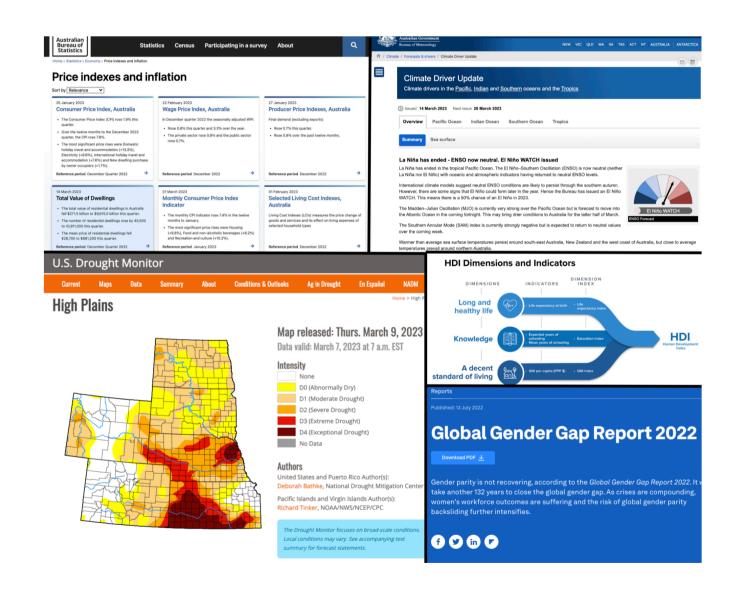
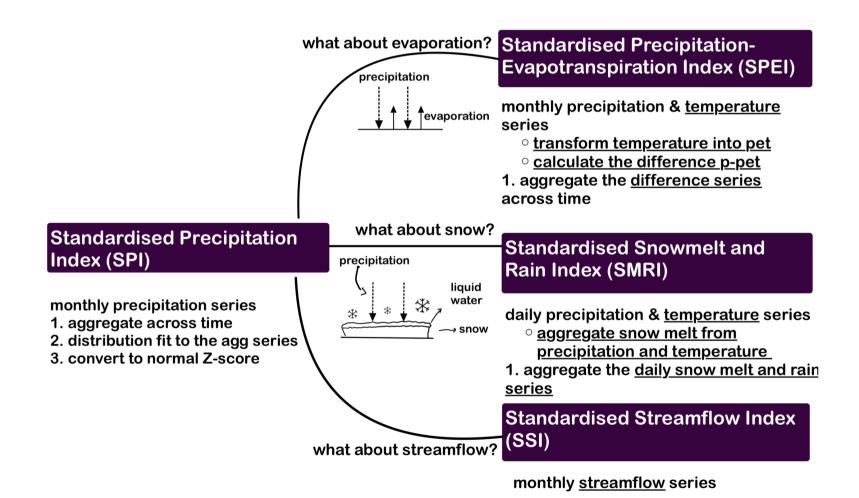
Indexes



A class of drought indexes



Pipeline envisaged

Standardised Precipitation Index (SPI)

data - precipitation %>%
temporal aggregation %>%
distribution fit %>%
augment

Standardised Snowmelt and Rain Index (SMRI)

```
data - precipitation
data - temperature %>%
temporal aggregation %>%
temporal aggregation %>%
distribution fit %>%
augment
```

Standardised Precipitation-Evapotranspiration Index (SPEI)

```
data - precipitation
data - temperature %>%
variable transformation %>%
dimension reduction %>%
temporal aggregation %>%
distribution fit %>%
augment
```

Standardised Streamflow Index (SSI)

```
data - streamflow %>%
temporal aggregation %>%
distribution fit %>%
augment
```

The pipeline design (9 modules)

data with spatial (s) and temporal (t) dimensions:

- Temporal processing: $f_{\psi}(x(s;t))$
- Spatial processing: $g_{\theta}(x(s;t))$

- Variable transformation: $h_{\tau}(x(s;t))$
- Scaling: $[x(s;t) \alpha]/\gamma$
- Normalising: $\Phi^{-1}[x(s;t)]$

- Distribution fit: $F_{\eta}(x(s;t))$
- Benchmarking: u[x(s; t)]
- Dimension reduction

$$x_{p^*}(s;t) \rightarrow x_p(s;t)$$

Simplification

$$\begin{cases} C_0 & c_1 \leq \mathbf{x}(\mathbf{s}; \mathbf{t}) < c_0 \\ C_1 & c_2 \leq \mathbf{x}(\mathbf{s}; \mathbf{t}) < c_1 \\ \dots \\ C_z & c_z \leq \mathbf{x}(\mathbf{s}; \mathbf{t}) \end{cases}$$

Pipeline for two drought indexes - SPI

```
idx_spi <- function(.scale, .dist, ...){</pre>
     data %>%
                                         # data contain `prcp`
       aggregate(.var = prcp,
                                         # step 1: temporal aggregation
                 .scale = .scale)%>%
                                                   aggregate `prcp` with time scale
                                                   `.scale` to create `.agg`, by default
                                         # step 2: distribution fit
       dist_fit(.dist = .dist,
                                       # using L-moment to fit `.dist`
                .method = "lmoms",
                                                   distribution on `.agg`
 9
                .var = .agg) %>%
       augment(.var = .agg)
                                         # step 3: normalising
10
                                                  find the normal density for `.agg`
11
12 }
```

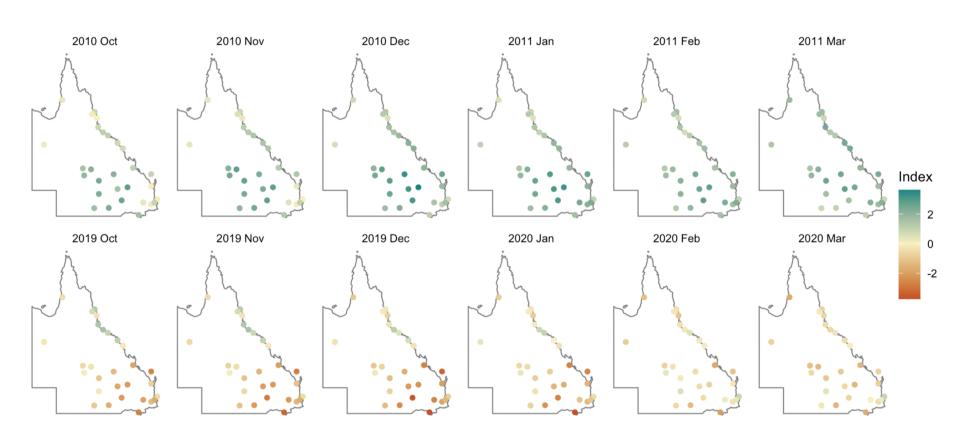
Pipeline for two drought indexes - SPEI

```
idx_spei <- function(.scale, .dist, ...){</pre>
     data %>%
                                                # data contain `tavg` and `prcp`
      var trans
                                                # step 1: variable transformation
                                                          using the thornthwaite function
         .method = "thornthwaite",
         vars = tavq, new name = "pet") %>% #
                                                          on `tavg` to create `pet`
       dim red(diff = prcp - pet) %>%
                                                # step 2: dimension reduction
       aggregate(
                                                # step 3: temporal aggregation
 9
         var = diff,
                                                          aggregate `diff` with time scale
                                                          `.scale` to create `.agg`
         .scale = .scale) %>%
10
                                                # step 4: distribution fit
11
       dist fit(
12
         .dist = .dist, .method = "lmoms",
                                                     using L-moment to fit `.dist`
         .var = .aqq) %>%
                                                          distribution on `.agg`
13
14
       augment(.var = .agg)
                                                # step 5: normalising
15
                                                          find the normal density for `.agg`
16 }
```

Example

```
.scale \leftarrow c(6, 12, 24, 36)
    (idx <- queensland %>%
      init(id = id, time = ym) %>%
 4
      compute indexes(
        spei = idx spei(
          .pet method = "thornthwaite", .tavg = tavg, .lat = lat,
 6
          .scale = .scale, .dist = c(gev(), loglogistic())),
        spi = idx spi(.scale = .scale)
 9
      ))
# A tibble: 128,586 × 19
   .idx
         .period id
                                         tmax tmin tavg long
                                                                   lat name
                               ym
                                   prcp
                                                                                pet
   <chr>
           <dbl> <chr>
                            <mth> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <
               6 ASN00... 1990 Jun
                                         29.7
                                               16.2
                                                    23.0
 1 spei
                                    170
                                                            142. -15.5 KOWA...
                                                                               86.3
                                         29.7
 2 spei
               6 ASN00... 1990 Jun
                                    170
                                               16.2
                                                    23.0
                                                            142. -15.5 KOWA...
                                                                               86.3
                                         23.0
                                               11.8 17.4 139. -20.7 MOUN...
               6 ASN00... 1990 Jun
                                                                               47.6
 3 spei
 4 spei
              6 ASN00... 1990 Jun
                                      0 23.0
                                               11.8 17.4 139. -20.7 MOUN...
                                                                               47.6
                                         25.8
                                                     21.9 146. -16.9 CAIR...
                                                                              80.3
 5 spei
              6 ASN00... 1990 Jun
                                    794
                                               18.1
                                                     21.9 146. -16.9 CAIR...
 6 spei
              6 ASN00... 1990 Jun
                                    794
                                         25.8
                                               18.1
                                                                              80.3
              6 ASN00... 1990 Jun
                                         23.0
                                               13.8
 7 spei
                                    504
                                                     18.4 145. -17.1 WALK...
                                                                              48.2
                                         23.0
                                               13.8
 8 spei
               6 ASN00... 1990 Jun
                                    504
                                                     18.4 145. -17.1 WALK...
                                                                               48.2
                                         23.9
                                               16.4
                                                      20.2 146. -17.6 SOUT...
 9 spei
               6 ASN00... 1990 Jun 1970
                                                                              70.3
               6 ASN00... 1990 Jun
                                  1970
                                         23.9
                                               16.4 20.2 146. -17.6 SOUT...
10 spei
# ... with 128,576 more rows, and 7 more variables: diff <dbl>, .scale <dbl>,
    .agg <dbl>, .method <chr>, .fitted <dbl>, .dist <chr>, .index <dbl>
```

2010 Queensland flood & 2019-20 Australia drought



All time scales agree on an extreme drought in 2019-20 bushfire season

