

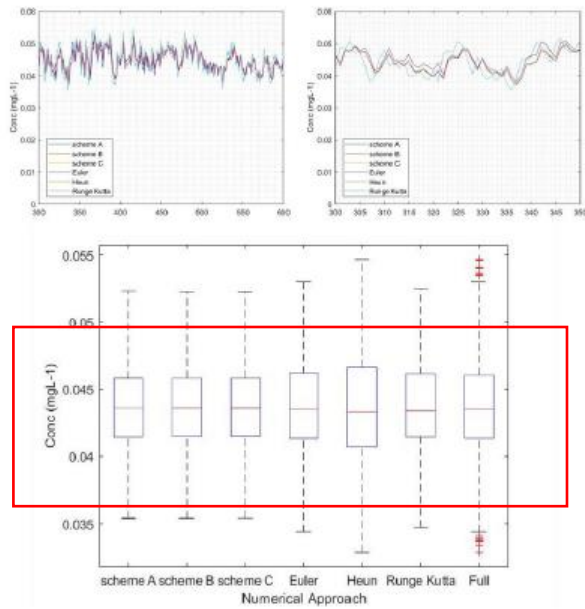
Comparison between numerical and parametrical uncertainty in the application of simplified water quality models

Joana Postal Pasqualini and Fernando Mainardi Fan

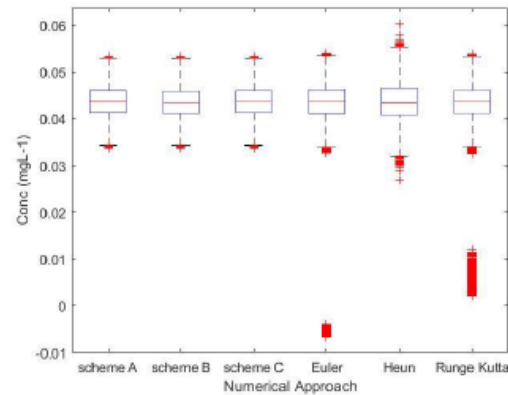
Hydrological condition A: low storage oscillation

Hydrological condition B: constant storage oscillation

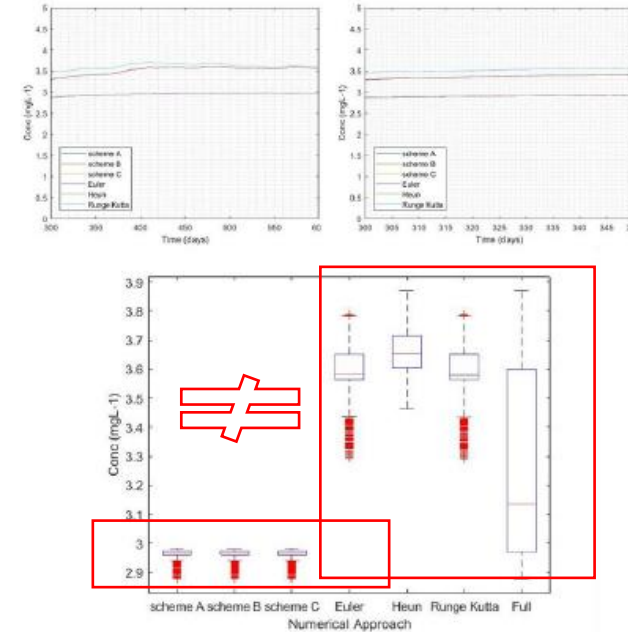
Numerical



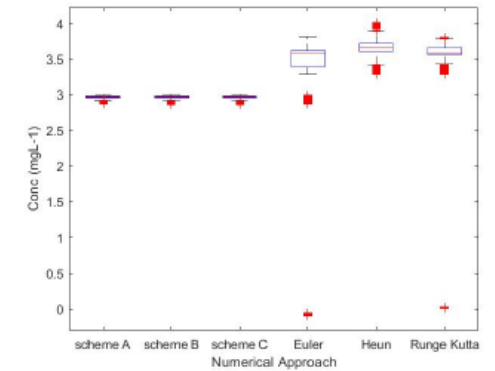
Parametrical



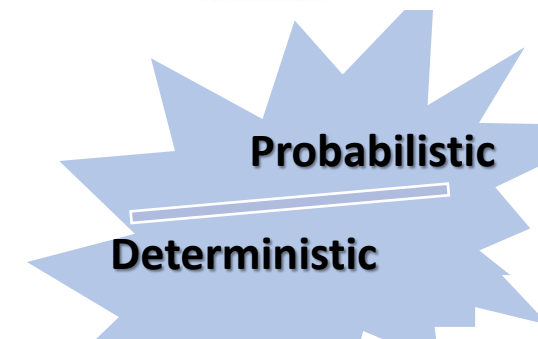
Numerical

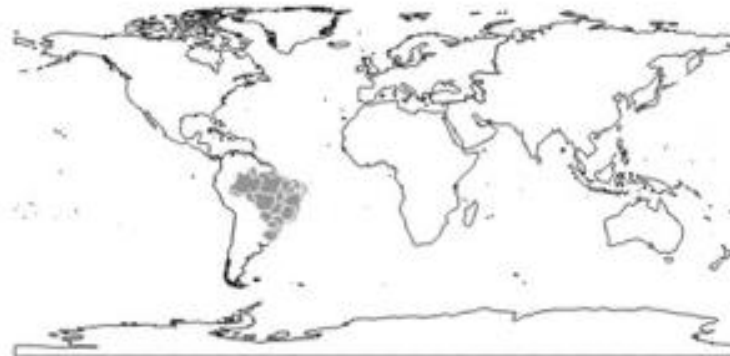
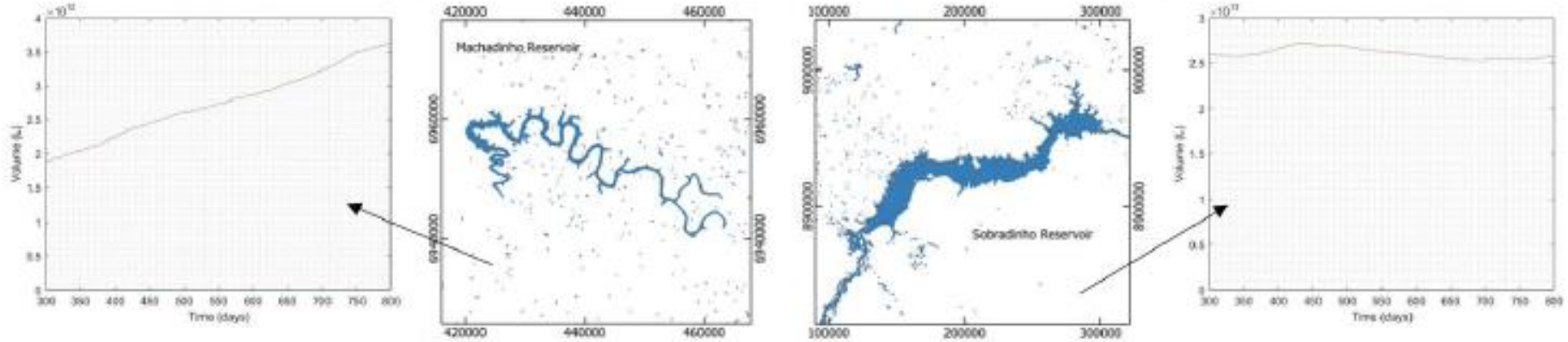
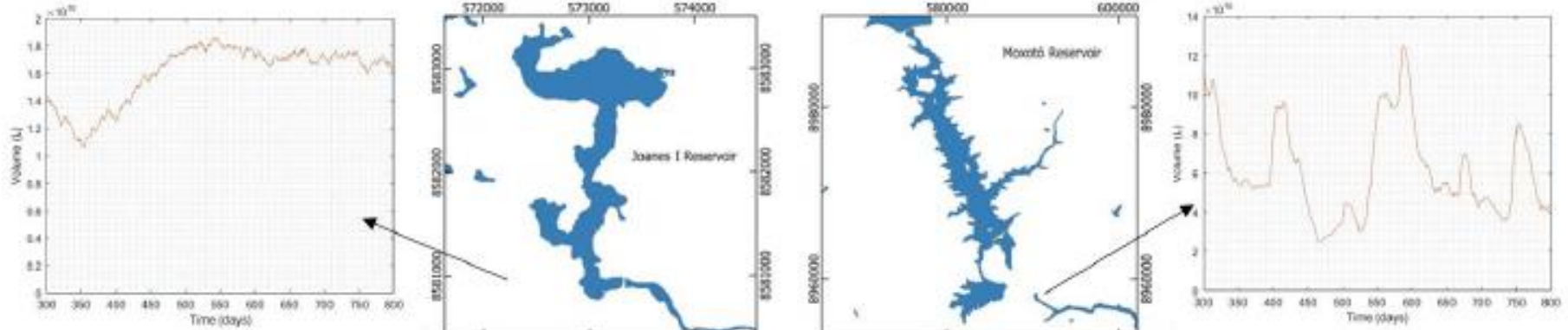


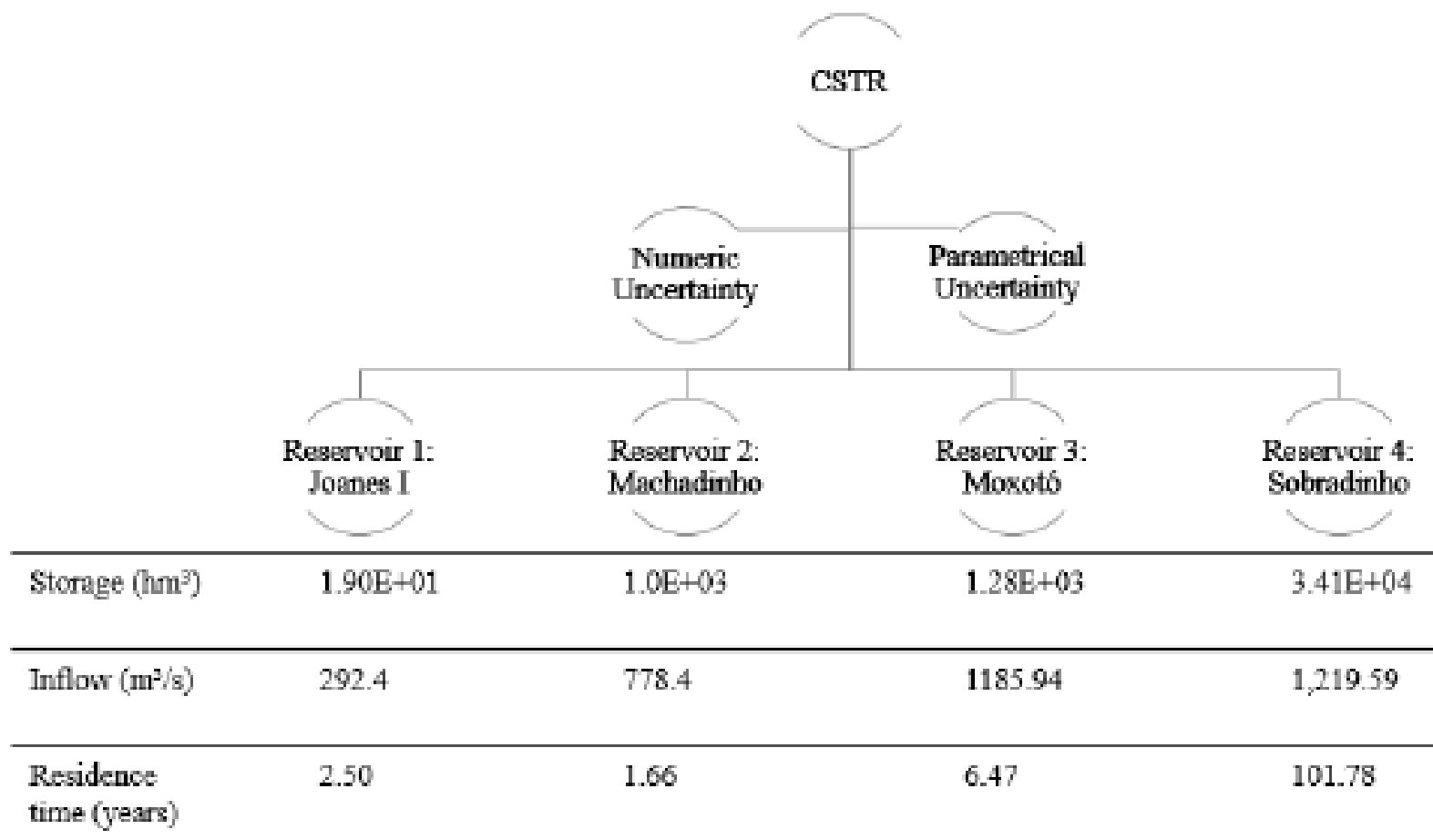
Parametrical



➡ **Uncertainties should be considered for better decision-making**



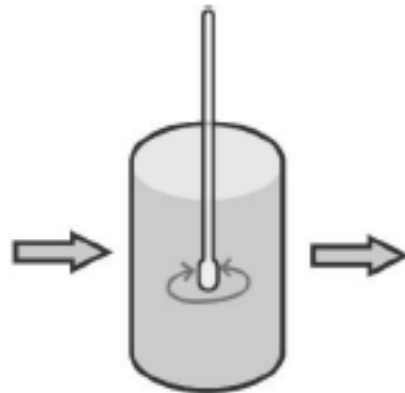




Data	Type	Source	Collection frequency
Flow	Variable	Embasa, National Water and Sanitation Agency (ANA)	Daily
Inflow concentrations	Variable	Embasa, Institute for the Environment and Water Resources, São Francisco Hydroelectric Company, National Water and Sanitation Agency (ANA)	Monthly and bimonthly
Reservoir capacity	Variable	Embasa, National Water and Sanitation Agency (ANA)	Daily
Production rate	Parameter	*	-
Consumption rate	Parameter	*	-

*estimated according to the residence time of each reservoir (Salas and Martino, 1991)

Mass accumulation = Mass in – Mass out + Sources – Sinks



$$\frac{d(C.V)}{dt} = Q_{in} \times C_{in} - Q_{out} \times C_{out} + r_p \times V - r_c \times V$$

I – Numeric Ensemble

Numerical Uncertainty consisted on the test of six different numerical approaches in solving the same CSTR problem

II – Parametrical Ensemble

Parametrical Uncertainty consisted on the probabilistic test according to Monte Carlo methodology, with a parameters variation of 20% and 50% among normal distribution for each numeric method, in each study area.

Question 1

Do different numerical approaches result in statistically different results in a deterministic approach?



Yes, it is possible to obtain statically different results especially in case studies with distinct volumetric ascension or recession.

Question 2

Which numerical method is less sensitive to parameters?



No different sensibility for situations of gradual volumetric oscillation over time.

Heun : most sensitive method for the greater volumetric oscillation.

3 Is it the uncertainty of the parameters or is the uncertainty of the numerical methods that generate the greatest range of possibilities?



metric oscillation: equivalent in proportion.

changes: numerical uncertainty exceeds the parametrical

15%

30%

Question 4

Which uncertainty source confers greatest proportion of possibilities?



Input Data.

40% - 70%.

(RADWAN; WIL
BERLAMONT, 20
WILLEMS, P., 20

Question 5

Is it possible to dissociate the structural uncertainty into numerical and parametrical for a simple application?



No.

we can have an idea of its estimate/proportion

Question 6

What is the benefit of knowing considering probabilistic risk for a simple application? Are there any for which there are more benefits?



Considering the probability of deviation from the deterministic result.

And collaborating for risk management engineering problem in question.

Main References

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THANK YOU!

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