

Introduction

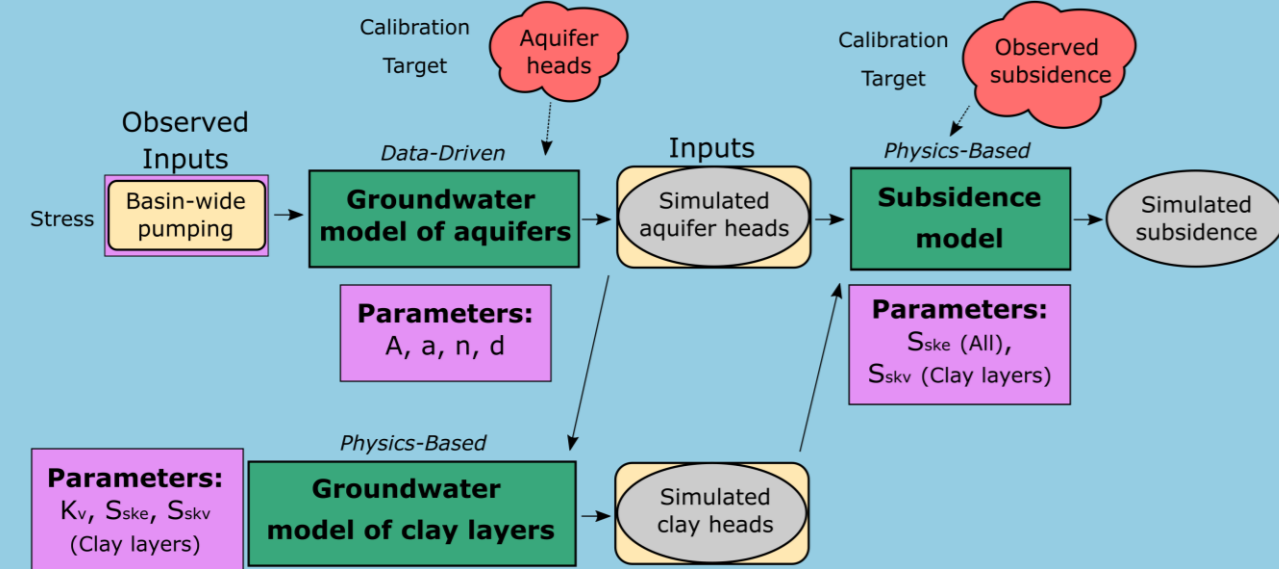
Subsidence is often caused by substantial groundwater pumping, especially in deltaic areas. Accurate subsidence simulation is greatly influenced by limited data availability, specifically input forcings/drivers and calibration data. In this study, an ensemble-based data-assimilation method is used to improve the estimates of land subsidence in Bangkok, Thailand, which is simulated by a linked data-driven and physics-based modeling approach. The approach is applied with limited groundwater and subsidence observations and only an estimate of basin-wide pumping. The assimilation of sparse and noisy head and subsidence observation data into the ESMDA algorithm results in improved estimates and uncertainty quantification of groundwater heads, localized groundwater pumping, and parameters.

Methods

Ensemble Smoother with Multiple Data Assimilation (ESMDA)

$$\mathbf{z}^a = \mathbf{z}^f + \mathbf{C}_{zz}\mathbf{H}^T(\mathbf{H}\mathbf{C}_{zz}\mathbf{H}^T + \alpha\mathbf{C}_{dd})^{-1}(\mathbf{d}_{uc} - \mathbf{g}(\mathbf{z}^f))$$

The update equation of ESMDA is based on Bayes' theorem, which combines prior knowledge and observations. Prior knowledge is represented through parameters and input (in purple boxes below) in \mathbf{z} (state) and models (in green boxes) in $\mathbf{g}()$. Observations added with error are represented by \mathbf{d}_{uc} . \mathbf{C}_{zz} represents the state covariance matrix, and the \mathbf{C}_{dd} observation error covariance matrix. α represents inflation factors that decreasingly overinflates the observation error for each ESMDA step. \mathbf{H} is a matrix aligning parameters to observations. The update equation is applied for each ESMDA step. ESMDA is implemented using the pyesmda package (Collet, 2022).



A 3-step approach is developed to simulate land subsidence at observation well nests.

1. Heads in the aquifer at an observation well are simulated using a data-driven groundwater model called Pastas (Collenteur et al., 2019). Groundwater observations are assimilated using ESMDA in this step to estimate pumping rates and parameters for improved groundwater modeling.
2. These heads are used as the boundary conditions to simulate the heads in the clay layers using a physics-based groundwater model.
3. The heads in both the aquifer and clay layers are used as inputs to compute land subsidence at a given location through a physics-based elastoplastic subsidence model. Observed subsidence rates are assimilated using ESMDA in this step to estimate subsidence parameters for improved subsidence modeling.

Study Site: Bangkok, Thailand

