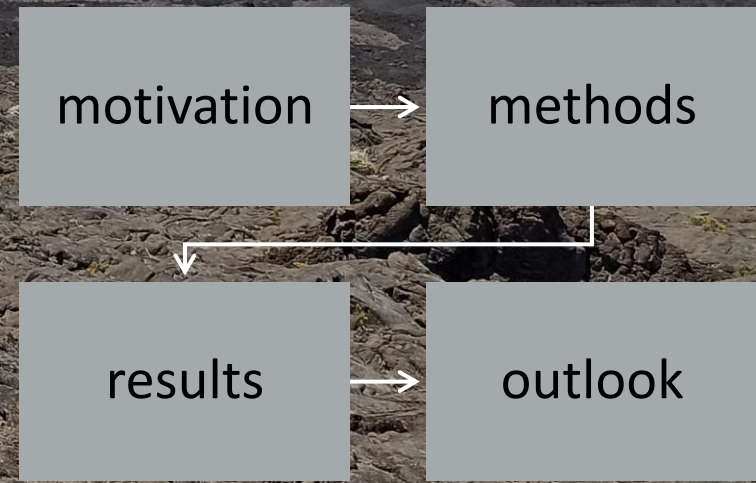


Comparison of a rotational sensor and an array on Piton de la Fournaise volcano, La Réunion

Nele I. K. Vesely¹, Eva P. S. Eibl¹, Valérie Ferrazzini^{2,3}, and Joachim Wassermann⁴



¹ Institute of Geosciences, University of Potsdam, Potsdam, Germany (vesely1@uni-potsdam.de)

² Université de Paris, Institut de physique du globe de Paris, CNRS, F-75005, Paris, France

³ Observatoire volcanologique du Piton de la Fournaise, Institut de physique du globe de Paris, La Plaine des Cafres, Réunion

⁴ Department of Earth and Environmental Sciences, Ludwig-Maximilians-University of Munich, Munich, Germany



Piton de la Fournaise volcano

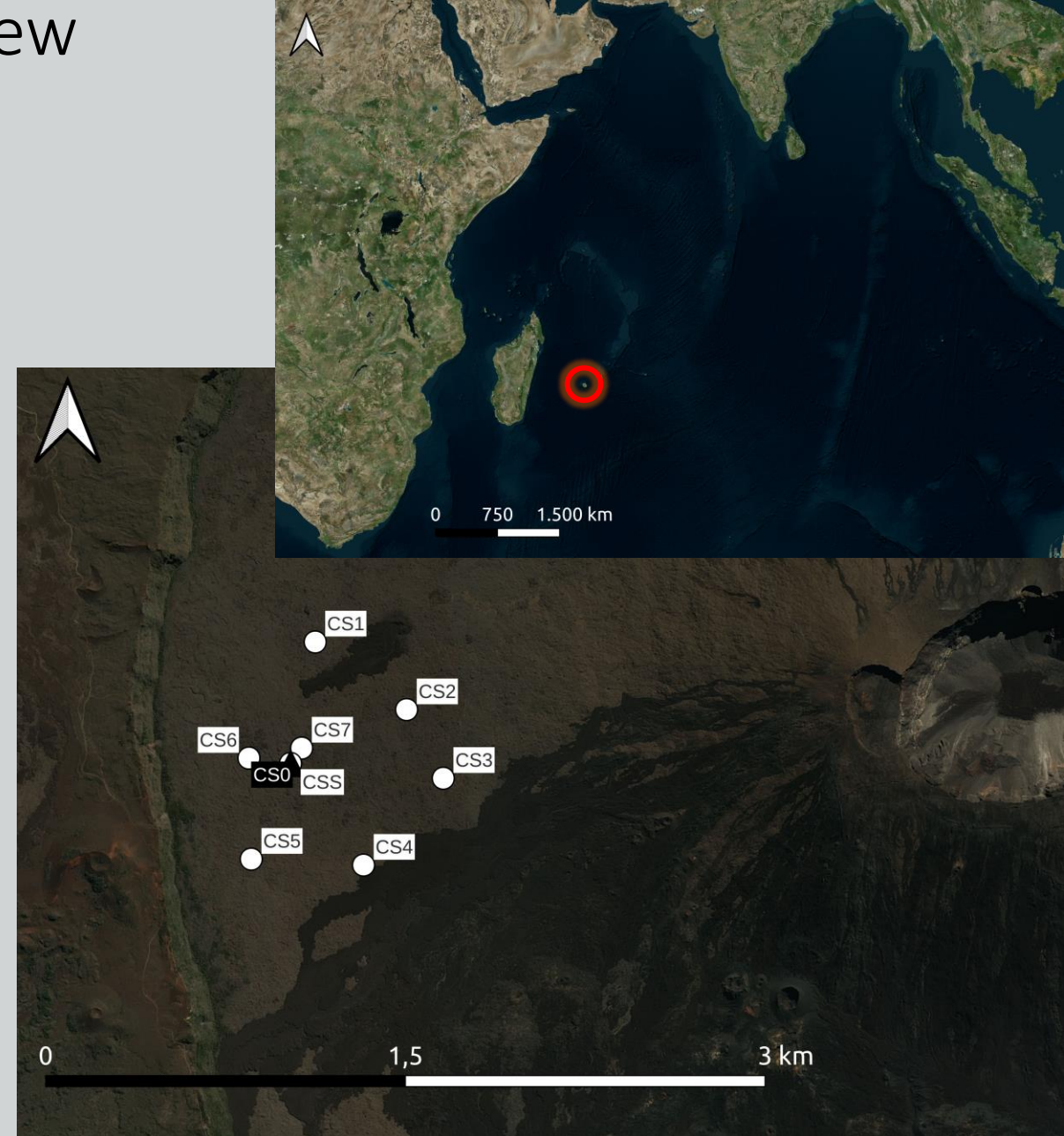
- recently 1-2 eruptions per year
- pre-eruptive signals: seismic swarm, tremor

Installation and methods

- rotational sensor, array (8 seismometers)
- ADR, SNR, BAZ for rockfall, local + summit EQ

Results

- array BAZ good for close & stronger events
- rotational sensor rockfall BAZ possibly true



ADR

Array Derived Rotation

SNR

Signal to Noise Ratio

BAZ

Back azimuth calculation

Array derived rotation (ADR)

- **displacement relation** between neighboring points assuming infinitesimal deformation to obtain rotation (Cochard et al. 2006, Spudich et al. 1995)
- rotation approximated by solving sampling points' linear equations; **finite difference approximation** by array stations (G) assuming uniformity of the strain tensor over array extent (Spudich et al. 2008, Suryanto 2006)

$$\mathbf{G} = \begin{bmatrix} u_{r,r} & u_{r,t} & u_{r,z} \\ u_{t,r} & u_{t,t} & u_{t,z} \\ -u_{r,z} & -u_{t,z} & -\eta(u_{r,r} + u_{t,t}) \end{bmatrix} \quad \longrightarrow \quad \begin{bmatrix} \omega_r \\ \omega_t \\ \omega_z \end{bmatrix} = \begin{bmatrix} u_{z,t} \\ -u_{z,r} \\ -\frac{1}{2}(u_{r,t} - u_{t,r}) \end{bmatrix}$$

Donner et al. 2017

frequency (f) range limited by array aperture (h)

- here: 1 - 3.5Hz from 225m distance of 3 array stations and ground heterogeneities

$$\frac{0.00238 \cdot c}{h} < f < \frac{0.25 \cdot c}{h}$$

Donner et al. 2017

Signal to noise ratio (SNR)

- Theoretical background:
 - calculation of averaged SNR as the **sum of the root mean square (RMS)** of all components' Signal (S) and divide by sum of RMS Noise (N)

$$SNR = \frac{\sqrt{\frac{1}{n} \sum_{i=0}^n S_{ei}^2 + S_{ni}^2 + S_{zi}^2}}{\sqrt{\frac{1}{n} \sum_{i=0}^n N_{ei}^2 + N_{ni}^2 + N_{zi}^2}}$$

Eibl et al. 2022

- Configuration here:
 - RMS of two **10s-time windows** before and during the event
 - gap of 5s between the signal and noise windows to avoid overlap

- Theoretical background:
 - Fast Fourier Transform of real input
 - computing **covariances** of signal at different **array stations**
 - creating slowness maps
 - calculating **BAZ from slowness map**
- Output:
 - BAZ
 - slowness
 - power (real, absolute)
 - semblance
- obspy code from Van Driel & Bayreuther 2010

- Theoretical background:
 - rotational sensor horizontal components for **orthogonal distance regression**
 - **ambiguity corrected** with co-located seismometer
 - assumption of only one source and planar incoming wavefield

$$\begin{aligned}\omega_x &= \frac{1}{2} Ak \sin \phi \sin(\omega t - \mathbf{k} \cdot \mathbf{r} + \varphi), \\ \omega_y &= -\frac{1}{2} Ak \cos \phi \sin(\omega t - \mathbf{k} \cdot \mathbf{r} + \varphi), \\ \omega_z &= 0.\end{aligned}$$

Sollberger et al. 2018

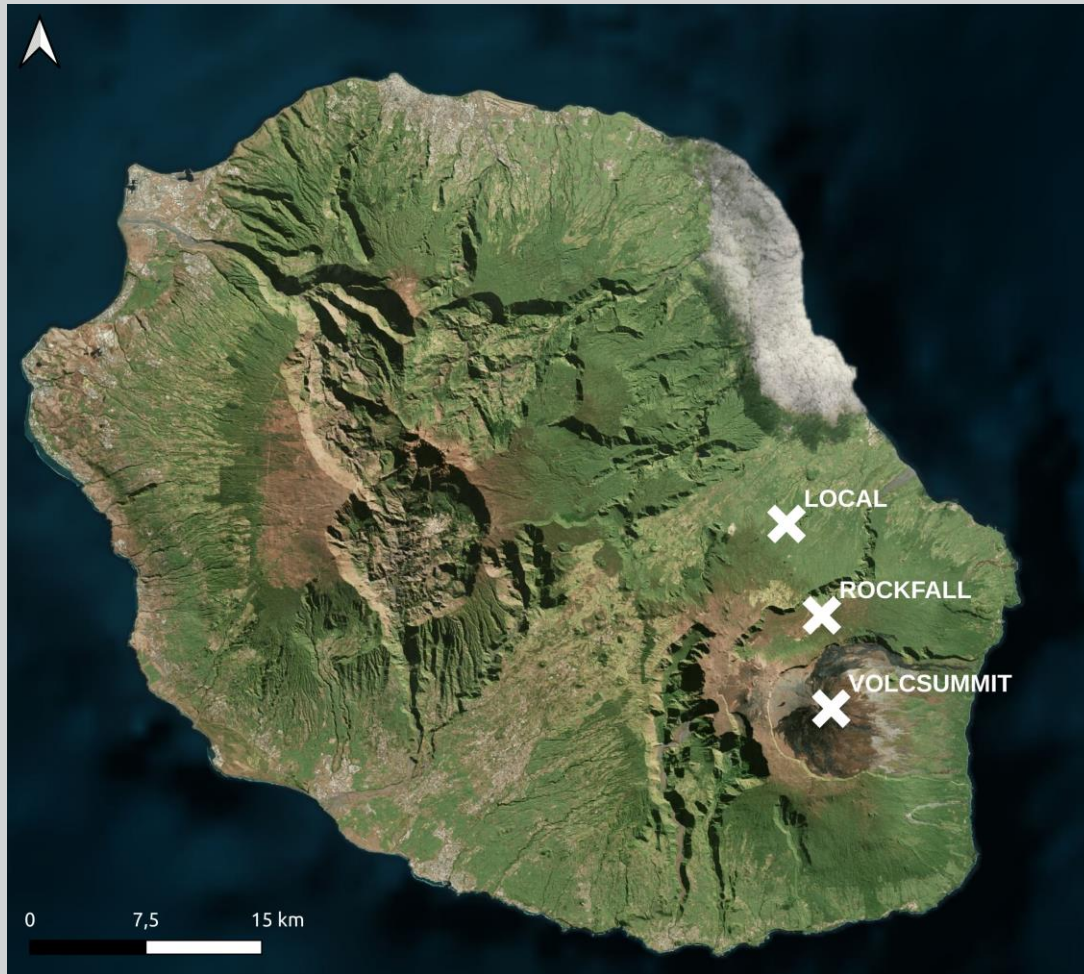
- Output: BAZ, standard error
- Configuration here: 1s sliding windows, overlap of 10%
- code from Wassermann et al. 2016 & Wassermann et al. 2020

- Theoretical background:
 - North and East seismometer components rotated around possible BAZ values
 - correlation of transverse and vertical rotation from rotational sensor
 - BAZ of highest correlation extracted
 - phase velocities estimated from amplitude ratios

$$\frac{a_T}{\dot{\omega}_z} = \frac{-k^2 c^2 A \sin(kx - kct)}{\frac{1}{2} k^2 c A \sin(kx - kct)} = -2c$$

Hadziioannou et al. 2012

- Output: BAZ, phase velocities
- Configuration: 1s sliding windows
- code from Hadziioannou et al. 2012



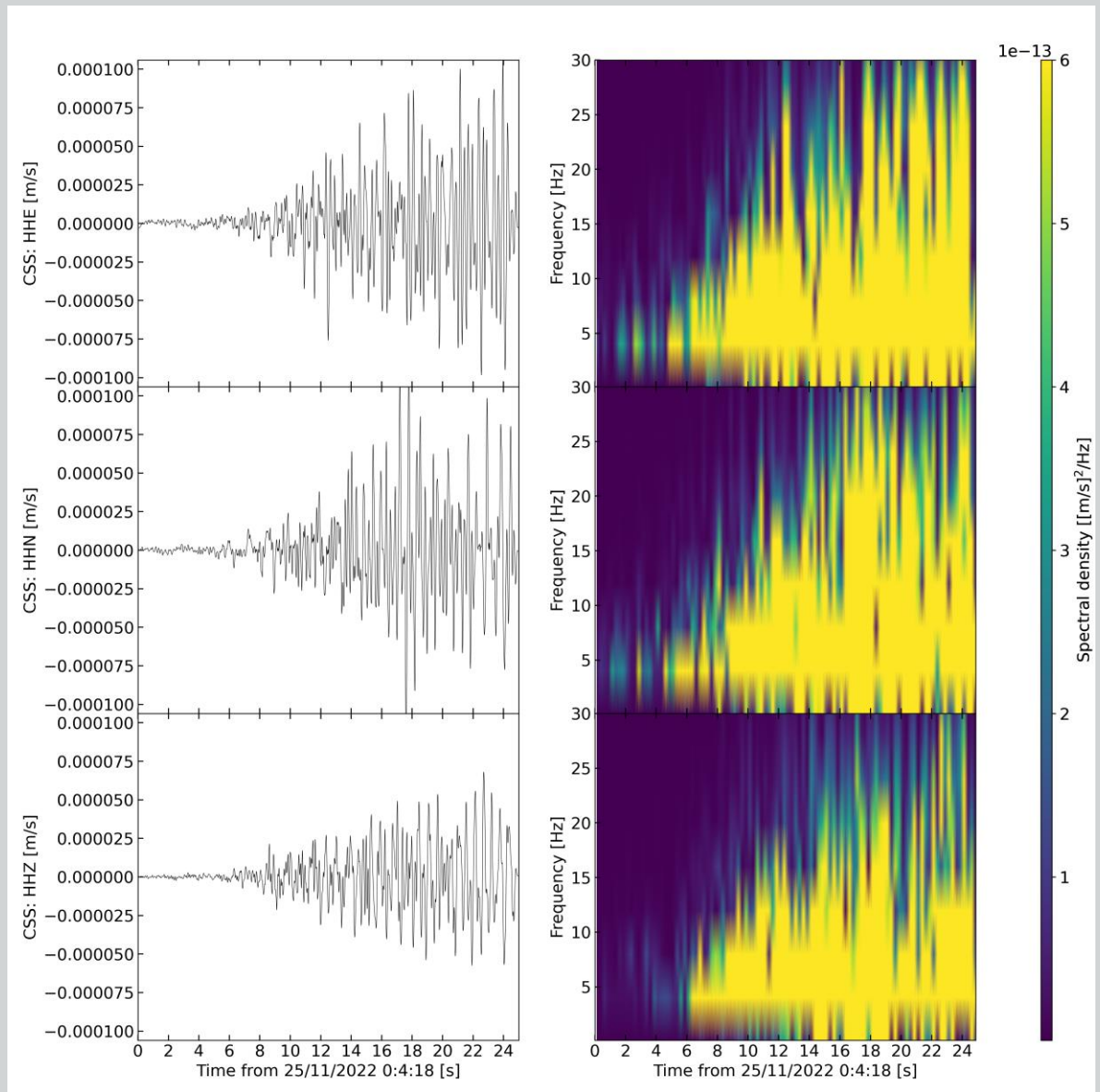
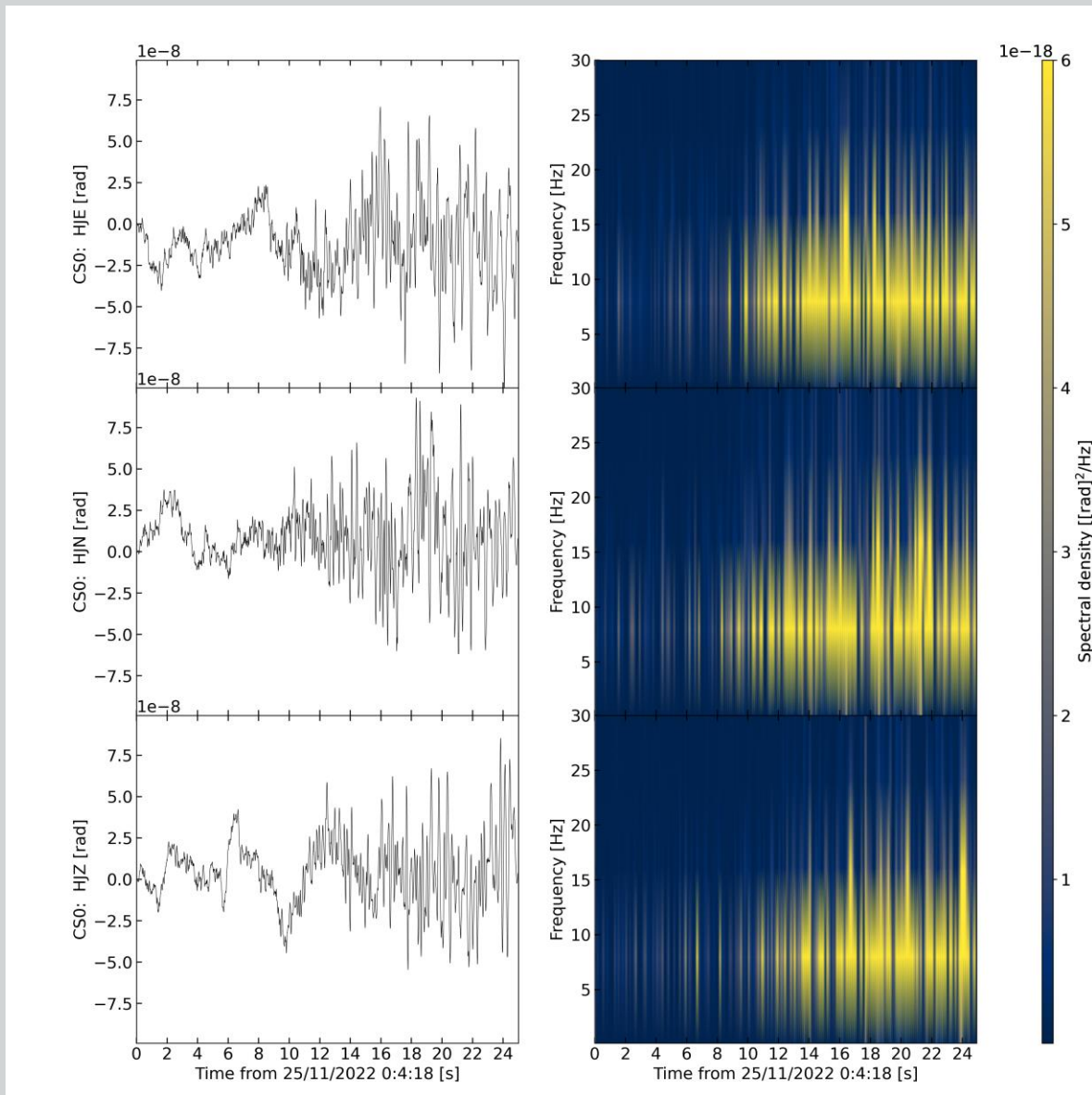
Spectrograms

SNR

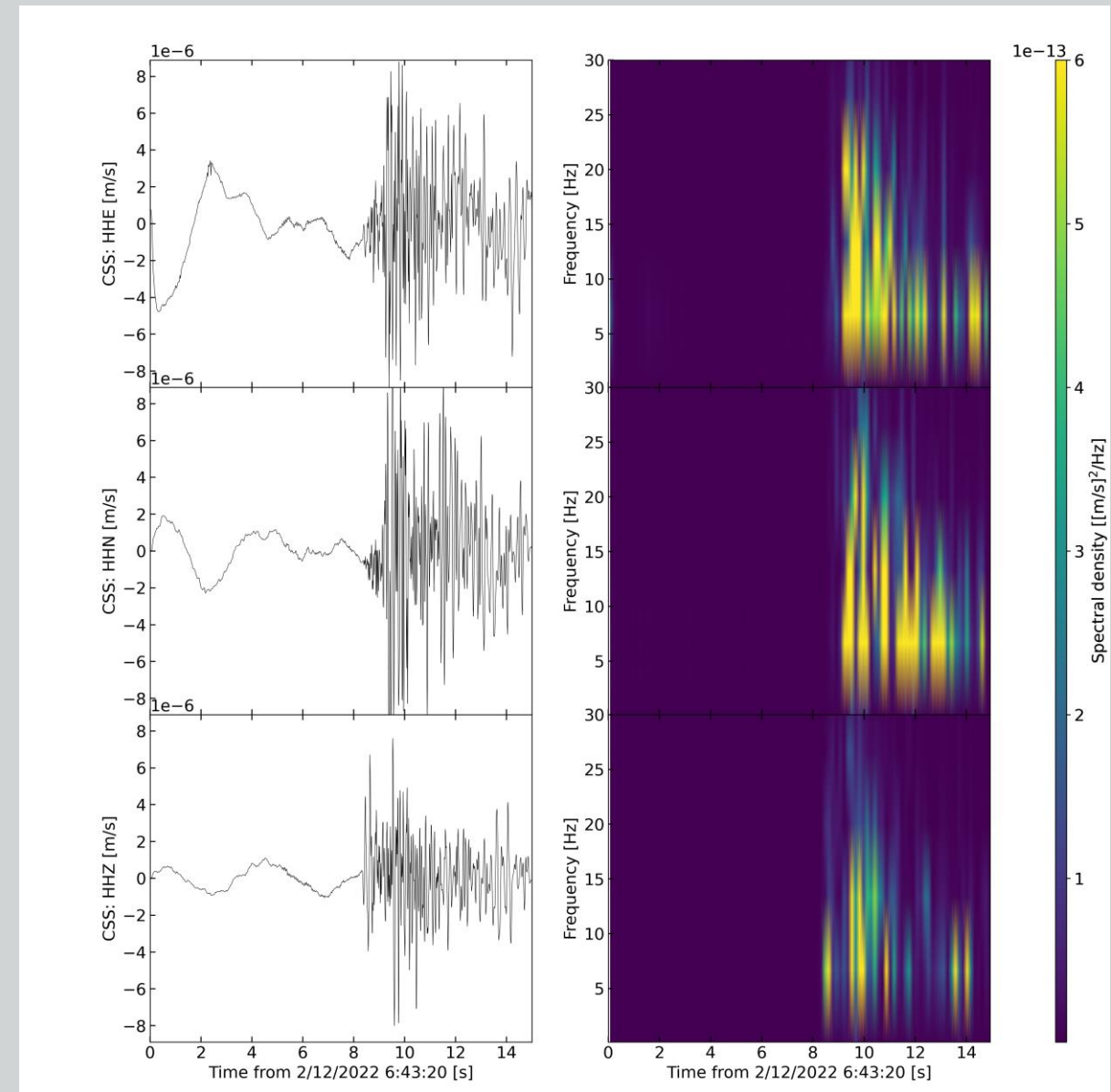
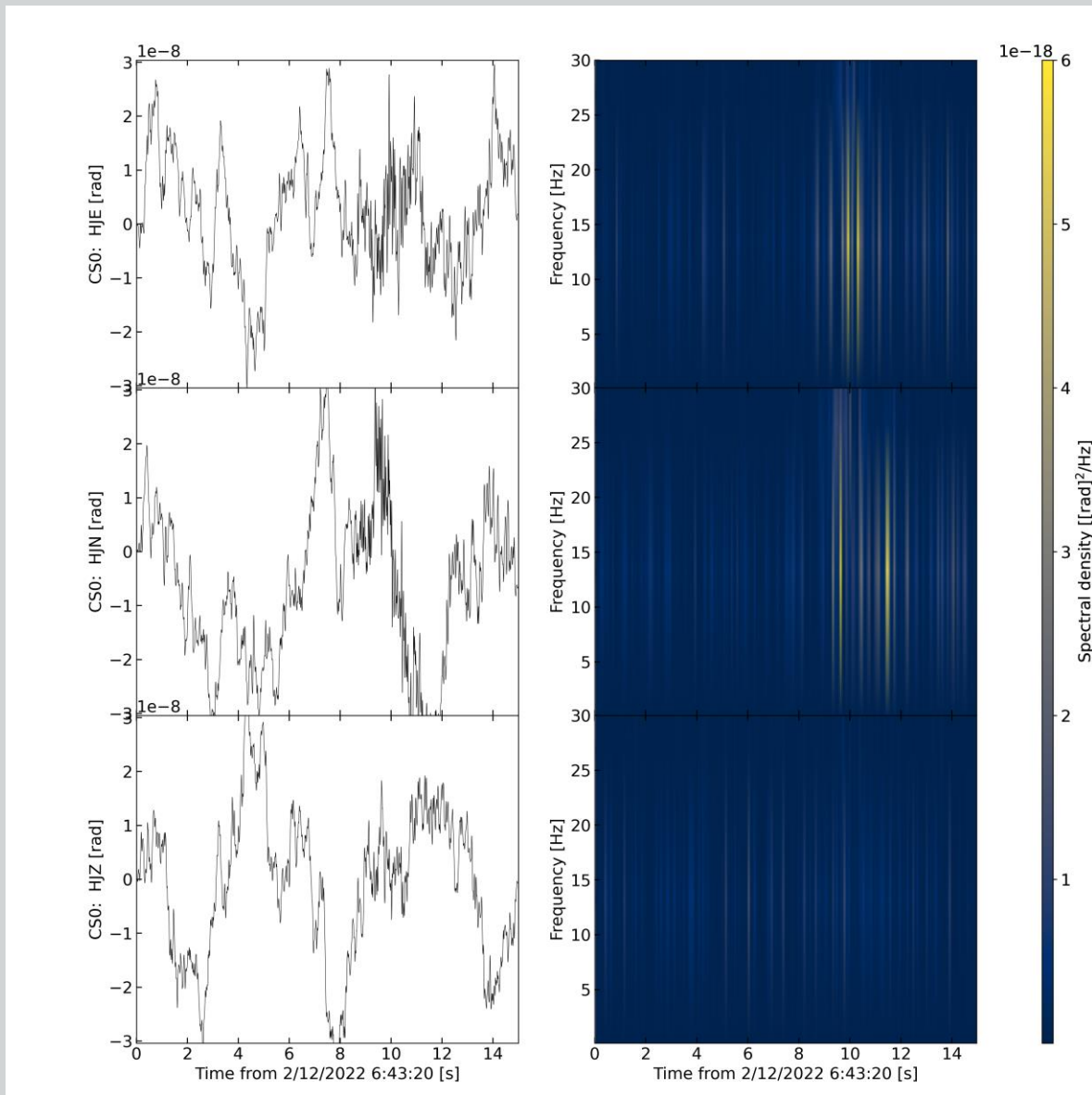
ADR

BAZ

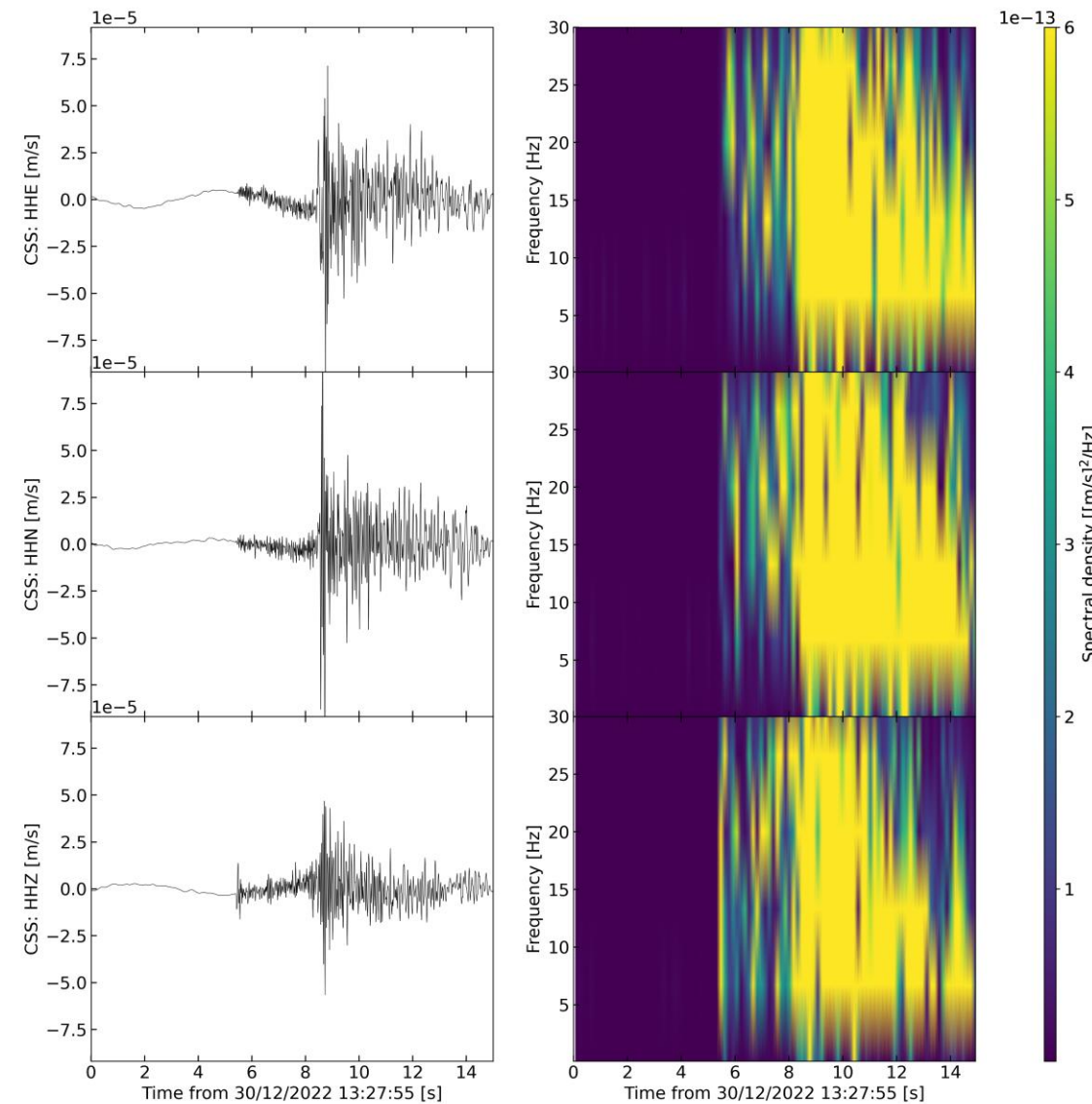
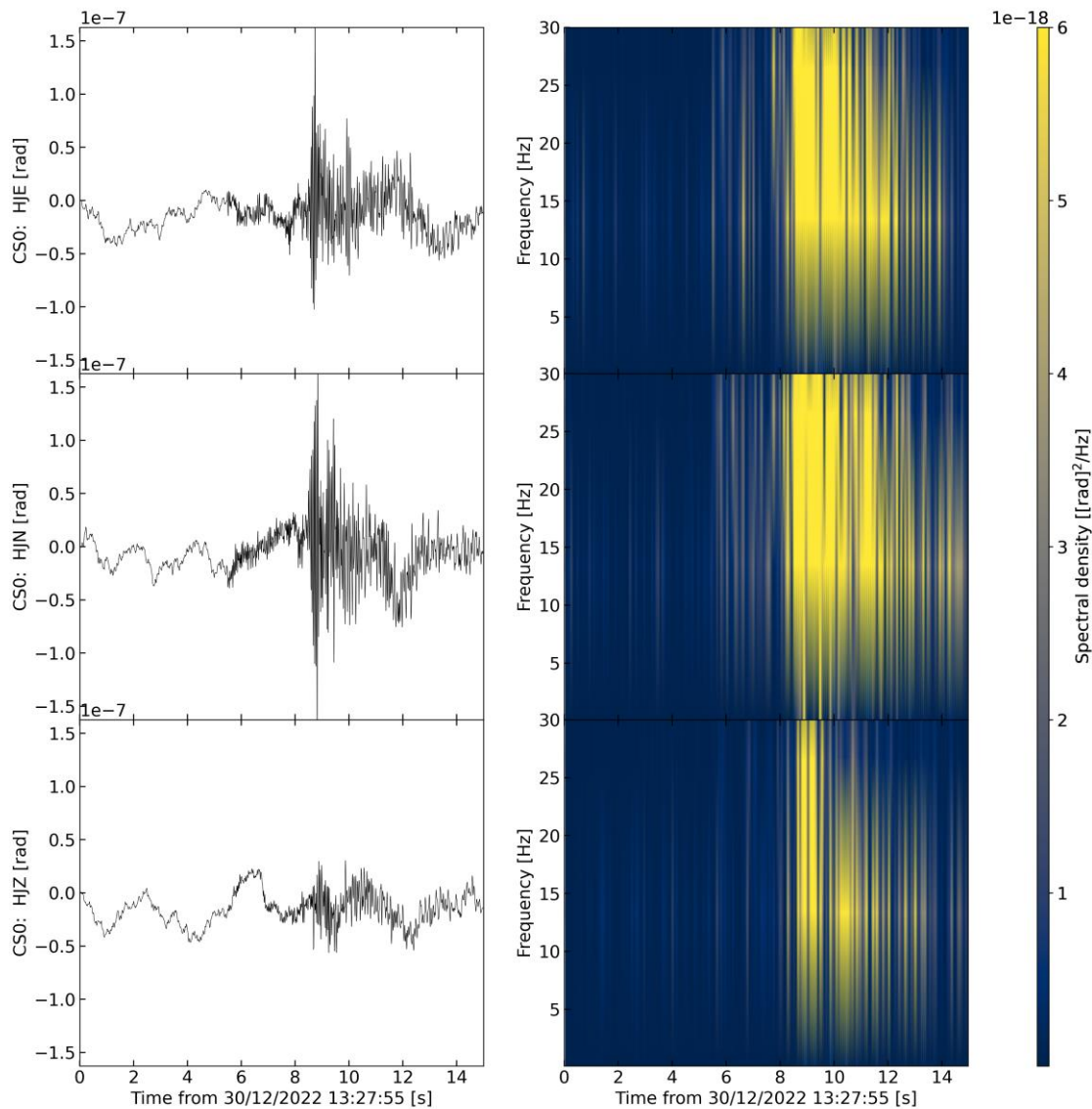
Spectrogram: Rockfall event 25.11.2022



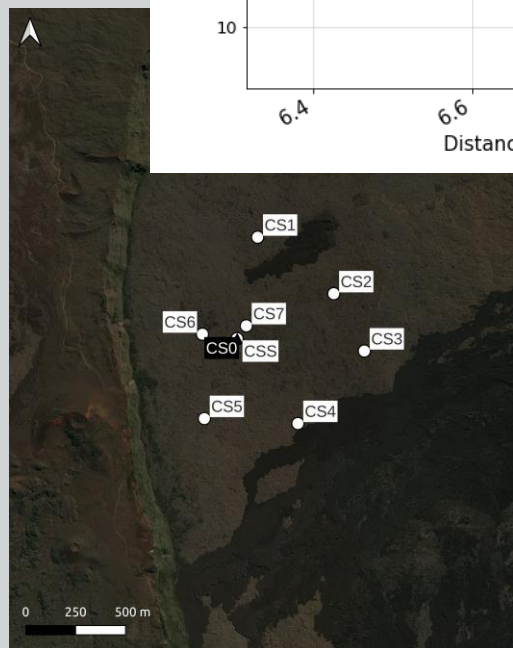
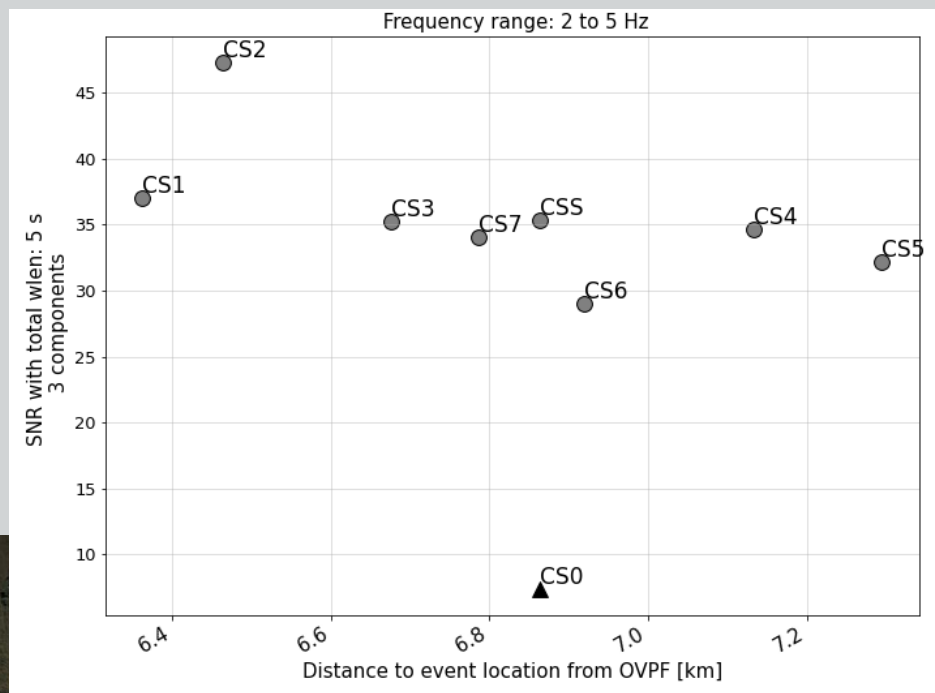
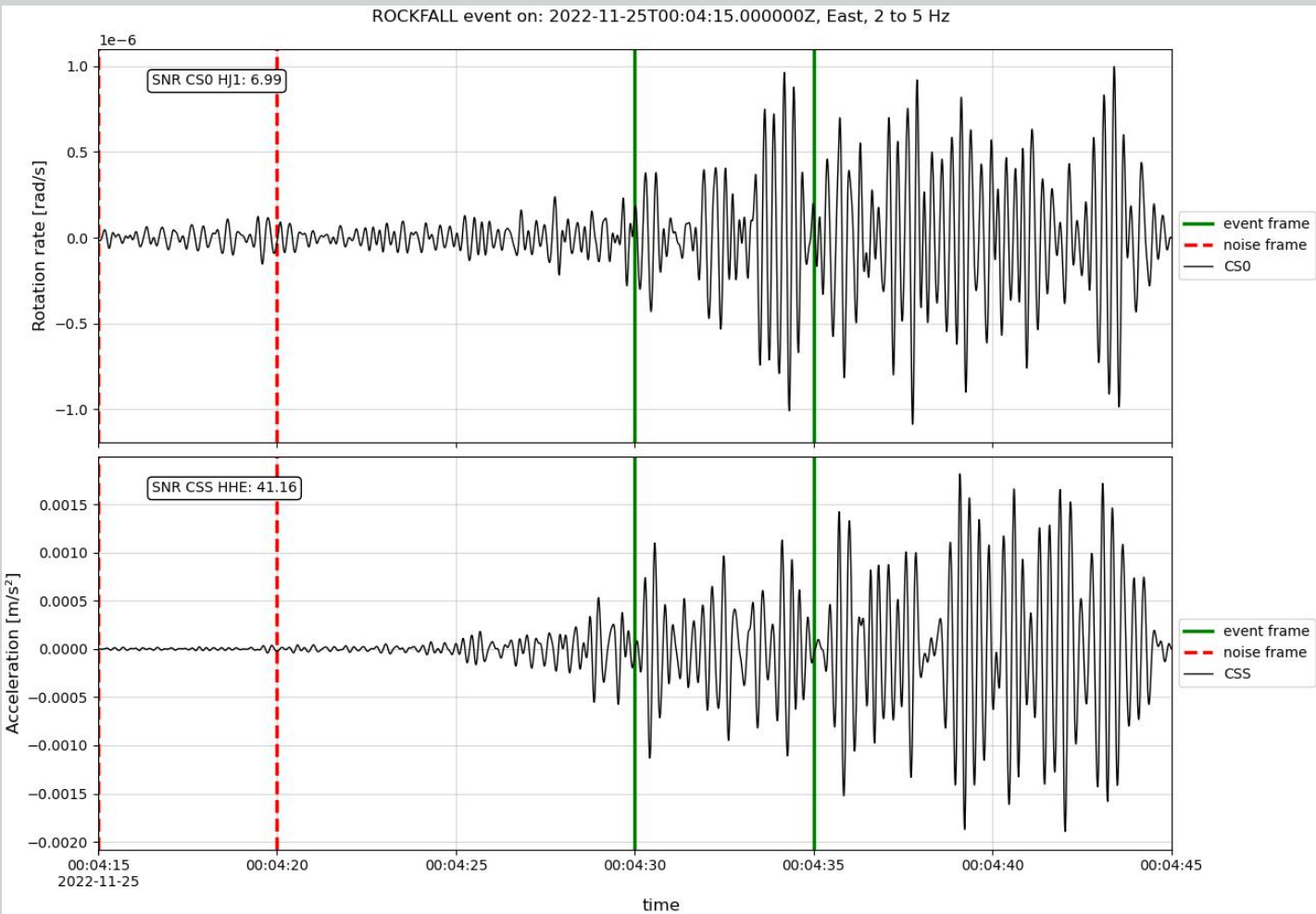
Spectrogram: Volcsummit 02.12.2022



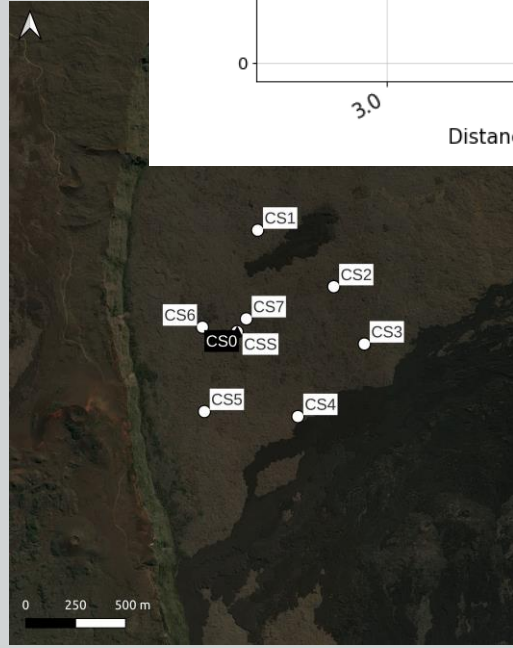
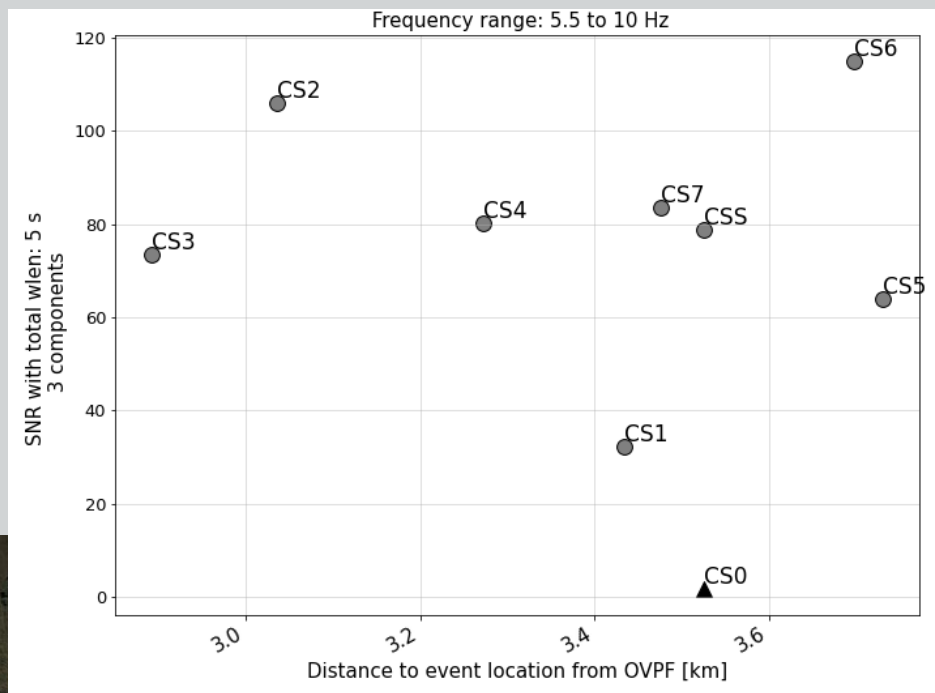
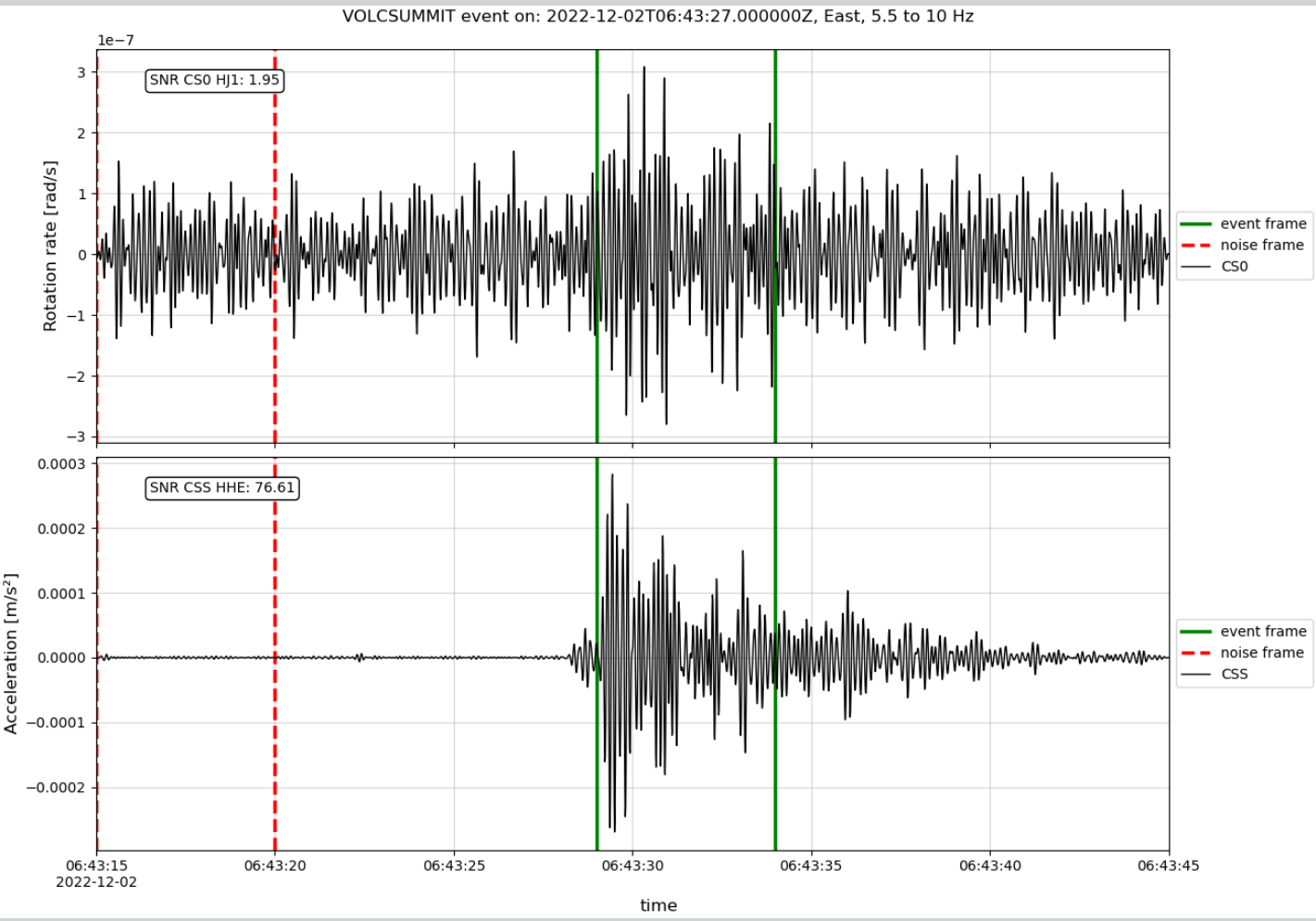
Spectrogram: Local event 30.12.2022



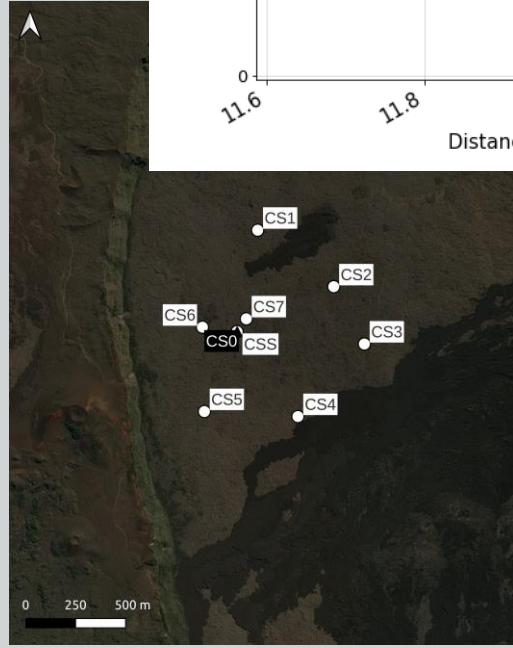
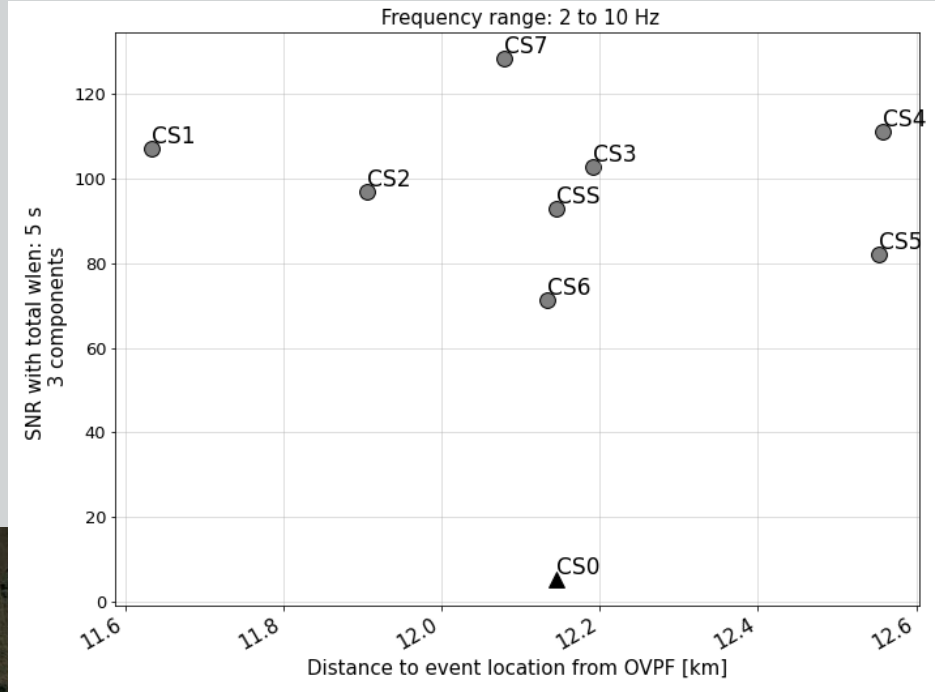
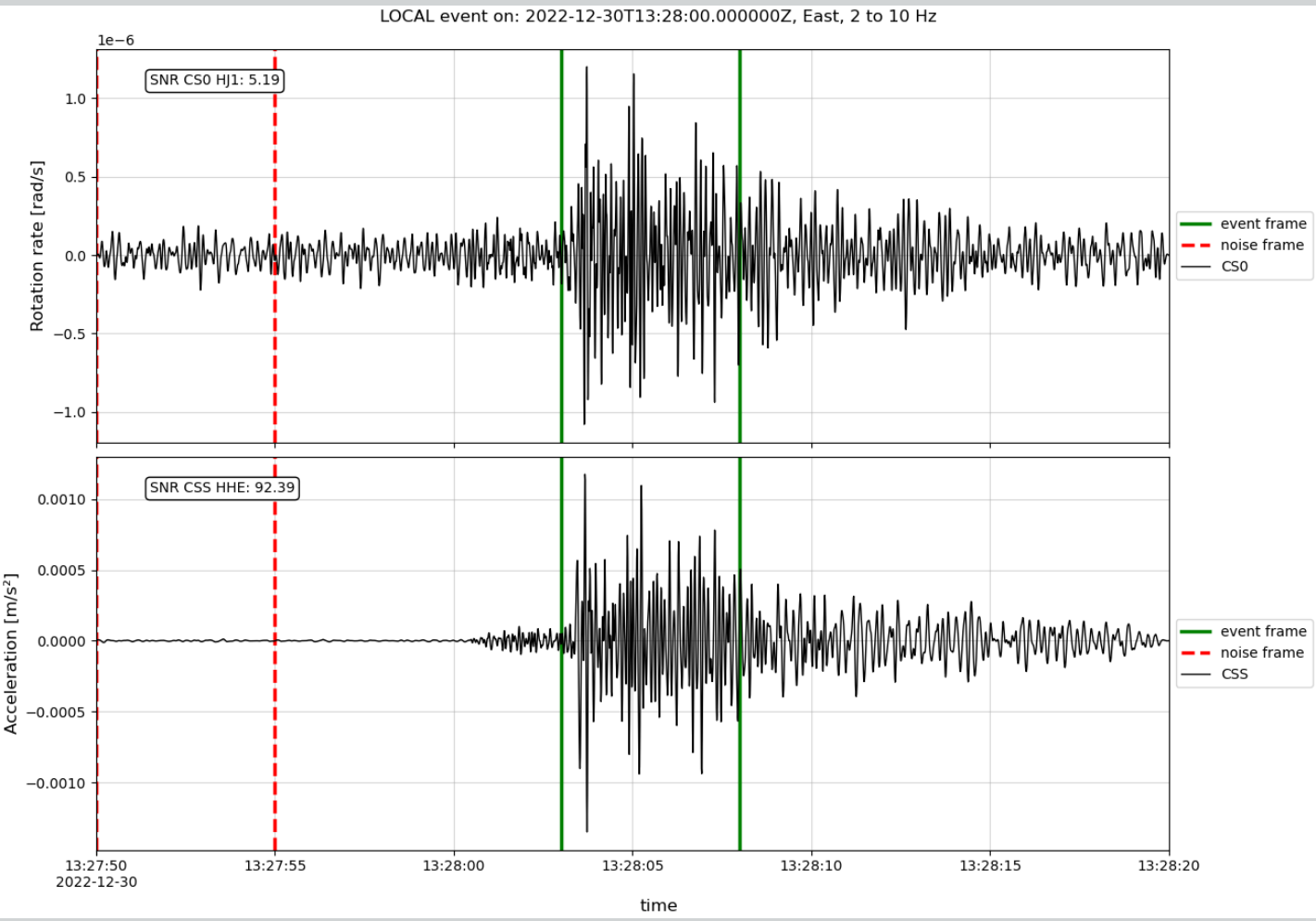
SNR: Rockfall event 25.11.2022



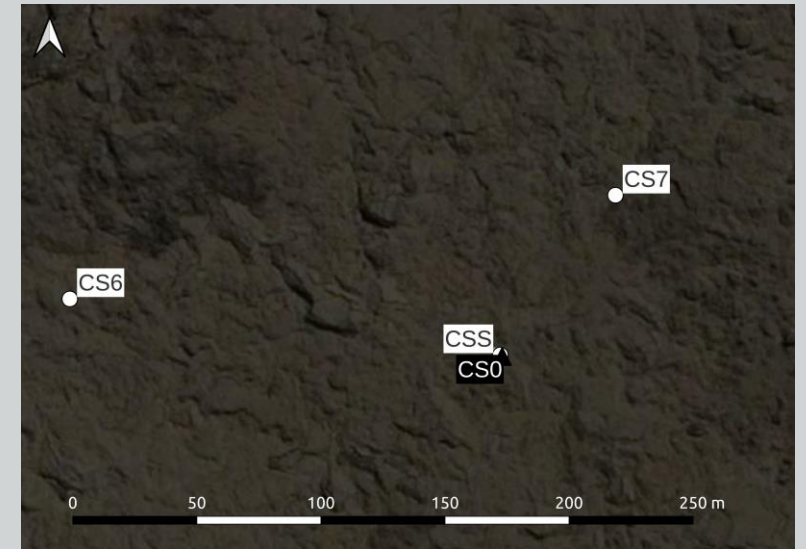
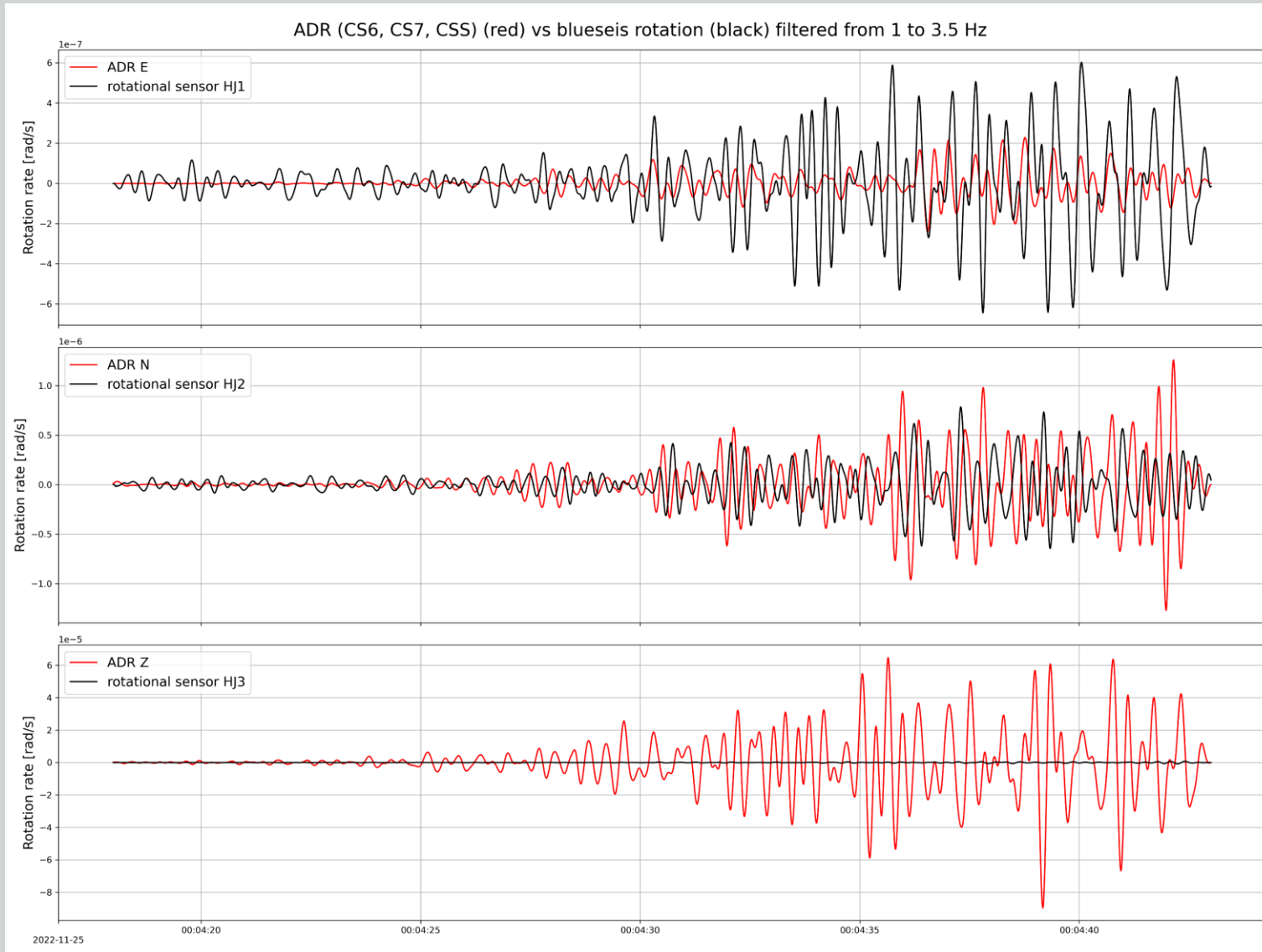
SNR: Volcsummit event 02.12.2022



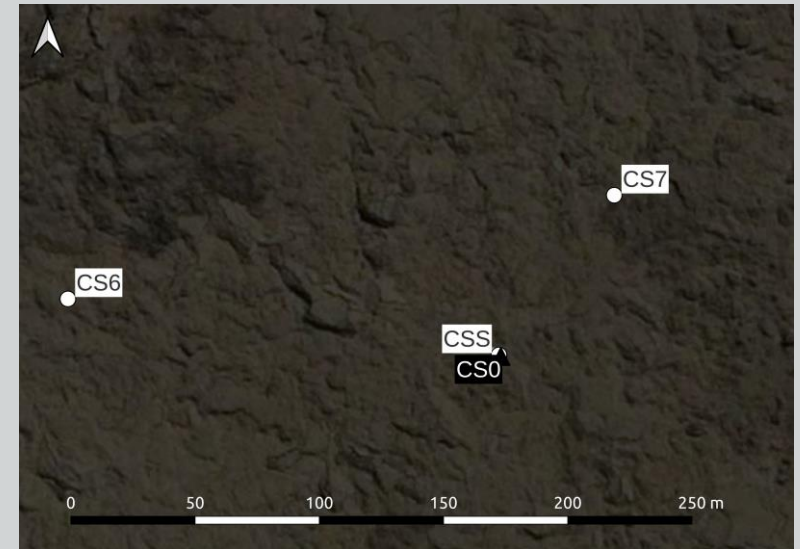
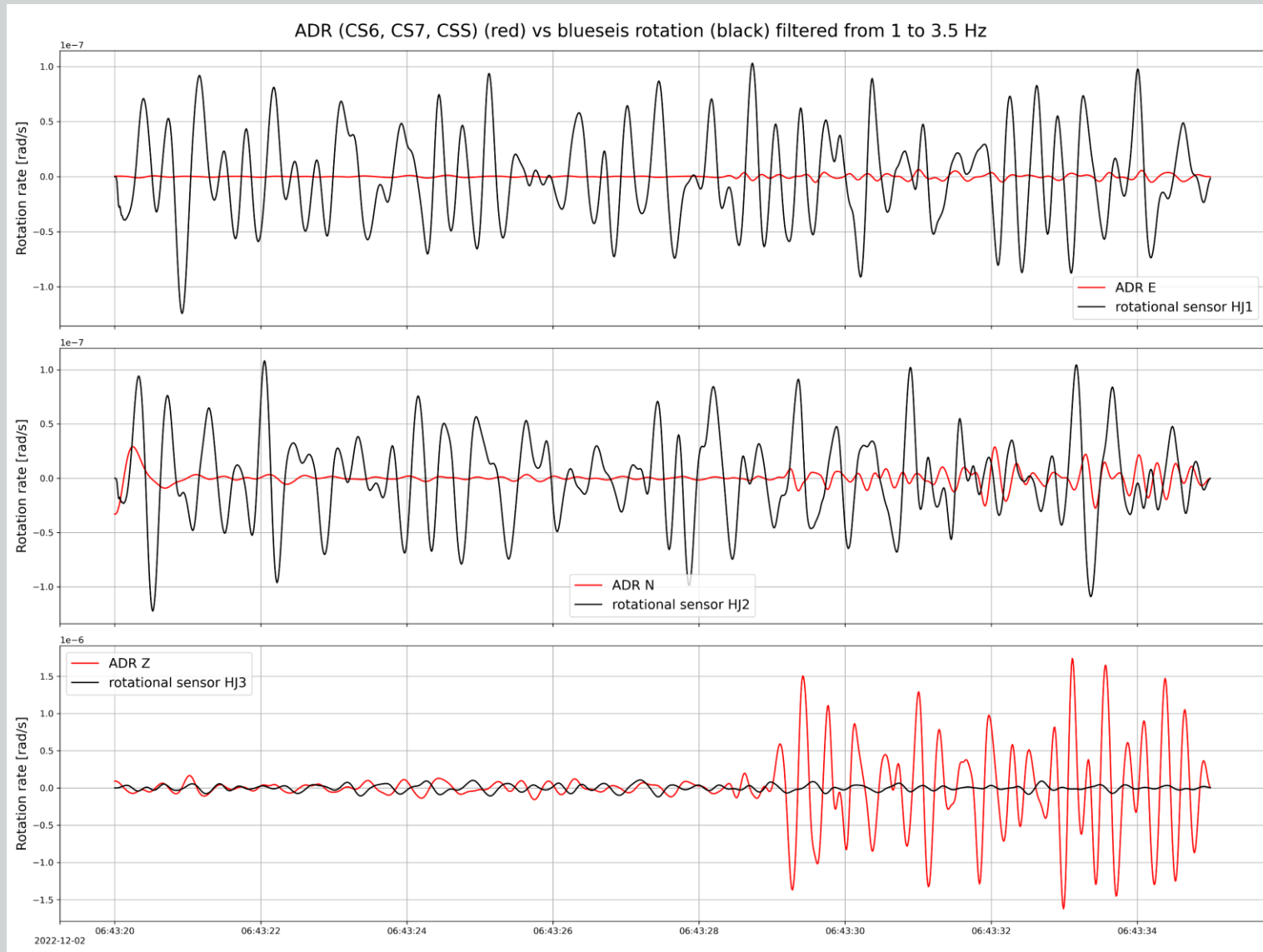
SNR: Local event 30.12.2022



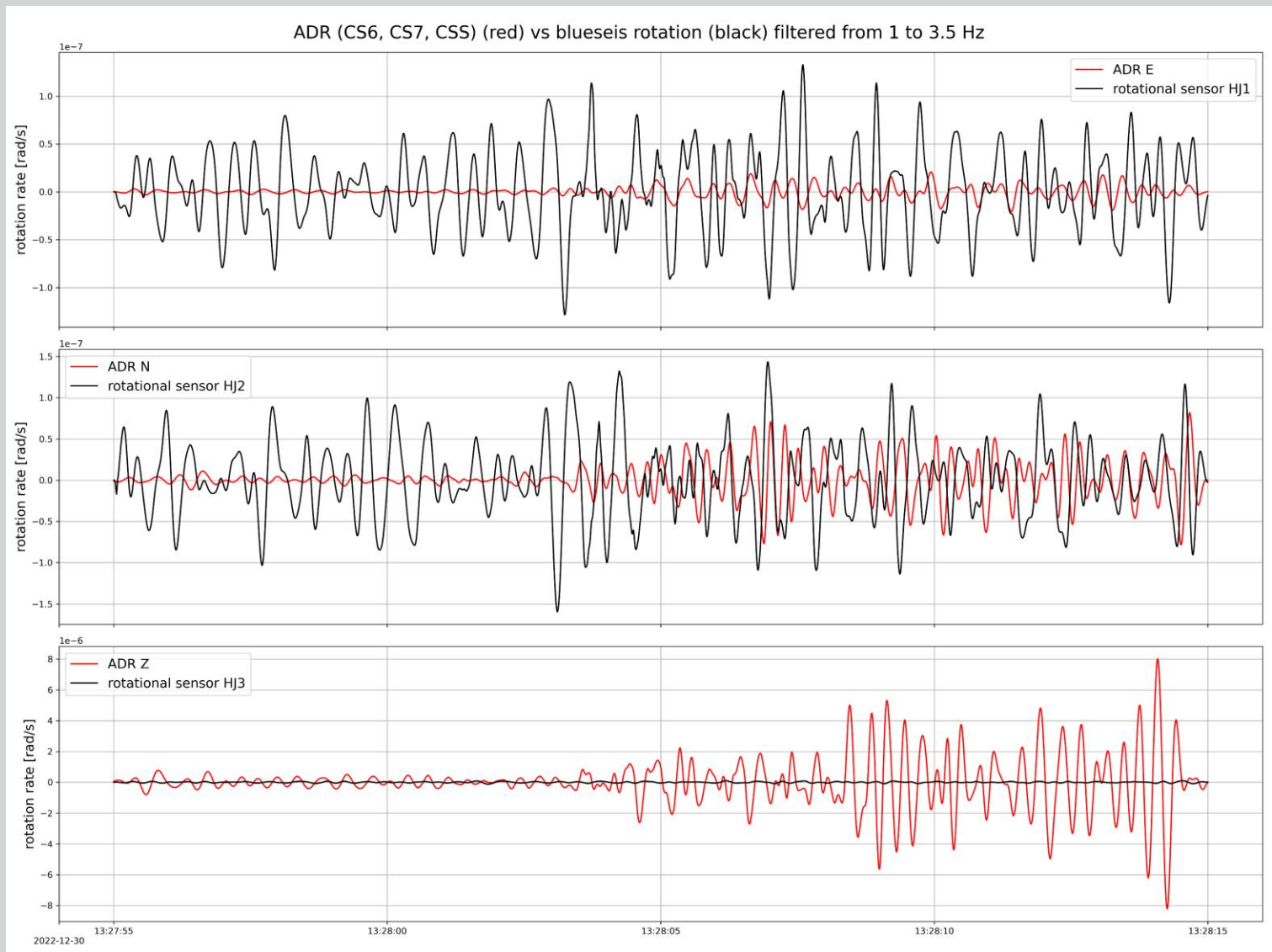
ADR: Rockfall event 25.11.2022



ADR: Volcsummit event 02.12.2022

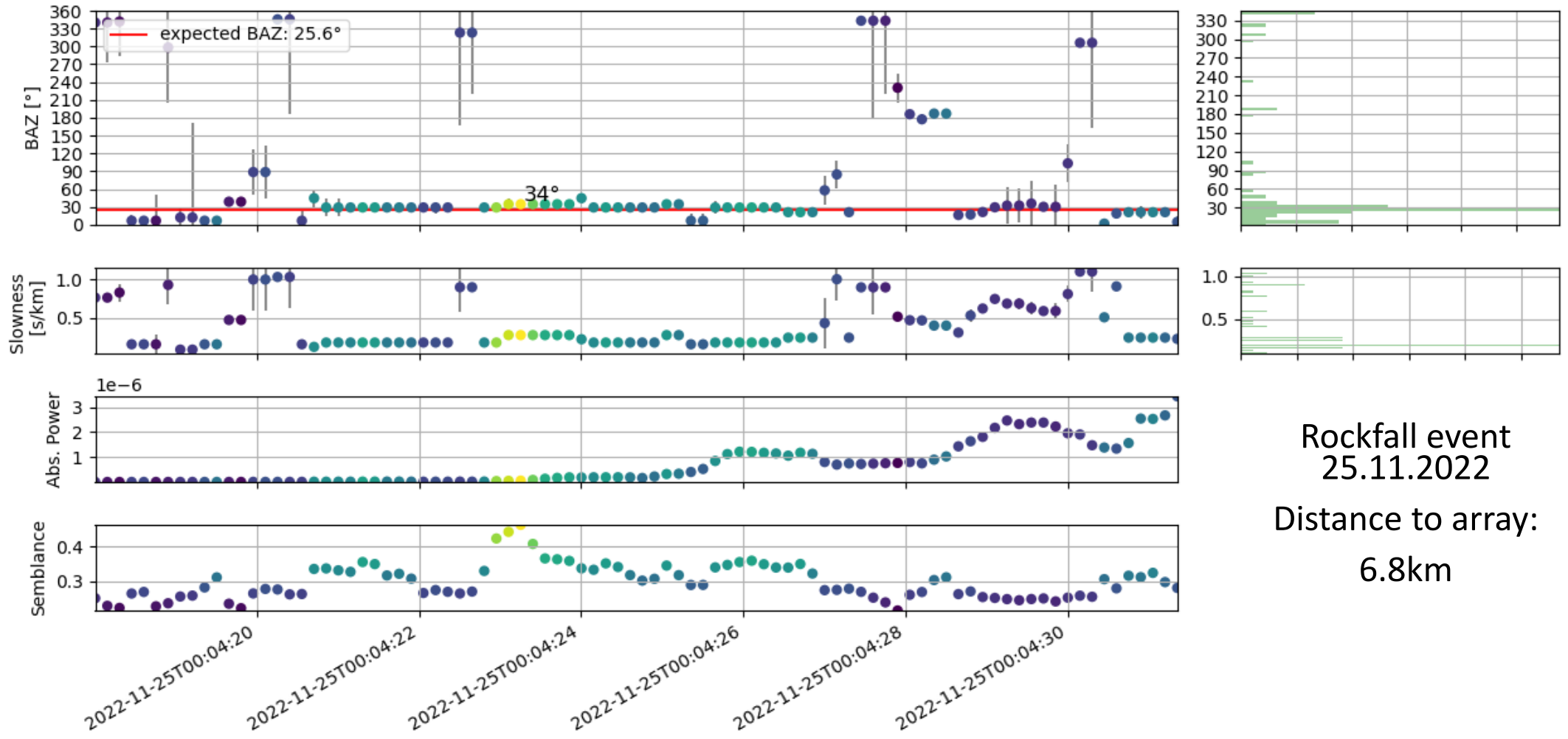


ADR: Local event 30.12.2022



Back azimuth array

ROCKFALL: 2-5Hz

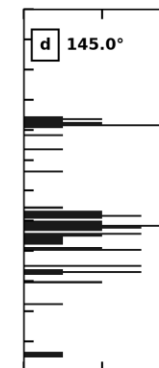
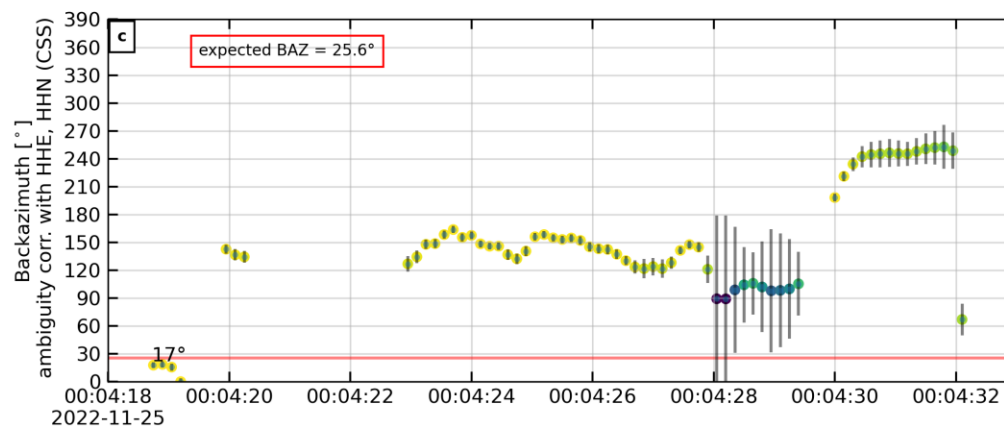
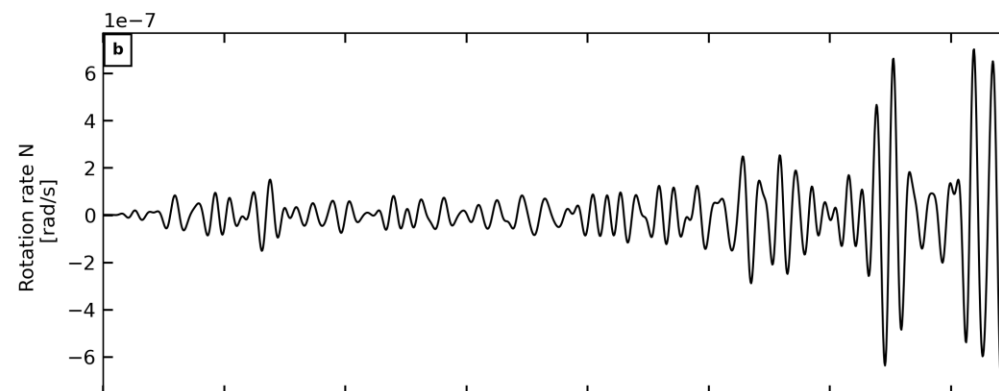
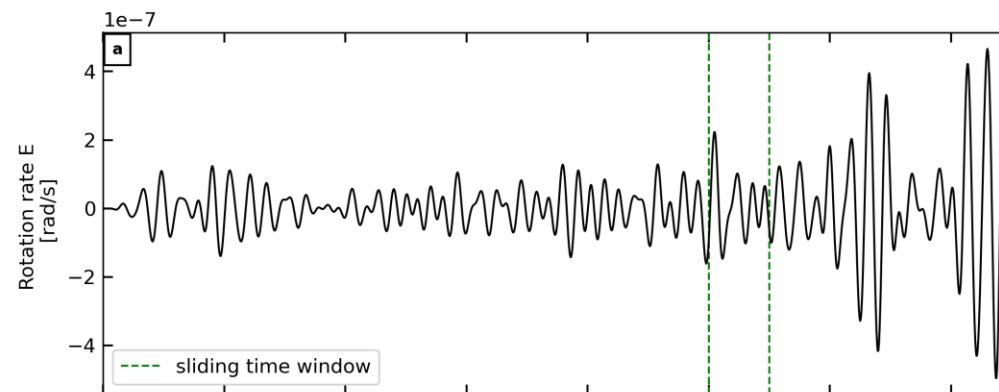


Rockfall event
25.11.2022
Distance to array:
6.8km

Back azimuth horizontal components

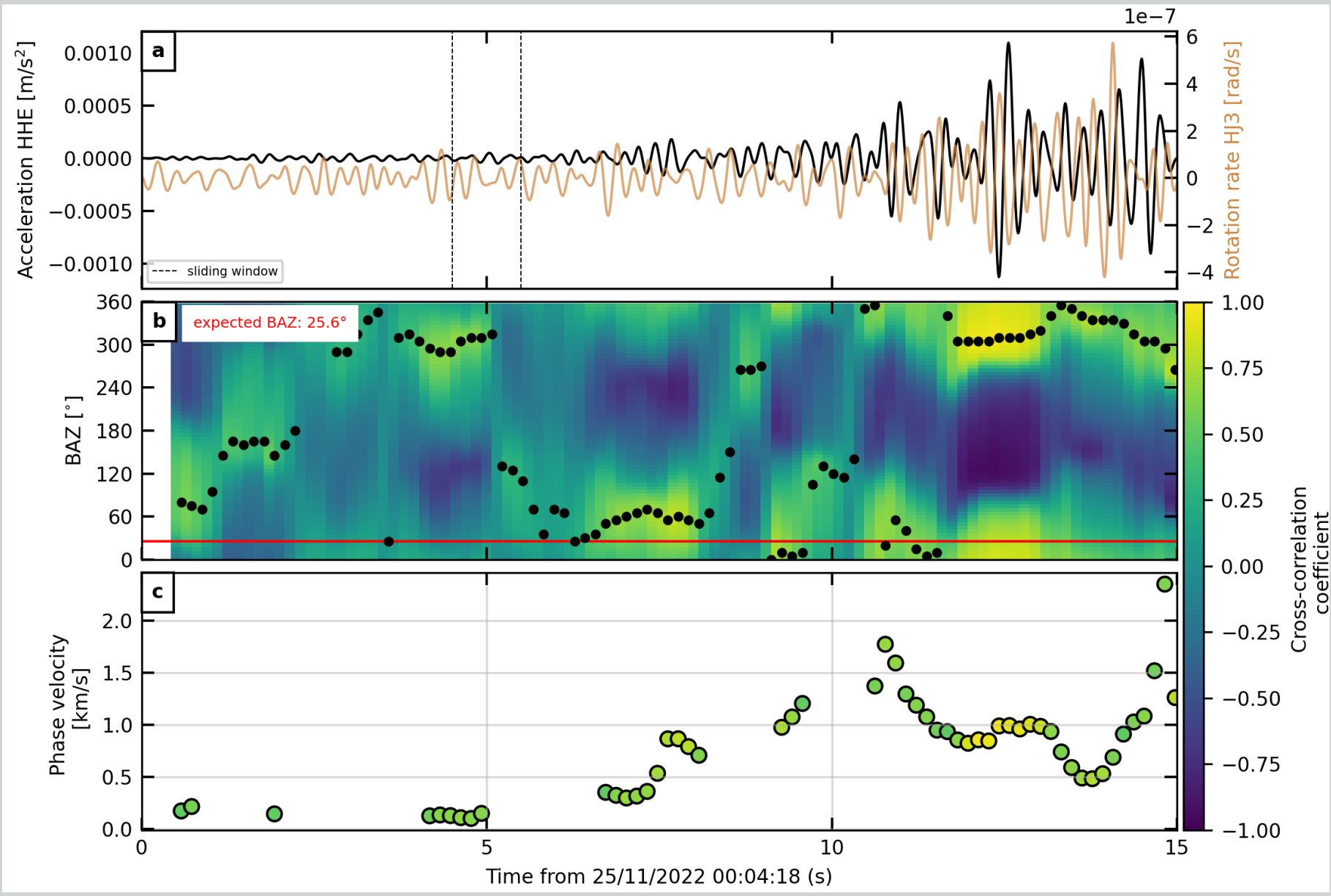
Rockfall event
25.11.2022

Distance to CS0: 6.9km

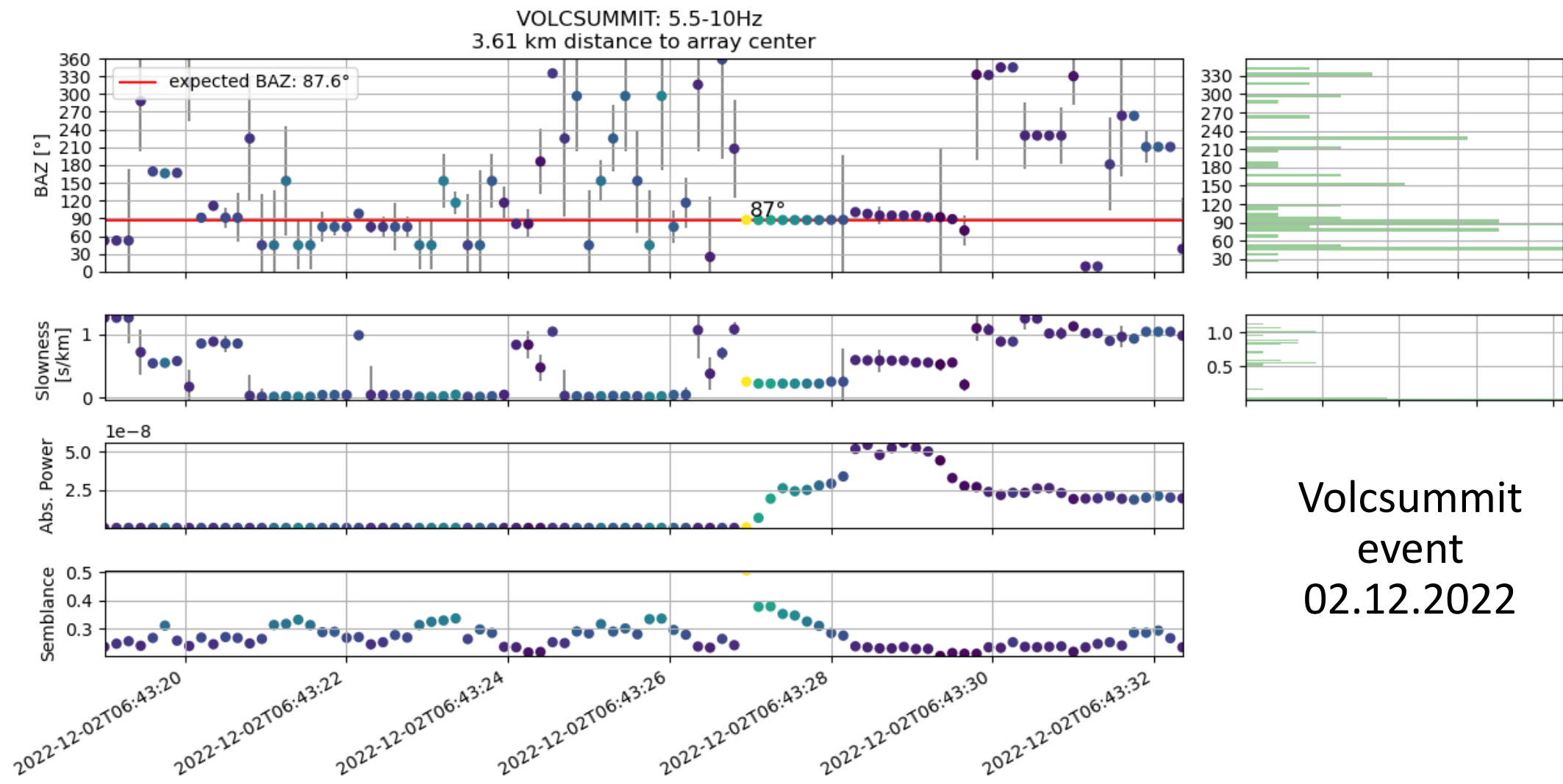


Back azimuth 6C method

Rockfall event
25.11.2022
Distance to CS0:
6.9km



Back azimuth array

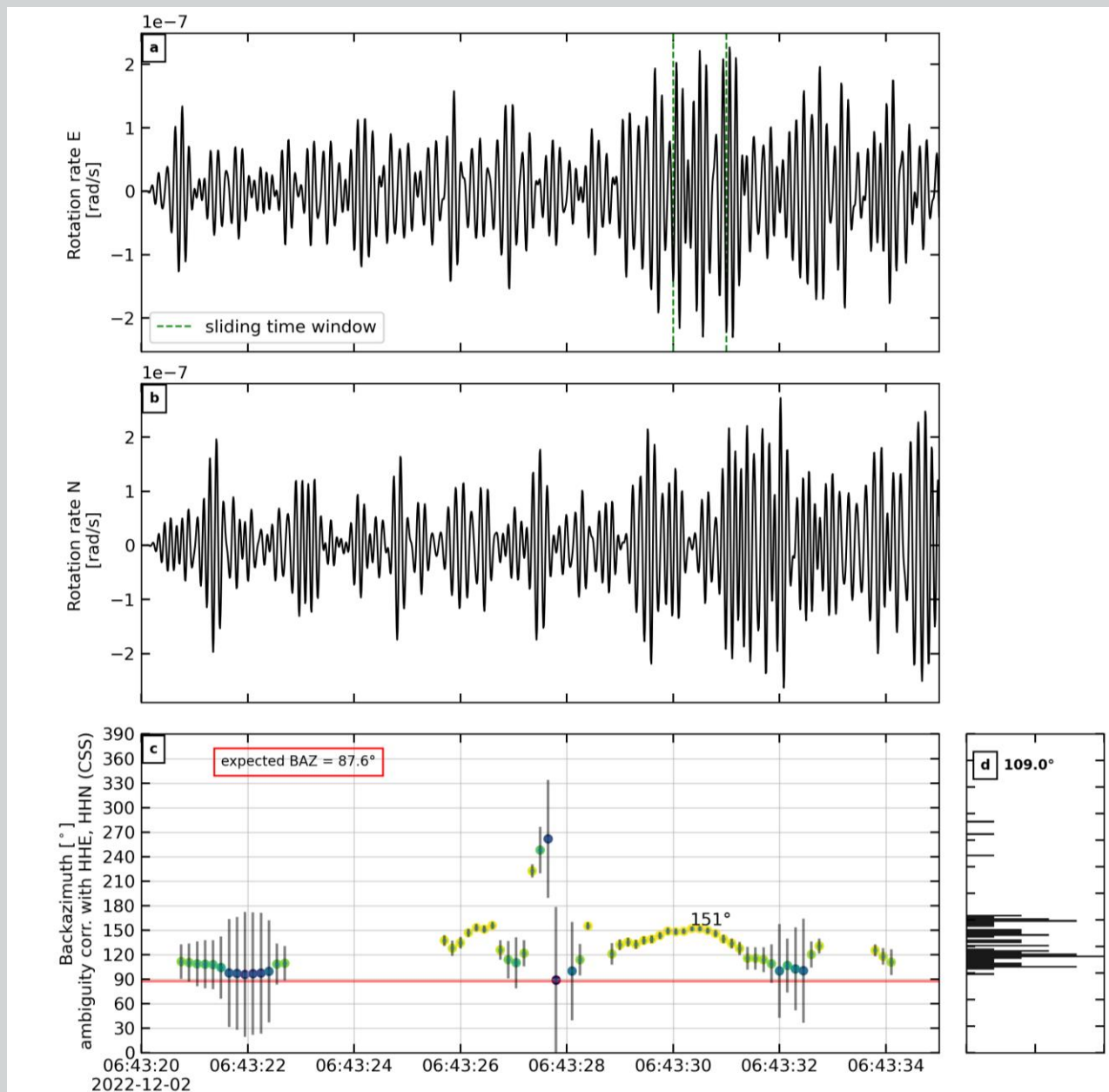


Volcsummit
event
02.12.2022

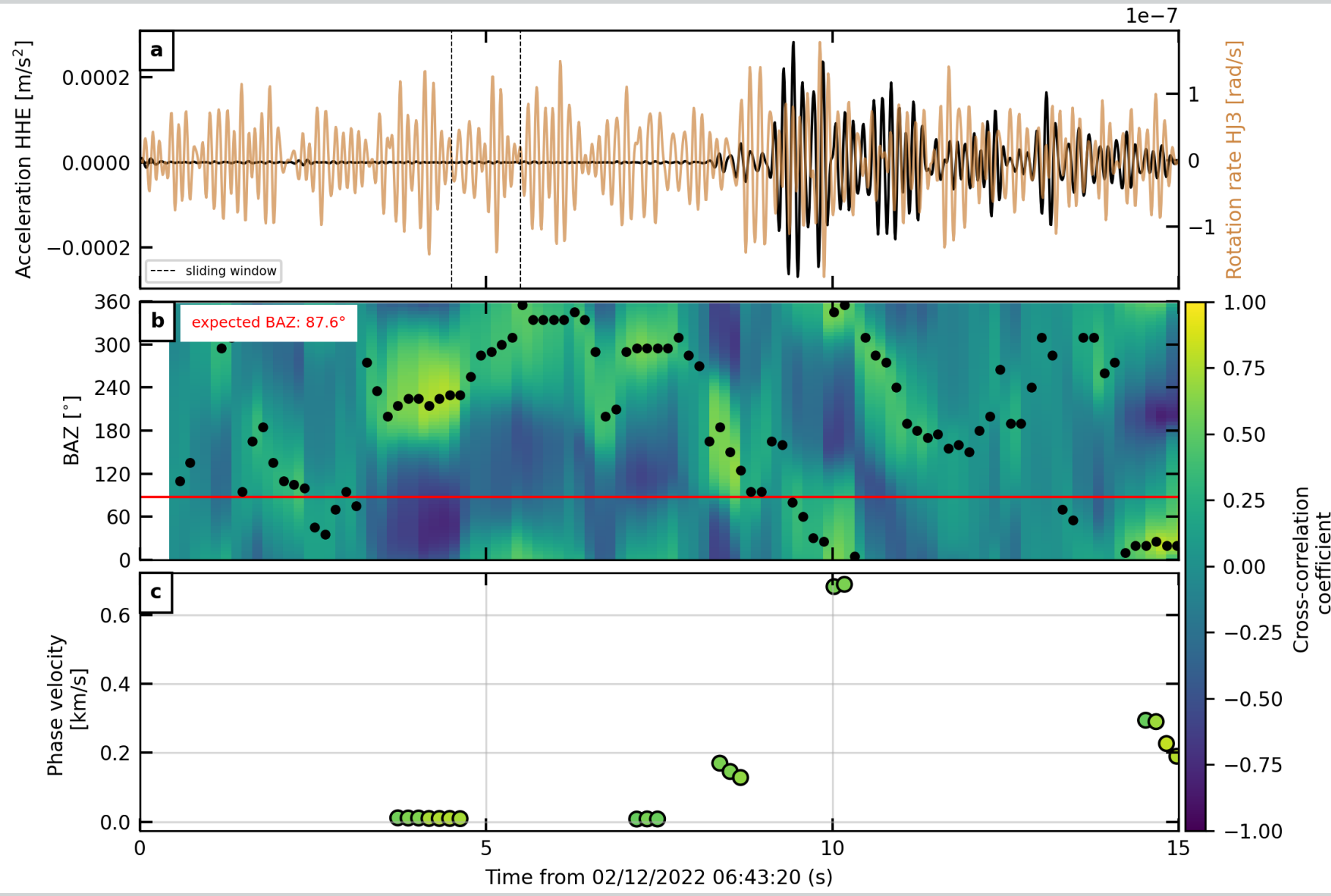
Back azimuth horizontal components

Volcsummit event
02.12.2022

Distance to CS0: 3.5km

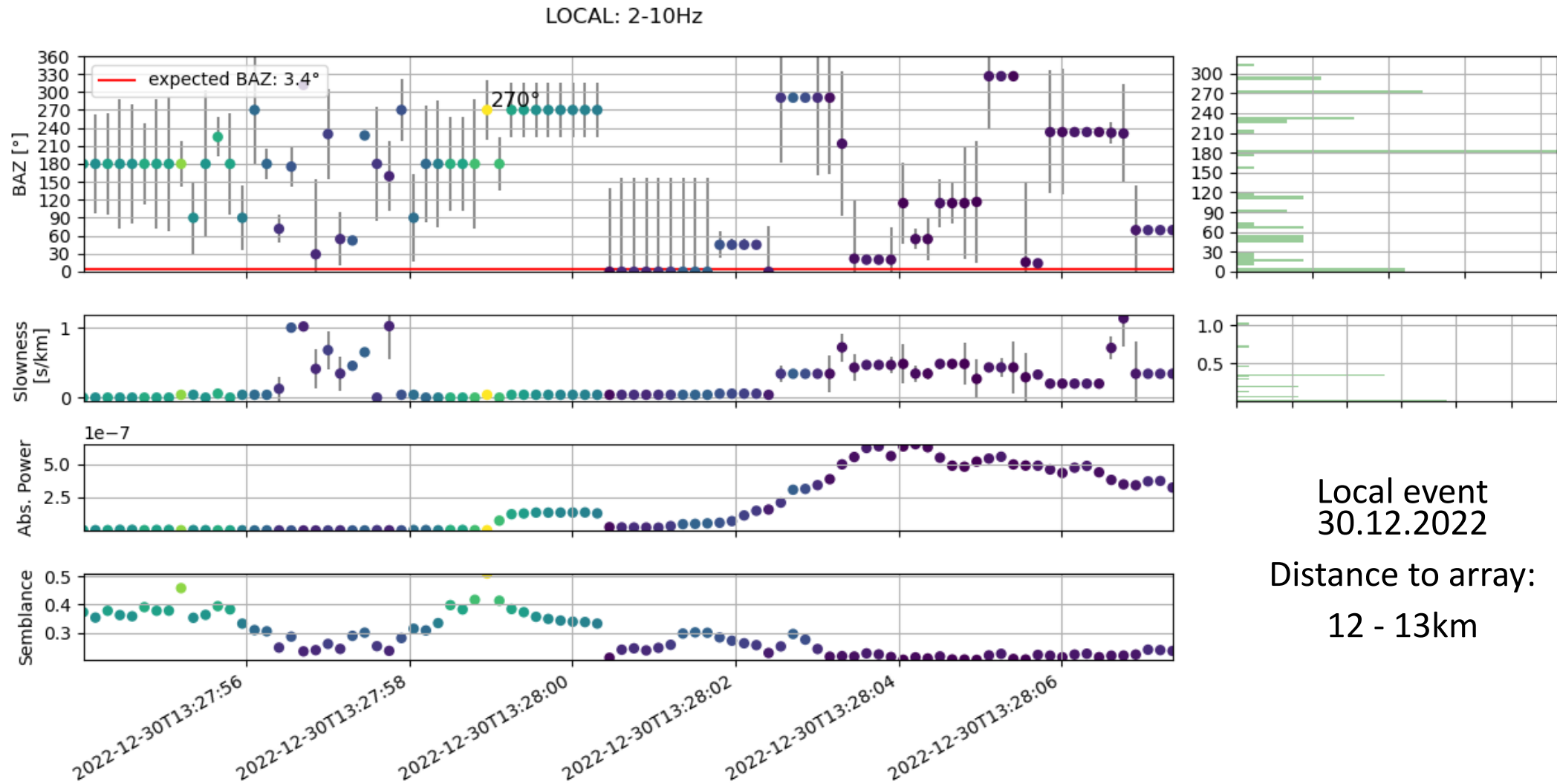


Back azimuth 6C method



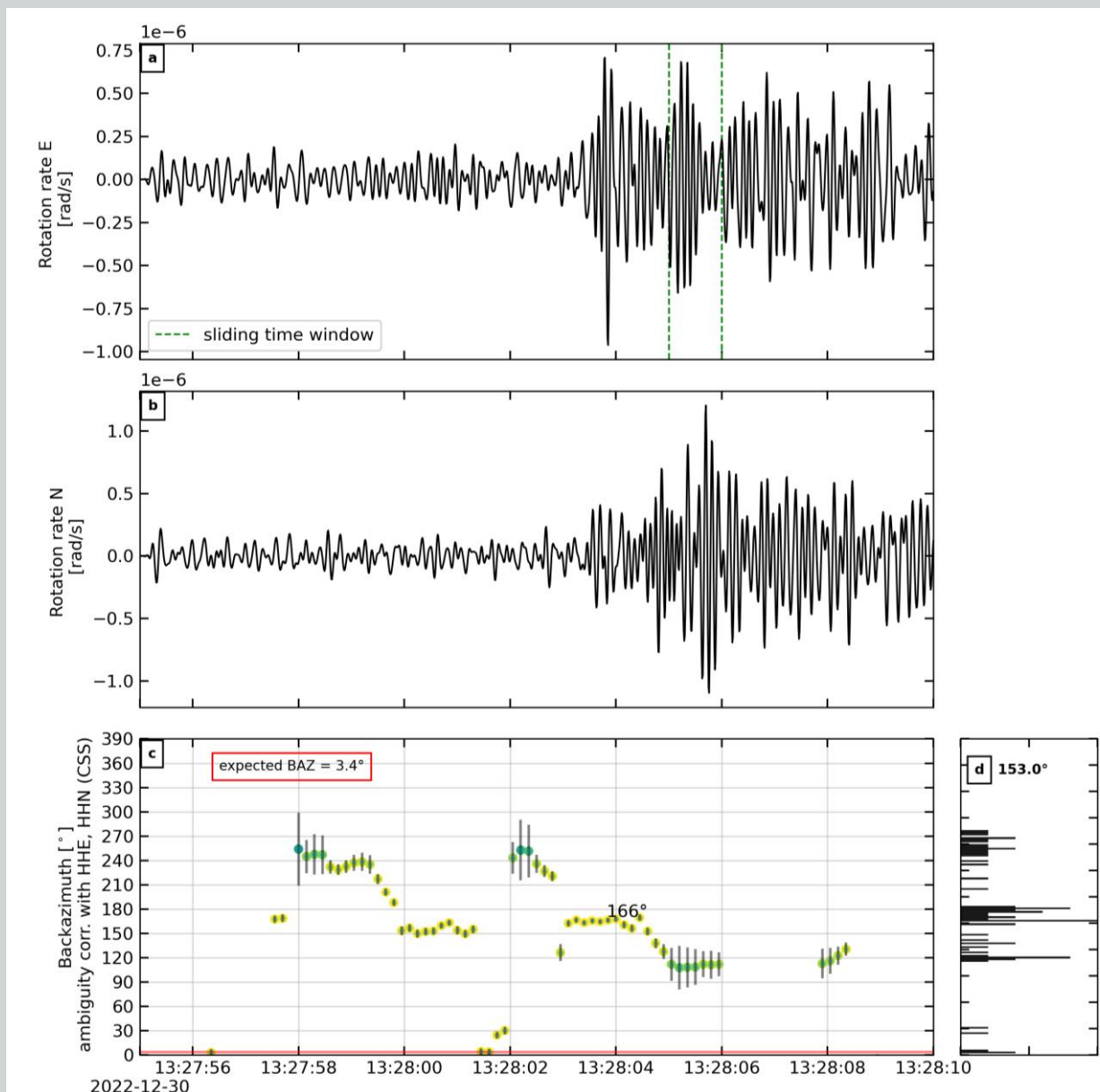
Volcsummit
event
02.12.2022
Distance to CS0:
3.5km

Back azimuth array



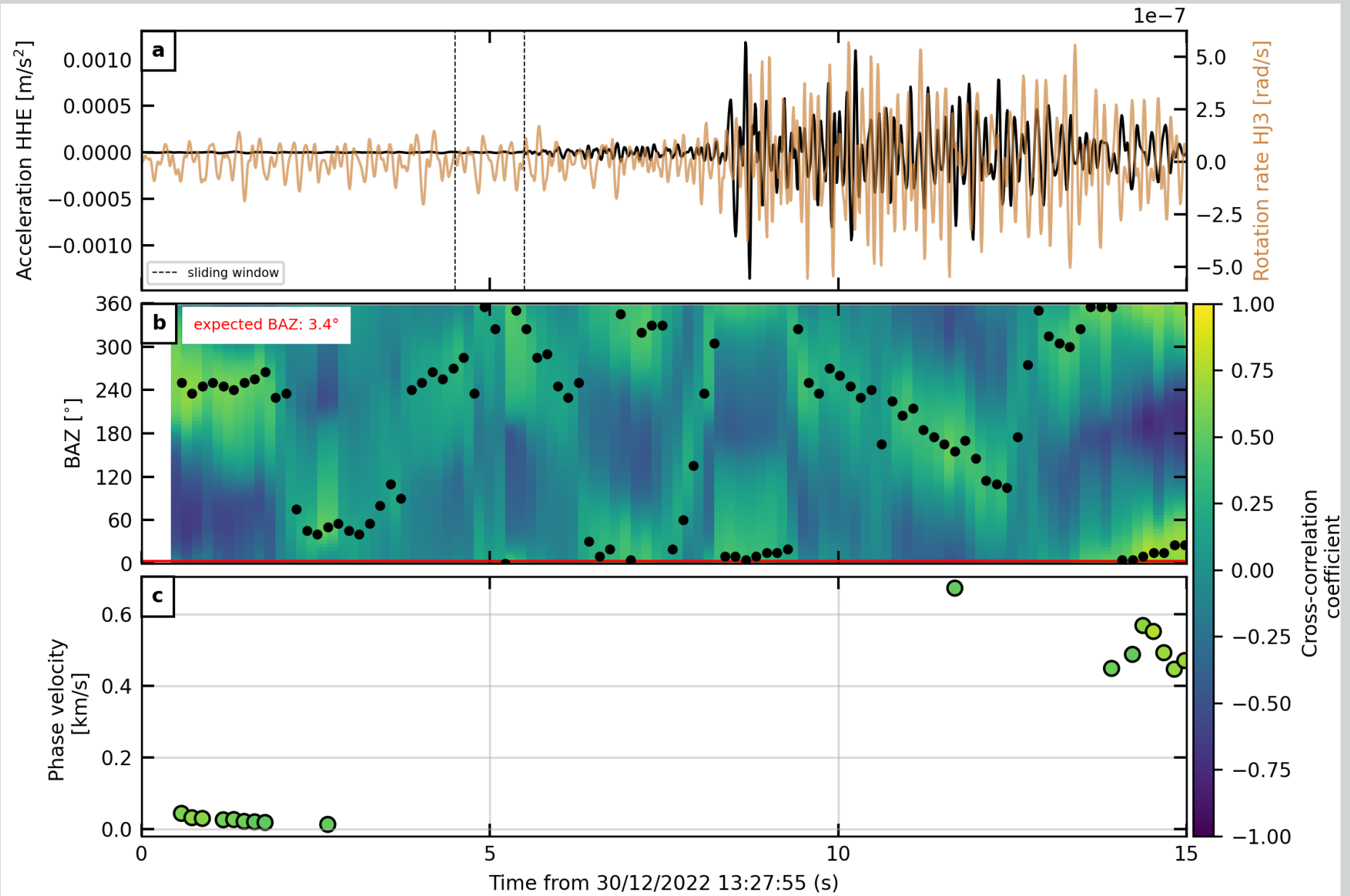
Back azimuth horizontal components

Local event 30.12.2022
Distance to CS0: 12.1km



Back azimuth 6C method

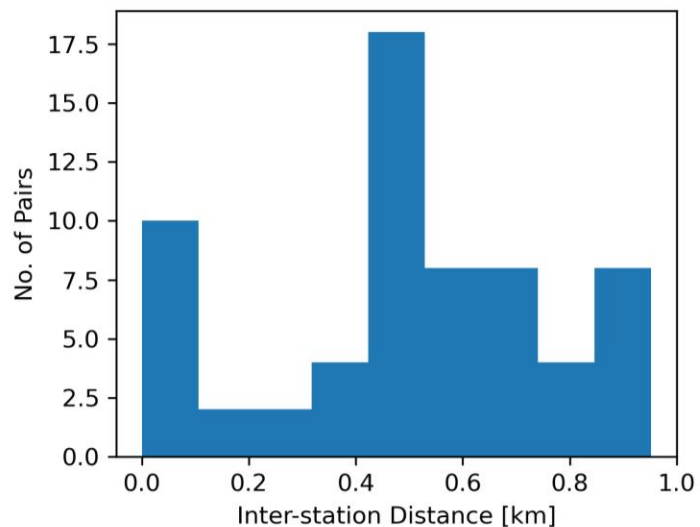
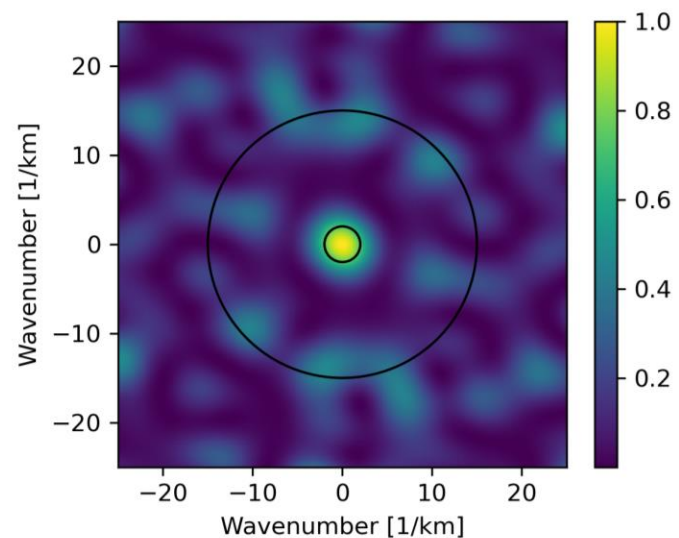
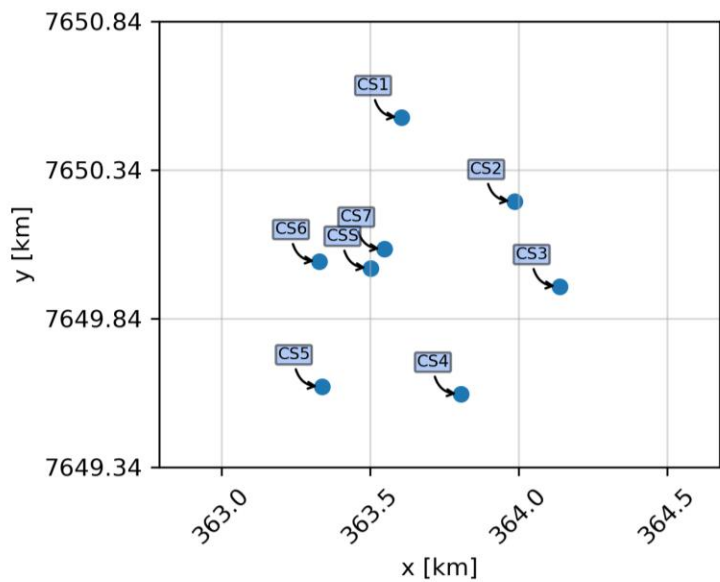
Local event
30.12.2022
Distance to
CSO:
12.1km



- stronger, closer events seem to work better
- more events needed for comparison, generalization of results
- BAZ influenced by site heterogeneity, sensitivity to noise
- further comparison with wind to understand noise

Aim: analysis of eruption tremor types 0.5 to 5Hz

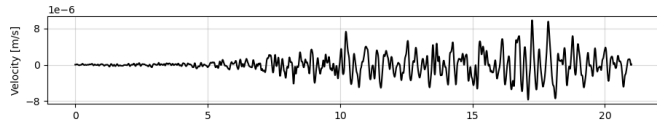
Appendix: Array response



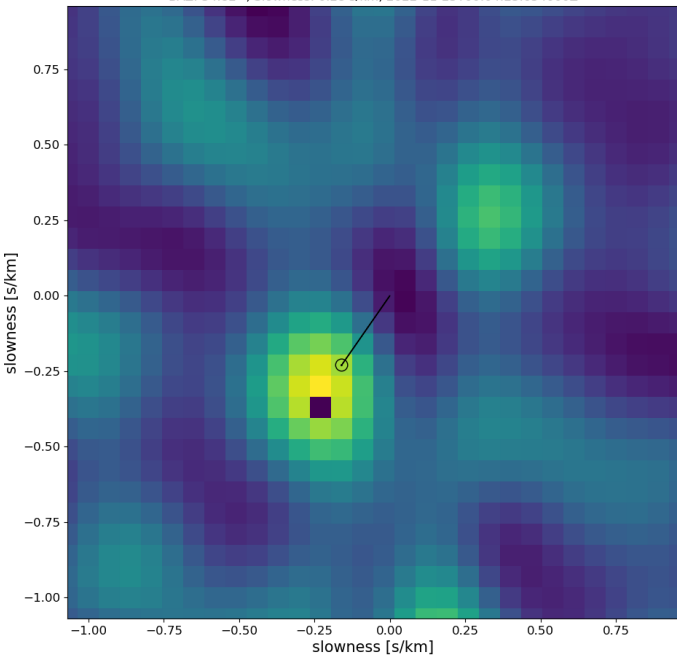
Avg. Dist. of seismometers = 0.491 km
 Min. Dist. of seismometers = 0.079 km
 Max. Δ elevation of seismometers = 39.99 m
 Array aperture = 0.953 km
 Apparent velocities expected = 1-10 [km/s]
 Array geometry constellation no. 71

Appendix: Array responses as slowness maps

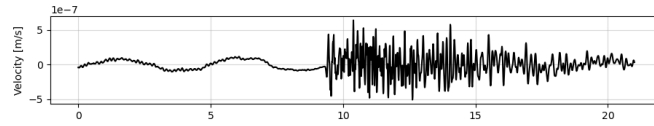
rockfall



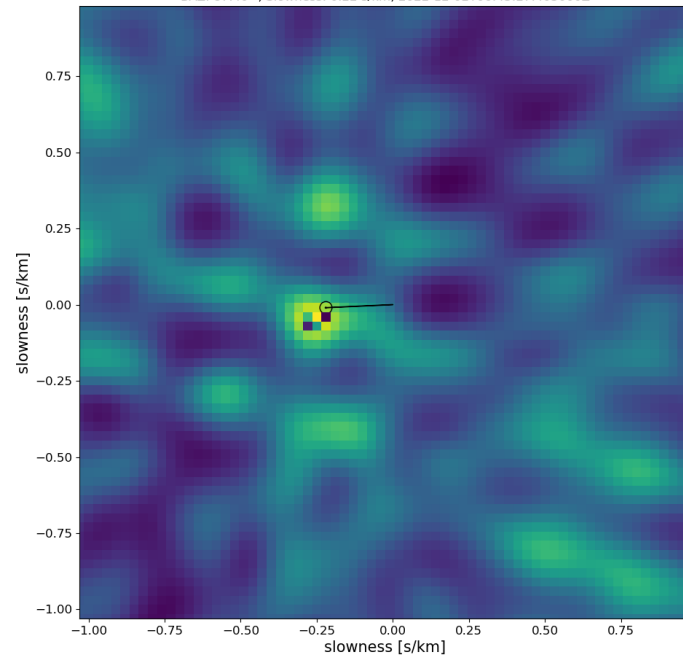
BAZ: 34.82 °, Slowness: 0.28 s/km, 2022-11-25T00:04:23.654000Z



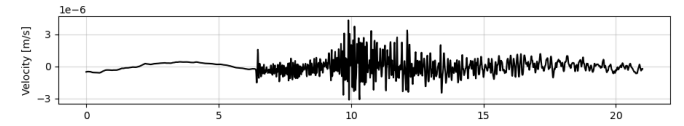
volcsummit



BAZ: 87.40 °, Slowness: 0.22 s/km, 2022-12-02T06:43:27.403000Z



local



BAZ: 0.00 °, Slowness: 0.04 s/km, 2022-12-30T13:28:00.455000Z

