

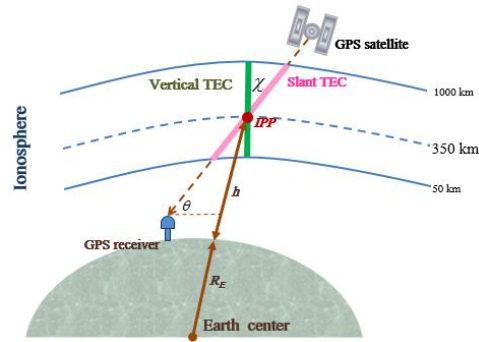
Global VTEC Modeling with Neural Networks

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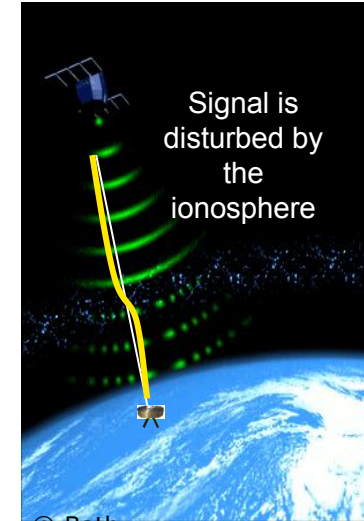
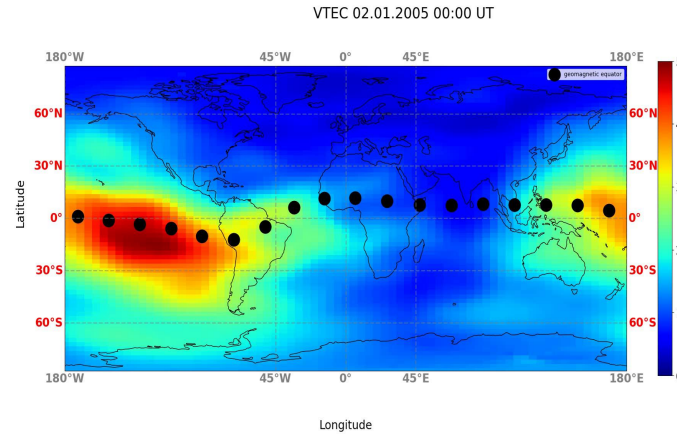
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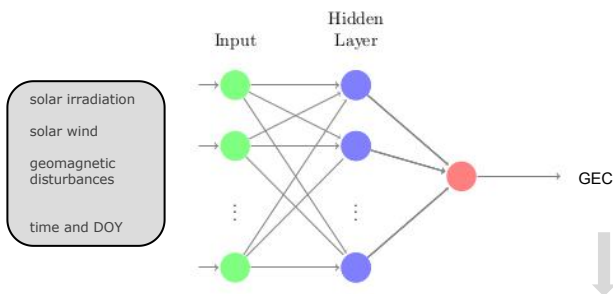


source: Thai GNSS and Space Weather
http://iono-gnss.kmitl.ac.th/?page_id=243



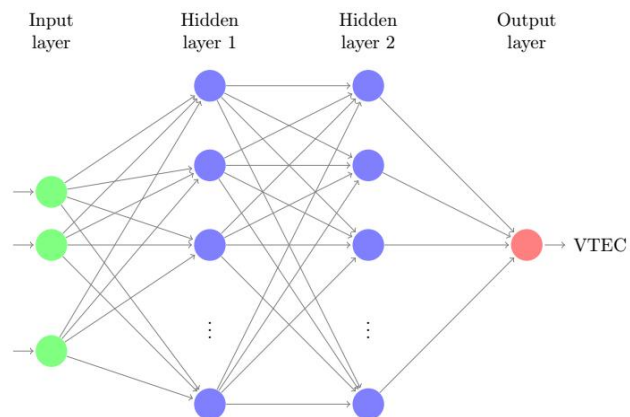
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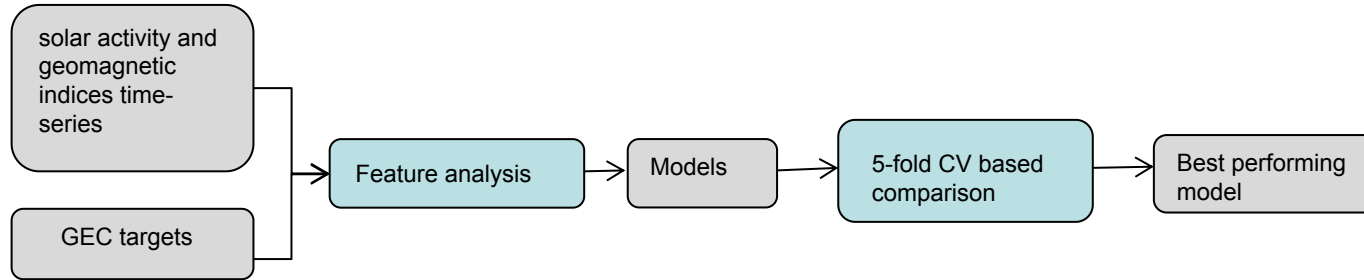
- Objective of the study: develop machine learning model of Vertical Total Electron Content (VTEC)
- VTEC: electron columnar number density
- Extracted by GNSS measurements from the IGS network
- Measured indirectly based on the GPS signal transmission delay



Local modeling

magnetic latitude
magnetic local time
 $\cos(\text{magnetic latitude})$
 $\sin(\text{magnetic latitude})$
solar elevation angle
 $\cos(\text{solar elevation angle})$
 $\sin(\text{solar elevation angle})$
 $\cos(\text{geographic longitude})$
 $\sin(\text{geographic longitude})$





Feature selection methods:

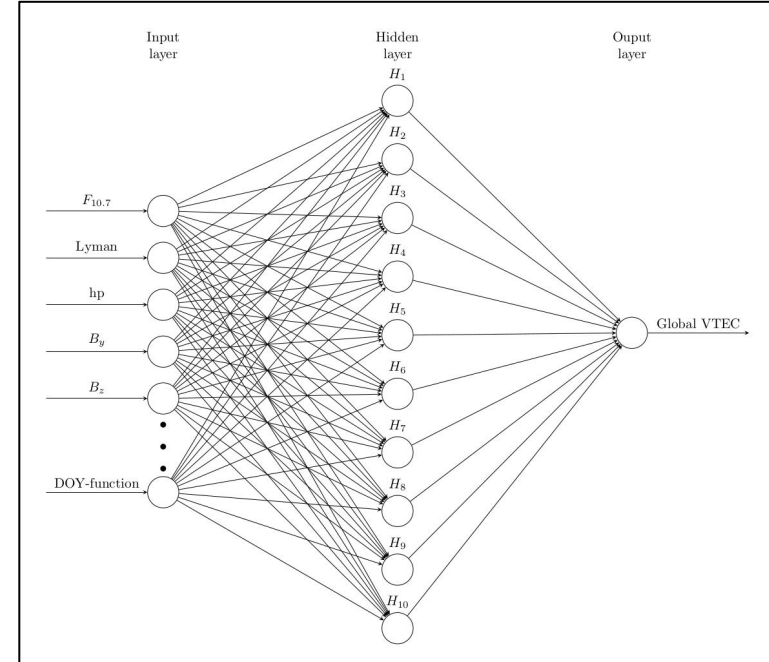
1. Related work of continuous 3D electron density model by Smirnov et al, 2020 adding time histories
2. Time-lagged Pearson cross-correlation
3. Permutation feature importance
4. Mutual information

X_A	X_B	X_C	Y
<i>xa1</i>	<i>xb1</i>	<i>xc1</i>	<i>y1</i>
<i>xa2</i>	<i>xb2</i>	<i>xc2</i>	<i>y2</i>
<i>xa3</i>	<i>xb3</i>	<i>xc3</i>	<i>y3</i>
<i>xa4</i>	<i>xb4</i>	<i>xc4</i>	<i>y4</i>
<i>xa5</i>	<i>xb5</i>	<i>xc5</i>	<i>y5</i>
<i>xa6</i>	<i>xb6</i>	<i>xc6</i>	<i>y6</i>

Permutation feature importance illustration

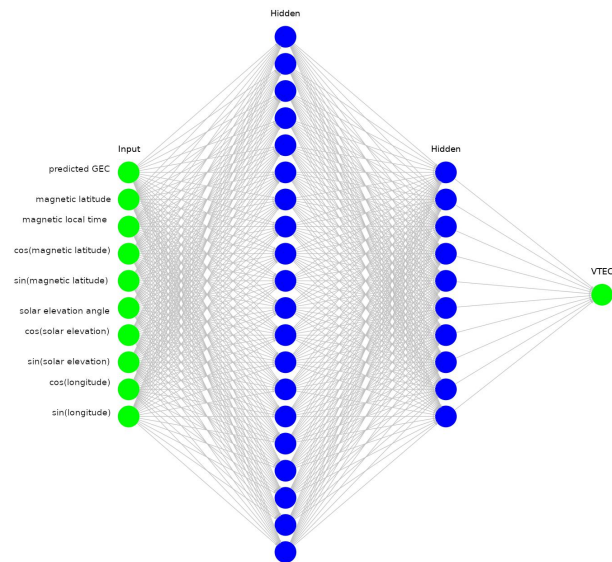
Source: Cerliani M., Feature Importance with Neural Network, Towards Data Science

- Neural network consists of ten neurons
- Feature set consists of Lyman alpha, $F_{10.7}$, B_y , B_z , V_x , SYM-H, H_p , trigonometric functions of DOY and universal time with time histories from the previous 72 and 96 hours

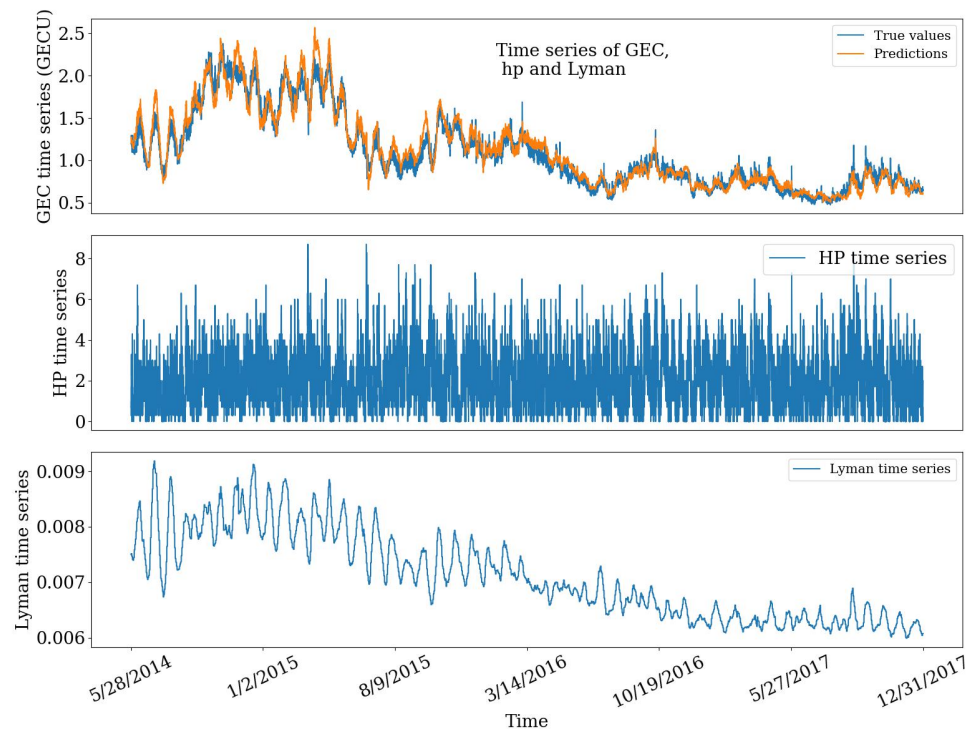


- Final neural network was tested on years 2004, 2006, 2011, 2016

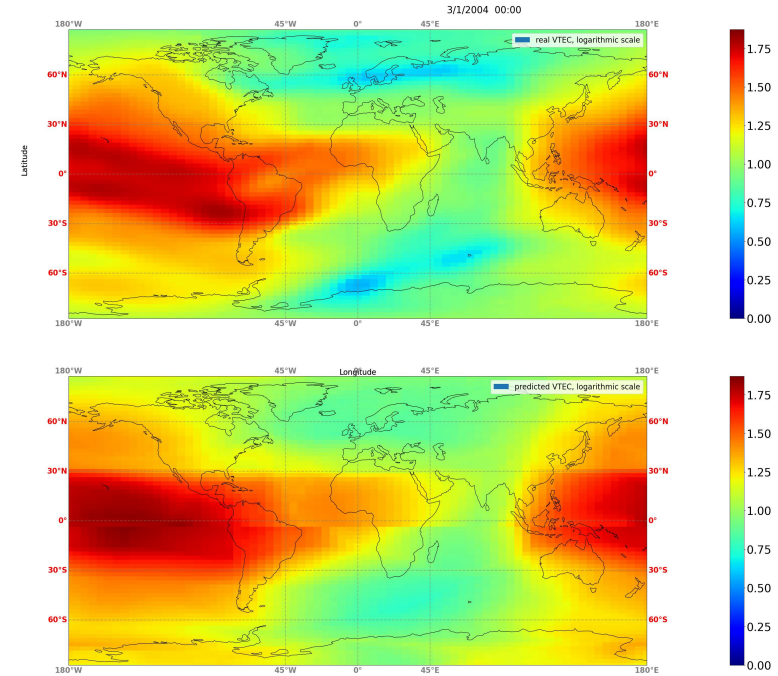
Period	RMSE	MAE
2004	4.9	3.6
2006	3.8	2.8
2011	6.6	4.7
2016	4.7	3.6
entire period	5.1	3.7



- Test data: 2014 - 2017
- Performance in test data expressed in correlation 97 %

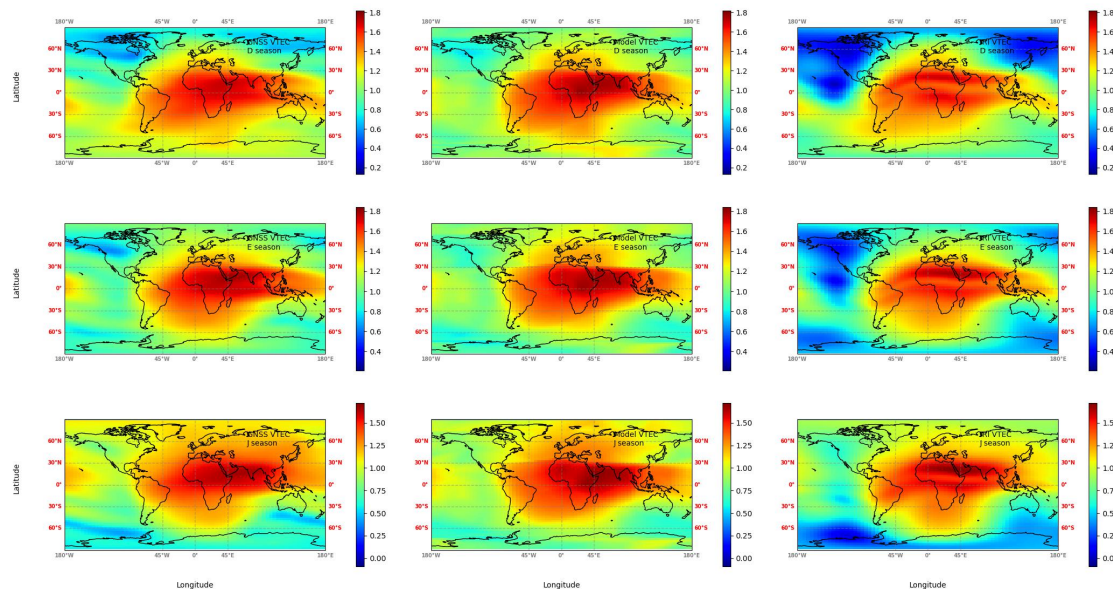
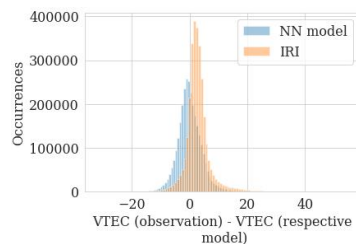


- Diurnal variation in logarithmic scale
- Model captures reasonably well the variations of the target
- Model was compared to 1-step variant and has better performance and reduces overfitting by 62%



- D-season or December solstice: January, February, November, December
- E-season or Equinoxes: March, April, September, October
- J-season or June solstice: June, July, May, August

Type	IRI	NN
RMSE	5.3	4.3
Dist. mean	2.8	-0.09



Future directions

- Incorporate information from tidal waves into the model
- Experiment extensively with data rebalancing techniques for a storm-time model

Summary

- A new approach for modeling VTEC is introduced with separation of global and local component
- The approach introduces significant advantages in terms of computational complexity
- In the global component, the GEC is predicted based on geomagnetic and solar indices
- The agreement of observations and model for GEC is 97 % in terms of correlation
- In the local component, the VTEC is predicted based on GEC and geographic and geomagnetic coordinates
- The final model achieves good results for different solar cycle activity periods

Acknowledgments

This research is supported by the Helmholtz Pilot Projects Information & Data Science II, MACHine learning based Plasma density model project (MAP) - ZT-I-0022.

Additional Slides

Measurements of VTEC

- TEC can be derived from electron density
$$\text{STEC}(x_r, x^s, t) = \int_{x_r}^{x^s} N_e(s, t) ds$$
- TEC can be derived from GNSS measurements
$$P_1 - P_2 = \frac{40.3(f_2^2 - f_1^2)}{f_1^2 f_2^2} \cdot mf(z) \cdot \text{VTEC} + c(\text{DCB}_s + \text{DCB}_r)$$

where P_1 and P_2 are the smoothed dual-frequency code measurements; f_1 and f_2 are the carrier frequencies of the L1 and L2 signals, respectively; mf is the ionospheric mapping function, which depends on the zenith distance z at the receiver's location; VTEC is the vertical TEC at the IPP; c is the speed of light; DCB_s and DCB_r are the differential code biases of satellites and receivers, respectively.

Mutual information and or pearson

- Mutual information in discrete case

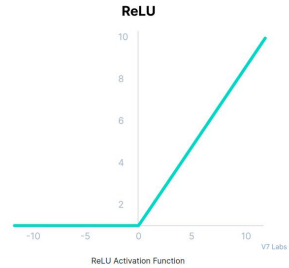
$$I(X; Y) = \sum_{y \in \mathcal{Y}} \sum_{x \in \mathcal{X}} p_{(X,Y)}(x, y) \log \left(\frac{p_{(X,Y)}(x, y)}{p_X(x) p_Y(y)} \right), \quad (\text{Eq. 1})$$

activation functions

- Sigmoid activation function $f(x) = \frac{1}{1 + e^{-x}}$



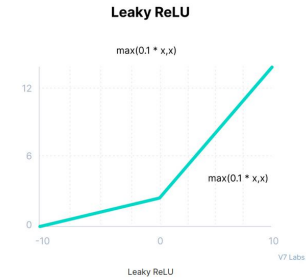
- Rectifier linear unit $f(x) = \max(0, x)$



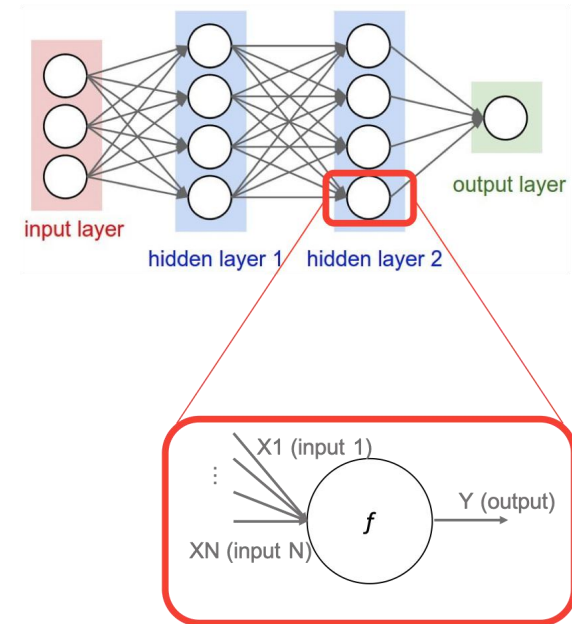
activation functions

- Leaky RELU

$$f(x) = \max(0.1x, x)$$



- Powerful algorithms used for classification, function approximation, pattern recognition, outlier detection etc
- Consist of input, one or more hidden layers and output layer
- Each hidden layer computes linear combination of the previous layer inputs and applies non-linear transformation
- Updates of weights and biases through gradient descent applied on difference between observation and prediction

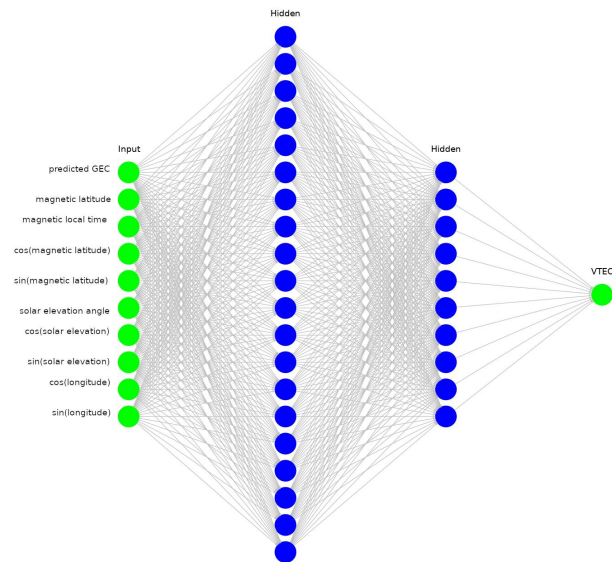


Output of neuron: $Y = f(w_1 * X_1 + \dots w_N * X_N + b)$

Source: Zhelavskaya I. (2020)

- Final neural network was tested on years 2004, 2006, 2011, 2016

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pearson correlation