

*New Routine for Calculating the non-LTE CO<sub>2</sub> 15 μm  
Cooling of Mesosphere and Lower Thermosphere in  
GCMs*

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*Any physical parameterization for GCM must be able to react as realistic as possible at steady changing local physical state of the atmosphere in the modeling process. This is particularly true for parametrizing the infrared radiation and its effects (local cooling or heating), which are critically important for adequate modeling of energy balance. The instantaneous  $p$ - $T$  distributions in modern GCMs of middle and upper atmosphere exhibit very strong variability, caused by the superposition of tidal and gravity waves of different amplitude and vertical scales. Therefore, the parameterization of the 15-micron  $\text{CO}_2$  cooling, which is a main radiative cooling mechanism of these layers, must properly react to this variability.*

*However, the matrix parameterizations of the 15-micron cooling are unable to provide adequate reaction to strongly disturbed  $T$  distributions. This was well known already 30 years ago for those who worked on developing the first version of the Fomichev et al, 1998 routine.*

*We present a new routine KF23 for calculating the non-local thermodynamic equilibrium (non-LTE) 15  $\mu\text{m}$  CO<sub>2</sub> cooling/heating of mesosphere and lower thermosphere in General Circulation Models (GCMs).*

*KF23 provides exact solution of the optimized models of the non-LTE in CO<sub>2</sub> for day and night conditions. It delivered cooling/heating with an error not exceeding 1 K/Day even for strong temperature disturbances.*

*Compares to this the Fomichev et al, 1998 (F98) routine errors reach 25 K/day.*

*These errors may not be removed in the framework of the parameterization approach, as the revised version of the Fomichev-98 algorithm presented by Lopez-Puertas et al, (2023), shows (see also Kutepov, 2023).*

*KF23 uses exact algorithm based on the Accelerated Lambda Iteration (ALI) and Opacity Distribution Function (ODF) techniques for the non-LTE cooling/heating calculations, and is about 1000 faster than the standard matrix/line-by-line calculations.*

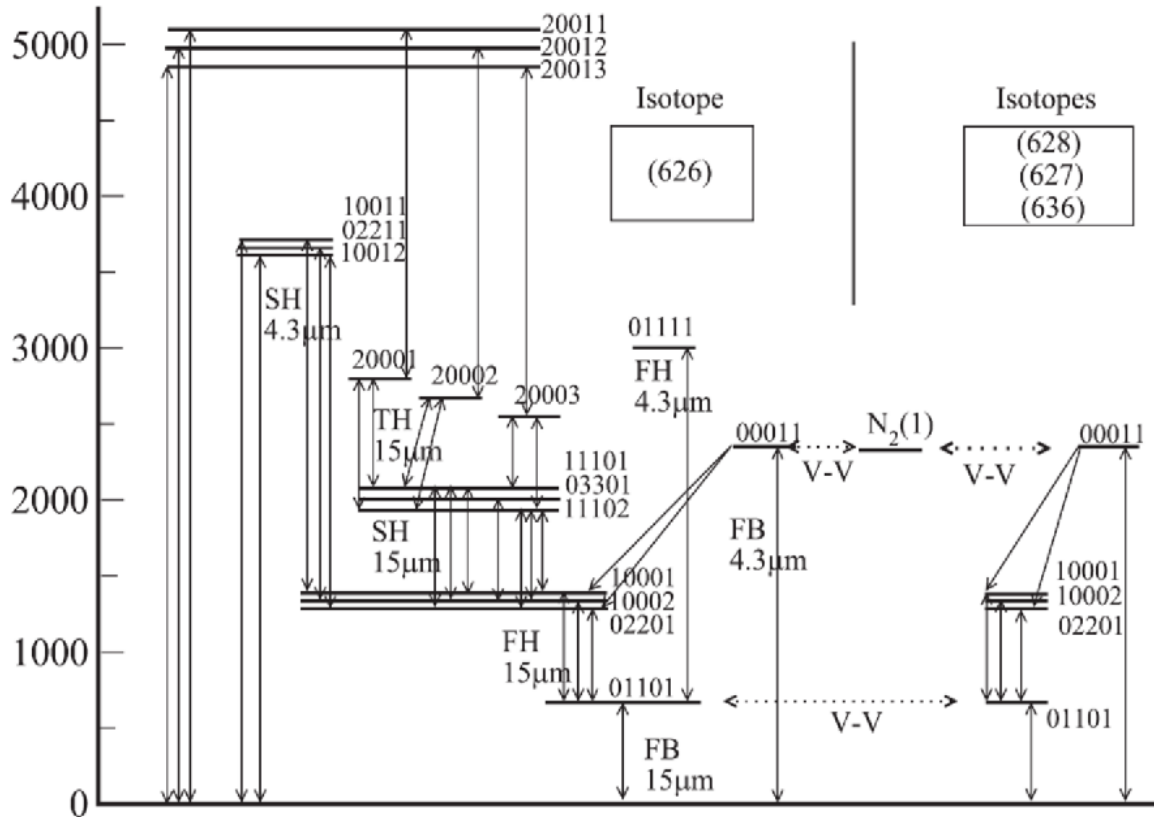
*KF23 has an interface for feed-backs from the model and is ready for implementation in any GCM.*

*KF23 may use any quenching rate coefficient of the  $\text{CO}_2(\text{v}_2)+\text{O}(3\text{P})$  reaction, any  $\text{O}(3\text{P})$  density and allows the user to vary the number of vibrational levels and bands to find a balance between the calculation speed and accuracy.*

*KF23 handles broad variation of  $\text{CO}_2$  both below and above the current volume mixing ratio, up to 4000 ppm. This allows using this routine for modeling the Earth's ancient atmospheres and the climate changes caused by increasing  $\text{CO}_2$ .*

### Reference

*Kutepov, A. and Feofilov, A.: New Routine NLTE15 $\mu\text{m}$ Cool-E v1.0 for Calculating the non-LTE  $\text{CO}_2$  15  $\mu\text{m}$  Cooling in GCMs of Earth's atmosphere, Geosci. Model Dev. Discuss., <https://doi.org/10.5194/gmd-2023-115>, in review, 2023.*



| Table 1. CO <sub>2</sub> vibrational levels included in the night- and daytime model |            |           |             |
|--------------------------------------------------------------------------------------|------------|-----------|-------------|
| Isotope, HITRAN level notification, energy in cm-1                                   |            |           |             |
| 626 00001                                                                            | 0.0        | 636 00001 | 0.0         |
| 626 01101                                                                            | 667.379960 | 636 01101 | 648.478030  |
| 626 10002                                                                            | 1285.40834 | 636 02201 | 1297.26326  |
| 626 02201                                                                            | 1335.13161 |           |             |
| 626 10001                                                                            | 1388.18432 | 628 00001 | 0.0         |
| 626 11102                                                                            | 1932.47013 | 628 01101 | 662.37335   |
| 626 03301                                                                            | 2003.24615 |           |             |
| 626 11101                                                                            | 2076.85588 | 627 00001 | 0.0         |
| D 626 00011                                                                          | 2349.14291 | 627 01101 | 664.72941   |
| D 626 01111                                                                          | 3004.01227 |           |             |
| D 626 10012                                                                          | 3612.84080 | 44        | 0 0.0       |
| D 626 02211                                                                          | 3659.27229 | D 44      | 1 2329.9116 |
| D 626 10011                                                                          | 3714.78193 |           |             |
| D 626 20013                                                                          | 4853.62341 | 66        | 0 0.0       |
| D 626 20012                                                                          | 4977.83500 | D 66      | 1 1556.3519 |
| D 626 20011                                                                          | 5099.66050 |           |             |
|                                                                                      |            | 6         | 0 0.0       |
| D marks levels added in daytime model                                                |            |           |             |

Figure 1. CO<sub>2</sub> vibrational levels diagram (Feofilov and Kutepov, 2012). Solid lines with arrows – main optical transitions, dashed lines with arrows - main V–V energy exchange processes, V–T transitions are not shown. Table 1 shows levels included new KF23 routine for night and day. Reverence model (not shown) includes 60 vibrational level of 5 CO<sub>2</sub> isotopes and about 200 bands

**Table 2. Numbers of operation and computing times. *Times are given in sec.***

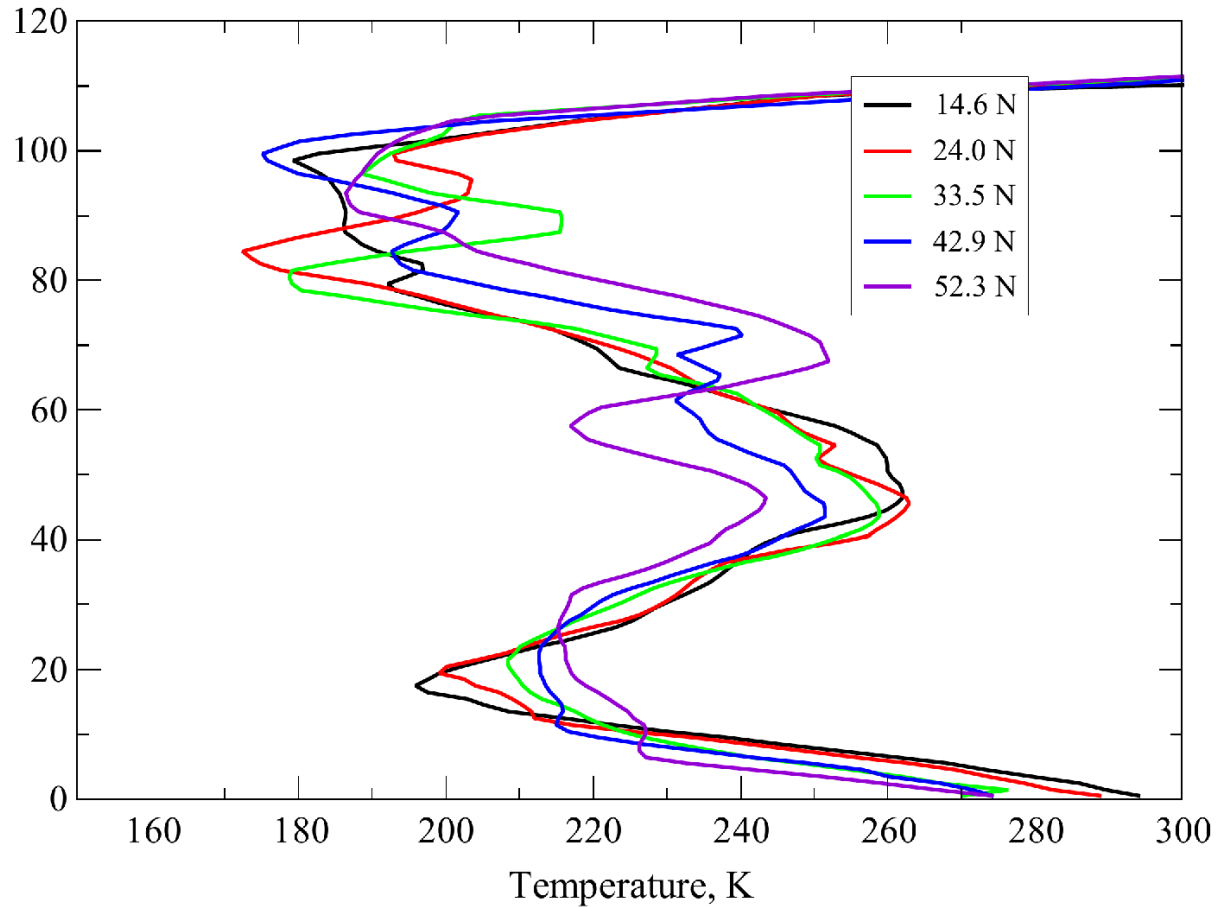
**NIGHT: NL=18; NB=18, NBr= 54, NRT=3078; NF=32; NA=2: ND=125; CO2x1**

| Night           | $N_{Aux}/T_{Aux}$ | $N_{Rad} / T_{Rad}$ | $N_{Inv} / T_{Inv}$ | $N_I$ | $T_{tot}$ | <b>K</b> |
|-----------------|-------------------|---------------------|---------------------|-------|-----------|----------|
| MM/LBL          | 2.8e5 / 5e-2      | 2.5e7 / 0.25        | 1.14e10/43          | 2     | 86        | 860      |
| LI / ALL, LBL   | 5e4 / 8.5e-3      | 2.5e7 / 0.25        | 7.3e5/7.7.0e-3      | 60/5  | 16/1.3    | 160/ 13  |
| <b>ALI, ODF</b> | 5e4 / 8.5e-3      | 4.5e5 / 4.5e-3      | 7.3e5/7.7.0e-3      | 5     | 0.1       | 1        |

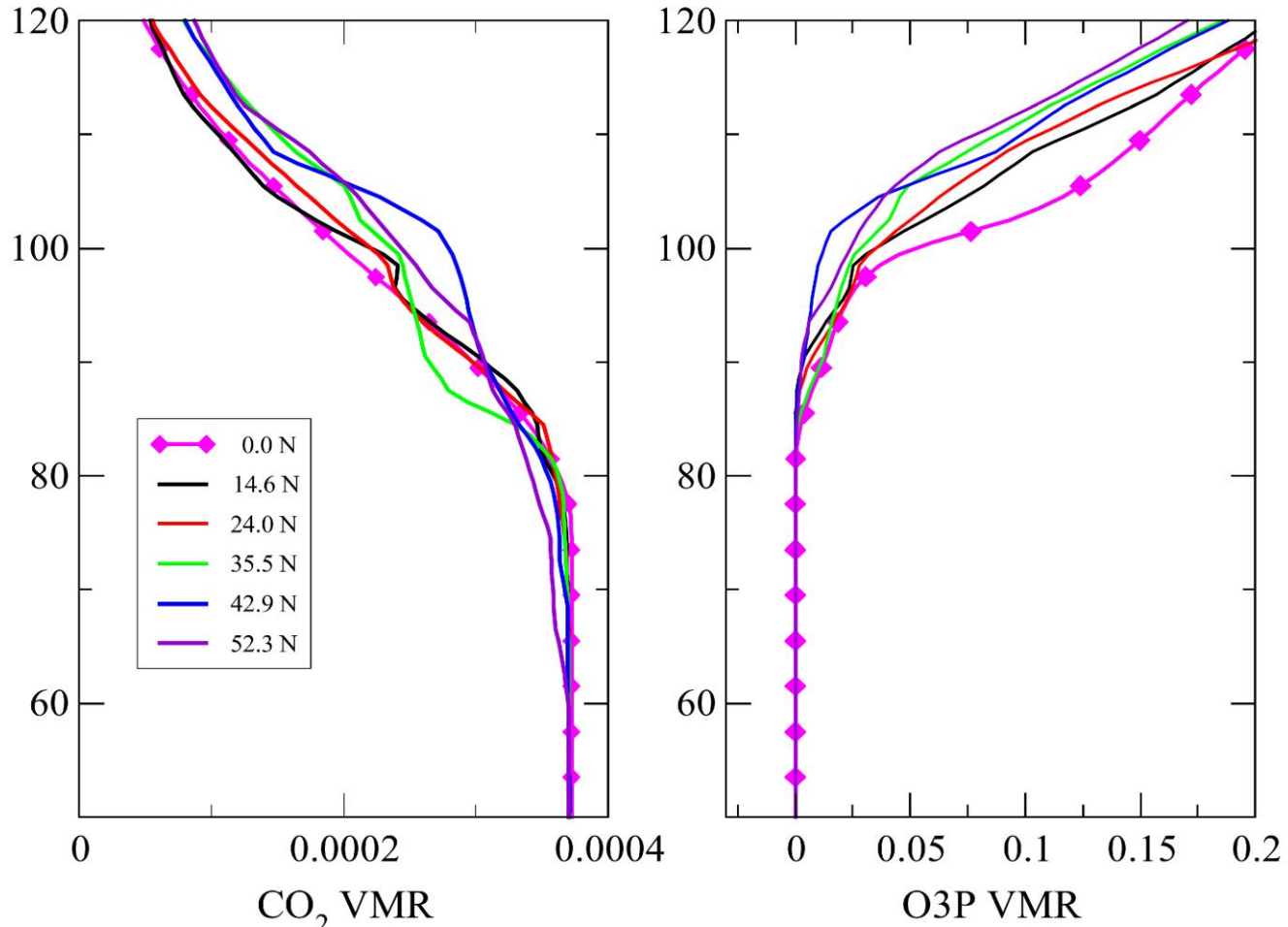
**DAY: NL=28; NB=46, NBr= 119, NRT=6039; NF=32; NA=2: ND=125; CO2x1**

| Day             | $N_{Aux}/T_{Aux}$ | $N_{Rad} / T_{Rad}$ | $N_{Inv} / T_{Inv}$ | $N_I$ | $T_{tot}$ | <b>K</b> |
|-----------------|-------------------|---------------------|---------------------|-------|-----------|----------|
| MM/LBL          | 4.4e5/2e-1        | 4.8e7/0.48          | 4.3e10/160          | 2     | 321       | 1284     |
| LI / ALL, LBL   | 1.1e5/1.9e-2      | 4.8e7/0.48          | 2.7e6/2.2e-2        | 60/5  | 31/2.6    | 124/10   |
| <b>ALI, ODF</b> | 1.1e5/1.9e-2      | 9.5e5/9.5e-3        | 2.7e6/2.2e-2        | 5     | 0,25      | 1        |

**New Routine KF23 (ALI/ODF in the table) calculate the cooling 860 times faster for night and 1286 times faster for day than the standard matrix method + line-by-line radiative transfer (MM/LBL in the table). For details see the paper at <https://doi.org/10.5194/gmd-2023-115>**

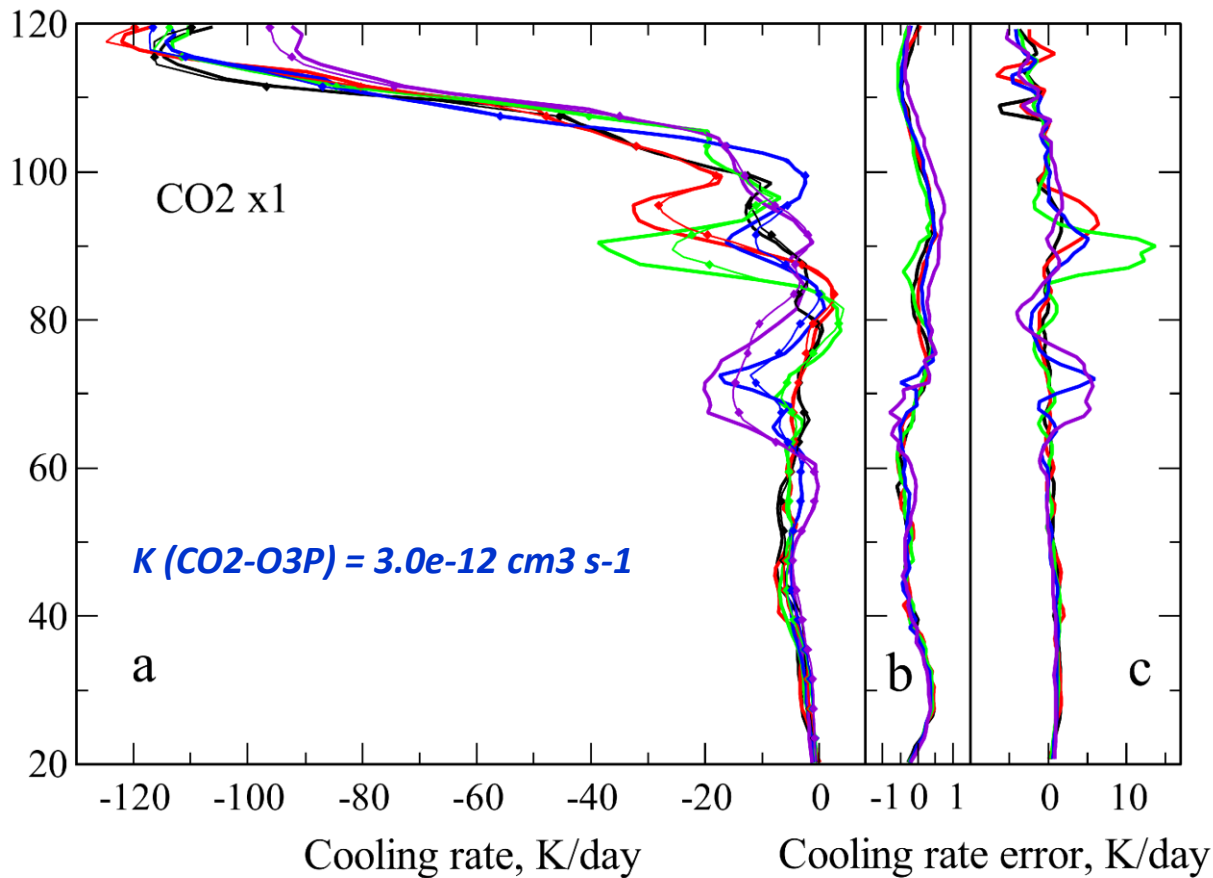


**Figure 2. WACCM6 CESM generated temperature profiles used for testing the accuracy of the CO<sub>2</sub> 15 μm cooling calculations**



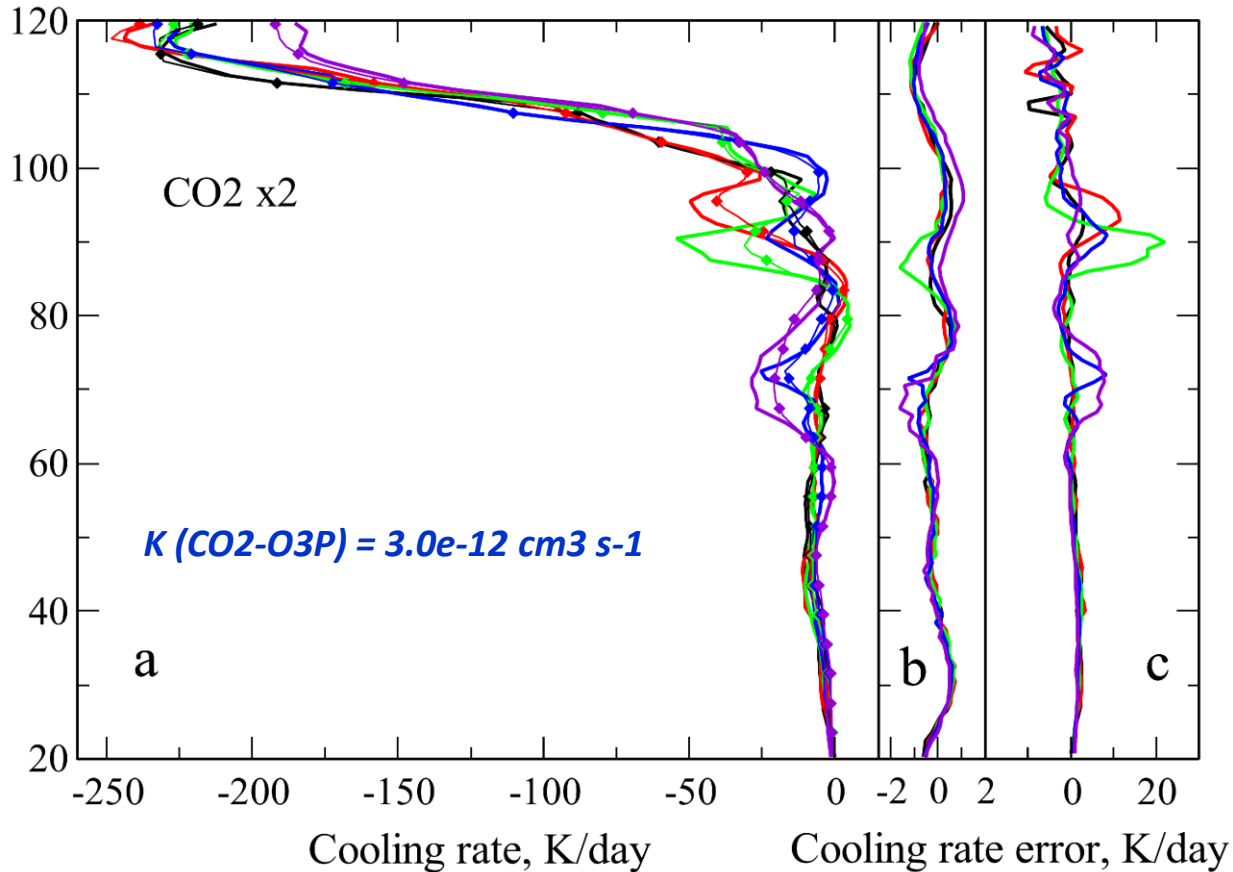
**Figure 3. WACCM6 CESM CO<sub>2</sub> and O<sub>3</sub>P vmr profiles used for testing the accuracy of the CO<sub>2</sub> 15  $\mu$ m cooling calculations. Magenta with diamonds shows data from Yudin et al, 2022 for diurnal tides at equator.**





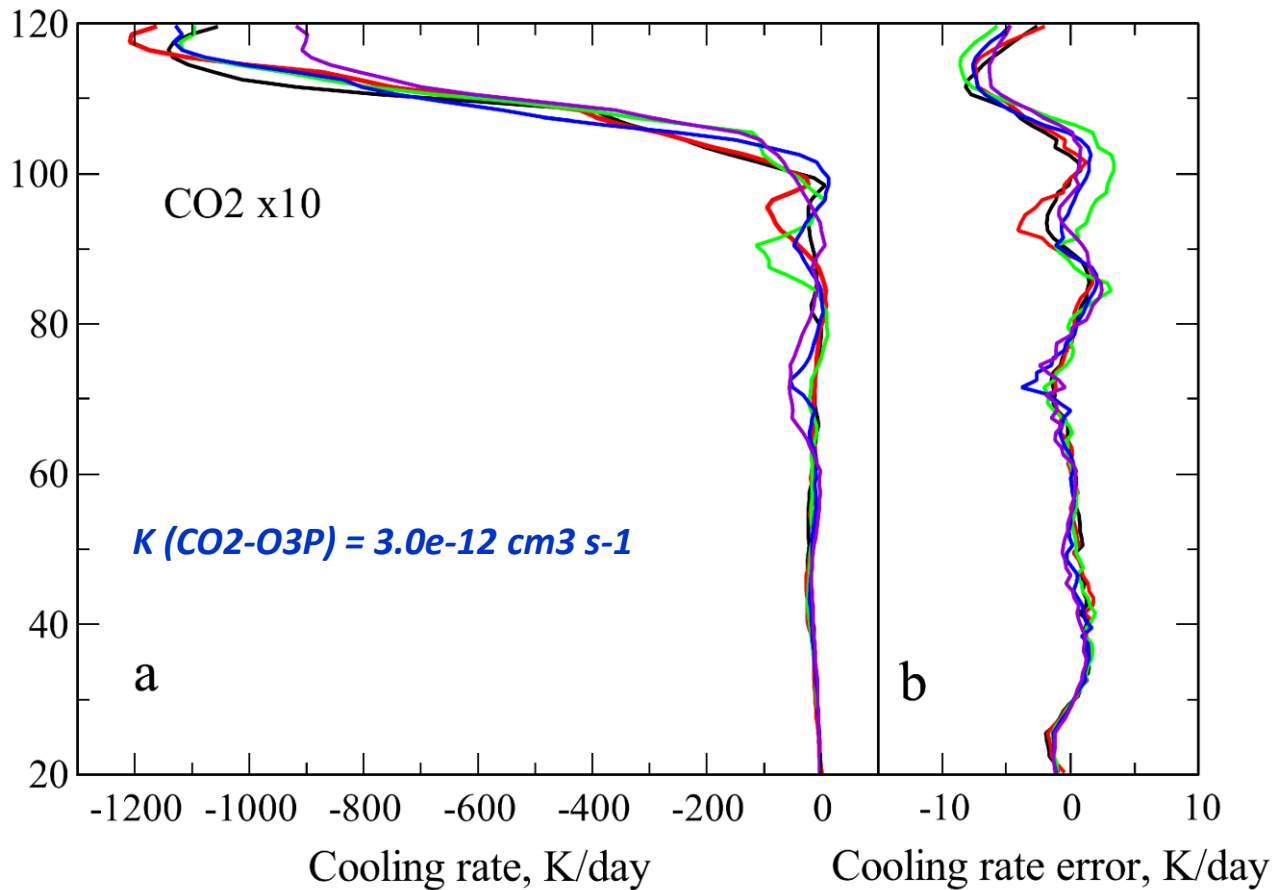
**Cooling errors of the Fomichev et al. 1998 routine (F98) around mesopause exceed 10 K/Day. Errors of new KF23 routine are < 1 K/Day for all altitudes.**

**Figure 4. Cooling rates in the CO<sub>2</sub> 15 μm band and cooling rates errors for the CO<sub>2</sub> VMR of 400 ppm for inputs shown in Figs. 2 and 3. (a): Thick solid lines - reference data (REF); thin solid lines with diamonds – Fomichev et al 1998 (F98); (b) new routine of Kutepov and Feofilov, 2023 (KF23) minus REF; (c) F98 minus REF.**



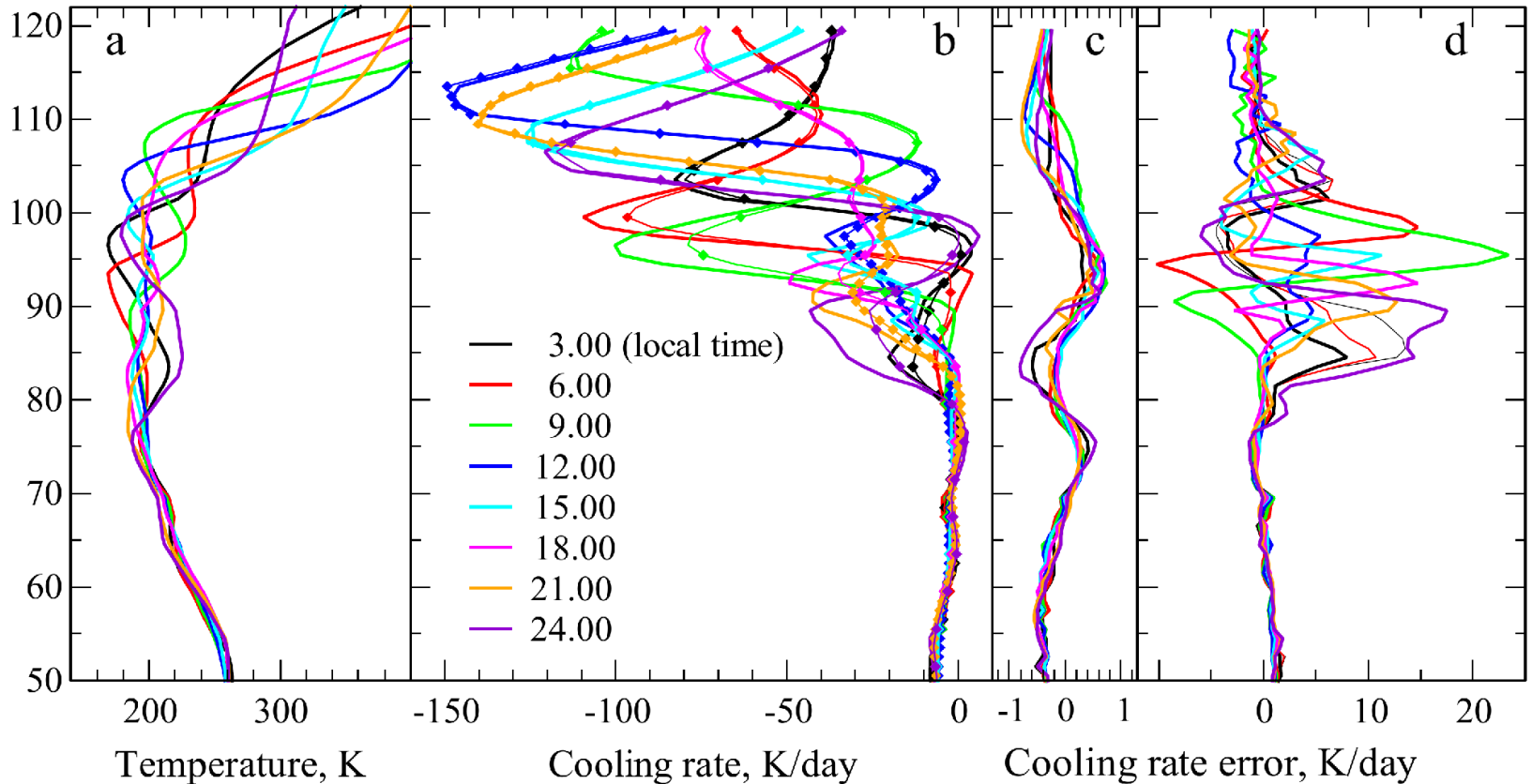
**Cooling errors of the Fomichev et al. 1998 routine (F98) around mesopause reach 20 K/Day. Errors of new KF2023 routine are < 2 K/Day for all altitudes .**

**Figure 5. Cooling rates in the CO2 15 μm band and cooling rates errors for the CO2 VMR of 800 ppm for inputs shown in Figs. 2 and 3. (a): Thick solid lines - reference data (REF); thin solid lines with diamonds – Fomichev et al 1998 (F98); (b) new routine of Kutepov and Feofilov, 2023 (KF23) minus REF; (c) F98 minus REF.**



*Errors of new  
KF2023 routine  
are < 10 K/Day  
for all altitudes .*

*Figure 7. Cooling rates in the CO<sub>2</sub> 15 μm band and cooling rates errors for the CO<sub>2</sub> VMR of 4000 ppm for inputs shown in Figs. 2 and 3. (a): Thick solid lines - reference data (REF); (b) new routine of Kutepov and Feofilov, 2023 (KF23) minus REF;*



**Figure 9. CO<sub>2</sub> 15 μm cooling rates for diurnal tides at equator. (a) Temperature profiles; (b) Cooling rates: thick solid lines - reference model (REF), thin solid lines with diamonds - F98 routine; (c) New KF23 routine minus REF; (d) F98 routine minus REF. The errors of Fomichev et al, 1998 routine (F98) reach 25 K/Day near the mesopause.**

*We present the new KF23 routine for calculating the non-LTE CO<sub>2</sub> 15 μm radiative cooling/heating in the GCMs of middle and upper Atmosphere*

- KF23 delivers high accuracy cooling rates for any temperature distributions including those disturbed by strong micro- and meso-scale structures:*

*Maximal errors of the 15 μm radiative cooling/heating for Fomichev et al, 1998 routine (F98) and Kutepov and Feofilov 2023 routine (KF23) for smooth/wave disturbed T profiles (in K/Day)*

| CO <sub>2</sub> vmr | F98      | KF23      |
|---------------------|----------|-----------|
| 400 ppm             | 1-2 / 25 | 0.2 / 1   |
| 800 ppm             | 2-4 / 47 | 0.3 / 2   |
| 1600 ppm            | ---      | 0.7 / 3.5 |
| 4000 ppm            | ---      | 1.5 / 10  |

- KF23 routine provides accurate cooling calculations in a very broad ranges of CO<sub>2</sub>(v<sub>2</sub>)- O(3P) quenching rate and O(3P) variation.*

- *KF23 routine provides accurate cooling calculations in a very broad ranges of CO<sub>2</sub>(v2) - O(3P) quenching rate and O(3P) variation.*
- *KF23 works for very broad variation of CO<sub>2</sub> both below and above the current density, up to 4000 ppm. This allows using this routine for modeling the Earth's ancient atmospheres and the climate changes caused by increasing CO<sub>2</sub> .*
- *Recently Lopez-Puertas et al., 2023 tried to update the parameterization of Fomichev et al, 1998. Unfortunately, the attempt to improve the parameterization accuracy failed (see Kutepov, 2023 for detailed analysis): for wavy temperature profiles the revised routine works no better that the standard Fomichev-1998 routine.*

- *Fomichev, V. I., Blanchet, J.-P., and Turner, D. S.: Matrix parameterization of the 15  $\mu\text{m}$  CO<sub>2</sub> band cooling in the middle and upper atmosphere for variable CO<sub>2</sub> concentration, Journal of Geophysical Research: Atmospheres, 103, 11 505–11 528, <https://doi.org/10.1029/98jd00799>, 1998.*
- *Kutepov, A. and Feofilov, A.: New Routine NLTE15 $\mu\text{m}$ Cool-E v1.0 for Calculating the non-LTE CO<sub>2</sub> 15  $\mu\text{m}$  Cooling in GCMs of Earth's atmosphere, Geosci. Model Dev. Discuss., <https://doi.org/10.5194/gmd-2023-115>, in review, 2023*
- *Kutepov, A. A., Comment to “An improved and extended parameterization ...” by López-Puertas, M., et al, 2023 ', <https://egusphere.copernicus.org/preprints/2023/egusphere-2023-2424/egusphere-2023-2424-CC1-supplement.pdf>. 2023.*
- *López-Puertas, M., et al. An improved and extended parameterization of the CO<sub>2</sub> 15  $\mu\text{m}$  cooling in the middle/upper atmosphere, <https://doi.org/10.5194/egusphere-2023-2424> Preprint. Discussion started: 6 November 2023.*