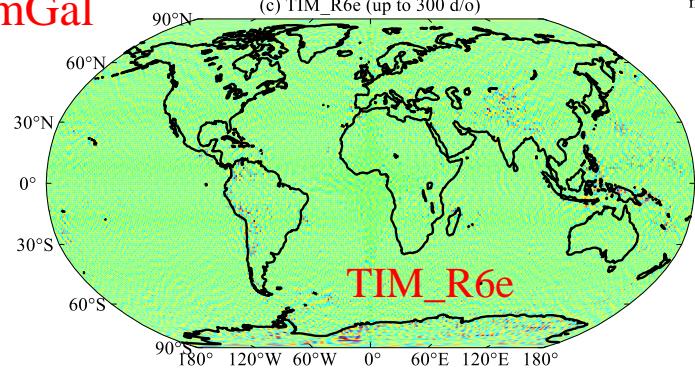
8.64 mGal



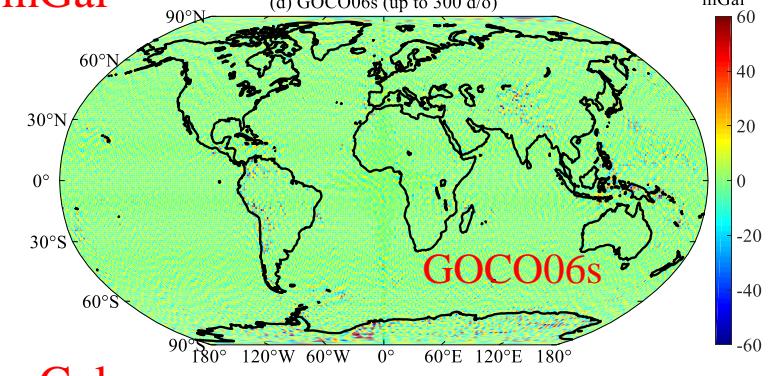
7.76 mGal



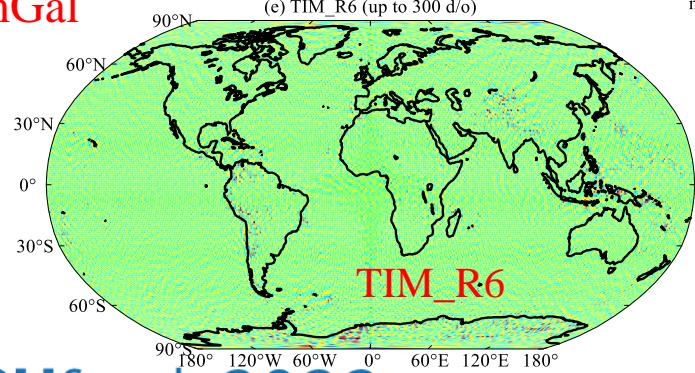
8.33 mGal



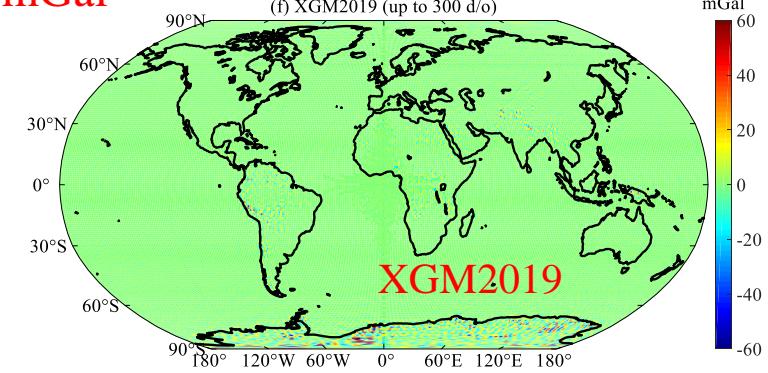
8.96 mGal



8.78 mGal



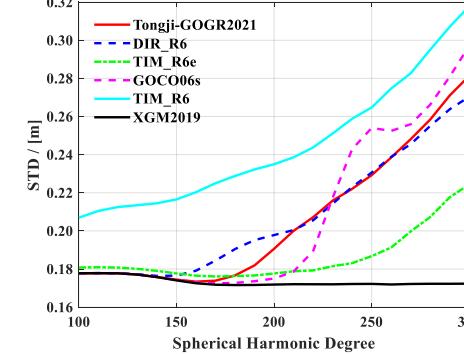
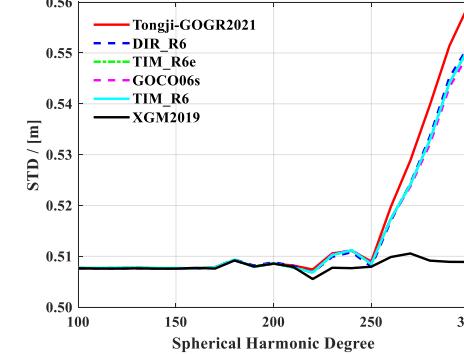
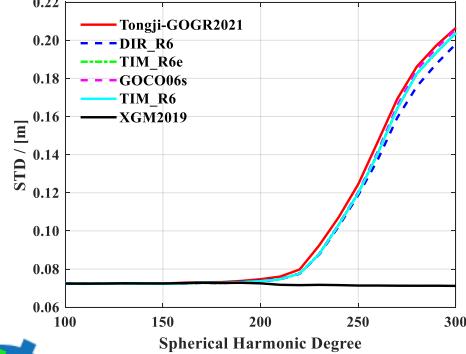
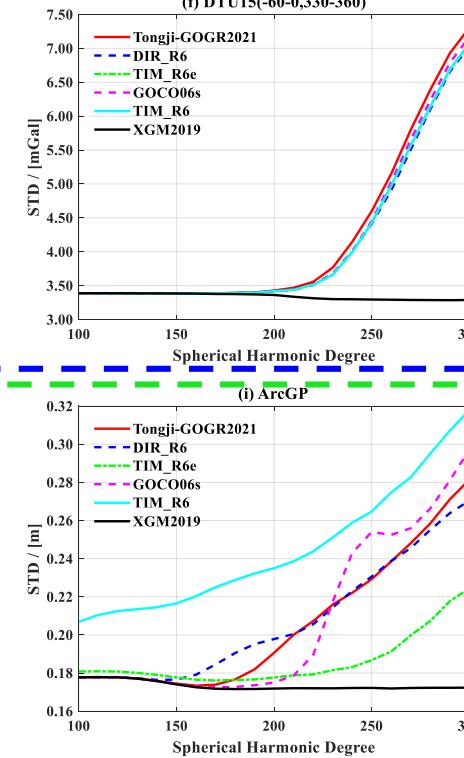
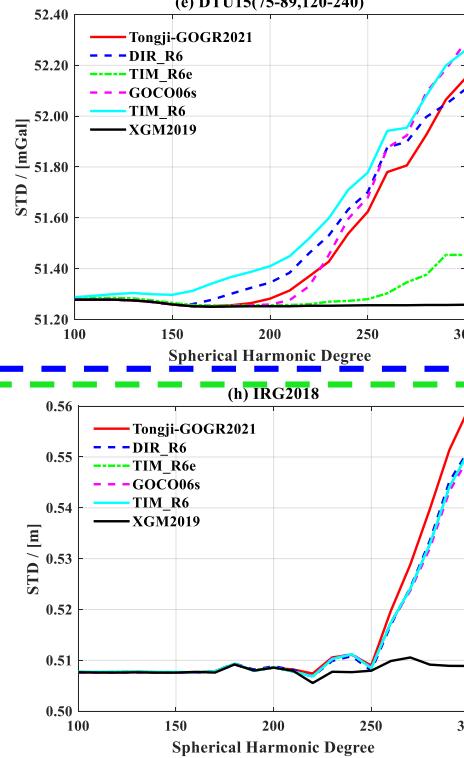
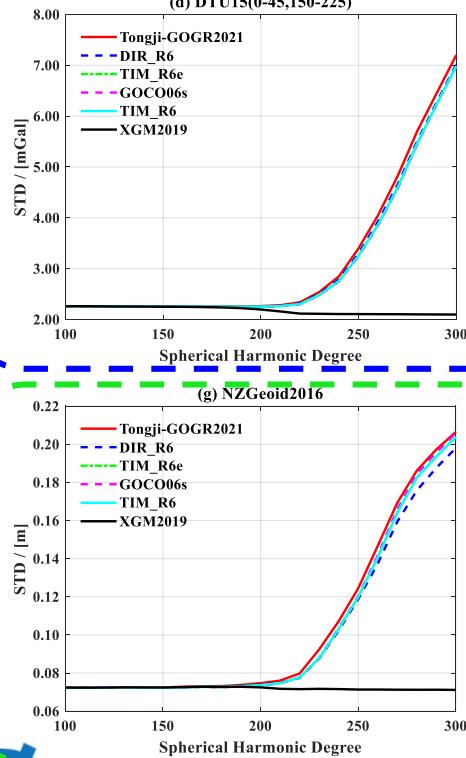
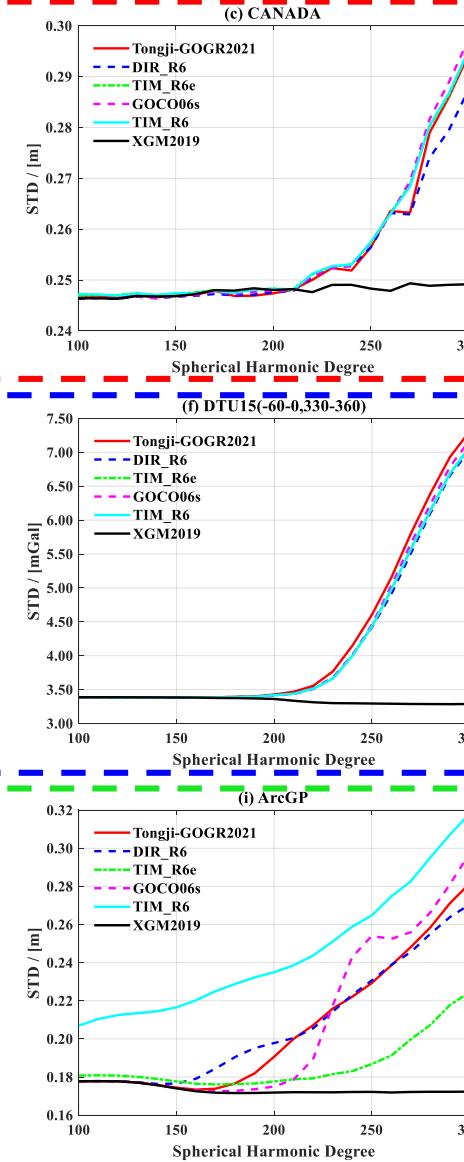
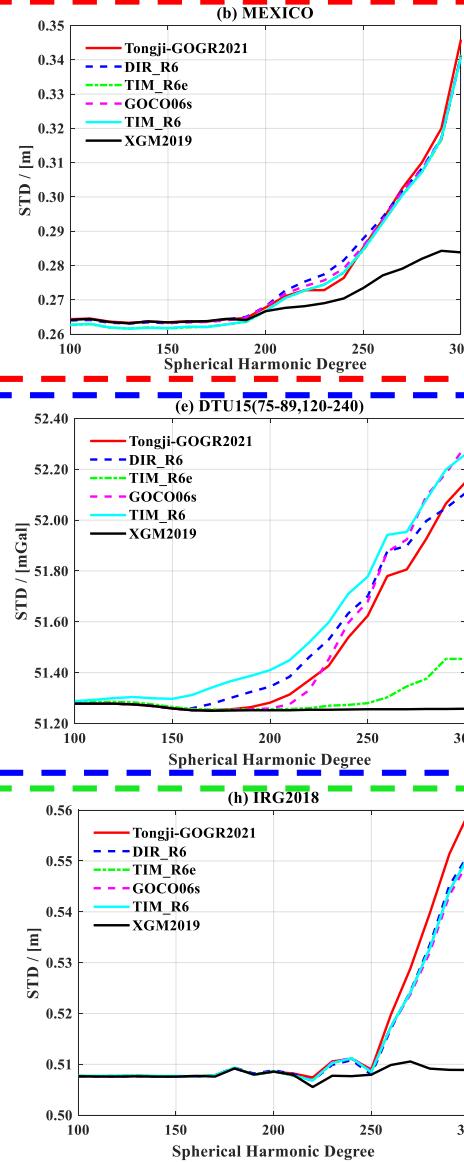
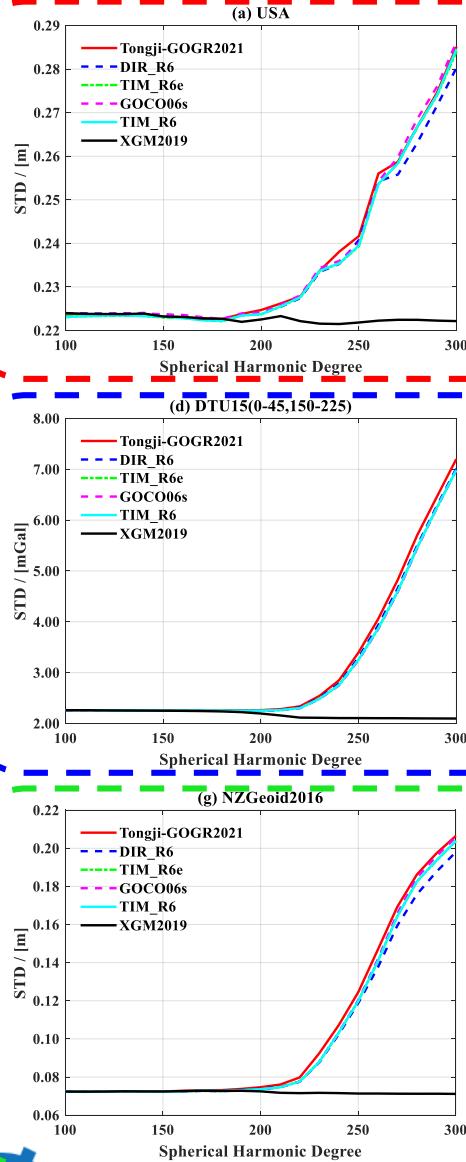
5.34 mGal



w.r.t EIGEN-6C4 Gravity Anomaly

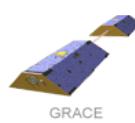


➤ Combined Recovery and Accuracy Analysis





➤ Conclusion



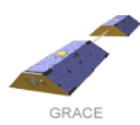
- The accuracy of the Tongji-GOGR2019S model of 220 degree/order is close to that of the GOCE R6 models.
- The constrained solution Tongji-GOGR2021 model of 300 degree/order is comparable to the GOCE R6 models in resolution and accuracy.

Outlook:

- ◆ We will combine satellite gravity data, ground gravity data, and Satellite altimetry data to recover the static gravity field model with higher resolution and higher accuracy.



GOCE



GRACE

Thanks for your attention!