

Package ‘WaverideR’

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Type Package

Title Extracting Signals from Wavelet Spectra

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Depends R (>= 3.5.0)

Imports DecomposeR, DescTools, Hmisc, Matrix,utils,
colorednoise, doSNOW, fANCOVA, foreach,stats,tcltk,
matrixStats,reshape2,truncnorm,grDevices,graphics,parallel

Description The continuous wavelet transform enables the observation of transient/non-stationary cyclicity in time-series. The goal of cyclostratigraphic studies is to define frequency/period in the depth/time domain. By conducting the continuous wavelet transform on cyclostratigraphic data series one can observe and extract cyclic signals/signatures from signals. These results can then be visualized and interpreted enabling one to identify/interpret cyclicity in the geological record, which can be used to construct astrochronological age-models and identify and interpret cyclicity in past en present climate systems.

License GPL (>= 2)

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Suggests testthat (>= 3.0.0)

Config/testthat/edition 3

R topics documented:

achor2time	2
age_model_zeeden	3
analyze_wavelet	4
astro_anchor	5
completed_series	11
curve2sedrate	13
curve2time	14
curve2tune	16
extract_power	17
extract_power_stable	19

extract_signal	20
extract_signal_stable	22
extract_signal_stable_V2	23
extract_signal_standard_deviation	24
grey	27
grey_track	27
Hilbert_transform	28
loess_auto	29
mag	30
mag_track_solution	31
max_detect	31
min_detect	32
model_red_noise_wt	33
percentile_from_red_noise	34
plot_avg_wavelet	35
plot_wavelet	36
sum_power_sedrate	38
track_period_wavelet	40
TSI	41
wavelet_uncertainty	42
WaverideR	44
WaverideR_Datasets	45
Index	46

achor2time

Convert a proxy record to the time domain using anchor points

Description

Convert a proxy record to the time domain using anchor points made using the [astro_anchor](#) function.

Usage

```
achor2time(anchor_points = NULL, data = NULL, genplot = TRUE)
```

Arguments

anchor_points	Anchor points made using the astro_anchor function or a matrix in which the first column is depth and the second column is time.
data	Data set which needs to be converted from the depth to time domain using set anchor points. The data set should consist of a matrix with 2 column the first column should be depth and the second column should be a proxy value.
genplot	If genplot=TRUE then 3 plots stacked on top of each other will be plotted. Plot 1: the original dataset Plot 2: the depth time plot Plot 3: the dataset in the time domain

Value

The output is a matrix with 2 columns. The first column is time. The second column sedimentation proxy value.

If `genplot=TRUE` then 3 plots stacked on top of each other will be plotted. Plot 1: the original dataset. Plot 2: the depth time plot. Plot 3: the dataset in the time domain.

Examples

```
# Use the age_model_zeeden example anchor points of Zeeden et al., (2013) \cr  
#to anchor the grey data set of Zeeden et al., (2013) in the time domain.
```

```
achored2time <- achor2time(anchor_points=age_model_zeeden,  
data=grey,  
genplot=TRUE)
```

age_model_zeeden	<i>Age model of Zeeden et al., (2013) for the (154-174m) interval of the IODP 926 grey scale record</i>
------------------	---

Description

Age model (anchor points) of the IODP 926 grey scale (154-174m) record of Zeeden et al., (2013) Anchored to the eccentricity-tilt-precession model p-0.5t of la 2004.

Details

Column 1: Depth (meters)
Column 2: Age (kyr)

References

Christian Zeeden, Frederik Hilgen, Thomas Westerhold, Lucas Lourens, Ursula Röhl, Torsten Bickert, Revised Miocene splice, astronomical tuning and calcareous plankton biochronology of ODP Site 926 between 5 and 14.4Ma, Palaeogeography, Palaeoclimatology, Palaeoecology, Volume 369,2013,Pages 430-451,ISSN 0031-0182, <doi:10.1016/j.palaeo.2012.11.009>

Laskar, Jacques, Philippe Robutel, Frédéric Joutel, Mickael Gastineau, Alexandre CM Correia, and Benjamin Levrard. "A long-term numerical solution for the insolation quantities of the Earth. " Astronomy & Astrophysics 428, no. 1 (2004): 261-285. <https://www.aanda.org/articles/aa/pdf/2004/46/aa1335.pdf>

analyze_wavelet	<i>Computes the wavelet power spectrum of a time series/signal</i>
-----------------	--

Description

Compute the continuous wavelet transform (CWT) using a Morlet wavelet

Usage

```
analyze_wavelet(
  data = NULL,
  dj = 1/20,
  lowerPeriod = 2,
  upperPeriod = 1024,
  verbose = TRUE,
  omega_nr = 6
)
```

Arguments

data	Input data, should be a matrix or data frame in which the first column is depth or time and the second column is proxy record.
dj	Spacing between successive scales Default=1/200.
lowerPeriod	Lowest period to be analyzed Default=2, scaling is done using power 2 so for the best plotting results select a value to the power or 2.
upperPeriod	Upper period to be analyzed Default=1024, scaling is done using power 2 so for the best plotting results select a value to the power or 2.
verbose	Print text Default=TRUE.
omega_nr	Number of cycles contained within the wavelet.

Value

The output is a list (wavelet object) with the results of the continuous wavelet transform (CWT).

Author(s)

Code based on the R package [WaveletComp-package](#) and [biwavelet-package](#) which are based on the wavelet MATLAB code written by Christopher Torrence and Gibert P. Compo.

References

Angi Roesch and Harald Schmidbauer (2018). WaveletComp: Computational Wavelet Analysis. R package version 1.1. <https://CRAN.R-project.org/package=WaveletComp>

Gouhier TC, Grinsted A, Simko V (2021). R package biwavelet: Conduct Univariate and Bivariate Wavelet Analyses. (Version 0.20.21), <https://github.com/tgouhier/biwavelet>

Torrence, C., and G. P. Compo. 1998. A Practical Guide to Wavelet Analysis. Bulletin of the American Meteorological Society 79:61-78.

Examples

```
#Example 1. Using the Total Solar Irradiance data set of Steinhilber et al., (2012)
TSI_wt <-
  analyze_wavelet(
    data = TSI,
    dj = 1/200,
    lowerPeriod = 16,
    upperPeriod = 8192,
    verbose = TRUE,
    omega_nr = 6
  )
```

```
#Example 2. Using the magnetic susceptibility data set of De pas et al., (2018)
mag_wt <-
  analyze_wavelet(
    data = mag,
    dj = 1/100,
    lowerPeriod = 0.1,
    upperPeriod = 254,
    verbose = TRUE,
    omega_nr = 10
  )
```

```
#Example 3. Using the greyscale data set of Zeeden et al., (2013)
grey_wt <-
  analyze_wavelet(
    data = grey,
    dj = 1/200,
    lowerPeriod = 0.02,
    upperPeriod = 256,
    verbose = TRUE,
    omega_nr = 8
  )
```

astro_anchor

Anchor proxy record to an astronomical solution

Description

Anchor the extracted signal to an astronomical solution using a GUI. The `astro_anchor` function allows one to tie minima or maxima in the proxy record to minima or maxima in an astronomical solution. By tying the proxy record to an astronomical solution one will generate tie-points which can be used to generate a astrochronological age-model. As minima or maxima in the proxy record are tied to minima or maxima in an astronomical solution it is important to provide input which has clearly definable minima and maxima. As such input should be of a "sinusoidal" nature otherwise the `extract_astrosolution=TRUE` and/or `extract_proxy_signal=TRUE` options need to be set to TRUE to create sinusoidal signals.

Astronomical solutions option are:

- La2004 Eccentricity solution available via the `getLaskar` function or downloadable via <http://vo.imcce.fr/insola/earth/online/earth/earth.html>

- La2004 Obliquity solution available via the [getLaskar](#) function or downloadable via <http://vo.imcce.fr/insola/earth/online/earth/earth.html>
- La2004 Precession solution available via the [getLaskar](#) function or downloadable via <http://vo.imcce.fr/insola/earth/online/earth/earth.html>
- La2010a Eccentricity solution available via the [getLaskar](#) function or downloadable via <http://vo.imcce.fr/insola/earth/online/earth/earth.html>
- La2010a Obliquity solution downloadable via the <http://vo.imcce.fr/insola/earth/online/earth/earth.html>
- La2010a Precession solution downloadable via <http://vo.imcce.fr/insola/earth/online/earth/earth.html>
- La2010b Eccentricity solution available via the [getLaskar](#) function or downloadable via <http://vo.imcce.fr/insola/earth/online/earth/earth.html>
- La2010b Obliquity solution downloadable via <http://vo.imcce.fr/insola/earth/online/earth/earth.html>
- La2010b Precession solution downloadable via <http://vo.imcce.fr/insola/earth/online/earth/earth.html>
- La2010c Eccentricity solution available via the [getLaskar](#) function or downloadable via <http://vo.imcce.fr/insola/earth/online/earth/earth.html>
- La2010c Obliquity solution downloadable via <http://vo.imcce.fr/insola/earth/online/earth/earth.html>
- La2010c Precession solution downloadable via <http://vo.imcce.fr/insola/earth/online/earth/earth.html>
- La2010d Eccentricity solution available via the [getLaskar](#) function or downloadable via <http://vo.imcce.fr/insola/earth/online/earth/earth.html>
- La2010d Obliquity solution downloadable via <http://vo.imcce.fr/insola/earth/online/earth/earth.html>
- La2010d Precession solution downloadable via <http://vo.imcce.fr/insola/earth/online/earth/earth.html>
- La2011 Eccentricity solution available via the [getLaskar](#) function or downloadable via <http://vo.imcce.fr/insola/earth/online/earth/earth.html>
- ZB17a Eccentricity solution downloadable via https://www.soest.hawaii.edu/oceanography/faculty/zeebe_files/Astro.html
- ZB17a Obliquity solution downloadable via https://www.soest.hawaii.edu/oceanography/faculty/zeebe_files/Astro.html
- ZB17b Eccentricity solution downloadable via https://www.soest.hawaii.edu/oceanography/faculty/zeebe_files/Astro.html
- ZB17b Obliquity solution downloadable via https://www.soest.hawaii.edu/oceanography/faculty/zeebe_files/Astro.html
- ZB17c Eccentricity solution downloadable via https://www.soest.hawaii.edu/oceanography/faculty/zeebe_files/Astro.html
- ZB17c Obliquity solution downloadable via https://www.soest.hawaii.edu/oceanography/faculty/zeebe_files/Astro.html
- ZB17d Eccentricity solution downloadable via https://www.soest.hawaii.edu/oceanography/faculty/zeebe_files/Astro.html
- ZB17d Obliquity solution downloadable via https://www.soest.hawaii.edu/oceanography/faculty/zeebe_files/Astro.html

- ZB20d Obliquity solution downloadable via https://www.soest.hawaii.edu/oceanography/faculty/zeebe_files/Astro.html
- 405kyr eccentricity 405 metronome can be generated using the formula:
 $e_{405} = 0.027558 - 0.010739 \cdot \cos(0.0118 + 2(\pi) \cdot (t/405000))$ (laskar et al., 2004 & laskar 2020)
- 173kyr obliquity metronome can be generated using using the formula:
 $es_3-s_6(t) = 0.144 \cdot \cos(1.961 + 2(\pi) \cdot (t/172800))$ (laskar et al., 2004 & laskar 2020)
- An etp model using the `etp` function of the [astrochron-package](#) package

Usage

```
astro_anchor(
  astro_solution = NULL,
  proxy_signal = NULL,
  proxy_min_or_max = "max",
  clip_astrosolution = FALSE,
  astrosolution_min_or_max = "max",
  clip_high = NULL,
  clip_low = NULL,
  extract_astrosolution = FALSE,
  astro_period_up = 1.2,
  astro_period_down = 0.8,
  astro_period_cycle = NULL,
  extract_proxy_signal = FALSE,
  proxy_period_up = 1.2,
  proxy_period_down = 0.8,
  proxy_period_cycle = NULL
)
```

Arguments

- `astro_solution` Input is an astronomical solution which the proxy record will be anchored to, the input should be a matrix or data frame with the first column being age and the second column should be a insolation/angle/value
- `proxy_signal` Input is the proxy data set which will be anchored to an astronomical solution, the input should be a matrix or data frame with the first column being depth/time and the second column should be a proxy value. For the best results either the astronomical components need to be pre-extracted before anchoring. This means that a filtering/cycle extracting need to be applied to the input data or the `extract_proxy_signal` option needs to be set to TRUE.
- `proxy_min_or_max` Tune proxy maxima or minima to the astronomical solution Default="max".
- `clip_astrosolution` Clip the astronomical solution Default=FALSE.
- `astrosolution_min_or_max` Tune to maximum or minimum values of the astronomical solution Default="max"
- `clip_high` Upper value to clip to.
- `clip_low` Lower value to clip to.
- `extract_astrosolution` Extract a certain astronomical cycle/component from a astronomical solution prior to anchoring Default=FALSE.

astro_period_up	Upper bound of the astronomical cycle which is extracted from an astronomical solution. The upper bound value is a factor with which the astronomical component is multiplied by. Default=1.2
astro_period_down	Lower bound of the astronomical cycle which is extracted from an astronomical solution. The upper bound value is a factor with which the astronomical component is multiplied by. Default=0.8
astro_period_cycle	Period (in kyr) of the to be extracted astronomical component from the astronomical solution.
extract_proxy_signal	Extract a certain astronomical cycle/component from a proxy signal Default=FALSE.
proxy_period_up	Upper bound of the astronomical cycle to be extracted from the proxy record. The upper bound value is a factor with which the astronomical component is multiplied by. Default=1.2.
proxy_period_down	Upper bound of the astronomical cycle to be extracted from the proxy record. The lower bound value is a factor with which the astronomical component is multiplied by. Default=0.8.
proxy_period_cycle	Period in kyr of the astronomical cycle/component which is extracted from the proxy record.

Value

The output is a matrix with the 4 columns. The first column is the depth/time of the proxy tie-point. The second column is the time value of the astronomical solution tie-point. The third column is the proxy value of the proxy tie-point. The fourth column is the proxy/insolation value of the astronomical solution tie-point.

References

- J. Laskar, P. Robutel, F. Joutel, M. Gastineau, A.C.M. Correia, and B. Levrard, B., 2004, A long term numerical solution for the insolation quantities of the Earth: *Astron. Astrophys.*, Volume 428, 261-285.
- Laskar, J., Fienga, A., Gastineau, M., Manche, H., 2011a, La2010: A new orbital solution for the long-term motion of the Earth: *Astron. Astrophys.*, Volume 532, A89
- Laskar, J., Gastineau, M., Delisle, J.-B., Farres, A., Fienga, A.: 2011b, Strong chaos induced by close encounters with Ceres and Vesta, *Astron: Astrophys.*, Volume 532, L4.
- J. Laskar, Chapter 4 - *Astrochronology*, Editor(s): Felix M. Gradstein, James G. Ogg, Mark D. Schmitz, Gabi M. Ogg, *Geologic Time Scale 2020*, Elsevier, 2020, Pages 139-158, ISBN 9780128243602, <doi:10.1016/B978-0-12-824360-2.00004-8> or <https://www.sciencedirect.com/science/article/pii/B9780128243602000048>
- Zeebe, R. E. and Lourens, L. J. Geologically constrained astronomical solutions for the Cenozoic era, *Earth and Planetary Science Letters*, 2022
- Zeebe, R. E. and Lourens, L. J. Solar system chaos and the Paleocene-Eocene boundary age constrained by geology and astronomy. *Science*, <doi:10.1126/science.aax0612>
- Zeebe, R. E. Numerical Solutions for the orbital motion of the Solar System over the Past 100 Myr: Limits and new results. *The Astronomical Journal*, 2017

Examples

```
## Not run:
# Use the \code{grey_track} example tracking points to anchor the grey scale data set \cr
# of Zeeden et al., (2013) to the p-0.5t la2004 solution

grey_wt <-
  analyze_wavelet(
    data = grey,
    dj = 1/200,
    lowerPeriod = 0.02,
    upperPeriod = 256,
    verbose = TRUE,
    omega_nr = 8
  )

grey_track <- completed_series(
  wavelet = grey_wt,
  tracked_curve = grey_track,
  period_up = 1.25,
  period_down = 0.75,
  extrapolate = TRUE,
  genplot = FALSE
)
# Extract precession, obliquity and eccentricity to create a synthetic insolation curve

grey_prec <- extract_signal(
  tracked_cycle_curve = grey_track[,c(1,2)],
  wavelet = grey_wt,
  period_up = 1.2,
  period_down = 0.8,
  add_mean = FALSE,
  tracked_cycle_period = 22,
  extract_cycle = 22,
  tune = FALSE,
  plot_residual = FALSE
)

grey_obl <- extract_signal(
  tracked_cycle_curve = grey_track[,c(1,2)],
  wavelet = grey_wt,
  period_up = 1.2,
  period_down = 0.8,
  add_mean = FALSE,
  tracked_cycle_period = 22,
  extract_cycle = 110,
  tune = FALSE,
  plot_residual = FALSE
)

grey_ecc <- extract_signal(
  tracked_cycle_curve = grey_track[,c(1,2)],
  wavelet = grey_wt,
  period_up = 1.25,
  period_down = 0.75,
  add_mean = FALSE,
  tracked_cycle_period = 22,
```

```

extract_cycle = 40.8,
tune = FALSE,
plot_residual = FALSE
)

insolation_extract <- cbind(grey_ecc[,1],grey_prec[,2]+grey_obl[,2]+grey_ecc[,2]+mean(grey[,2]))
insolation_extract <- as.data.frame(insolation_extract)
insolation_extract_mins <- min_detect(insolation_extract)

#download ETP solution (p-0.5t la2004 solution) from the astrochron package \cr
#to create a insolation curve.
#install.packages("astrochron") if not install package.
#library("astrochron") load package to download p-0.5t la2004 solution.

astrosignal=astrochron::etp(tmin=5000,tmax=6000,pWt=1,oWt=-0.5,eWt=0,genplot=FALSE,verbose=FALSE)
astrosignal[,2] <- -1*astrosignal[,2]
astrosignal <- as.data.frame(astrosignal)

#anchor the synthetic insolation curve extracted from the greyscale record to the insolation curve.

anchor_points <- astro_anchor(
astro_solution = astrosignal,
proxy_signal = insolation_extract,
proxy_min_or_max = "min",
clip_astrosolution = FALSE,
astrosolution_min_or_max = "min",
clip_high = NULL,
clip_low = NULL,
extract_astrosolution = FALSE,
astro_period_up = NULL,
astro_period_down = NULL,
astro_period_cycle = NULL,
extract_proxy_signal = FALSE,
proxy_period_up = NULL,
proxy_period_down = NULL,
proxy_period_cycle = NULL
)
## End(Not run)

```

completed_series

Complete the tracking of cycle in a wavelet spectra

Description

Use the traced series and the existing wavelet spectra to complete the tracking of a cycle of the wavelet spectra. The selected points using the [track_period_wavelet](#) function form a incomplete line unless every point is tracked. However clicking every individual point along a wavelet ridge is time intensive and error prone. To avoid errors and save time the [completed_series](#) function can be used to complete the tracing of a cycle in a wavelet spectra. The [completed_series](#) function interpolates the data points selected using the [track_period_wavelet](#). A search algorithm then looks up and replaces the interpolated curve values with the values of the nearest spectral peak in the wavelet spectra.

Usage

```
completed_series(
  wavelet = NULL,
  tracked_curve = NULL,
  period_up = 1.2,
  period_down = 0.8,
  extrapolate = TRUE,
  genplot = TRUE
)
```

Arguments

wavelet	Wavelet object created using the analyze_wavelet function.
tracked_curve	Traced period result from the track_period_wavelet function.
period_up	The upper period parameter is a factor of the to be completed curve Default=1.2, which puts a limit on how far the code completed_series function can "look up" to find the next spectral peak. if no spectral peak is found data is interpolated between spectral peaks.
period_down	The lower period parameter is a factor of the to be completed curve Default=0.8, which puts a limit on how far the code completed_series function can "look down" to find the next spectral peak. if no spectral peak is found data is interpolated between spectral peaks.
extrapolate	Extrapolate the completed curve when through parts where no spectral peaks could be traced Default=TRUE.
genplot	Generate a plot Default=TRUE. The red curve is the completed curve, the black curve is the original curve.

Value

Returns a matrix with 2 columns The first column is the depth axis The second column is the completed tracking of the period a cycle of the wavelet spectra

Examples

```
#Use the grey_track example points to complete the tracking of the \cr
# precession cycle in the wavelet spectra of the greyscale data set \cr
# of Zeeden et al., (2013).
```

```
grey_wt <-
analyze_wavelet(
  data = grey,
  dj = 1/200,
  lowerPeriod = 0.02,
  upperPeriod = 256,
  verbose = TRUE,
  omega_nr = 8
)
```

```
#The ~22kyr precession cycle is between 0.25 and 1m The grey_track data \cr
#set is a pre-loaded uncompleted tracking of the precession cycle
```

```

#grey_track <- track_period_wavelet(
#astro_cycle = 22,
#wavelet = NULL,
#n.levels = 100,
#periodlab = "Period (metres)",
#x_lab = "depth (metres)"
#)

grey_track <- completed_series(
  wavelet = grey_wt,
  tracked_curve = grey_track,
  period_up = 1.25,
  period_down = 0.75,
  extrapolate = TRUE,
  genplot = TRUE
)

```

curve2sedrate

Converts a tracked tracked to a sedimentation rate curve

Description

Converts the period of a tracked cycle to a sedimentation rate curve by assigning a duration (in kyr) to the period of a tracked cycle

Usage

```
curve2sedrate(tracked_cycle_curve = NULL, tracked_cycle_period = NULL)
```

Arguments

tracked_cycle_curve

A cycle tracked using the [track_period_wavelet](#) function

Any input (matrix or dataframe) in which the first column is depth in meters and the second column is period in meters

tracked_cycle_period

Period of the tracked cycle (in kyr).

Value

The output is a matrix with 2 columns The first column is depth The second column sedimentation rate in cm/kyr

Examples

```

#Conversion of the period (in meters) of a 405 kyr eccentricity cycle tracked \cr
#in a wavelet spectra by assigning a duration of 405 kyr to the tracked cycle.
# perform the CWT
mag_wt <- analyze_wavelet(data = mag,
dj = 1/100,

```

```

lowerPeriod = 0.1,
upperPeriod = 254,
verbose = TRUE,
omega_nr = 10)

#Track the 405 kyr eccentricity cycle in a wavelet spectra

#mag_track <- track_period_wavelet(astro_cycle = 405,
#                                wavelet=mag_wt,
#                                n.levels = 100,
#                                periodlab = "Period (metres)",
#                                x_lab = "depth (metres)")

#Instead of tracking, the tracked solution data set \link{mag_track_solution} is used \cr
mag_track <- mag_track_solution

mag_track_complete <- completed_series(
  wavelet = mag_wt,
  tracked_curve = mag_track,
  period_up = 1.2,
  period_down = 0.8,
  extrapolate = TRUE,
  genplot = TRUE
)

# smooth the tracking of the 405 kyr eccentricity cycle
mag_track_complete <- loess_auto(time_series = mag_track_complete,
  genplot = TRUE, print_span = TRUE)

#convert period in meters to sedrate in cm/kyr
mag_track_sedrate <- curve2sedrate(tracked_cycle_curve=mag_track_complete,
  tracked_cycle_period=405)

```

curve2time

Converts the tracked curve to a depth time space

Description

Converts the tracked curve to a depth time space.

Usage

```

curve2time(
  tracked_cycle_curve = NULL,
  tracked_cycle_period = NULL,
  genplot = TRUE
)

```

Arguments

tracked_cycle_curve

Curve of the cycle tracked using the [track_period_wavelet](#) function

Any input (matrix or data frame) in which the first column is depth in meters and the second column is period in meters can be used.

tracked_cycle_period
 Period of the tracked curve in kyr.

genplot Generates a plot with depth vs time Default=TRUE.

Value

The output is a matrix with 2 columns. The first column is depth. The second column sedimentation rate in cm/kyr. If genplot=TRUE then a depth vs time plot will be plotted.

Author(s)

Based on the the [sedrate2time](#) function of the [astrochron-package](#).

References

Routines for astrochronologic testing, astronomical time scale construction, and time series analysis
[doi:<doi:10.1016/j.earscirev.2018.11.015>](https://doi.org/10.1016/j.earscirev.2018.11.015).

Examples

```
#Convert a tracked curve to a depth time space. The examples uses the \cr
#magnetic susceptibility data set of De pas et al., (2018).\cr

## perform the CWT
mag_wt <- analyze_wavelet(data = mag,
dj = 1/100,
lowerPeriod = 0.1,
upperPeriod = 254,
verbose = TRUE,
omega_nr = 10)

#Track the 405 kyr eccentricity cycle in a wavelet spectra

#mag_track <- track_period_wavelet(astro_cycle = 405,
#                                  wavelet=mag_wt,
#                                  n.levels = 100,
#                                  periodlab = "Period (metres)",
#                                  x_lab = "depth (metres)")

#Instead of tracking, the tracked solution data set \code{\link{mag_track_solution}} is used \cr
mag_track <- mag_track_solution

mag_track_complete <- completed_series(
  wavelet = mag_wt,
  tracked_curve = mag_track,
  period_up = 1.2,
  period_down = 0.8,
  extrapolate = TRUE,
  genplot = TRUE
)

# smooth the tracking of the 405 kyr eccentricity cycle
mag_track_complete <- loess_auto(time_series = mag_track_complete,
genplot = TRUE, print_span = TRUE)

#convert period in meters to sedrate depth vs time
```

```
mag_track_time<- curve2time(tracked_cycle_curve=mag_track_complete,
tracked_cycle_period=405,
genplot=TRUE)
```

curve2tune

Converts data from the depth to the time domain

Description

Converts a data set from the depth to the time domain using a tracked curve/cycle to depth domain an assigning a duration (in kyr) set tracked curve/cycle.

Usage

```
curve2tune(
  data = NULL,
  tracked_cycle_curve = NULL,
  tracked_cycle_period = NULL,
  genplot = TRUE
)
```

Arguments

data	Data set (matrix with 2 columns 1st column depth 2nd column proxy value) which was used as input for the analyze_wavelet function. That result was then used to tracked a cycle using the track_period_wavelet function
tracked_cycle_curve	Tracking result of a cycle tracked using the track_period_wavelet function Any input (matrix or data frame) in which the first column is depth in meters and the second column is period in meters can be used.
tracked_cycle_period	Period of the tracked curve (in kyr).
genplot	If genplot=TRUE 3 plots stacked on top of each other will be plotted. Plot 1: the original data set. Plot 2: the depth time plot. Plot 3: the data set in the time domain.

Value

The output is a matrix with 2 columns. The first column is time. The second column sedimentation proxy value.

If genplot=TRUE then 3 plots stacked on top of each other will be plotted. Plot 1: the original dataset. Plot 2: the depth time plot. Plot 3: the dataset in the time domain.

Author(s)

Based on the the [sedrate2time](#) function of the [astrochron-package](#)

References

Routines for astrochronologic testing, astronomical time scale construction, and time series analysis
[doi:10.1016/j.earscirev.2018.11.015](https://doi.org/10.1016/j.earscirev.2018.11.015)

Examples

```
#The example uses the magnetic susceptibility data set of De pas et al., (2018).
# perform the CWT
mag_wt <- analyze_wavelet(data = mag,
  dj = 1/100,
  lowerPeriod = 0.1,
  upperPeriod = 254,
  verbose = TRUE,
  omega_nr = 10)

#Track the 405 kyr eccentricity cycle in a wavelet spectra

#mag_track <- track_period_wavelet(astro_cycle = 405,
#                                wavelet=mag_wt,
#                                n.levels = 100,
#                                periodlab = "Period (metres)",
#                                x_lab = "depth (metres)")

#Instead of tracking, the tracked solution data set \link{mag_track_solution} is used
mag_track <- mag_track_solution

mag_track_complete <- completed_series(
  wavelet = mag_wt,
  tracked_curve = mag_track,
  period_up = 1.2,
  period_down = 0.8,
  extrapolate = TRUE,
  genplot = TRUE
)

# smooth the tracking of the 405 kyr eccentricity cycle
mag_track_complete <- loess_auto(time_series = mag_track_complete,
  genplot = TRUE, print_span = TRUE)

mag_track_time<- curve2tune(data=mag,
  tracked_cycle_curve=mag_track_complete,
  tracked_cycle_period=405,
  genplot=TRUE)
```

extract_power

Extract power from a wavelet spectra

Description

Extracts the the spectral power from a wavelet spectra in the depth domain using a traced period and boundaries surround the traced period. The extraction of spectral is useful for cyclostratigraphic studies because the spectral power of an astronomical cycle is modulated by higher order astronomical cycles. The spectral power record from an astronomical cycle can thus be used as a proxy for


```

#                                     x_lab = "depth (metres)")

#Instead of tracking, the tracked solution data set \link{mag_track_solution} \cr
#is used
mag_track <- mag_track_solution

mag_track_complete <- completed_series(
  wavelet = mag_wt,
  tracked_curve = mag_track,
  period_up = 1.2,
  period_down = 0.8,
  extrapolate = TRUE,
  genplot = TRUE
)

#Smooth the completed tracking of the 405 kyr eccentricity cycle in the wavelet spectra

mag_track_complete <- loess_auto(time_series = mag_track_complete,
  genplot = TRUE, print_span = TRUE)

#extract the spectral power of the 405 kyr eccentricity cycle
mag_power <- extract_power(
  completed_series = mag_track_complete,
  wavelet = mag_wt,
  period_up = 1.2,
  period_down = 0.8,
  tracked_cycle_period = 405,
  extract_cycle_power = 405
)

```

`extract_power_stable` *Extract power from a wavelet spectra by using a constant period/duration*

Description

Extract spectral power from the wavelet using a constant period/duration and boundaries as selection criteria. The extraction of spectral is useful for cyclostratigraphic studies because the spectral power of an astronomical cycle is modulated by higher order astronomical cycles. The spectral power record from an astronomical cycle can thus be used as a proxy for amplitude modulating cycles. The spectral power is extracted from a wavelet spectra which was created using the [analyze_wavelet](#) function for a given, cycle, period_up and period_down

Usage

```

extract_power_stable(
  wavelet = NULL,
  cycle = NULL,
  period_up = 1.2,
  period_down = 0.8
)

```

Arguments

wavelet	Wavelet object created using the analyze_wavelet function.
cycle	Period of cycle for which the power will be extracted from the record.
period_up	Upper period as a factor of the to be extracted power Default=1.2.
period_down	Lower period as a factor of the to be extracted power Default=0.8.

Value

Returns a matrix with 3 columns. The first column is depth/time. The second column is extracted power. The third column is extracted power/total power.

Examples

```
#Extract the spectral power of the 210 yr de Vries cycle from the Total Solar \cr
#Irradiance data set of Steinhilber et al., (2012).
```

```
TSI_wt <-
  analyze_wavelet(
    data = TSI,
    dj = 1/200,
    lowerPeriod = 16,
    upperPeriod = 8192,
    verbose = TRUE,
    omega_nr = 6
  )
TSI_wt_pwr_de_Vries_cycle <- extract_power_stable(
  wavelet = TSI_wt,
  cycle = 210,
  period_up = 1.2,
  period_down = 0.8
)
```

extract_signal

Extract signal from a wavelet spectra using a traced period curve

Description

Extract signal power from the wavelet in the depth domain using the traced period.

Usage

```
extract_signal(
  tracked_cycle_curve = NULL,
  wavelet = NULL,
  period_up = 1.2,
  period_down = 0.8,
  add_mean = TRUE,
  tracked_cycle_period = NULL,
  extract_cycle = NULL,
  tune = FALSE,
```

```
    plot_residual = FALSE
  )
```

Arguments

tracked_cycle_curve	Traced period result from the track_period_wavelet function completed using the completed_series. The input can be pre-smoothed using the the loess_auto function.
wavelet	wavelet object created using the analyze_wavelet function.
period_up	Upper period as a factor of the to be extracted cycle Default=1.2.
period_down	Lower period as a factor of the to be extracted cycle Default=0.8.
add_mean	Add mean to the extracted cycle Default=TRUE.
tracked_cycle_period	Period in time of the traced cycle.
extract_cycle	Period of the to be extracted cycle.
tune	Convert record from the depth to the time domain using the traced period Default=FALSE.
plot_residual	Plot the residual signal after extraction of set cycle Default=FALSE.

Value

Returns a matrix with 2 columns The first column is depth/time The second column is extracted signal

Examples

```
#Extract the 405 kyr eccentricity cycle from the the magnetic susceptibility \cr
#record of the Sullivan core and use the Gabor uncertainty principle to define \cr
#the mathematical uncertainty of the analysis and use a factor of that standard \cr
#deviation to define boundaries.
```

```
#Perform the CWT
mag_wt <- analyze_wavelet(data = mag,
  dj = 1/100,
  lowerPeriod = 0.1,
  upperPeriod = 254,
  verbose = TRUE,
  omega_nr = 10)
```

```
#Track the 405 kyr eccentricity cycle in a wavelet spectra
```

```
#mag_track <- track_period_wavelet(astro_cycle = 405,
#                               wavelet=mag_wt,
#                               n.levels = 100,
#                               periodlab = "Period (metres)",
#                               x_lab = "depth (metres)")
```

```
#Instead of tracking, the tracked solution data set \code{\link{mag_track_solution}} is used \cr
mag_track <- mag_track_solution
```

```
mag_track_complete <- completed_series(
  wavelet = mag_wt,
```

```

    tracked_curve = mag_track,
    period_up = 1.2,
    period_down = 0.8,
    extrapolate = TRUE,
    genplot = TRUE
  )

# smooth the tracking of the 405 kyr eccentricity cycle
mag_track_complete <- loess_auto(time_series = mag_track_complete,
  genplot = TRUE, print_span = TRUE)

# extract the 405 kyr eccentricity cycle from the wavelet spectrum and use the \cr
# tracked cycle curve and set factors of the extracted cycle as boundaries

mag_405_ecc <- extract_signal(
  tracked_cycle_curve = mag_track_complete,
  wavelet = mag_wt,
  period_up = 1.2,
  period_down = 0.8,
  add_mean = TRUE,
  tracked_cycle_period = 405,
  extract_cycle = 405,
  tune = FALSE,
  plot_residual = FALSE
)

```

`extract_signal_stable` *Extract a signal/cycle from a wavelet spectra using a set period and boundaries*

Description

Extracts a cycle from the wavelet object created using the [analyze_wavelet](#) function using a fixed period and fixed period boundaries defined as factors of the original cycle

Usage

```

extract_signal_stable(
  wavelet = NULL,
  cycle = NULL,
  period_up = 1.2,
  period_down = 0.8,
  add_mean = TRUE,
  plot_residual = FALSE
)

```

Arguments

<code>wavelet</code>	Wavelet object created using the analyze_wavelet function.
<code>cycle</code>	Period of the cycle which needs to be extracted.
<code>period_up</code>	Upper period as a factor of the to be extracted cycle Default=1.2.
<code>period_down</code>	Lower period as a factor of the to be extracted cycle Default=0.8.

add_mean Add mean to the extracted cycle Default=TRUE.
 plot_residual plot the residual signal after extraction of set cycle Default=FALSE.

Value

#Returns a matrix with 2 columns. The first column is time/depth. The second column is the extracted signal/cycle.

Examples

```
#Example in which the ~210yr de Vries cycle is extracted from the Total Solar
#Irradiance data set of Steinhilber et al., (2012)\cr
```

```
#Perform the CWT
TSI_wt <-
analyze_wavelet(
  data = TSI,
  dj = 1/200,
  lowerPeriod = 16,
  upperPeriod = 8192,
  verbose = TRUE,
  omega_nr = 6
)
```

```
#Extract the 210 yr de Vries cycle from the wavelet spectra
de_Vries_cycle <- extract_signal_stable(wavelet=TSI_wt,
  cycle=210,
  period_up =1.25,
  period_down = 0.75,
  add_mean=TRUE,
  plot_residual=FALSE)
```

```
extract_signal_stable_V2
```

Extract signal from a wavelet spectrum using a upper and lower period boundary

Description

Extract a signal from the wavelet using a upper and lower period boundary

Usage

```
extract_signal_stable_V2(
  wavelet = NULL,
  period_max = NULL,
  period_min = NULL,
  add_mean = TRUE,
  plot_residual = FALSE
)
```

Arguments

wavelet	wavelet object created using the analyze_wavelet function.
period_max	Maximum period (upper boundary) to be used to extract a cycle.
period_min	Minimum period (lower boundary) to be used to extract a cycle.
add_mean	Add mean to the extracted cycle Default=TRUE.
plot_residual	Plot the signal from which the extracted cycle is subtracted Default=FALSE.

Value

Signal extracted from the wavelet spectra. Output is a matrix with the first column being depth/time and the second column is the cycle extracted from the proxy record.

Examples

```
#Example in which the ~210yr de Vries cycle is extracted from the Total Solar \cr
# Irradiance data set of Steinhilber et al., (2012)\cr

TSI_wt <-
analyze_wavelet(
  data = TSI,
  dj = 1/200,
  lowerPeriod = 16,
  upperPeriod = 8192,
  verbose = TRUE,
  omega_nr = 6
)

de_Vries_cycle <- extract_signal_stable_V2(wavelet=TSI_wt,
  period_max = 240,
  period_min = 180,
  add_mean=TRUE,
  plot_residual=FALSE)
```

extract_signal_standard_deviation

Extract a signal using standard deviation

Description

Extract signal from a wavelet spectra in the depth domain using a the standard deviation of the omega (number of cycles) as boundaries. The uncertainty is based on the Gabor uncertainty principle applied to the continuous wavelet transform using a Morlet wavelet. The calculated uncertainty is the underlying analytical uncertainty which is the result of applying the Gabor uncertainty principle to the continuous wavelet transform using a Morlet wavelet.

Usage

```
extract_signal_standard_deviation(
  wavelet = NULL,
  tracked_cycle_curve = NULL,
  multi = 1,
  extract_cycle = NULL,
  tracked_cycle_period = NULL,
  add_mean = TRUE,
  tune = FALSE,
  genplot_uncertainty_wt = TRUE,
  genplot_extracted = TRUE
)
```

Arguments

wavelet Wavelet object created using the [analyze_wavelet](#) function.

tracked_cycle_curve Curve of the cycle tracked using the [track_period_wavelet](#) function. Any input (matrix or dataframe) in which the first column is depth or time and the second column is period should work.

multi multiple of the standard deviation to be used as boundaries for the cycle extraction Default=1.

extract_cycle Period of the cycle to be extracted.

tracked_cycle_period Period of the tracked cycle.

add_mean Add mean to the extracted cycle Default=TRUE.

tune Tune data set using the Default=tracked_cycle_curve curve Default=FALSE.

genplot_uncertainty_wt Generate a wavelet spectra plot with the tracked curve and its analytical uncertainty based the Gabor uncertainty principle applied continuous wavelet transform using a Morlet wavelet on superimposed on top of it. In the plot the red curve and blue curves are the upper and lower bounds based on the `multi` parameter which x-times the standard deviation of uncertainty. The black curve is the Default=tracked_cycle_curve curve.

genplot_extracted Generates a plot with the data set and the extracted cycle on top Default=TRUE of it.

Value

Signal extracted from the wavelet spectra. Output is a matrix with the first column being depth/time and the second column is the astronomical cycle extracted from the proxy record

If `genplot_uncertainty_wt=TRUE` then a wavelet spectra will be plotted with the uncertainty superimposed on top of it. In the plot the red curve and blue curves are the upper and lower bounds based on the `multi` parameter. The black curve is the Default=tracked_cycle_curve curve. If `genplot_extracted=TRUE` plot with the data set and the extracted cycle on top of it will be plotted.

References

Gabor, Dennis. "Theory of communication. Part 1: The analysis of information." Journal of the Institution of Electrical Engineers-part III: radio and communication engineering 93, no. 26 (1946): 429-441.

Russell, Brian, and Jiajun Han. "Jean Morlet and the continuous wavelet transform. " CREWES Res. Rep 28 (2016): 115.

Examples

```
#Extract the 405 kyr eccentricity cycle from the the magnetic susceptibility \cr
#record of the Sullivan core and use the Gabor uncertainty principle to define \cr
# the mathematical uncertainty of the analysis and use a factor of that standard \cr
# deviation to define boundaries

# perform the CWT
mag_wt <- analyze_wavelet(data = mag,
  dj = 1/100,
  lowerPeriod = 0.1,
  upperPeriod = 254,
  verbose = TRUE,
  omega_nr = 10)

#Track the 405 kyr eccentricity cycle in a wavelet spectra

#mag_track <- track_period_wavelet(astro_cycle = 405,
#                                wavelet=mag_wt,
#                                n.levels = 100,
#                                periodlab = "Period (metres)",
#                                x_lab = "depth (metres)")

#Instead of tracking, the tracked solution data set \link{mag_track_solution} is used \cr
mag_track <- mag_track_solution

mag_track_complete <- completed_series(
  wavelet = mag_wt,
  tracked_curve = mag_track,
  period_up = 1.2,
  period_down = 0.8,
  extrapolate = TRUE,
  genplot = TRUE
)

# smooth the tracking of the 405 kyr eccentricity cycle
mag_track_complete <- loess_auto(time_series = mag_track_complete,
  genplot = TRUE, print_span = TRUE)

# extract the 405 kyr eccentricity cycle from the wavelet spectrum and use \cr
# the Gabor uncertainty principle to define the mathematical uncertainty of \cr
# the analysis and use a multiple of the derived standard deviation to define boundaries

mag_405_ecc <- extract_signal_standard_deviation(
  wavelet = mag_wt,
  tracked_cycle_curve = mag_track_complete,
  multi = 1,
  extract_cycle = 405,
  tracked_cycle_period = 405,
```

```

add_mean = TRUE,
tune = FALSE,
genplot_uncertainty_wt = TRUE,
genplot_extracted = TRUE
)

```

grey

Grey scale record IODP 926 of Zeeden et al., (2013)

Description

IODP 926 grey scale record of Zeeden et al., (2013) for the (154-174m) interval. The (154-174m) interval spans the Miocene.

Details

Column 1: depth (meters)
Column 2: greyscale value

References

Christian Zeeden, Frederik Hilgen, Thomas Westerhold, Lucas Lourens, Ursula Röhl, Torsten Bickert, Revised Miocene splice, astronomical tuning and calcareous plankton biochronology of ODP Site 926 between 5 and 14.4Ma, *Palaeogeography, Palaeoclimatology, Palaeoecology*, Volume 369, 2013, Pages 430-451, ISSN 0031-0182, <doi:10.1016/j.palaeo.2012.11.009>

grey_track

Tracking points of the precession (22 kyr cycle) IODP 926 grey scale (154-174m) record of Zeeden et al., (2013)

Description

Example data which consists of tracking points of the precession (22 kyr cycle) in the wavelet spectra of the IODP 926 grey scale (154-174m) record of Zeeden et al., (2013)

Details

Column 1: Depth (meters)
Column 2: period (meters)

References

Christian Zeeden, Frederik Hilgen, Thomas Westerhold, Lucas Lourens, Ursula Röhl, Torsten Bickert, Revised Miocene splice, astronomical tuning and calcareous plankton biochronology of ODP Site 926 between 5 and 14.4Ma, *Palaeogeography, Palaeoclimatology, Palaeoecology*, Volume 369, 2013, Pages 430-451, ISSN 0031-0182, <doi:10.1016/j.palaeo.2012.11.009>

Hilbert_transform *Perform a Hilbert transform on a signal*

Description

Extract the amplitude modulation using the Hilbert transform.

Usage

```
Hilbert_transform(data = NULL, demean = TRUE)
```

Arguments

data	Input is a time series with the first column being depth or time and the second column being a proxy.
demean	Remove the mean from the time series.

Value

Returns a matrix with 2 columns. The first column is depth/time. The second column is the hilbert transform of the signal.

Author(s)

Based on the the [inst.pulse](#) function of the [DecomposeR](#)

References

Wouters, S., Crucifix, M., Sinnesael, M., Da Silva, A.C., Zeeden, C., Zivanovic, M., Boulvain, F., Devleeschouwer, X., 2022, "A decomposition approach to cyclostratigraphic signal processing". *Earth-Science Reviews* 225 (103894).<doi:10.1016/j.earscirev.2021.103894>

Huang, Norden E., Zhaohua Wu, Steven R. Long, Kenneth C. Arnold, Xianyao Chen, and Karin Blank. 2009. "On Instantaneous Frequency". *Advances in Adaptive Data Analysis* 01 (02): 177–229. <doi:10.1142/S1793536909000096>

Examples

```
#Example in which the Hilbert transform (eg. amplitude modulation) of the ~210yr \cr
#de Vries cycle is extracted from the Total Solar Irradiance data set of \cr
#Steinhilber et al., (2012)
```

```
#Perform the CWT
TSI_wt <-
analyze_wavelet(
  data = TSI,
  dj = 1/200,
  lowerPeriod = 16,
  upperPeriod = 8192,
  verbose = TRUE,
  omega_nr = 6
)
```

```
#Extract the 210 yr de Vries cycle from the wavelet spectra
de_Vries_cycle <- extract_signal_stable(wavelet=TSI_wt,
cycle=210,
period_up =1.25,
period_down = 0.75,
add_mean=TRUE,
plot_residual=FALSE)

#Perform the Hilbert transform on the amplitude record of the 210 yr de Vries \cr
# cycle which was extracted from the wavelet spectra

de_Vries_cycle_hilbert <- Hilbert_transform(data=de_Vries_cycle,demean=TRUE)
```

loess_auto

Perform an automatically loess based smoothing of a timeseries

Description

Perform an automatically loess based smoothing of a timeseries. The local polynomial regression with automatic smoothing parameter selection is based on an optimization using the aicc bias-corrected AIC criterion and the gcv generalized cross-validation criterion.

Usage

```
loess_auto(time_series = NULL, genplot = TRUE, print_span = TRUE)
```

Arguments

time_series	Input is a time series with the first column being depth or time and the second column being a proxy
genplot	Option to generate plot Default=TRUE. The plot will consist of the original signal in blue, the smoothed plot is displayed in black and the + and - 1 sd bounds of the smoothing are displayed in red.
print_span	Print span length as a fraction of the total length of the record.

Value

A matrix with 3 columns. The first column is depth/time. The second column is the smoothed curve. The third column is difference between the original curve and the smoothed curve.

Author(s)

Based on the the [loess.as](#) function of the fANCOVA package.

References

Cleveland, W. S. (1979) Robust locally weighted regression and smoothing scatterplots. *Journal of the American Statistical Association*. 74, 829–836. Hurvich, C.M., Simonoff, J.S., and Tsai, C.L. (1998), Smoothing Parameter Selection in Nonparametric Regression Using an Improved Akaike Information Criterion. *Journal of the Royal Statistical Society B*. 60, 271–293 Golub, G., Heath, M. and Wahba, G. (1979). Generalized cross validation as a method for choosing a good ridge parameter. *Technometrics*. 21, 215–224.

Examples

```

#'smooth the period curve of the 405 kyr eccentricity cycle extracted from \cr
# the magnetic susceptibility data set of De pas et al., (2018) \cr
#perform the CWT on the magnetic susceptibility data set of De pas et al., (2018)

mag_wt <- analyze_wavelet(data = mag,
  dj = 1/100,
  lowerPeriod = 0.1,
  upperPeriod = 254,
  verbose = TRUE,
  omega_nr = 10)

#Track the 405 kyr eccentricity cycle in a wavelet spectra

#mag_track <- track_period_wavelet(astro_cycle = 405,
#                                wavelet=mag_wt,
#                                n.levels = 100,
#                                periodlab = "Period (metres)",
#                                x_lab = "depth (metres)")

#Instead of tracking, the tracked solution data set \code{\link{mag_track_solution}} is used \cr
mag_track <- mag_track_solution

mag_track_complete <- completed_series(
  wavelet = mag_wt,
  tracked_curve = mag_track,
  period_up = 1.2,
  period_down = 0.8,
  extrapolate = TRUE,
  genplot = TRUE
)

#Smooth the completed tracking of the 405 kyr eccentricity cycle as tracked in the wavelet spectra
mag_track_complete <- loess_auto(time_series = mag_track_complete,
  genplot = TRUE, print_span = TRUE)

```

mag

Magnetic susceptibility data of the Sullivan core of De Pas et al., (2018)

Description

The magnetic susceptibility data set consists of the magnetic susceptibility measurements of De Pas et al., (2018), which measured the magnetic susceptibility on the Sullivan core which is of Famennian age.

Details

Column 1: depth value (meters depoth)
 Column 2: magnetic susceptibility value

References

Damien Pas, Linda Hinnov, James E. (Jed) Day, Kenneth Kodama, Matthias Sinnesael, Wei Liu, Cyclostratigraphic calibration of the Famennian stage (Late Devonian, Illinois Basin, USA), Earth and Planetary Science Letters, Volume 488, 2018, Pages 102-114, ISSN 0012-821X, <doi:10.1016/j.epsl.2018.02.010>

mag_track_solution	<i>Period of the 405 kyr ecc cycle in the magnetic susceptibility record of the Sullivan core</i>
--------------------	---

Description

Data points which give the period (in meters) of the 405 kyr eccentricity cycle tracked in the wavelet spectra of the magnetic susceptibility record of the Sullivan core
 The period was tracked using the [track_period_wavelet](#) function
 The tracking is based on the original age model of De Pas et al., (2018)

Details

Column 1: Depth (meters)
 Column 2: tracked period of 405 kyr eccentricity cycle (meters)

References

Damien Pas, Linda Hinnov, James E. (Jed) Day, Kenneth Kodama, Matthias Sinnesael, Wei Liu, Cyclostratigraphic calibration of the Famennian stage (Late Devonian, Illinois Basin, USA), Earth and Planetary Science Letters, Volume 488, 2018, Pages 102-114, ISSN 0012-821X, <doi:10.1016/j.epsl.2018.02.010>

max_detect	<i>Detect and filter out all maxima in a signal</i>
------------	---

Description

The [max_detect](#) function is used to detect and filter out local maxima in a sinusoidal signal.

Usage

```
max_detect(data = NULL)
```

Arguments

data	Matrix or data frame with the first column being depth or time and the second column being a proxy
------	--

Value

#Returns a matrix with 2 columns first column is depth/time the second column are local maxima values

Examples

```

#Example in which the ~210yr de Vries cycle is extracted from the Total Solar
#Irradiance data set of Steinhilber et al., (2012)\cr
#after which all maxima are extracted

TSI_wt <-
analyze_wavelet(
  data = TSI,
  dj = 1/200,
  lowerPeriod = 16,
  upperPeriod = 8192,
  verbose = TRUE,
  omega_nr = 6
)

de_Vries_cycle <- extract_signal_stable(wavelet=TSI_wt,
  cycle=210,
  period_up =1.25,
  period_down = 0.75,
  add_mean=TRUE,
  plot_residual=FALSE)

min_de_Vries_cycle <- min_detect(de_Vries_cycle)

```

min_detect

Detect and filter out all minima in a signal

Description

The `min_detect` function is used to detect and filter out local minima in a sinusoidal signal

Usage

```
min_detect(data)
```

Arguments

data	Matrix or data frame with first column being depth or time and the second column being a proxy
------	--

Value

#Returns a matrix with 2 columns first column is depth/time the second column are local minima values

Examples

```

#Example in which the ~210yr de Vries cycle is extracted from the Total Solar \cr
#Irradiance data set of Steinhilber et al., (2012)\cr
#after which all minima are extracted

```



```

TSI_wt <-
analyze_wavelet(
  data = TSI,
  dj = 1/200,
  lowerPeriod = 16,
  upperPeriod = 8192,
  verbose = TRUE,
  omega_nr = 6
)

de_Vries_cycle <- extract_signal_stable(wavelet=TSI_wt,
  cycle=210,
  period_up =1.25,
  period_down = 0.75,
  add_mean=TRUE,
  plot_residual=FALSE)

min_de_Vries_cycle <- min_detect(de_Vries_cycle)

```

model_red_noise_wt	<i>Models average spectral power based curves based on a red-noise signal generated using the characteristics of an input signal.</i>
--------------------	---

Description

The `model_red_noise_wt` function is used to generate average spectral power curves based on and input signal and set wavelet settings.

Usage

```
model_red_noise_wt(wavelet = NULL, n_simulations = NULL, verbose = TRUE)
```

Arguments

wavelet	Wavelet object created using the analyze_wavelet function.
n_simulations	Number of red noise simulations.
verbose	Print text Default=TRUE.

Value

Returns a matrix in which each column represents the average spectral power resulting from a red-noise run.

Examples

```

## Not run:
## #generate average spectral power curves based on red noise curves which are\cr
# based on the magnetic susceptibility record of the Sullivan core of De pas et al., (2018)

mag_wt <- analyze_wavelet(data = mag,
  dj = 1/100,

```

```

lowerPeriod = 0.1,
upperPeriod = 254,
verbose = FALSE,
omega_nr = 10)

#increase n_simulations to better define the red noise spectral power curve
mag_wt_red_noise <- model_red_noise_wt(wavelet=mag_wt,
n_simulations=100,
verbose=FALSE)

## End(Not run)

```

percentile_from_red_noise

Calculate average spectral power from red noise curves for a given percentile

Description

The `percentile_from_red_noise` function is used to generate and average spectral power curve based on a set percentile based. To generate the percentile curve the results of the `model_red_noise_wt` function are used.

Usage

```
percentile_from_red_noise(red_noise = NULL, wavelet = NULL, percentile = NULL)
```

Arguments

<code>red_noise</code>	Red noise curves generated using the <code>model_red_noise_wt</code> function.
<code>wavelet</code>	Wavelet object created using the <code>analyze_wavelet</code> function.
<code>percentile</code>	Percentile value (0-1).

Value

Returns a matrix with 2 columns.
The first column is the period (m).
The second column is the spectral power at percentile x based on the red noise modelling runs.

Examples

```

## Not run:
##generate red noise curves based on the magnetic susceptibility record of \cr
##the Sullivan core of De pas et al., (2018)

mag_wt <- analyze_wavelet(data = mag,
dj = 1/100,
lowerPeriod = 0.1,
upperPeriod = 254,

```

```

verbose = FALSE,
omega_nr = 10)

mag_wt_red_noise <- model_red_noise_wt(data=NULL,
n_simulations =1000,
verbose=FALSE)

prob_curve <- percentile_from_red_noise(
red_noise = mag_wt_red_noise,
wavelet = mag_wt,
percentile = 0.9
)
## End(Not run)

```

plot_avg_wavelet *Plot the average spectral power of a wavelet spectra*

Description

Plot the average spectral power of a wavelet spectra using the results of the [analyze_wavelet](#) function.

Usage

```
plot_avg_wavelet(wavelet = NULL, y_lab = "Power", x_lab = "period (metres)")
```

Arguments

wavelet	Wavelet object created using the analyze_wavelet function.
y_lab	Label for the y-axis Default="Power".
x_lab	Label for the x-axis Default="depth (metres)".

Value

The output is a plot of the average spectral power of a wavelet spectra

Examples

```

#Example 1. Plot the average spectral power of the wavelet spectra of \cr
# the Total Solar Irradiance data set of Steinhilber et al., (2012)
TSI_wt <-
analyze_wavelet(
  data = TSI,
  dj = 1/200,
  lowerPeriod = 16,
  upperPeriod = 8192,
  verbose = TRUE,
  omega_nr = 6
)

plot_avg_wavelet(wavelet=TSI_wt,
                 y_lab= "power",

```

```

x_lab="period (years)")

#Example 2. Plot the average spectral power of the wavelet spectra of \cr
# the magnetic susceptibility data set of De pas et al., (2018)
mag_wt <-
analyze_wavelet(
  data = mag,
  dj = 1/100,
  lowerPeriod = 0.1,
  upperPeriod = 254,
  verbose = TRUE,
  omega_nr = 10
)
plot_avg_wavelet(wavelet=mag_wt,
  y_lab= "power",
  x_lab="period (metres)")

#Example 3. Plot the average spectral power of the wavelet spectra of \cr
#the greyscale data set of Zeeden et al., (2013)
grey_wt <-
analyze_wavelet(
  data = grey,
  dj = 1/200,
  lowerPeriod = 0.02,
  upperPeriod = 256,
  verbose = TRUE,
  omega_nr = 8
)

plot_avg_wavelet(wavelet=grey_wt,
  y_lab= "power",
  x_lab="period (metres)")

```

plot_wavelet	<i>Plots a wavelet power spectra</i>
--------------	--------------------------------------

Description

Plot wavelet spectra using the outcome of the [analyze_wavelet](#) function.

Usage

```

plot_wavelet(
  wavelet = NULL,
  plot.COI = TRUE,
  n.levels = 100,
  color.palette = "rainbow(n.levels, start = 0, end = 0.7)",
  useRaster = TRUE,
  periodlab = "Period (metres)",

```

```

    x_lab = "depth (metres)"
  )

```

Arguments

wavelet	wavelet object created using the analyze_wavelet function.
plot.COI	Option to plot the cone of influence Default=TRUE.
n.levels	Number of color levels Default=100.
color.palette	Definition of color palette Default="rainbow(n.levels, start = 0, end = 0.7)".
useRaster	plot as a raster or vector image Default=TRUE. WARNING plotting as a vector image is computationally intensive.
periodlab	label for the y-axis Default="Period (metres)".
x_lab	label for the x-axis Default="depth (metres)".

Value

The output is a plot of a wavelet spectra.

Author(s)

Code based on the R packages :WaveletComp and biwavelet which are based on the wavelet MATLAB program written by Christopher Torrence and Gibert P. Compo.

References

Angi Roesch and Harald Schmidbauer (2018). WaveletComp: Computational Wavelet Analysis. R package version 1.1. <https://CRAN.R-project.org/package=WaveletComp>

Gouhier TC, Grinsted A, Simko V (2021). R package biwavelet: Conduct Univariate and Bivariate Wavelet Analyses. (Version 0.20.21), <https://github.com/tgouhier/biwavelet>

Torrence, C., and G. P. Compo. 1998. A Practical Guide to Wavelet Analysis. Bulletin of the American Meteorological Society 79:61-78.

Examples

```

#Example 1. A plot of a wavelet spectra using the Total Solar Irradiance \cr
# data set of Steinhilber et al., (2012)
TSI_wt <-
  analyze_wavelet(
    data = TSI,
    dj = 1/200,
    lowerPeriod = 16,
    upperPeriod = 8192,
    verbose = TRUE,
    omega_nr = 6
  )

plot_wavelet(
  wavelet = TSI_wt,
  plot.COI = TRUE,
  n.levels = 100,
  color.palette = "rainbow(n.levels, start = 0, end = 0.7)",
  useRaster = TRUE,
  periodlab = "Period (years)",

```

```

x_lab = "years (before present)"
)

#Example 2. A plot of a wavelet spectra using the magnetic susceptibility \cr
#data set of De pas et al., (2018)
mag_wt <-
analyze_wavelet(
  data = mag,
  dj = 1/100,
  lowerPeriod = 0.1,
  upperPeriod = 254,
  verbose = TRUE,
  omega_nr = 10
)
plot_wavelet(
  wavelet = mag_wt,
  plot.COI = TRUE,
  n.levels = 100,
  color.palette = "rainbow(n.levels, start = 0, end = 0.7)",
  useRaster = TRUE,
  periodlab = "Period (metres)",
  x_lab = "depth (metres)"
)

#Example 3. A plot of a wavelet spectra using the greyscale \cr
# data set of Zeeden et al., (2013)
grey_wt <-
analyze_wavelet(
  data = grey,
  dj = 1/200,
  lowerPeriod = 0.02,
  upperPeriod = 256,
  verbose = TRUE,
  omega_nr = 8
)
plot_wavelet(
  wavelet = grey_wt,
  plot.COI = TRUE,
  n.levels = 100,
  color.palette = "rainbow(n.levels, start = 0, end = 0.7)",
  useRaster = TRUE,
  periodlab = "Period (metres)",
  x_lab = "depth (metres)"
)

```

Description

The `sum_power_sedrate` function is used calculate the sum of maximum spectral power for a list of astronomical cycles from a wavelet spectra. The data is first normalized using the average spectral power curves for a given percentile based on results of the `model_red_noise_wt` function

Usage

```
sum_power_sedrate(
  red_noise = NULL,
  wavelet = NULL,
  percentile = NULL,
  sedrate_low = NULL,
  sedrate_high = NULL,
  spacing = NULL,
  cycles = c(NULL),
  x_lab = "depth",
  y_lab = "sedrate",
  genplot = TRUE
)
```

Arguments

<code>red_noise</code>	Red noise curves generated using the <code>model_red_noise_wt</code> function
<code>wavelet</code>	Wavelet object created using the <code>analyze_wavelet</code> function
<code>percentile</code>	Percentile value (0-1) of the rednoise runs which is used to normalize the data for. To account for the distribution/distortion of the spectral power distribution based on the analytical technique and random red-noise the data is normalized against a percentile based red-noise curve which is the results of the <code>'model_red_noise_wt'</code> modelling runs.
<code>sedrate_low</code>	Minimum sedimentation rate (cm/kyr)for which the sum of maximum spectral power is calculated for.
<code>sedrate_high</code>	Maximum sedimentation rate (cm/kyr) for which the sum of maximum spectral power is calculated for.
<code>spacing</code>	Spacing (cm/kyr) between sedimentation rates
<code>cycles</code>	Astronomical cycles (in kyr) for which the combined sum of maximum spectral power is calculated for
<code>x_lab</code>	label for the y-axis Default="depth"
<code>y_lab</code>	label for the y-axis Default="sedrate"
<code>genplot</code>	Generate plot Default="TRUE"

Value

Returns a matrix with sum of maximum spectral power for a given sedimentation rates and a given depths.

If Default="TRUE" a plot is created with 3 subplots. Subplot 1 is plot in which the the sum of maximum spectral power for a given sedimentation rate is plotted for each depth given depth. Subplot 2 is a plot in which the average sum of maximum spectral power is plotted fro each sedimentation Subplot 3 is a color scale for subplot 1.

Examples

```
## Not run:
#estimate sedimentation rate for the the magnetic susceptibility record \cr
# of the Sullivan core of De pas et al., (2018).

mag_wt <- analyze_wavelet(data = mag,
  dj = 1/100,
  lowerPeriod = 0.1,
  upperPeriod = 254,
  verbose = FALSE,
  omega_nr = 10)

#increase n_simulations to better define the red noise spectral power curve
mag_wt_red_noise <- model_red_noise_wt(wavelet=mag_wt,
  n_simulations=100,
  verbose=FALSE)

sedrates <- sum_power_sedrate(red_noise=mag_wt_red_noise,
  wavelet=mag_wt,
  percentile=0.75,
  sedrate_low = 0.5,
  sedrate_high = 4,
  spacing = 0.05,
  cycles = c(2376,1600,1180,696,406,110),
  x_lab="depth",
  y_lab="sedrate",
  genplot = TRUE)

## End(Not run)
```

track_period_wavelet *Track the period of a cycle in a wavelet spectra*

Description

Interactively select points in a wavelet spectra to trace a period in a wavelet spectra. The [track_period_wavelet](#) function plots a wavelet spectra in which spectral peaks can be selected allowing one to track a ridge hence one can track the a cycle with a changing period.

Usage

```
track_period_wavelet(
  astro_cycle = 405,
  wavelet = NULL,
  n.levels = 100,
  periodlab = "Period (metres)",
  x_lab = "depth (metres)"
)
```


Arguments

astro_cycle	Duration (in kyr) of the cycle which traced.
wavelet	Wavelet object created using the analyze_wavelet function.
n.levels	Number of color levels Default=100.
periodlab	label for the y-axis Default="Period (metres)".
x_lab	label for the x-axis Default="depth (metres)".

Value

Results of the tracking of a cycle in the wavelet spectra is a matrix with 3 columns. The first column is depth/time The second column is the period of the tracked cycle The third column is the sedimentation rate based on the duration (in time) of the tracked cycle

Examples

```
## Not run:
#Track the 405kyr eccentricity cycle in the magnetic susceptibility record \cr
# of the Sullivan core of De pas et al., (2018)

mag_wt <- analyze_wavelet(data = mag,
  dj = 1/100,
  lowerPeriod = 0.1,
  upperPeriod = 254,
  verbose = TRUE,
  omega_nr = 10)

mag_track <- track_period_wavelet(astro_cycle = 405,
  wavelet=mag_wt,
  n.levels = 100,
  periodlab = "Period (metres)",
  x_lab = "depth (metres)")

## End(Not run)
```

 TSI

Total solar irradiation data (0-9400ka) of steinhilber et al., (2012)

Description

The Total solar irradiation data set consists of the TSI values of steinhilber et al., (2012)

Details

Column 1: Age (kyr)
 Column 2: Total solar Irradiation (TSI)

References

Steinhilber, Friedhelm & Abreu, Jacksiel & Beer, Juerg & Brunner, Irene & Christl, Marcus & Fischer, Hubertus & Heikkilä, U. & Kubik, Peter & Mann, Mathias & Mccracken, K. & Miller, Heinrich & Miyahara, Hiroko & Oerter, Hans & Wilhelms, Frank. (2012). 9,400 Years of cosmic radiation and solar activity from ice cores and tree rings. Proceedings of the National Academy of Sciences of the United States of America. 109. 5967-71. 10.1073/pnas.1118965109. <doi:10.1073/pnas.1118965109>

wavelet_uncertainty	<i>Calculate the uncertainty associated with the wavelet analysis based on the Gabor uncertainty principle</i>
---------------------	--

Description

The `wavelet_uncertainty` function is used to calculate uncertainties associated with the wavelet analysis based on the Gabor uncertainty principle applied to the continuous wavelet transform using a Mortlet wavelet. The calculated uncertainty is the underlying analytical uncertainty which is the result of applying the Gabor uncertainty principle to the continuous wavelet transform using a Mortlet wavelet.

Usage

```

wavelet_uncertainty(
  tracked_cycle = NULL,
  period_of_tracked_cycle = NULL,
  wavelet = NULL,
  multi = 1,
  verbose = TRUE,
  genplot_time = TRUE,
  genplot_uncertainty = TRUE,
  genplot_uncertainty_wt = TRUE
)

```

Arguments

<code>tracked_cycle</code>	Curve of the cycle tracked using the <code>track_period_wavelet</code> function Any input (matrix or dataframe) in which the first column is depth or time and the second column is period should work
<code>period_of_tracked_cycle</code>	period of the tracked curve (in kyr).
<code>wavelet</code>	wavelet object created using the <code>analyze_wavelet</code> function.
<code>multi</code>	multiple of the standard deviation to be used for defining uncertainty Default=1.
<code>verbose</code>	Print text Default=TRUE.
<code>genplot_time</code>	plot time curves with a upper and lower uncertainty based on Gabor uncertainty principle applied to the continuous wavelet transform using a Mortlet wavelet, which uses which uses the omega number (number of cycles in the wavelet) at one standard deviation to define the analytical uncertainty Default=TRUE

genplot_uncertainty

Plot period curves with upper and lower uncertainty based on Gabor uncertainty principle applied to the continuous wavelet transform using a Morlet wavelet, which uses which uses the omega number (number of cycles in the wavelet) to define uncertainty at one standard deviation Default=TRUE

genplot_uncertainty_wt

generate a wavelet plot with the uncertainty based on Gabor uncertainty principle applied to the continuous wavelet transform using a Morlet wavelet superimposed on top of original wavelet plot. The red curve is period of the tracked curve plus the analytical uncertainty. The blue curve is period of the tracked curve minus the analytical uncertainty. The black curve is the curve tracked using the 'Default=tracked_cycle_curve' function Default=TRUE

Value

Results pertaining to the uncertainty calculated based on the Gabor uncertainty principle.

If the `genplot_time` is TRUE then a depth time plot will be plotted with 3 lines, the mean age, age plus x times the standard deviation and age minus x times the standard deviation .

If the `genplot_uncertainty` is TRUE then a curve will be plotted with the mean period, the tracked period plus x times the standard deviation and the tracked period minus x times the standard deviation.

If the `genplot_uncertainty_wt` is TRUE a wavelet spectra will be plotted with the tracked period, the tracked period plus x times the standard deviation, the tracked period minus x times the standard deviation and the area in between will be shaded in grey.

Returns a matrix with 8 columns.

The first column is called "depth" eg. depth

The second column is "period" of the originally tracked period.

The third column is "frequency" of the originally tracked period.

The fourth column "uncertainty in frequency FWHM" is the uncertainty in frequency based on the Gabor uncertainty principle defined as (FWHM) full width at half maximum.

The fifth column "uncertainty in frequency x_times SD" is the uncertainty in frequency based on the Gabor uncertainty principle defined as times x standard deviations.

The sixth column "time mean" is the mean time based on the tracked period.

The seventh column "time plus x_times sd" is the time based on the tracked period plus x times the standard deviation.

The eighth column "time min x_times sd" is the time based on the tracked period minus x times the standard deviation.

References

Gabor, Dennis. "Theory of communication. Part 1: The analysis of information." *Journal of the Institution of Electrical Engineers-part III: radio and communication engineering* 93, no. 26 (1946): 429-441.

Russell, Brian, and Jiajun Han. "Jean Morlet and the continuous wavelet transform. " *CREWES Res. Rep* 28 (2016): 115.

Examples

```
#calculate the gabor uncertainty derived mathematical uncertainty of the \cr
#magnetic susceptibility record of the Sullivan core
```

```

mag_wt <- analyze_wavelet(data = mag,
  dj = 1/100,
  lowerPeriod = 0.1,
  upperPeriod = 254,
  verbose = TRUE,
  omega_nr = 10)

#Track the 405 kyr eccentricity cycle in a wavelet spectra

#mag_track <- track_period_wavelet(astro_cycle = 405,
#                                wavelet=mag_wt,
#                                n.levels = 100,
#                                periodlab = "Period (metres)",
#                                x_lab = "depth (metres)")

#Instead of tracking, the tracked solution data set \link{mag_track_solution} is used \cr
mag_track <- mag_track_solution

mag_track_complete <- completed_series(
  wavelet = mag_wt,
  tracked_curve = mag_track,
  period_up = 1.2,
  period_down = 0.8,
  extrapolate = FALSE,
  genplot = FALSE
)

mag_track_complete <- loess_auto(time_series = mag_track_complete,
  genplot = TRUE, print_span = TRUE)

uncertainty <- wavelet_uncertainty(
  tracked_cycle = mag_track_complete,
  period_of_tracked_cycle = 405,
  wavelet = mag_wt,
  multi=1,
  verbose = TRUE,
  genplot_time = TRUE,
  genplot_uncertainty = TRUE,
  genplot_uncertainty_wt = TRUE
)

```

Description

The functions of the WaverideR package aid in the manipulation and extraction of cyclic signals using wavelets

Details

Package: WaverideR

Type: R package

Version: 0.2.0 (begin of 2023)

License: GPL (≥ 2)

Note

If you want to use this package for publication or research purposes, please cite: to be submitted

Author(s)

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WaverideR_Datasets *Example data sets for the WaverideR package*

Description

Data sets for testing the WaverideR package:

The mag data set is the magnetic susceptibility record of De Pas et al., (2018)

The TSI data set is the Total Solar Irradiance record of Steinhilber et al., (2012)

The grey data set is the grey scale record of IODP 926 for the interval (154-174m) which originates from Zeeden et al., (2013)

The mag_track_solution is the period of the 405 kyr ecc cycle in the magnetic susceptibility record of rom De Pas et al., (2018)

the age_model_zeeden data set is and age model (anchor points) for the IODP 926 grey scale (154-174m) record of Zeeden et al., (2013)

the grey_track data set consists of tracking points of the precession (22 kyr cycle) in the IODP 926 grey scale (154-174m) record of Zeeden et al., (2013)

References

Damien Pas, Linda Hinnov, James E. (Jed) Day, Kenneth Kodama, Matthias Sinnesael, Wei Liu, Cyclostratigraphic calibration of the Famennian stage (Late Devonian, Illinois Basin, USA), Earth and Planetary Science Letters, Volume 488,2018,Pages 102-114,ISSN 0012-821X, <doi:10.1016/j.epsl.2018.02.010>

Steinhilber, Friedhelm & Abreu, Jacksiel & Beer, Juerg & Brunner, Irene & Christl, Marcus & Fischer, Hubertus & Heikkilä, U. & Kubik, Peter & Mann, Mathias & Mccracken, K. & Miller, Heinrich & Miyahara, Hiroko & Oerter, Hans & Wilhelms, Frank. (2012). 9,400 Years of cosmic radiation and solar activity from ice cores and tree rings. Proceedings of the National Academy of Sciences of the United States of America. 109. 5967-71. 10.1073/pnas.1118965109. <doi:10.1073/pnas.1118965109>

Christian Zeeden, Frederik Hilgen, Thomas Westerhold, Lucas Lourens, Ursula Röhl, Torsten Bickert, Revised Miocene splice, astronomical tuning and calcareous plankton biochronology of ODP Site 926 between 5 and 14.4Ma, Palaeogeography, Palaeoclimatology, Palaeoecology, Volume 369,2013,Pages 430-451,ISSN 0031-0182, <doi:10.1016/j.palaeo.2012.11.009>

Index

achor2time, [2](#)
age_model_zeeden, [3](#)
analyze_wavelet, [4](#), [12](#), [16](#), [18–22](#), [24](#), [25](#),
[33–37](#), [39](#), [41](#), [42](#)
astro_anchor, [2](#), [5](#), [5](#)
astrochron-package, [8](#), [15](#), [16](#)

biwavelet-package, [4](#)

completed_series, [11](#), [11](#), [12](#), [18](#)
curve2sedrate, [13](#)
curve2time, [14](#)
curve2tune, [16](#)

DecomposeR, [28](#)

etp, [8](#)
extract_power, [17](#)
extract_power_stable, [19](#)
extract_signal, [20](#)
extract_signal_stable, [22](#)
extract_signal_stable_V2, [23](#)
extract_signal_standard_deviation, [24](#)

getLaskar, [5](#), [6](#)
grey, [27](#)
grey_track, [27](#)

Hilbert_transform, [28](#)

inst.pulse, [28](#)

loess.as, [29](#)
loess_auto, [18](#), [29](#)

mag, [30](#)
mag_track_solution, [31](#)
max_detect, [31](#), [31](#)
min_detect, [32](#), [32](#)
model_red_noise_wt, [33](#), [33](#), [34](#), [39](#)

percentile_from_red_noise, [34](#), [34](#)
plot_avg_wavelet, [35](#)
plot_wavelet, [36](#)

sedrate2time, [15](#), [16](#)

sum_power_sedrate, [38](#), [39](#)

track_period_wavelet, [11](#), [13](#), [14](#), [16](#), [18](#),
[25](#), [31](#), [40](#), [40](#), [42](#)
TSI, [41](#)

wavelet_uncertainty, [42](#), [42](#)
WaveletComp-package, [4](#)
WaverideR, [44](#)
WaverideR_Datasets, [45](#)