Evolution of marine ice sheets with bed sedimentation

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Introduction & Motivation

Sedimentation occurs near grounding lines, causing formation of a grounding-zone wedge (GZW)

The presence/growth of a wedge can help to stabilise the grounding line (by locally reducing the water depth)

At the same time, the generation of an upward-sloping bed may influence subsequent retreat.





We seek to understand the *coupled* dynamics of ice flow and sediment deformation in a marine-ice-sheet setting.

Introduction & Motivation

Alley et al 2007 use a numerical model to investigate how presence of a till wedge impacts grounding-line position. Wedge shape is imposed, and static.

Effect of Sedimentation on Ice-Sheet Grounding-Line Stability

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Kowal & Worster (2020) develop theory and laboratory experiments to examine dynamics of two viscous fluid layers (one buoyant, one dense) near a grounding line.

The formation of grounding zone wedges: theory and experiments

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Prescribed fluxes of ice and sediment at left hand boundary.

$$\frac{\partial h}{\partial t} + \frac{\partial q}{\partial x} = -m \qquad \qquad q = \begin{cases} -\frac{\rho_i g h^2}{C} \frac{\partial s}{\partial x} & x < x_g \\ -\frac{(\rho_w - \rho_i)g h w}{12\eta_i} \frac{\partial h}{\partial x} & x > x_g \end{cases}$$

Conservation of sediment

 $\frac{\partial h_s}{\partial t} + \frac{\partial q_s}{\partial x} = 0$

$$q_{s} = \begin{cases} -\frac{\rho_{i}gh_{s}h}{2C}\frac{\partial s}{\partial x} - \frac{\rho_{i}gh_{s}^{3}}{3\eta_{s}}\left(\left(\frac{\rho_{s}-\rho_{i}}{\rho_{i}}\right)\frac{\partial s_{s}}{\partial x} + \frac{\partial s}{\partial x}\right) & x < x_{g} \\ -\frac{(\rho_{s}-\rho_{w})gh_{s}^{3}}{3\eta_{s}}\frac{\partial s_{s}}{\partial x} & x > x_{g} \end{cases}$$

$$s = \begin{cases} b+h_s+h & x < x_g\\ \left(\frac{\rho_w-\rho_i}{\rho_i}\right)h & x > x_g \end{cases} \quad s_s = b+h_s \qquad h = -\frac{\rho_w}{\rho_i}(b+h_s) \quad \text{at} \quad x = x_g \qquad q = q_0, \ q_s = q_{s0} \quad \text{at} \quad x = 0 \end{cases}$$

Steady states with no sediment motion

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Grounding line position depends on ice-shelf melt rate

Sediment deposition causes advance of grounding line (to eventual new steady state)

Repeated rapid retreat followed by re-growth of sediment wedge

Conclusions

- 1. Sediment deformation produces a grounding zone wedge, which facilitates advance of the grounding line.
- 2. The steady state with a grounding zone wedge appears to be stable.
- 3. Sufficiently sudden increases in ice-shelf melting induce punctuated pattern of grounding-line retreat.

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