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NP0 – L.F. Richardson's 1922 centennial

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Global view of oceanic cascades from the Global Circulation Model

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Lewis F. Richardson
1881-1953

Exceptionally low diffusivities have been measured at night by L. F. Richardson (32) in the cold air near the earth. Airmen are very familiar with the increased bumpiness of the wind caused by sun shining on the ground below them. All these facts show that the production of eddies in the wind is greatly facilitated when the thermal equilibrium becomes less stable, although we may not suppose that actual thermal instability is reached in the majority of cases, because such an event is unusual among the collected observations made either by registering balloons or from aeroplanes.

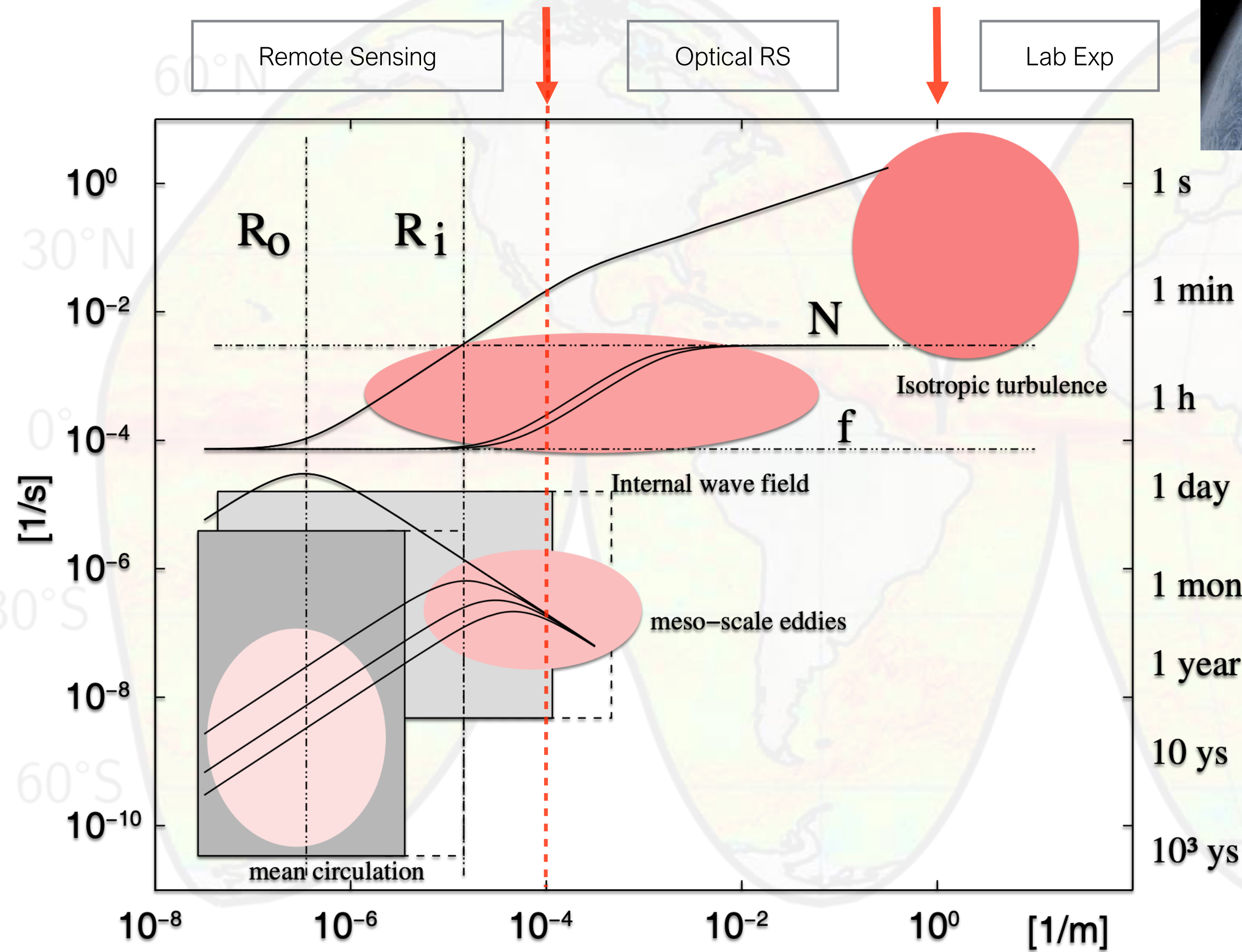
A quantitative theory of the criterion of turbulence has been given by L. F. Richardson (32).

On the other hand we find that convectional motions are hindered by the formation of small eddies resembling those due to dynamical instability. Thus C. K. M. Douglas writing of observations from aeroplanes remarks: "The upward currents of large cumuli give rise to much turbulence within, below, and around the clouds, and the structure of the clouds is often very complex." One gets a similar impression when making a drawing of a rising cumulus from a fixed point; the details change before the sketch can be completed. We realize thus that: big whirls have little whirls that feed on their velocity, and little whirls have lesser whirls and so on to viscosity—in the molecular sense.

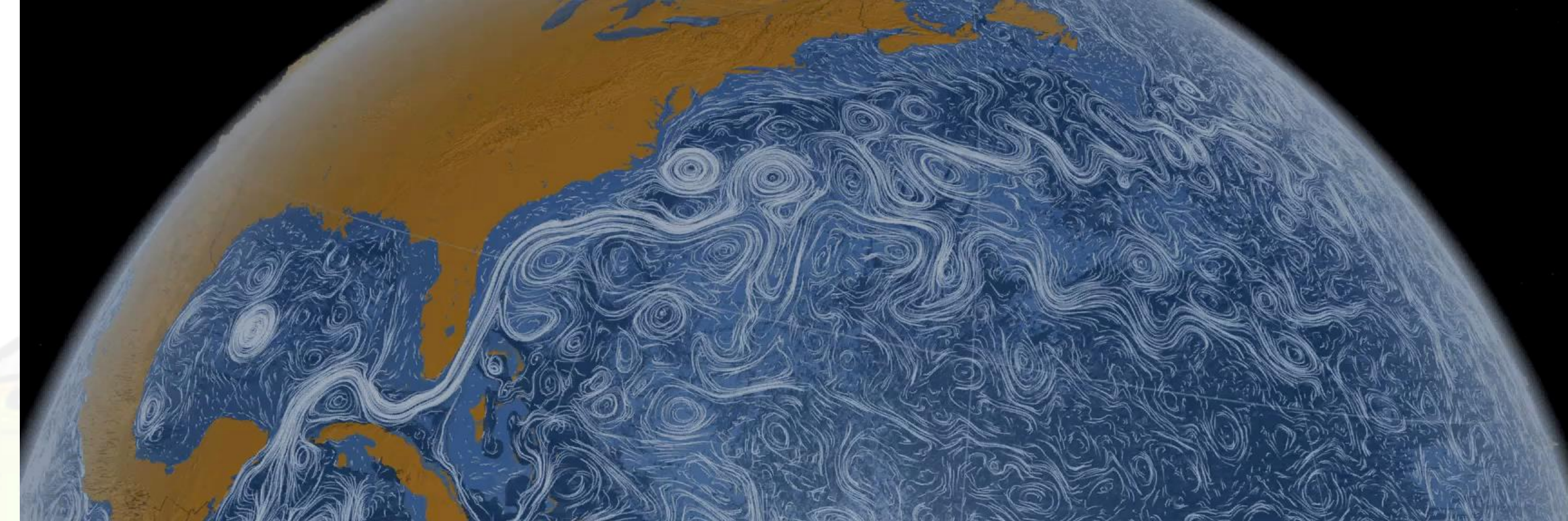
Thus, because it is not possible to separate eddies into clearly defined classes according to the source of their energy; and as there is no object, for present purposes, in making a distinction based on size between cumulus eddies and eddies a few in diameter (since both are small compared with our coordinate chequer), the single coefficient is used to represent the effect produced by eddies of all sizes and descriptions. We have then to study the variations of this coefficient. But we must consider the differential equation. In doing so the aim has been to lay down theoretically only so much as can be determined with strictness, leaving uncertainties to be decided by observation.

Computational Fluid Dynamics

Colorful Fluid Dynamics



Olbers, et al., Ocean Dynamics, 2012



<http://svs.gsfc.nasa.gov/vis/a000000/a003800/a003827/>

Real ocean is much complex than ideally model.

- ▶ Waves, tidal
- ▶ Air-sea interactions
- ▶ Stratification
- ▶ Rotation
- ▶ Large-scale circulation

Models are established based on cascade picture with a lot of parameterizations.

Diagnosing Cascade

3rd structure-functions

Kolmogorov 1941

Derived from NS Eqs



Easy to implement.



Local



Knowing balance



Spectral Method

Inverse-cascade is found for all scales.

Derived from NS Eqs



FFT-based/fast



Global



Regular domains.



Filter-Space-Technique

Large-Eddy-Simulation

Derived from NS Eqs



Heavy comput. cost



Local



Partially continued data



Each method has its own advantages and disadvantages.

Diagnosing Cascade

Filter-Space-Technique

Scale-to-Scale Energy Flux

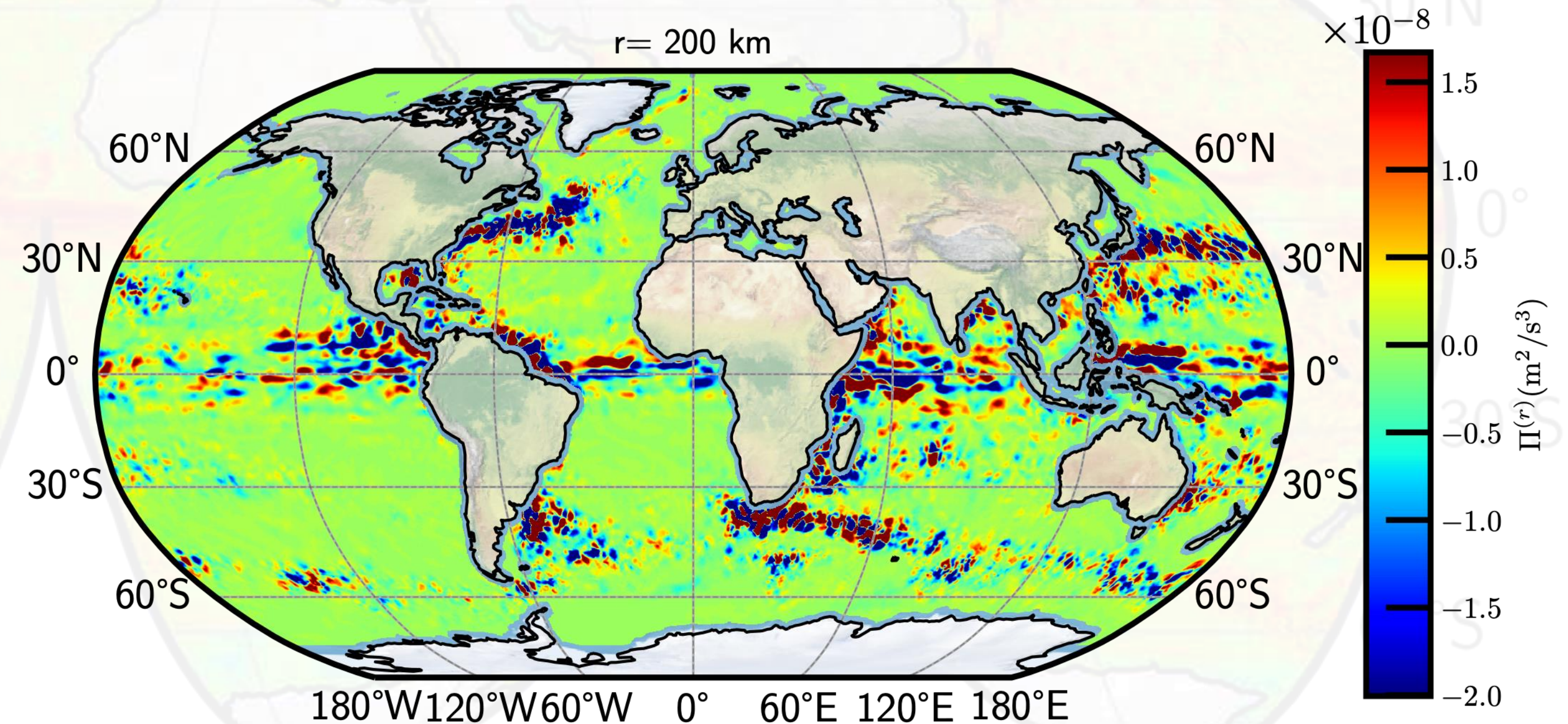
$$\Pi^{(r)}(\vec{x}, t) = - \sum \left((u_i u_j)^{(r)} - u_i^{(r)} u_j^{(r)} \right) \frac{\partial u_i^{(r)}}{\partial x_j}$$

Forward cascade

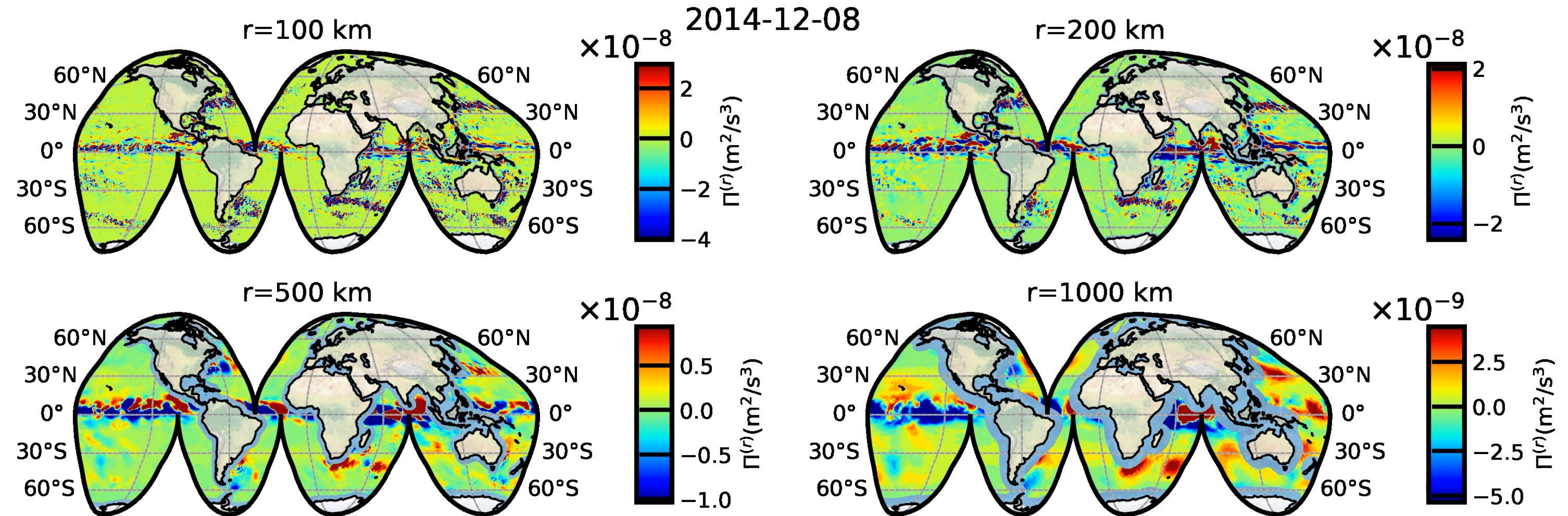
$\Pi^{(r)} > 0$ Energy transfer from large scale to small ones.

Inverse cascade

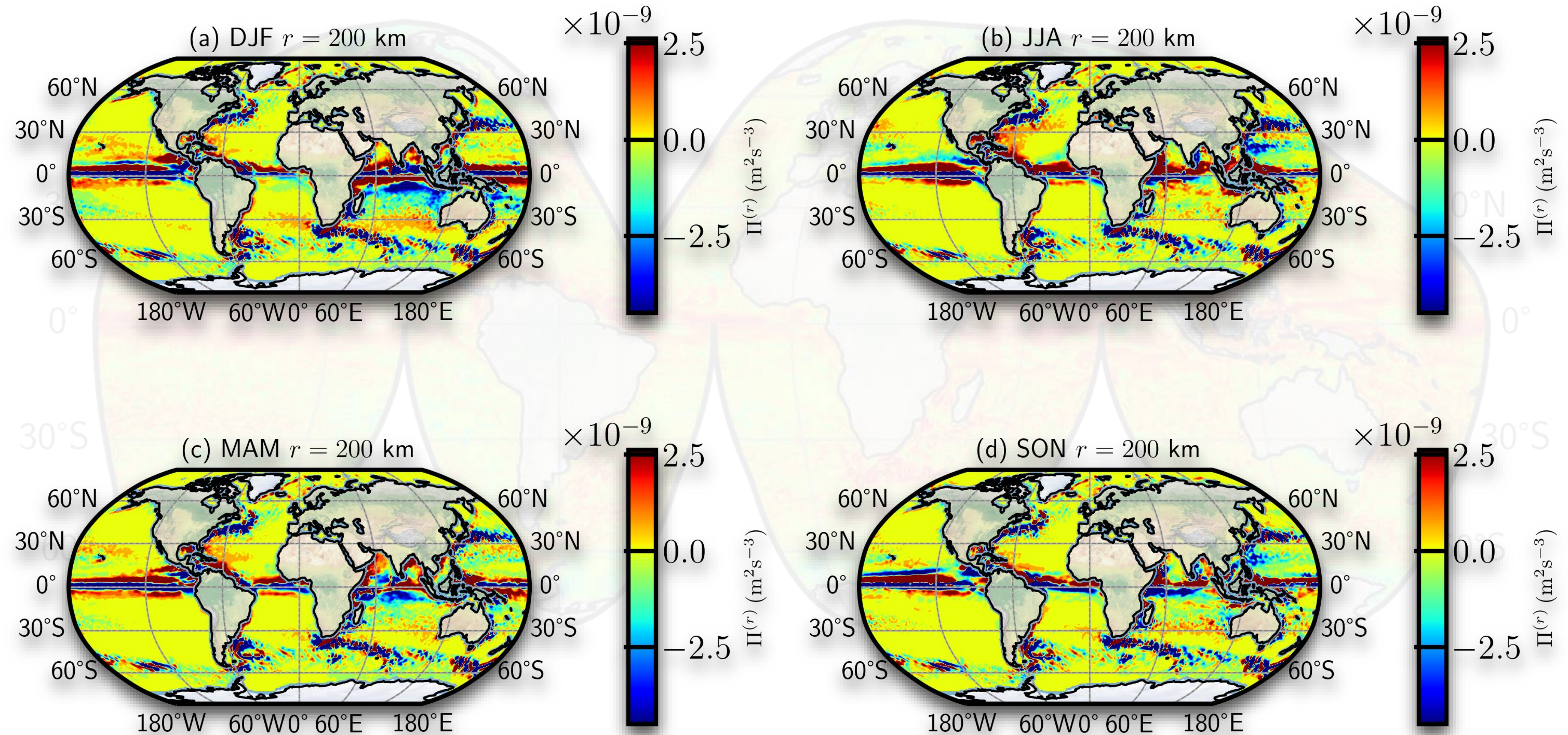
$\Pi^{(r)} < 0$ Energy transfer from small scale to larger ones.



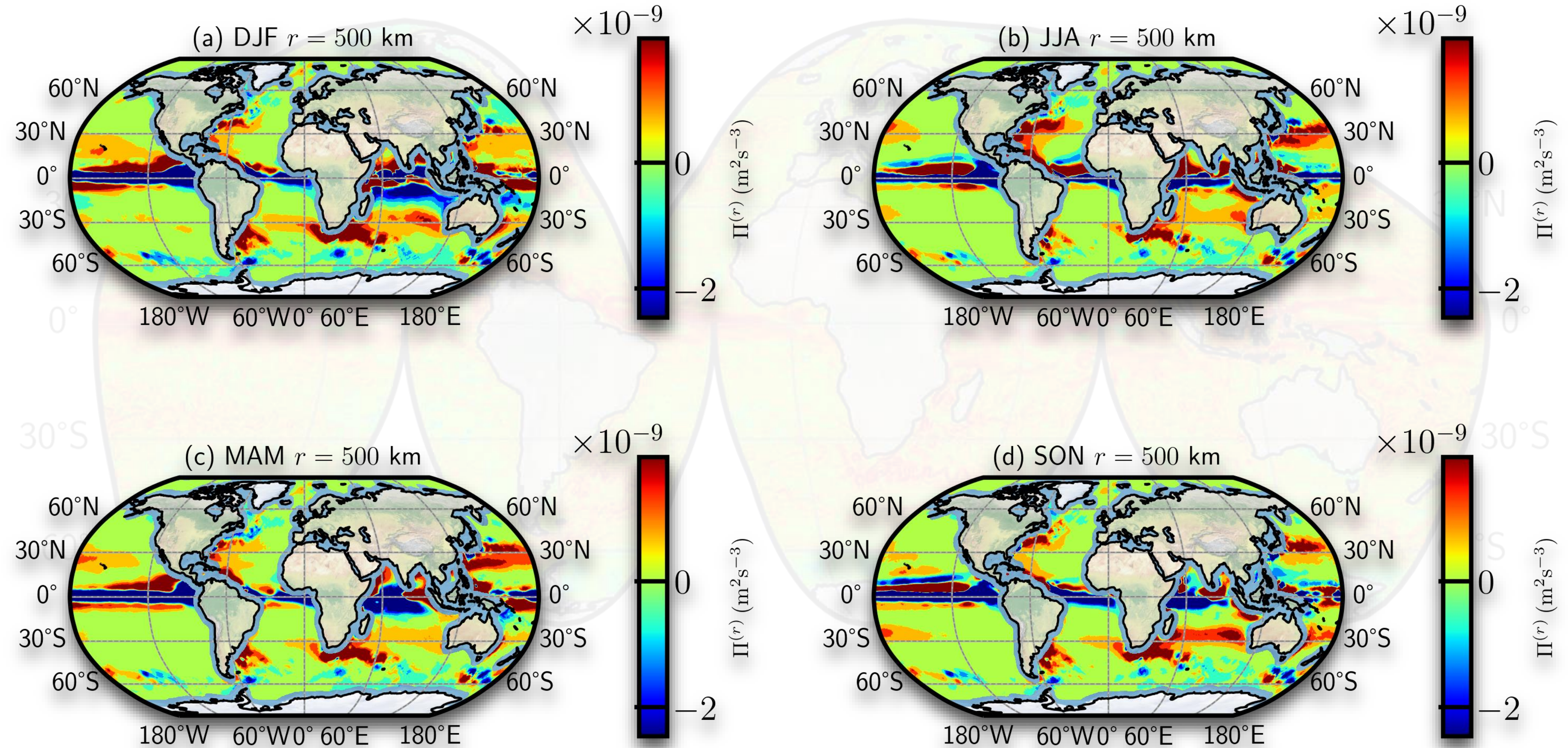
Diagnosing Cascade



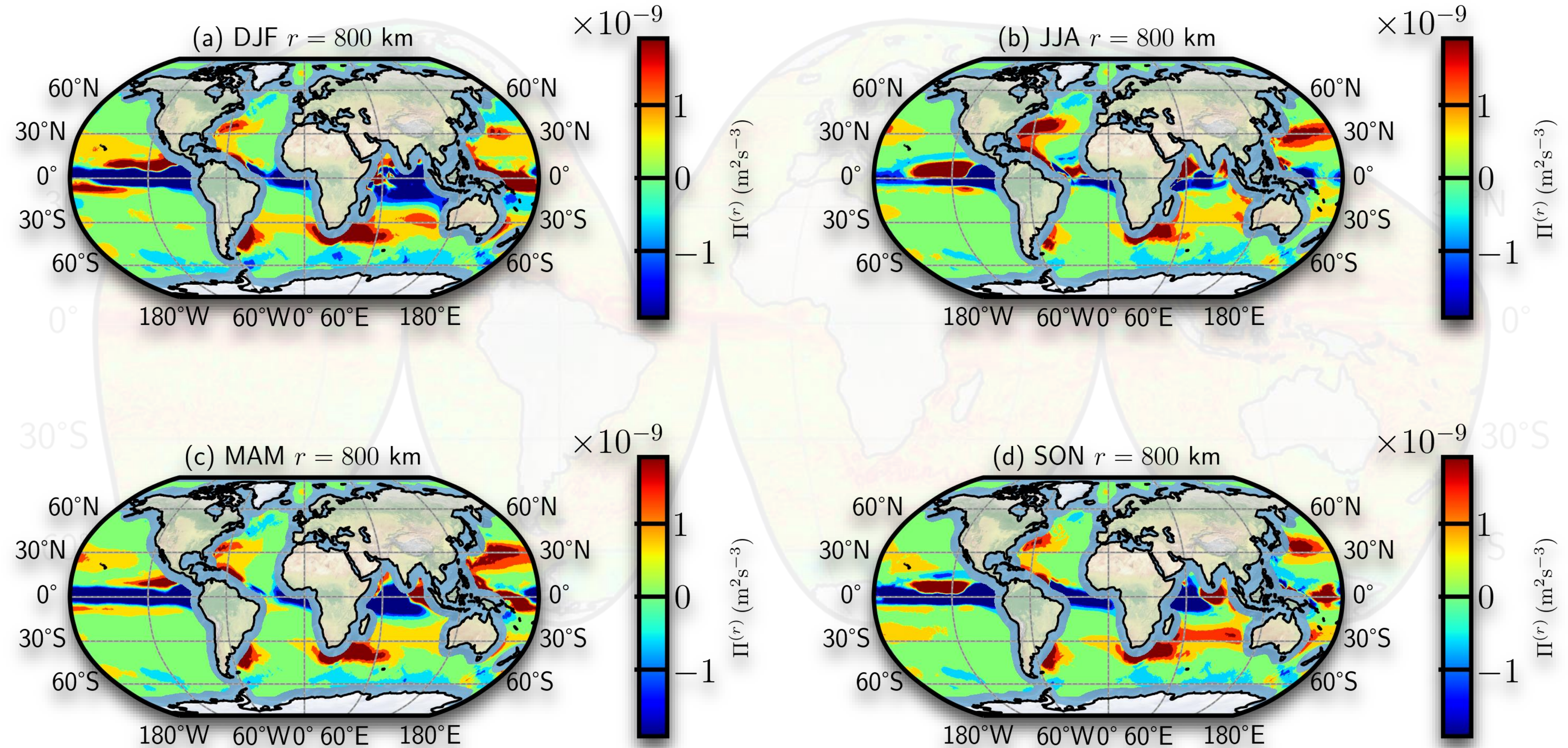
Diagnosing Cascade



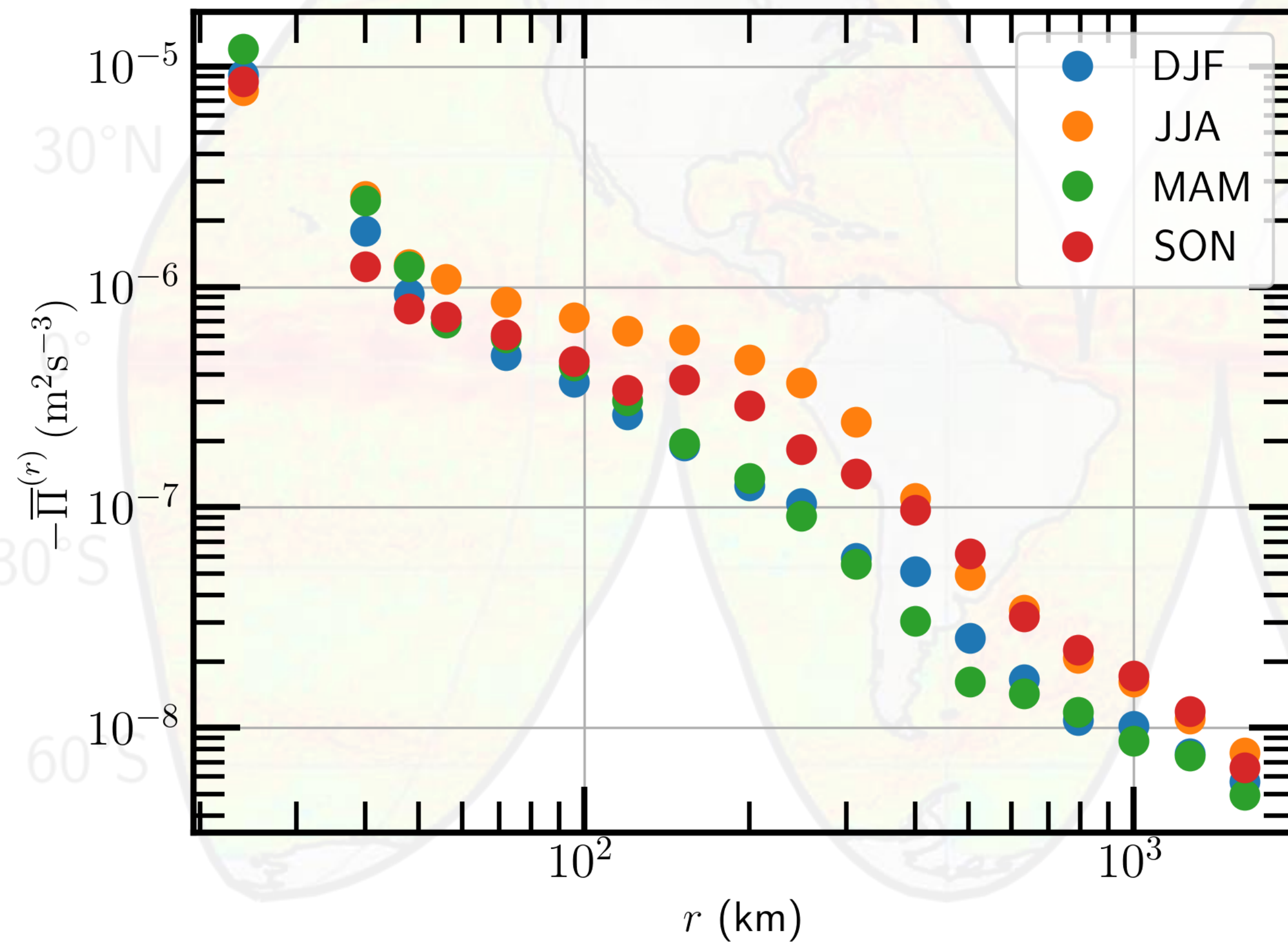
Diagnosing Cascade



Diagnosing Cascade



Diagnosing Cascade



Global average energy flux

Summary

- ▶ Scale-to-Scale energy flux is extracted.
- ▶ An extremely rich dynamics is visible.
- ▶ Seasonable variation is evident.
- ▶ Inverse-cascade is found for all scales.