

Storm-time Evolution and Empirical Modelling of the Equatorial Electron Pitch Angle Distributions in Earth's Outer Radiation Belt

Artem Smirnov^{1,2}, Yuri Shprits^{1,2,3}, Hayley Allison¹, Nikita Aseev¹, Alexander Drozdov³, Peter Kollmann⁴, Dedong Wang¹, Anthony Saikin³

¹ GFZ German Research Centre for Geosciences, Potsdam, Germany

² University of Potsdam, Germany

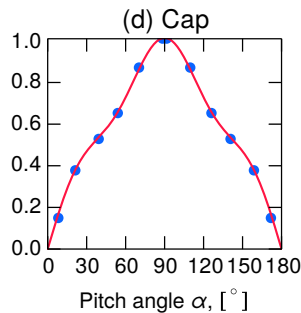
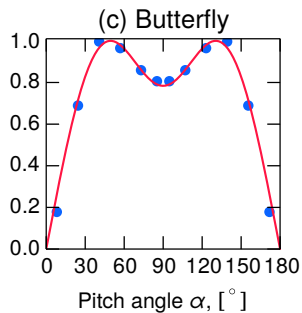
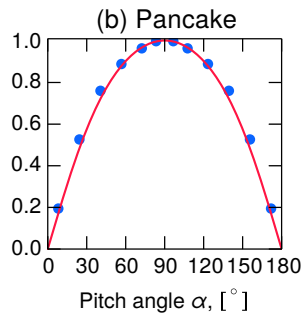
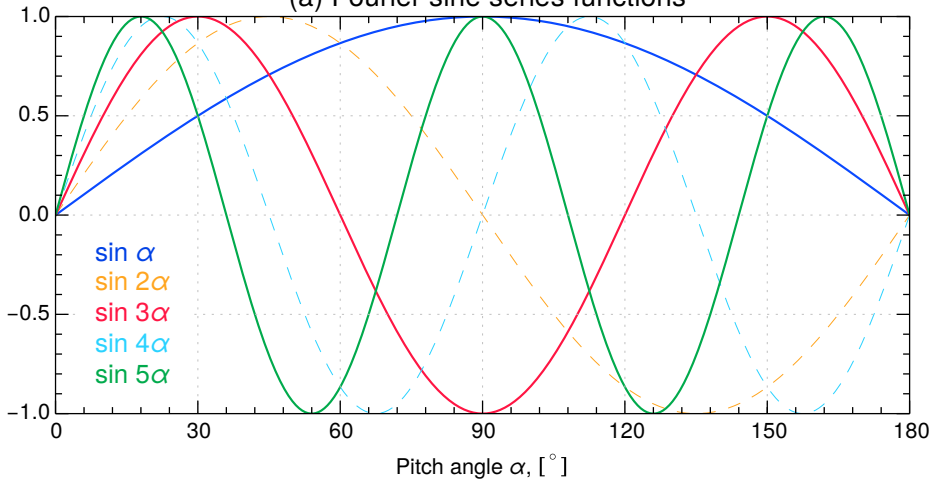
³ University of California, Los Angeles, CA, USA

⁴ Johns-Hopkins University (Applied Physics Laboratory), Laurel, MD, USA

EGU-2022

Pitch Angle Distributions

(a) Fourier sine series functions



$A_1 \sim \text{pancake}$
 $A_3 \sim \text{butterfly}$
 $A_5 \sim \text{cap}$

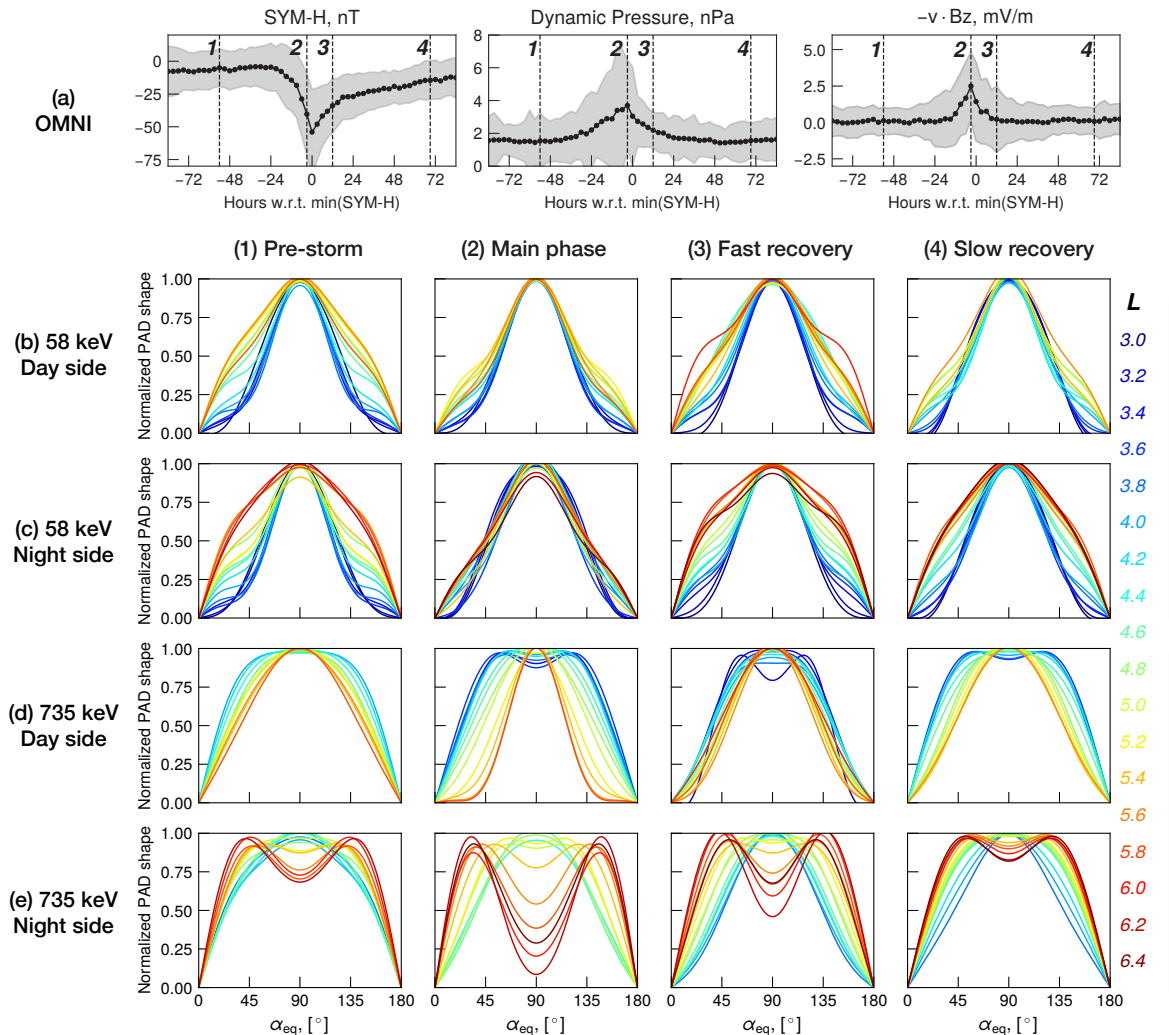
- Equatorial electron PADs can be well approximated using Fourier sine series expansion to degree 5:

$$j(\alpha) = A_0 + A_1 \sin \alpha + A_3 \sin 3\alpha + A_5 \sin 5\alpha$$

- Coefficients before the second and fourth harmonics are not used, because they represent asymmetric terms
- In order to remove flux levels, we normalize each PAD measured by the Van Allen Probes using:

$$\tilde{A}_i = \frac{A_i}{j_{max} - A_0}, i = \{1, 3, 5\}$$

Superposed PAD shapes

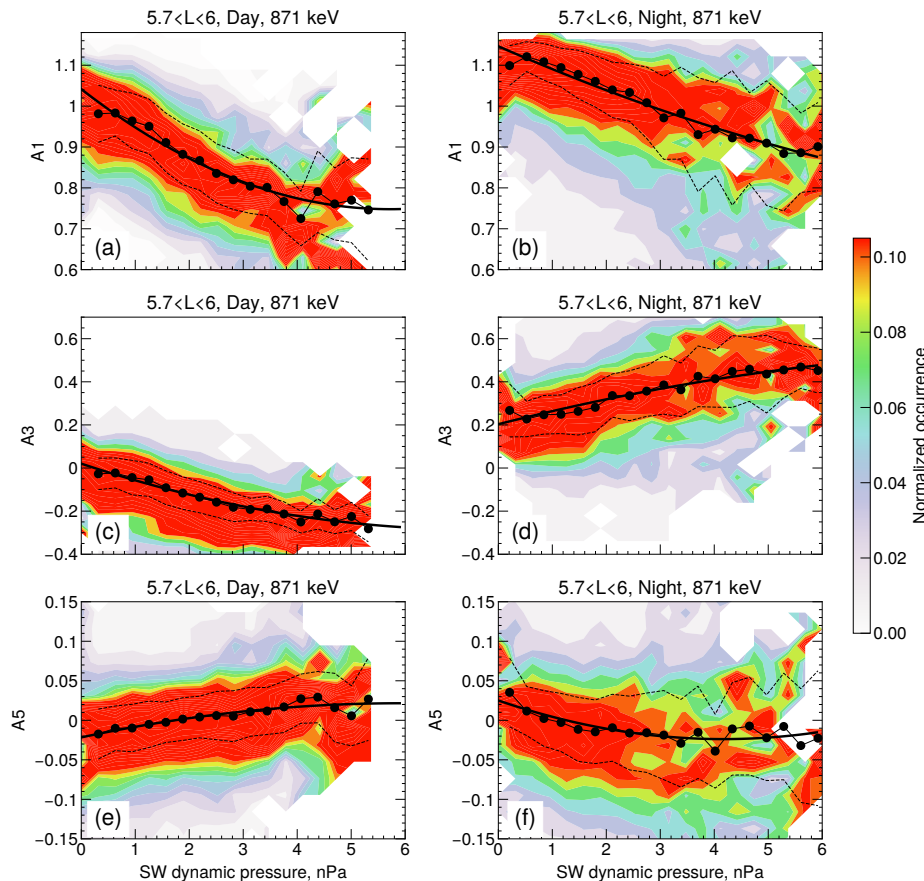


→ At lower energies, PADs are quite stable throughout the geomagnetic storms

→ At higher energies,

- At day side MLT, pancake PADs become steeper around the main phase
- At night side, the butterfly distributions become more pronounced

Generalized dependence on P_{dyn}



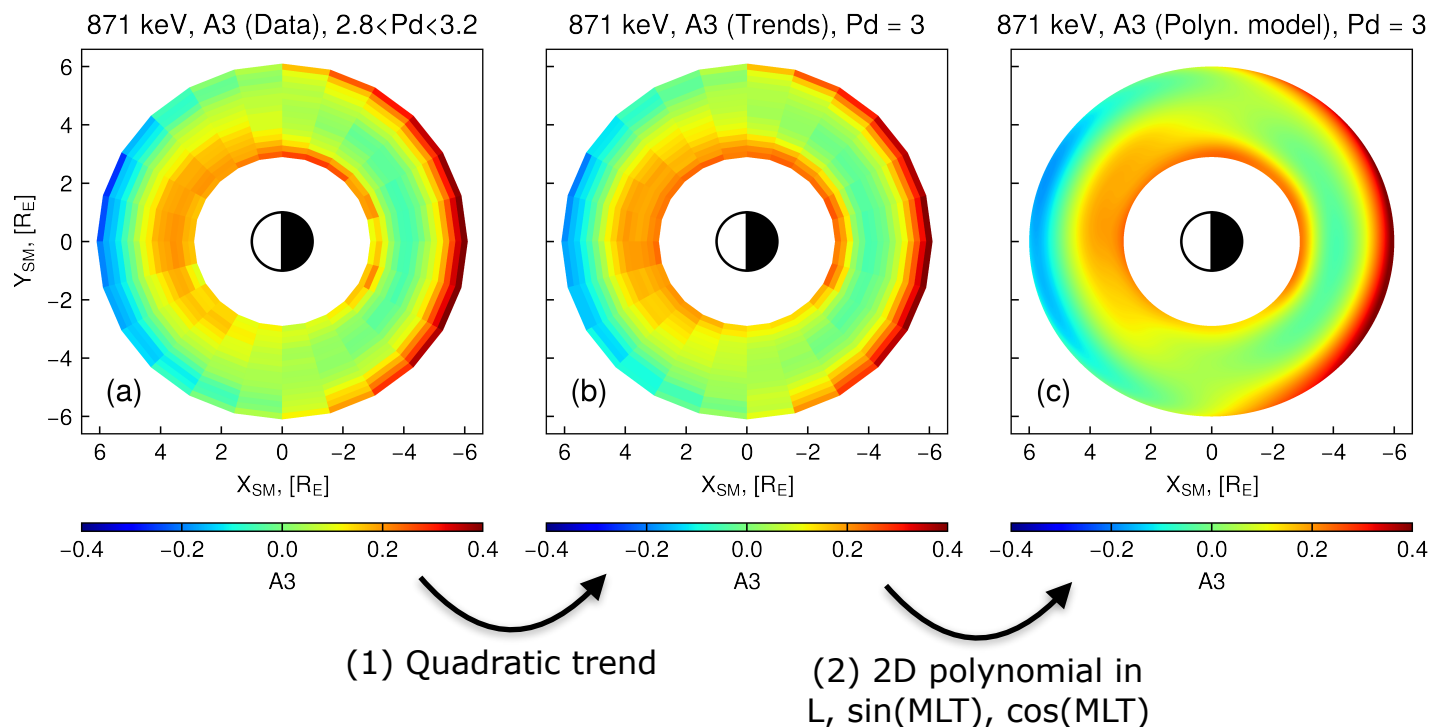
Normalized occurrence plots of the pancake (A1), butterfly (A3) and cap (A5) coefficients based on P_{dyn} for L > 5.7

- We now analyze, whether we can draw a generalised dependence of the A1, A3 and A5 coefficients on activity
- At each bin of 0.2L x 1hr MLT, we fit the quadratic dependence on dynamic pressure:

$$A_i = c_0 P_{\text{dyn}}^2 + c_1 P_{\text{dyn}} + c_2$$

- One can see that there is a strong dependence on P_{dyn}, and the values coincide with our previous analysis
- We now need to introduce a dependence on L and MLT.

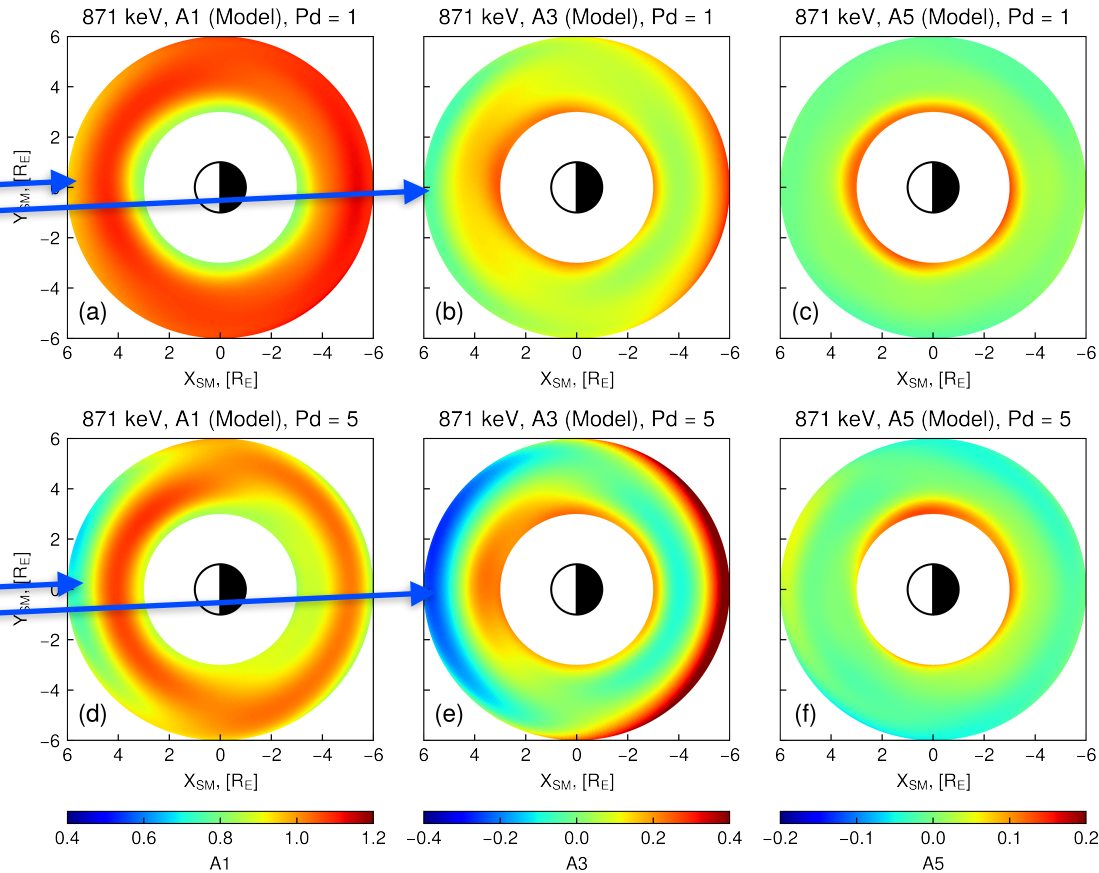
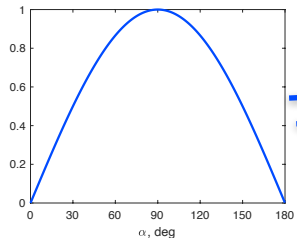
Model setup



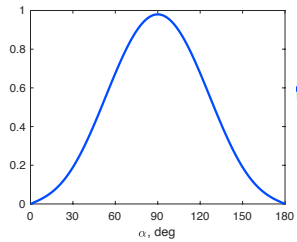
We get a model that has a continuous dependence on L , MLT and dynamic pressure, for each energy channel

Model dependence on dynamic pressure

Dayside/ Quiet



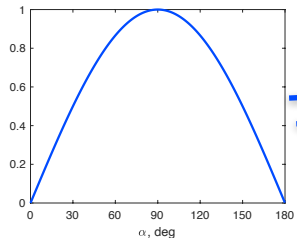
Dayside/ Active



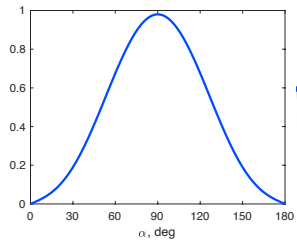
Pancake
distributions
become steeper

Model dependence on dynamic pressure

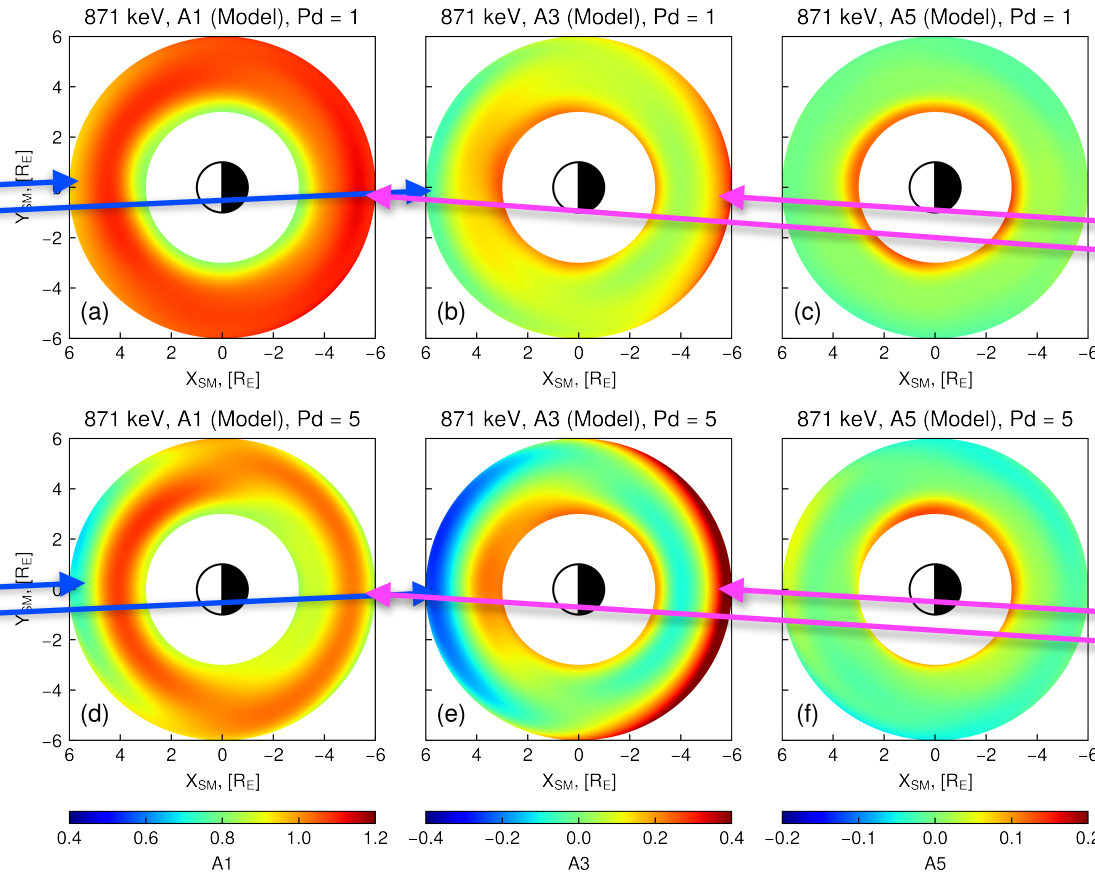
Dayside/ Quiet



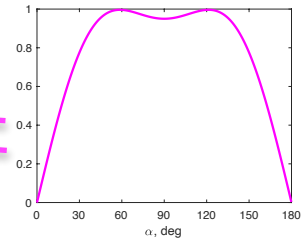
Dayside/ Active



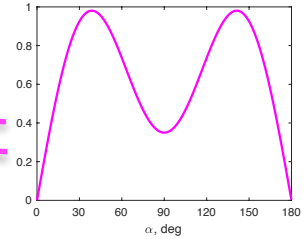
Pancake distributions become steeper



Nightside/ Quiet



Nightside/ Active

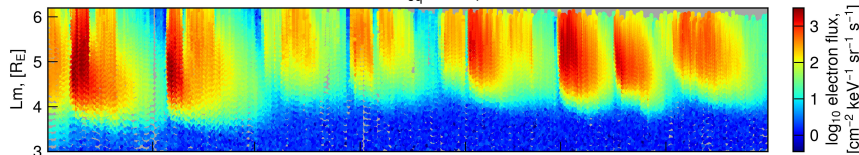


Butterfly distributions are more pronounced

This agrees well with the superposed epoch analysis.
The model reproduces the activity dependence well.

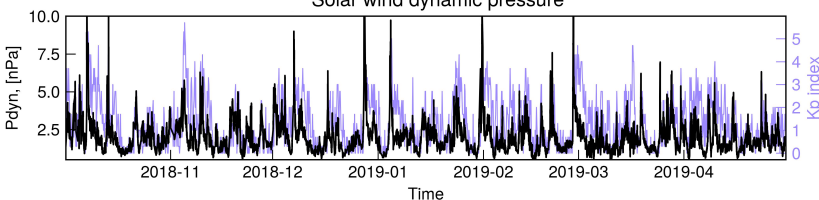
Model validation: 1 MeV

RBSP flux at $\alpha_{\text{eq}} = 80^\circ$, 1.08 MeV

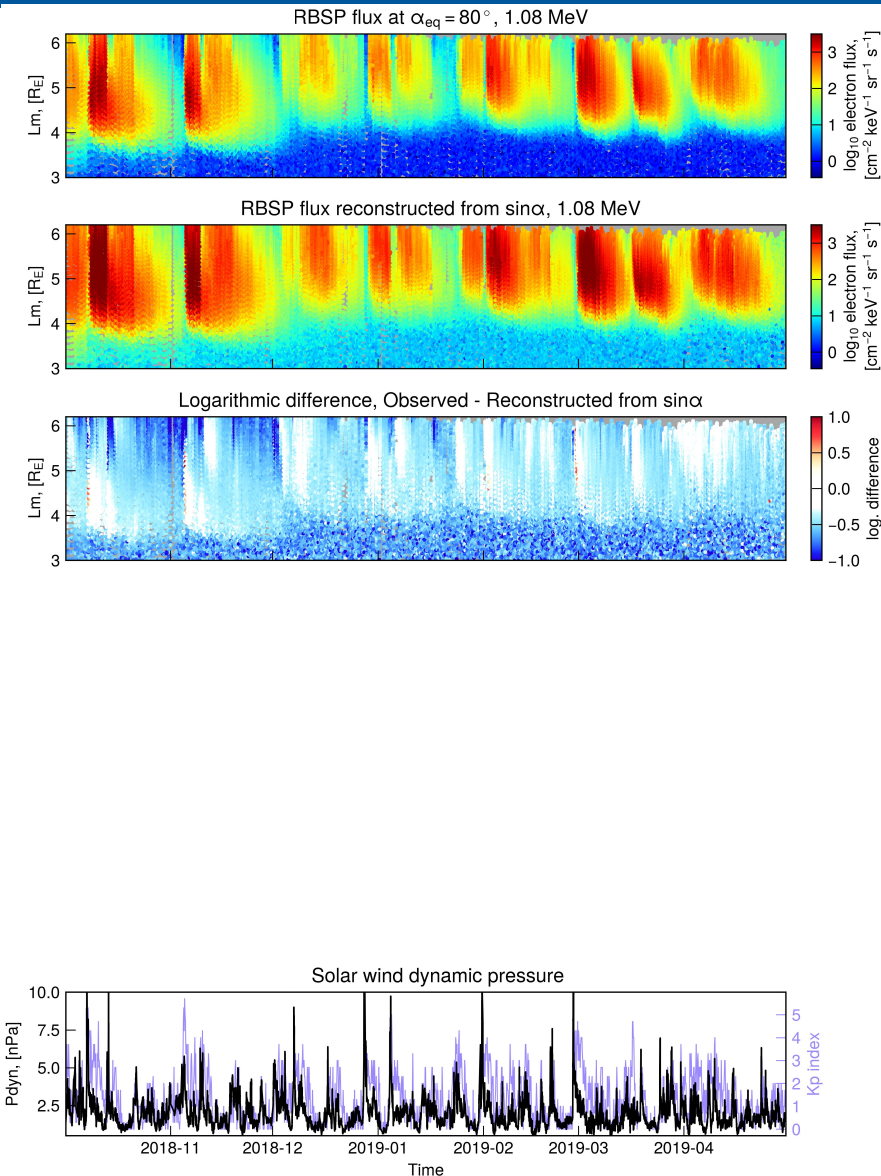


- We use two directional flux measurements at low pitch angles to reconstruct flux values at 90 degrees equatorial p.a.
- We use 2 lowest MagEIS pitch angles, 8 and 17 degrees
- By having 2 observations, we can reconstruct both A0 that we previously omitted, and the normalization factor
- We also reconstruct the equatorial 90-degrees flux using the standard sine approximation
- The **skill score** (improvement in performance) of our Fourier-based model compared to the standard approach **is 92%**.

Solar wind dynamic pressure

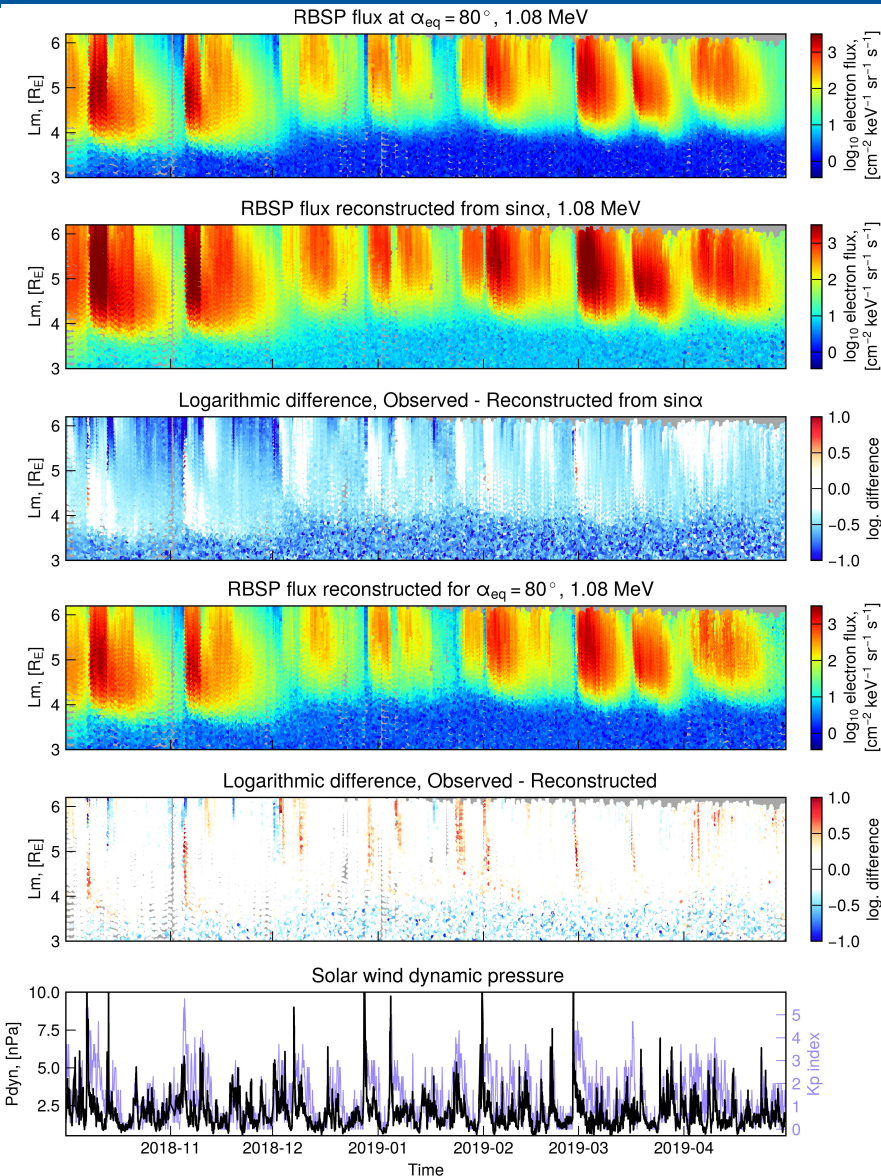


Model validation: 1 MeV



- We use two directional flux measurements at low pitch angles to reconstruct flux values at 90 degrees equatorial p.a.
- We use 2 lowest MagEIS pitch angles, 8 and 17 degrees
- By having 2 observations, we can reconstruct both A0 that we previously omitted, and the normalization factor
- We also reconstruct the equatorial 90-degrees flux using the standard sine approximation
- The **skill score** (improvement in performance) of our Fourier-based model compared to the standard approach **is 92%**.

Model validation: 1 MeV



- We use two directional flux measurements at low pitch angles to reconstruct flux values at 90 degrees equatorial p.a.
- We use 2 lowest MagEIS pitch angles, 8 and 17 degrees
- By having 2 observations, we can reconstruct both A0 that we previously omitted, and the normalization factor
- We also reconstruct the equatorial 90-degrees flux using the standard sine approximation
- The **skill score** (improvement in performance) of our Fourier-based model compared to the standard approach is **92%**.

Conclusions

- Pitch angle distributions in the outer radiation belt region can be well approximated by a Fourier series expansion up to degree 5
- Storm-time evolution of PADs was investigated in terms of L-MLT variation
- A simple polynomial model, based on dynamic pressure, is developed. It reproduces the PAD behaviour in the outer belt well
- The model can be used to reconstruct the full equatorial PADs from LEO data. It outperforms the standard sine approximation by 92%
- The model can also be used to reconstruct equatorial PADs from omnidirectional measurements, for instance, at MEO orbits.

This study has received funding from the European Union's Horizon 2020 research and innovation programme under grant agreement No. 870452 (PAGER).